

$$F(t) = \frac{1}{2} - \frac{1}{2\pi j} \times \text{c.p.v.} \int_{-\infty}^{\infty} \frac{e^{-j\omega t}}{\omega(1+\omega^2)} d\omega, \quad (10)$$

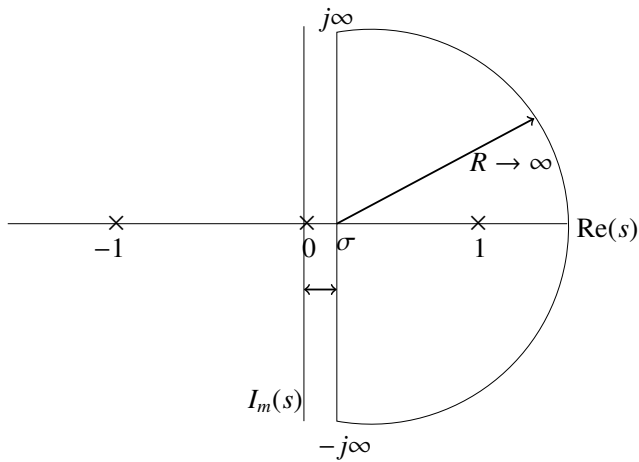


Fig. 7.2

where c.p.v. denotes the Cauchy Principal Value. Use the contour in Fig. 8 to evaluate  $F(t)$ ,  $t < 0$  by showing that

$$1) \lim_{r \rightarrow 0} \int_{C_r} \frac{e^{-jzt}}{z(1+z^2)} dz = -j\pi,$$

$C_r : z = re^{j\theta}, 0 < \theta < \pi$   
where  $C_r$  is in the clockwise direction.

$$2) \lim_{\substack{r \rightarrow 0 \\ R \rightarrow \infty}} \int_{-R}^{-r} \frac{e^{-j\omega t}}{\omega(1+\omega^2)} d\omega + \int_r^R \frac{e^{-j\omega t}}{\omega(1+\omega^2)} d\omega \\ = j\pi + \oint_C \frac{e^{-jzt}}{z(1+z^2)} dz$$

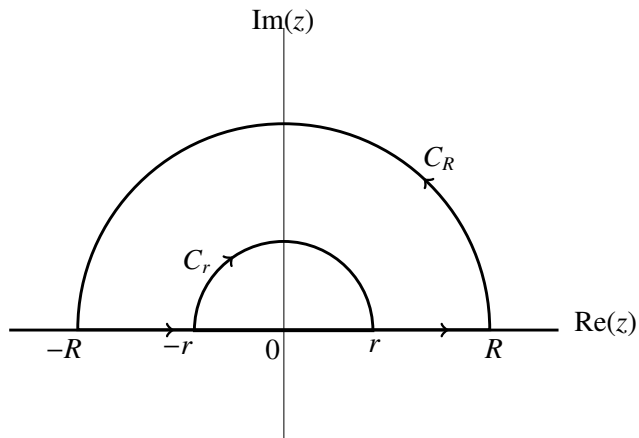


Fig. 8

**Problem 9.** Using a suitable contour, evaluate  $F(t)$ ,  $t > 0$ .