GATE 2011 MA

AI25BTECH11012 - UNNATHI GARIGE

Q. 1 – Q. 25 carry one mark each.

1) The distinct eigenvalues of the matrix

$$\begin{pmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

are GATE MA 2011

a) 0 and 1 b) 1 and -1 c) 1 and 2 d) 0 and 2

2) The minimal polynomial of the matrix

$$\begin{pmatrix} 3 & 3 & 0 \\ 3 & 3 & 0 \\ 0 & 0 & 6 \end{pmatrix}$$

is GATE MA 2011

a) $x(x-1)(x-6)$ b) $x(x-3)$ c) $(x-3)(x-6)$ d) $x(x-6)$

3) Which of the following is the imaginary part of a possible value of $\ln(\sqrt{i})$? GATE MA 2011

a) π b) $\frac{\pi}{2}$ c) $\frac{\pi}{4}$ d) $\frac{\pi}{8}$

4) Let $f : \mathbb{C} \to \mathbb{C}$ be analytic except for a simple pole at $z = 0$ and let $g : \mathbb{C} \to \mathbb{C}$ be analytic. Then,

$$\frac{\text{Res}z = 0\, f(z)g(z)}{\text{Res}z = 0\, f(z)}$$

is GATE MA 2011

a) $g(0)$ b) $g'(0)$ c) $\lim_{z\to 0} zf(z)$ d) $\lim_{z\to 0} zf(z)g(z)$

5) Let $I = \oint_C (2x^2 + y^2)\,dx + e^y\,dy$, where C is the boundary (oriented anticlockwise) of the region in the first quadrant bounded by $y = 0$, $x^2 + y^2 = 1$ and $x = 0$. The value of I is GATE MA 2011

a) -1 b) $\frac{2}{3}$ c) $\frac{2}{3}$ d) 1

6) The series $\sum_{m=1}^{\infty} \frac{\ln^m x}{m!}$, $x > 0$, is convergent on the interval GATE MA 2011

a) $(0, 1/e)$ b) $(1/e, e)$ c) $(0, e)$ d) $(1, e)$

7) While solving the equation $x^2 - 3x + 1 = 0$ using the Newton–Raphson method with the initial guess of a root as 1, the value of the root after one iteration is GATE MA 2011

a) 1.5 b) 1 c) 0.5 d) 0

8) Consider the system of equations

$$\begin{pmatrix} 5 & 2 & 1 \\ -2 & 5 & 2 \\ -1 & 2 & 8 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} 13 \\ -22 \\ 14 \end{pmatrix}$$

With the initial guess of the solution $(x_1, x_2, x_3)^T = (1, 1, 1)^T$, the approximate value of the solution $(x_1, x_2, x_3)^T$ after one iteration by the Gauss Seidel method is
GATE MA 2011

a) $[2, -4.4, 1.625]^T$
b) $[2, -4, -3]^T$
c) $[2, 4.4, 1.625]^T$
d) $[2, -4, 3]^T$

9) Let y be the solution of the initial value problem

$$\frac{dy}{dx} = y^2 + x, \quad y(0) = 1.$$

Using Taylor series method of order 2 with the step size $h = 0.1$, the approximate value of $y(0.1)$ is GATE MA 2011

a) 1.315 b) 1.415 c) 1.115 d) 1.215

10) The partial differential equation

$$x^2 \frac{\partial^2 z}{\partial x^2} + (y^2 - 1) \frac{\partial^2 z}{\partial x \partial y} + (y^2 - 1) \frac{\partial^2 z}{\partial y^2} + \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 0$$

is hyperbolic in a region in the XY plane if GATE MA 2011

a) $x \neq 0$ and $y = 1$ b) $x \neq 0$ and $y \neq 1$ c) $x = 0$ and $y \neq 1$ d) $x = 0$ and $y = 1$

