# Digital Logic Design

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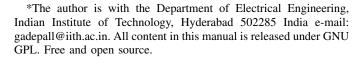
Abstract—This manual provides a simple introduction to Digital Design.

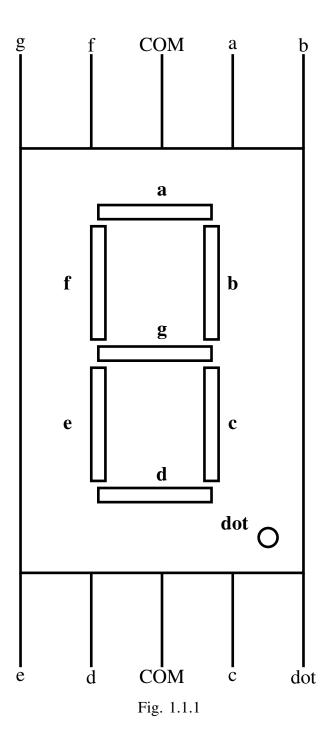
#### 1 SEVEN SEGMENT DISPLAY

- 1.1. Fig. 1.1.1 shows a seven segment display with pins a, b, c, d, e, f, g. Each of these pins is connected to an LED (light emitting device).
- 1.2. Fig. 1.2.1 shows how to generate the numbers on the display using Table 1.2.1. Complete Table 1.2.1 by drawing the figures for all numbers from 0-9.

a	b	c	d	e	f	g	decimal
1	0	0	1	1	1	1	1
0	0	1	0	0	1	0	2

**TABLE 1.2.1** 





#### 2 Incrementing Decoder

2.1. The incrementing decoder takes the numbers  $0, 1, \ldots, 9$  in binary as inputs and generates the

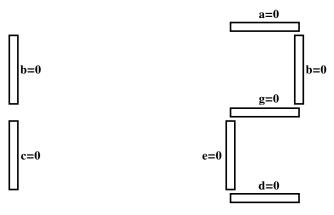


Fig. 1.2.1

consecutive number as output. The corresponding truth table is available in Table. 2.1.1.

Z	Y	X	W	D	C	В	A
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0

TABLE 2.1.1: Truth table for the incrementing decoder

2.2. Using Boolean logic, outputs A, B, C and D in Table 2.1.1 can be expressed in terms of the inputs W, X, Y, Z as

$$A = W'X'Y'Z' + W'XY'Z' + W'X'YZ' + W'XYZ' + W'XYZ' + W'X'Y'Z$$
 (2.2.1) <sup>4</sup>

$$B = WX'Y'Z' + W'XY'Z' + WX'YZ' + WX'YZ' + W'XYZ'$$
 (2.2.2)

$$C = WXY'Z' + W'X'YZ'$$

$$D = WXYZ' + W'X'Y'Z \tag{2.2.4}$$

(2.2.3)

2.3. Execute the following code for different input values to verify (2.2.1)-(2.2.4).

+WX'YZ'+W'XYZ'

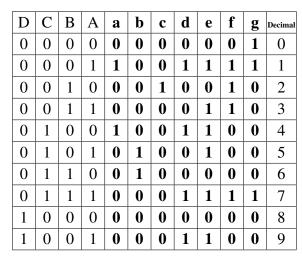


TABLE 3.1.1: Truth table for display decoder.

#### 3 DISPLAY DECODER

3.1. Using Boolean logic, outputs a, b, c, d, e, f, g in Table 3.1.1 can be expressed in terms of the inputs A, B, C, D as

$$a = (3.1.1)$$

$$b = AB'CD' + A'BCD' \tag{3.1.2}$$

$$c = (3.1.3)$$

$$d = (3.1.4)$$

$$e = (3.1.5)$$

$$f = (3.1.6)$$

$$g = (3.1.7)$$

3.2. Execute the following code for different input values to verify (3.1.1)-(3.1.7).

#### 4 KARNAUGH MAP

4.1 Incrementing Decoder

(2.2.1) 4.1.1. K-Map for A: The expression in (2.2.1) can be minimized using the K-map in Fig. 4.1.1.1. In Fig. 4.1.1.1, the *implicants* in boxes 0,2,4,6 result in W'Z'. The implicants in boxes 0,8 result in W'X'Y'. Thus, after minimization using Fig. 4.1.1.1, (2.2.1) can be expressed as

$$A = W'Z' + W'X'Y' \tag{4.1.1.1}$$

Using the fact that

$$X + X' = 1 XX' = 0, (4.1.1.2)$$

derive (4.1.1.1) from (2.2.1) algebraically.

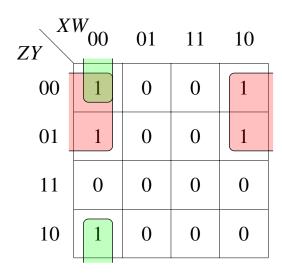


Fig. 4.1.1.1: K-map for *A*.

4.1.2. K-Map for *B*: From Table 2.1.1, using boolean logic, Show that (2.2.2) can be reduced to

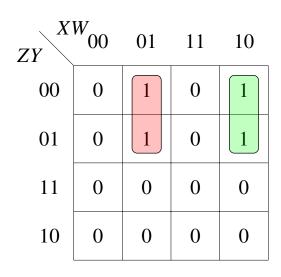


Fig. 4.1.2.1: K-map for *B*.

$$B = WX'Z' + W'XZ' (4.1.2.1)$$

using Fig. 4.1.2.1.

