

1 Definitions

1. The pmf for a Binomial Random variable $Y \sim (n, p)$ is given by

$$p_Y(Y = k) = \binom{n}{k} p^k (1 - p)^{n-k}, \quad 0 \le k \le n$$
 (1.1)

2. The pdf of an Exponential Random variable X is given by

$$p_X(x) = ce^{-cx}u(x) (1.2)$$

2 Problems

1. Show that the solution of

$$\max_{p} p_Y(Y=k) \tag{2.1.1}$$

is

$$\hat{p} = \frac{k}{n} \tag{2.1.2}$$

2. Find

$$\Pr\left(X > T\right) \tag{2.2.1}$$

where T is a constant.

3. If X represents the lifetime of a bulb, show that the value of c that maximizes the probability of k out of n bulbs working after T hours is

$$c = \frac{1}{T} \log \left(\frac{n}{k} \right) \tag{2.3.1}$$