11) Which of the following functions is a probability density function of a random variable X? GATE MA 2011

a) $f(x) = \begin{cases} x(2-x), & 0 < x < 2 \\ 0, & \text{elsewhere} \end{cases}$

b) $f(x) = \begin{cases} x(1-x), & 0 < x < 1 \\ 0, & \text{elsewhere} \end{cases}$

c) $f(x) = \begin{cases} 2xe^{-x^2}, & -1 < x < 1 \\ 0, & \text{elsewhere} \end{cases}$

d) $f(x) = \begin{cases} 2xe^{-x}, & x > 0 \\ 0, & \text{elsewhere} \end{cases}$

12) Let X_1, X_2, X_3, X_4 be independent standard normal random variables. The distribution of

$$W = \frac{1}{2}\left((X_1 - X_2)^2 + (X_3 - X_4)^2\right)$$

is GATE MA 2011

a) $N(0,1)$ b) $N(0,2)$ c) χ_2^2 d) χ_4^2

13) For $n \geq 1$, let $\{X_n\}$ be a sequence of independent random variables with

$$P(X_n = n) = P(X_n = -n) = \frac{1}{2}$$

Then, which of the following statements is **TRUE** for the sequence $\{X_n\}$? GATE MA 2011

a) Weak Law of Large Numbers holds but Strong Law of Large Numbers does not hold
b) Weak Law of Large Numbers does not hold but Strong Law of Large Numbers holds
c) Both Weak Law of Large Numbers and Strong Law of Large Numbers hold
d) Both Weak Law of Large Numbers and Strong Law of Large Numbers do not hold

14) The Linear Programming Problem:
Maximize $z = x_1 + x_2$ subject to

$$\begin{aligned} x_1 + 2x_2 &\leq 20, \\ x_1 + x_2 &\leq 15, \\ x_2 &\leq 6, \\ x_1, x_2 &\geq 0 \end{aligned}$$

GATE MA 2011

a) has exactly one optimum solution
b) has more than one optimum solutions
c) has unbounded solution
d) has no solution

15) Consider the Primal Linear Programming Problem:
Maximize $z = c_1x_1 + c_2x_2 + \cdots + c_nx_n$
subject to GATE MA 2011

$$\text{P:} \quad \begin{cases} a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n \leq b_1, \\ a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n \leq b_2, \\ \quad \vdots \\ a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n \leq b_m, \\ x_j \geq 0, \quad j = 1, \ldots, n \end{cases}$$

The Dual of P is
Minimize $\quad z' = b_1w_1 + b_2w_2 + \cdots + b_mw_m$
subject to

$$\text{D:} \quad \begin{cases} a_{11}w_1 + a_{21}w_2 + \cdots + a_{m1}w_m \geq c_1, \\ a_{12}w_1 + a_{22}w_2 + \cdots + a_{m2}w_m \geq c_2, \\ \quad \vdots \\ a_{1n}w_1 + a_{2n}w_2 + \cdots + a_{mn}w_m \geq c_n, \\ w_i \geq 0, \quad i = 1, \ldots, m \end{cases}$$

Which of the following statements is **FALSE**?

a) If P has an optimal solution, then D also has an optimal solution
b) The dual of the dual problem is a primal problem
c) If P has an unbounded solution, then D has no feasible solution
d) If P has no feasible solution, then D has a feasible solution

16) The number of irreducible quadratic polynomials over the field of two elements F_2 is GATE MA 2011

a) 0 b) 1 c) 2 d) 3

17) The number of elements in the conjugacy class of the 3-cycle (2 3 4) in the symmetric group S_6 is GATE MA 2011

a) 20 b) 40 c) 120 d) 216

18) The initial value problem

$$x\frac{dy}{dx} = y + x^2, \quad x > 0; \quad y(0) = 0,$$

has GATE MA 2011

a) infinitely many solutions
b) exactly two solutions
c) a unique solution
d) no solution

19) The subspace $P = \{(x, y, z) \in \mathbb{R}^3 : z = x^2 + y^2 + 1\}$ is GATE MA 2011

a) compact and connected
b) compact but not connected
c) not compact but connected
d) neither compact nor connected