- 4.1.3. Derive (4.1.2.1) from (2.2.2) algebraically using (4.1.1.2).
- 4.1.4. K-Map for *C*: From Table 2.1.1, using boolean logic, Show that (2.2.3) can be reduced to

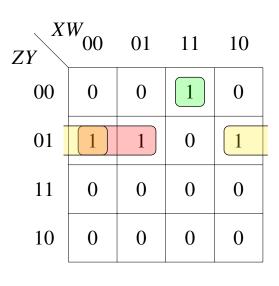


Fig. 4.1.4.1: K-map for *C*.

$$C = WXY'Z' + X'YZ' + W'YZ'$$
 (4.1.4.1)

using Fig. 4.1.4.1.

- 4.1.5. Derive (4.1.4.1) from (2.2.3) algebraically using (4.1.1.2).
- 4.1.6. K-Map for *D*: From Table 2.1.1, using boolean logic,

$$D = WXYZ' + W'X'Y'Z (4.1.6.1)$$

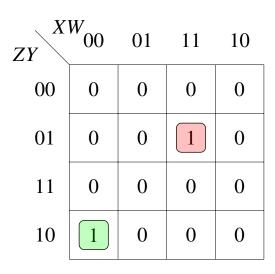


Fig. 4.1.6.1: K-map for *D*.

4.1.7. Minimize (4.1.6.1) using Fig. 4.1.6.1.

- 4.1.8. Modify your C program to verify the K-Map equations for A,B,C and D in (4.1.1.1), (4.1.1.1) and (4.1.1.1) respectively.
- 4.1.9. Revise by using don't care conditions and verify through a C code.

### 4.2 Display Decoder

Use K-maps to obtain the minimized expressions for a, b, c, d, e, f, g in terms of A, B, C, D in Table 3.1.1 without don't care conditions.

4.2.1. Obtain the expression for *b* using Fig. 4.2.1.1 **Solution:** 

$$b = AB'CD' + A'BCD' \tag{4.2.1.1}$$

$$= CD'(AB' \oplus A'B) \tag{4.2.1.2}$$

where  $\oplus$  denotes the XOR operation.

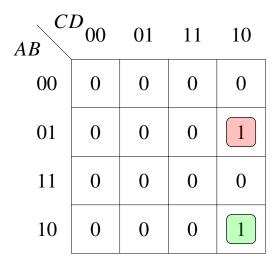


Fig. 4.2.1.1: K-map for *b*.

4.2.2. Obtain the expression for *d* using Fig. 4.2.2.1 **Solution:** 

$$d = AB'C' + A'B'CD' + ABCD'$$
 (4.2.2.1)

where  $\oplus$  denotes the XOR operation.

4.2.3. Obtain the expression for e using Fig. 4.2.3.1

- 5.1 Incrementing Decoder
- 5.1.1. Obtain the expression for B using Fig. 5.1.1.1

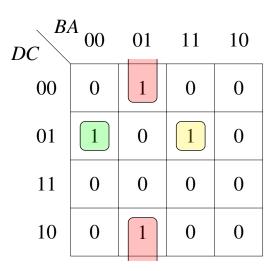


Fig. 4.2.2.1: K-map for *d*.

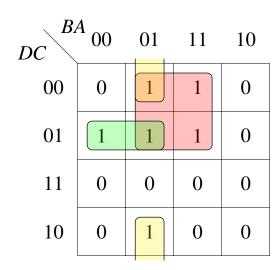


Fig. 4.2.3.1: K-map for *e*.

#### **Solution:**

$$B = W'X + WX'Z' (5.1.1.1)$$

where  $\oplus$  denotes the XOR operation.

5.1.2. Obtain the expression for C using Fig. 5.1.2.1

$$C = Y'X + W'XZ' + YX'$$
 (5.1.2.1)

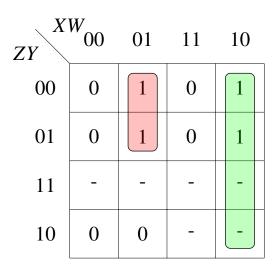


Fig. 5.1.1.1: K-map for *B*.

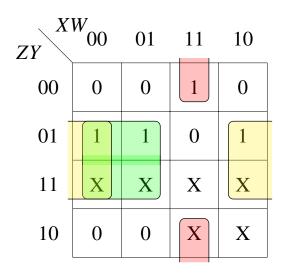


Fig. 5.1.2.1: K-map for *C*.

## 1 ig. 3.1.2.1. K-map ic

## 5.2 Display Decoder

5.2.1. Obtain the expression for *b* using Fig. 5.2.1.1 **Solution:** 

$$b = B' + CD + C'D'$$
 (5.2.1.1)

6 Programming

7 Logic Gates

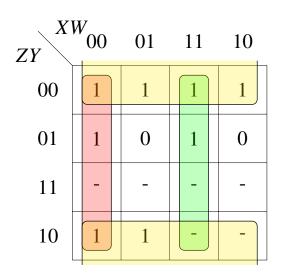


Fig. 5.2.1.1: K-map for b using don't care.