

*Problem 1:* To separate two sinusoidal signals of frequencies 1 kHz and 2 kHz.

- 1) Sketch the spectrum of  
 $s_1(t) = \cos(2\pi f_1 t)$  and  
 $s_2(t) = \cos(2\pi f_2 t)$   
where,  $f_1 = 1$  kHz and  $f_2 = 2$  kHz
- 2) Let  $y(t) = s_1(t) + s_2(t)$ . Obtain the filter  $h(t)$  that can be used to get  $s_1(t)$  from  $y(t)$ .

*Problem 2:* Let  $H(z) = G \frac{1-z^{-2}}{1-2r\cos(\omega_0)z^{-1}+r^2z^{-2}}$  where  $r = 0.95$ ,  $\omega_0 = \pi/3$  and  $\max\{|H(e^{j\omega})|\} = 1$

- 1) Find G.
- 2) Write the input output relation for this discrete system.
- 3) Plot  $|H(e^{j\omega})|$ .
- 4) Find the impulse response for the given system.

*Problem 3:* Consider  $x_1(n) = \{1, 1, 1, 1\}$

- 1) Find  $x_1(n) * x_1(-n)$ .
- 2) Let  $x_2(n) = \{1, 1, -1, -1\}$ , find  $x_1(n) * x_2(-n)$ .
- 3) Let  $x_3(n) = \{1, 1, 1, -1\}$ , find  $x_1(n) * x_3(-n)$ .