20) Let
$P = (0, 1); Q = [0, 1]; U = (0, 1]; S = [0, 1]; T = \mathbb{R}$ and $A = \{P, Q, U, S, T\}$
The equivalence relation 'homeomorphism' induces which one of the following as the partition of A? GATE MA 2011

a) $\{P, Q, U, S\}, \{T\}$
b) $\{P, T\}, \{Q\}, \{U\}, \{S\}$
c) $\{P, T\}, \{Q, U, S\}$
d) $\{P, T\}, \{Q, U\}, \{S\}$

21) Let $x = (x_1, x_2, \dots) \in l^p, x \neq 0$. For which one of the following values of p, the series $\sum_{i=1}^{\infty} x_i y_i$ converges for every $y = (y_1, y_2, \dots) \in l^{p'}$? GATE MA 2011

a) 1
b) 2
c) 3
d) 4

22) Let H be a complex Hilbert space and H' be its dual. The mapping $\phi : H \to H'$ defined by $\phi(y) = f_y$ where $f_y(x) = \langle x, y \rangle$ is GATE MA 2011

a) not linear but onto
b) both linear and onto
c) linear but not onto
d) neither linear nor onto

23) A horizontal lever is in static equilibrium under the application of vertical forces F_1 at a distance l_1 from the fulcrum and F_2 at a distance l_2 from the fulcrum. The equilibrium for the above quantities can be obtained if GATE MA 2011

a) $F_1 l_1 = 2F_2 l_2$
b) $2F_1 l_1 = F_2 l_2$
c) $F_1 l_1 = F_2 l_2$
d) $F_1 l_1 < F_2 l_2$

24) Assume F to be a twice continuously differentiable function.
Let $J(y)$ be a functional of the form GATE MA 2011

$$J(y) = \int_0^1 F(x, y') dx, \quad 0 \leq x \leq 1$$

defined on the set of all continuously differentiable functions y on $[0, 1]$ satisfying $y(0) = a$, $y(1) = b$. For some arbitrary constant c, a necessary condition for y to be an extremum of J is

a) $\frac{\partial F}{\partial x} = c$
b) $\frac{\partial F}{\partial y'} = c$
c) $\frac{\partial F}{\partial y} = c$
d) $\frac{\partial F}{\partial x} = 0$

25) The eigenvalue λ of the following Fredholm integral equation

$$y(x) = \lambda \int_0^1 x^2 t\, y(t)\, dt$$

is GATE MA 2011

a) -2
b) 2
c) 4
d) -4

26) The application of Gram Schmidt process of orthonormalization to

$$u_1 = (1, 1, 0), \quad u_2 = (1, 0, 0), \quad u_3 = (1, 1, 1)$$

yields GATE MA 2011

a) $\frac{1}{\sqrt{2}}(1,1,0),\ (1,0,0),\ (0,0,1)$
b) $\frac{1}{\sqrt{2}}(1,1,0),\ \frac{1}{\sqrt{2}}(1,-1,0),\ \frac{1}{\sqrt{2}}(1,1,1)$
c) $\frac{1}{\sqrt{2}}(1,1,0),\ \frac{1}{\sqrt{2}}(1,-1,0),\ (0,0,1)$
d) $(0,1,0),\ (1,0,0),\ (0,0,1)$

27) Let $T:\mathbb{C}^3 \to \mathbb{C}^3$ be defined by

$$T\begin{pmatrix} z_1 \\ z_2 \\ z_3 \end{pmatrix} = \begin{pmatrix} z_1 + iz_2 \\ iz_1 + z_2 \\ z_1 + z_2 + iz_3 \end{pmatrix}.$$

Then, the adjoint T^* of T is given by GATE MA 2011

$$T\begin{pmatrix} z_1 \\ z_2 \\ z_3 \end{pmatrix}$$

a) $\begin{pmatrix} z_1 + iz_2 \\ -iz_1 + z_2 \\ z_1 + z_2 - iz_3 \end{pmatrix}$
b) $\begin{pmatrix} z_1 - iz_2 + z_3 \\ iz_1 + z_2 + z_3 \\ iz_3 \end{pmatrix}$
c) $\begin{pmatrix} z_1 - iz_2 + z_3 \\ iz_1 + z_2 + z_3 \\ -iz_3 \end{pmatrix}$
d) $\begin{pmatrix} iz_1 + z_2 \\ z_1 - iz_2 \\ z_1 - iz_2 - iz_3 \end{pmatrix}$

28) Let $f(z)$ be an entire function such that $|f(z)| \le K|z|,\ \forall z \in \mathbb{C}$, for some $K > 0$. If $f(i) = i$, the value of $f'(i)$ is GATE MA 2011

a) 1
b) -1
c) i
d) $-i$

29) Let y be the solution of the initial value problem GATE MA 2011

$$\frac{d^2y}{dx^2} + y = 6\cos 2x, \quad y(0) = 3, \quad y'(0) = 1.$$

Let the Laplace transform of y be $F(s)$. Then, the value of $F(1)$ is

a) $\frac{17}{5}$
b) $\frac{13}{5}$
c) $\frac{11}{5}$
d) $\frac{9}{5}$

30) For $0 \le x \le 1$, let GATE MA 2011

$$f_n(x) = \begin{cases} \frac{n}{1+n}, & \text{if } x \text{ is irrational,} \\ 0, & \text{if } x \text{ is rational.} \end{cases}$$

and $f(x) = \lim_{n\to\infty} f_n(x)$. Then, on the interval $[0,1]$,

a) f is measurable and Riemann integrable
b) f is measurable and Lebesgue integrable
c) f is not measurable
d) f is not Lebesgue integrable

31) If x, y, and z are positive real numbers, then the minimum value of GATE MA 2011

$$x^2 + 8y^2 + 27z^2$$

a) 108 b) 216 c) 405 d) 1048

32) Let $T : \mathbb{R}^4 \to \mathbb{R}^4$ be defined by

$$T(x, y, z, w) = (x + y + 5w, x + 2y + w, -z + 2w, 5x + y + 2z).$$

The dimension of the eigenspace of T is GATE MA 2011

a) 1 b) 2 c) 3 d) 4

33) Let y be a polynomial solution of the differential equation

$$(1 - x^2)y'' - 2xy' + 6y = 0.$$

If $y(1) = 2$, then the value of the integral $\int_{-1}^{1} y^2\, dx$ is GATE MA 2011

a) $\frac{1}{5}$ b) $\frac{2}{5}$ c) $\frac{4}{5}$ d) $\frac{8}{5}$

34) The value of the integral

$$I = \int_{1}^{2} \exp(x^2) dx$$

using a rectangular rule is approximated as 2. Then, the approximation error $|I - 2|$ lies in the interval GATE MA 2011

a) $(2e, 3e]$ b) $(2/3, 2e]$ c) $(e/8, 2/3]$ d) $(0, e/8]$

35) The integral surface for the Cauchy problem

$$\frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} = 1,$$

which passes through the circle $z = 0$, $x^2 + y^2 = 1$ is GATE MA 2011

a) $x^2 + y^2 + 2z^2 + 2zx - 2yz - 1 = 0$
b) $x^2 + y^2 + 2z^2 + 2zx + 2yz - 1 = 0$
c) $x^2 + y^2 + 2z^2 - 2zx - 2yz - 1 = 0$
d) $x^2 + y^2 + 2z^2 + 2z + 2yz + 1 = 0$

36) The vertical displacement u(x, t) of an infinitely long elastic string is governed by the ini

$$\frac{\partial^2 u}{\partial t^2} = 4\frac{\partial^2 u}{\partial x^2}, \quad -\infty < x < \infty,\ t > 0,$$

$$u(x, 0) = -x \quad \text{and} \quad \frac{\partial u}{\partial t}(x, 0) = 0.$$

The value of u(x, t) at x=2 and t=2 is equal to GATE MA 2011

a) 2 b) 4 c) -2 d) -4

37) We have to assign four jobs I, II, III, IV to four workers A, B, C, and D. The time taken by different workers (in hours) in completing different jobs is given below:

	I	II	III	IV
A	5	3	2	8
B	7	9	2	6
C	8	5	1	7
D	5	7	7	8

The optimal assignment is as follows:
Job III to worker A; Job IV to worker B; Job II to worker C; Job I to worker D and hence the time taken by different workers in completing different jobs is now changed as:

	I	II	III	IV
A	7	9	2	5
B	8	7	9	2
C	4	2	7	5
D	5	7	7	5

Then the minimum time (in hours) taken by the workers to complete all the jobs is GATE MA 2011

a) 10 b) 12 c) 15 d) 17

38) The following table shows the information on the availability of supply to each warehouse, the requirement of each market and unit transportation cost (in rupees) from each warehouse to each market.

	M_1	M_2	M_3	M_4	Supply
W_1	6	3	5	4	22
W_2	5	9	8	7	15
W_3	7	5	9	8	8
Requirement	7	12	17	9	

The present transportation schedule is as follows:
W_1 to M_2: 12 units; W_1 to M_1: 1 unit; W_1 to M_4: 9 units; W_2 to M_3: 15 units; W_3 to M_1: 7 units and W_3 to M_3: 1 unit. Then the minimum total transportation cost (in rupees) is GATE MA 2011

a) 150 b) 149 c) 148 d) 147

39) If $\mathbb{Z}[i]$ is the ring of Gaussian integers, the quotient $\mathbb{Z}[i]/(3 - i)$ is isomorphic to GATE MA 2011

a) Z b) Z/3Z c) Z/4Z d) Z/10Z

40) For the rings

$$L = \frac{\mathbb{R}[x]}{(x^2 - x + 1)}, \quad M = \frac{\mathbb{R}[x]}{(x^2 + x + 1)}, \quad N = \frac{\mathbb{R}[x]}{(x^2 + 2x + 1)}$$

which one of the following is **TRUE**? GATE MA 2011

a) L is isomorphic to M; L is not isomorphic to N; M is not isomorphic to N
b) M is isomorphic to N; M is not isomorphic to L; N is not isomorphic to L
c) L is isomorphic to M; M is isomorphic to N
d) L is not isomorphic to M; L is not isomorphic to

41) The time to failure (in hours) of a component is a continuous random variable T with the probability density function

$$f(t) = \begin{cases} \frac{1}{10}e^{-t/10}, & t > 0, \\ 0, & t \le 0 \end{cases}$$

Ten of these components are installed in a system and they work independently. Then, the probability that NONE of these fail before ten hours, is GATE MA 2011

a) e^{-10} b) $1 - e^{-10}$ c) $10e^{-10}$ d) $1 - 10e^{-10}$

42) Let X be the real normed linear space of all real sequences with finitely many non-zero terms, with supremum norm and $T : X \to X$ be a one to one and onto linear operator defined by

$$T(x_1, x_2, x_3, \ldots) = (x_1, \frac{x_2}{2}, \frac{x_3}{3}, \ldots).$$

Then, which of the following is **TRUE**? GATE MA 2011

a) T is bounded but T^{-1} is not bounded
b) T is not bounded but T^{-1} is bounded
c) Both T and T^{-1} are bounded
d) Neither T nor T^{-1} is bounded

43) Let $e_i = (0, \ldots, 0, 1, 0, \ldots)$ (i.e., e_i is the vector with 1 at the i^{th} place and 0 elsewhere) for $i = 1, 2, \ldots$.
Consider the statements:
P: $\{f(e_i)\}$ converges for every continuous linear functional on l^2.
Q: $\{e_i\}$ converges in l^2.
Then, which of the following holds? GATE MA 2011

a) Both P and Q are TRUE
b) P is TRUE but Q is not TRUE
c) P is not TRUE but Q is TRUE
d) Neither P nor Q is TRUE

44) For which subspace $X \subseteq \mathbb{R}$ with the usual topology and with $\{0, 1\} \subseteq X$, will a continuous function $f : X \to \{0, 1\}$ satisfying $f(0) = 0$ and $f(1) = 1$ exist? GATE MA 2011

a) $X = [0, 1]$
b) $X = [-1, 1]$
c) $X = \mathbb{R}$
d) $[0, 1] \subset X$

45) Suppose X is a finite set with more than five elements. Which of the following is **TRUE**? GATE MA 2011
   a) There is a topology on X which is T_3
   b) There is a topology on X which is T_2 but not T_3
   c) There is a topology on X which is T_1 but not T_2
   d) There is no topology on X which is T_1
46) A massless wire is bent in the form of a parabola $z = r^2$ and a bead slides on it smoothly. The wire is rotated about z-axis with a constant angular acceleration α. Assume that m is the mass of the bead, ω is the initial angular velocity and g is the acceleration due to gravity. Then, the Lagrangian at any time t is GATE MA 2011
   a) $\frac{m}{2}\left(\frac{dr}{dt}\right)^2\left[(1+4r^2)+r^2(\omega+\alpha t)^2+2gr^2\right]$
   b) $\frac{m}{2}\left(\frac{dr}{dt}\right)^2\left[(1+4r^2)-r^2(\omega+\alpha t)^2+2gr^2\right]$
   c) $\frac{m}{2}\left(\frac{dr}{dt}\right)^2\left[(1+4r^2)-r^2(\omega+\alpha t)^2-2gr^2\right]$
   d) $\frac{m}{2}\left(\frac{dr}{dt}\right)^2\left[(1+4r^2)+r^2(\omega+\alpha t)^2-2gr^2\right]$
47) On the interval $[0, 1]$, let y be a twice continuously differentiable function which is an extremal of the functional

$$J(y) = \int_0^1 \frac{\sqrt{1+2y'^2}}{x}\,dx$$

with $y(0) = 1, y(1) = 2$. Then, for some arbitrary constant c, y satisfies GATE MA 2011

a) $y'^2(2 - c^2x^2) = c^2x^2$
b) $y'^2(2 + c^2x^2) = c^2x^2$
c) $y'^2(1 - c^2x^2) = c^2x^2$
d) $y'^2(1 + c^2x^2) = c^2x^2$

Common Data Questions

Common Data for Questions 48 and 49:

Let X and Y be two continuous random variables with the joint probability density function

$$f(x,y) = \begin{cases} 2, & 0 < x+y < 1,\ x > 0,\ y > 0, \\ 0, & \text{elsewhere.} \end{cases}$$

48) $P\left(X + Y < \frac{1}{2}\right)$ is GATE MA 2011

a) $\frac{1}{4}$
b) $\frac{1}{2}$
c) $\frac{3}{4}$
d) 1

49) $E\left(X \mid Y = \frac{1}{2}\right)$ is GATE MA 2011

a) $\frac{1}{4}$ b) $\frac{1}{2}$ c) 1 d) 2

Common Data for Questions 50 and 51:
Let

$$f(z) = \frac{z}{8 - z^3}, \qquad z = x + iy.$$

50)

$$\mathrm{Res}_{z=2}\, f(z)$$

is GATE MA 2011

a) $-\frac{1}{8}$ b) $\frac{1}{8}$ c) $-\frac{1}{6}$ d) $\frac{1}{6}$

51) The Cauchy principal value of $\int_{-\infty}^{\infty} f(x)dx$ is GATE MA 2011

a) $-\frac{\pi}{6}\sqrt{3}$ b) $-\frac{\pi}{8}\sqrt{3}$ c) $\pi\sqrt{3}$ d) $-\pi\sqrt{3}$

Linked Answer Questions

Statement for Linked Answer Questions 52 and 53:
Let

$$f_n(x) = \frac{x}{\{(n-1)x+1\}\{nx+1\}}$$

and

$$s_n(x) = \sum_{j=1}^{n} f_j(x) \quad \text{for } x \in [0,1].$$

52) The sequence $\{s_n\}$ GATE MA 2011

a) converges uniformly on $[0,1]$
b) converges pointwise on $[0,1]$ but not uniformly
c) converges pointwise for $x = 0$ but not for $x \in (0,1]$
d) does not converge for $x \in [0,1]$

53)

$$\lim_{n\to\infty} \int_0^1 s_n(x)dx = 1$$

a) by dominated convergence theorem
b) by Fatous lemma
c) by the fact that $\{s_n\}$ converges uniformly on $[0,1]$
d) by the fact that $\{s_n\}$ converges pointwise on $[0,1]$ GATE MA 2011

Statement for Linked Answer Questions 54 and 55:
The matrix

$$A = \begin{pmatrix} 1 & 1 & 1 \\ 2 & 1 & 2 \\ 1 & 3 & 2 \end{pmatrix}$$

can be decomposed into the product of a lower triangular matrix L and an upper triangular matrix U as $A = LU$ where

$$L = \begin{pmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{pmatrix} \quad \text{and} \quad U = \begin{pmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{pmatrix}$$

Let $x, z \in \mathbb{R}^3$ and $b = [1, 1, 1]^T$.

54) The solution $z = [z_1, z_2, z_3]^T$ of the system $Lz = b$ is GATE MA 2011

a) $[-1, -1, -2]^T$ b) $[1, -1, 2]^T$ c) $[1, -1, -2]^T$ d) $[-1, 1, 2]^T$

55) The solution $x = [x_1, x_2, x_3]^T$ of the system $Ux = z$ is GATE MA 2011

a) $[2, 1, -2]^T$ b) $[2, 1, 2]^T$ c) $[-2, -1, -2]^T$ d) $[-2, 1, -2]^T$

General Aptitude (GA) Questions
Q.56 – Q.60 carry one mark each.

56) Choose the most appropriate word from the options given below to complete the following sentence:
It was her view that the country's problems had been ___________ by foreign technocrats, so that to invite them to come back would be counter-productive.
GATE MA 2011

a) identified
b) ascertained
c) exacerbated
d) analysed

57) There are two candidates P and Q in an election. During the campaign, 40% of the voters promised to vote for P, and rest for Q. However, on the day of election 15% of the voters went back on their promise to vote for P and instead voted for Q. 25% of the voters went back on their promise to vote for Q and instead voted for P.
Suppose, P lost by 2 votes, then what was the total number of voters?
GATE MA 2011

a) 100 b) 110 c) 90 d) 95

58) The question below consists of a pair of related words followed by four pairs of words. Select the pair that best expresses the relation in the original pair:
Gladiator : Arena

GATE MA 2011

a) dancer : stage

b) commuter : train
c) teacher : classroom
d) lawyer : courtroom

59) Choose the most appropriate word from the options given below to complete the following sentence:
Under ethical guidelines recently adopted by the Indian Medical Association, human genes are to be manipulated only to correct diseases for which ___________ treatments are unsatisfactory.

a) similar GATE MA 2011
b) most
c) uncommon
d) available

60) Choose the word from the options given below that is most nearly opposite in meaning to the given word:
Frequency GATE MA 2011

a) periodicity
b) rarity
c) gradualness
d) persistency

Q.61 to Q.65 carry two marks each.

61) Three friends, R, S and T shared toffee from a bowl. R took $\frac{1}{3}$ of the toffees, but returned four to the bowl. S took $\frac{1}{4}$ of what was left but returned three toffees to the bowl. T took half of the remainder but returned two back into the bowl. If the bowl had 17 toffees left, how many toffees were originally there in the bowl? GATE MA 2011

a) 38 b) 31 c) 48 d) 41

62) The fuel consumed by a motorcycle during a journey while traveling at various speeds is indicated in the graph below. GATE MA 2011
The distances covered during four laps of the journey are listed in the table below:

Lap	Distance (kilometres)	Average speed (kilometres per hour)
P	15	15
Q	75	45
R	40	75
S	10	10

From the given data, we can conclude that the fuel consumed per kilometre was **least** during the lap

a) P b) Q c) R d) S

63) **The horse has played a little known but very important role in the field of medicine. Horses were injected with toxins of diseases until their blood built**

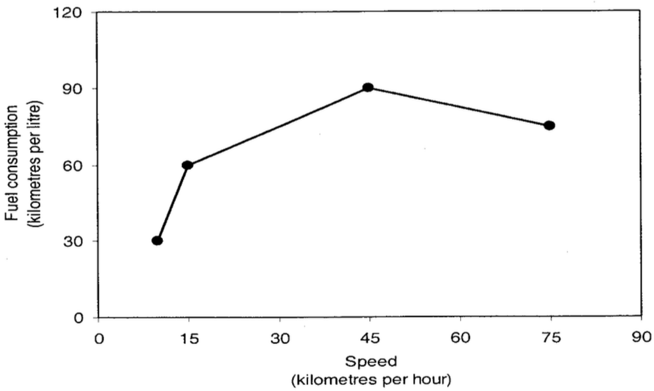

Fig. 62.1

up immunities. Then a serum was made from their blood. Serums to fight with diphtheria and tetanus were developed this way.

It can be inferred from the passage, that horses were GATE MA 2011

a) given immunity to diseases
b) generally quite immune to diseases
c) given medicines to fight toxins
d) given diphtheria and tetanus serums

64) The sum of n terms of the s GATE MA 2011

a) $(4/81)[10^{n+1} - 9n - 1]$
b) $(4/81)[10^{n+1} - 9n - 1]$
c) $(4/81)[10^{n+1} - 9n - 10]$
d) $(4/81)[10^{n} - 9n - 10]$

65) Given that $f(y) = |y|/y$, and q is any non-zero real number, the value of $|f(q) - f(-q)|$ is GATE MA 2011

a) 0 b) -1 c) 1 d) 2

END OF THE QUESTION PAPER