#### 1

# Assignment 1: GATE 2010 PH: Physics

# EE25BTECH11055 - Subhodeep Chakraborty

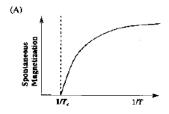
1) Consider an anti-symmetric tensor $P_U$ with the indices i and j running from 1 to 5. The number of independent components of the tensor is (GATE PH 2010)					
a) 3	b) 10	c) 9	d) 6		
2) The value of the inte	egral $\oint_C \frac{e^z \sin(z)}{z^2} dz$ where the c	ontour C is the unit circle	z-2  = 1, is(GATE PH 2010)		
a) $2\pi i$	b) $4\pi i$	c) πi	d) 0		
3) The eigenvalues of	the matrix $ \begin{pmatrix} 2 & 3 & 0 \\ 3 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} $ are		(GATE PH 2010)		
a) 5, 2, -2	b) -5, -1, -1	c) 5, 1, -1	d) -5, 1, 1		
4) If $f(x) = \begin{cases} 0 & \text{for } x = 0 \\ x - 3 & \text{for } x = 0 \end{cases}$	or $x < 3$ , then the Laplace or $x \ge 3$ ,	transform of $f(x)$ is	(GATE PH 2010)		
a) $s^{-2}e^{3s}$	b) $s^2e^{-3s}$	c) $s^{-2}$	d) $s^{-2}e^{-3s}$		
5) The valence electro	ns do not directly determin	ne the following property	of a metal.(GATE PH 2010)		
<ul><li>a) Electrical conduct</li><li>b) Thermal conduct</li></ul>	•	<ul><li>c) Shear modulus</li><li>d) Metallic lustre</li></ul>			
6) Consider X-ray diffraction from a crystal with a face-centered-cubic (fcc) lattice. The lattice plane for which there is NO diffraction peak is (GATE PH 2010)					
a) (2, 1, 2)	b) (1, 1, 1)	c) (2, 0, 0)	d) (3, 1, 1)		
<ul> <li>7) The Hall coefficient, R<sub>H</sub>, of sodium depends on</li> <li>a) The effective charge carrier mass and carrier density</li> <li>b) The charge carrier density and relaxation time</li> <li>c) The charge carrier density only</li> <li>d) The effective charge carrier mass</li> <li>8) The Bloch theorem states that within a crystal, the wavefunction, ψ(<b>r</b>), of an electron has the form</li> </ul>					
(GATE PH 2010) a) $\psi(\mathbf{r}) = u(\mathbf{r})e^{i\mathbf{k}\cdot\mathbf{r}}$ where $u(\mathbf{r})$ is an arbitrary function and $\mathbf{k}$ is an arbitrary vector					

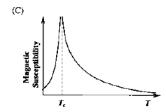
b)  $\psi(\mathbf{r}) = u(\mathbf{r})e^{i\mathbf{G}\cdot\mathbf{r}}$  where  $u(\mathbf{r})$  is an arbitrary function and **G** is a reciprocal lattice vector

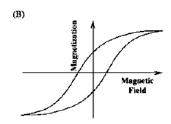
d)  $\psi(\mathbf{r}) = u(\mathbf{r})e^{i\mathbf{k}\cdot\mathbf{r}}$  where  $u(\mathbf{r}) = u(\mathbf{r} + \mathbf{\Lambda})$ ,  $\mathbf{\Lambda}$  is a lattice vector and  $\mathbf{k}$  is an arbitrary vector

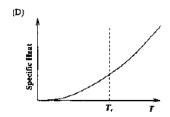
c)  $\psi(\mathbf{r}) = u(\mathbf{r})e^{i\mathbf{G}\cdot\mathbf{r}}$  where  $u(\mathbf{r}) = u(\mathbf{r} + \mathbf{\Lambda})$ ,  $\mathbf{\Lambda}$  is a lattice vector and  $\mathbf{G}$  is a reciprocal lattice vector

9) In an experiment involving a ferromagnetic medium, the following observations were made. Which one of the plots does NOT correctly represent the property of the medium? ( $T_C$  is the Curie (GATE PH 2010) temperature)









10) The thermal conductivity of a given material reduces when it undergoes a transition from its normal state to the superconducting state. The reason is: (GATE PH 2010)

- a) The Cooper pairs cannot transfer energy to the lattice
- b) Upon the formation of Cooper pairs, the lattice becomes less efficient in heat transfer
- c) The electrons in the normal state lose their ability to transfer heat because of their coupling to the Cooper pairs
- d) The heat capacity increases on transition to the superconducting state leading to a reduction in thermal conductivity

11) The basic process underlying the neutron  $\beta$ -decay is

(GATE PH 2010)

a) 
$$d \rightarrow u + e^- + \overline{v}_e$$
 b)  $d \rightarrow u + e^-$  c)  $s \rightarrow u + e^- + \overline{v}_e$  d)  $u \rightarrow d + e^+ + \overline{v}_e$ 

b) 
$$d \rightarrow u + e^-$$

c) 
$$s \rightarrow u + e^- + \overline{v}$$
.

d) 
$$u \rightarrow d + e^+ + \overline{v}$$

12) In the nuclear shell model the spin parity of  $^{15}N$  is given by

(GATE PH 2010)

a) 
$$\frac{1}{2}^{-}$$

b) 
$$\frac{1}{2}^{+}$$

c) 
$$\frac{3}{2}^{-}$$

d) 
$$\frac{3}{2}^{+}$$

13) Match the reactions on the left with the associated interactions on the right. (GATE PH 2010)

a) 
$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

b) 
$$\pi^0 \rightarrow \gamma + \gamma$$

b) 
$$\pi^0 \rightarrow \gamma + \gamma$$
  
c)  $\pi^0 + n \rightarrow \pi^- + p$ 

14) To detect trace amounts of a gaseous species in a mixture of gases, the preferred probing tool is (GATE PH 2010)

- a) Ionization spectroscopy with X-rays
- c) ESR spectroscopy

b) NMR spectroscopy

d) Laser spectroscopy

15)	A collection of N atoms is exposed to a strong resonant electromagnetic	radiation with	$N_g$	atoms in
	the ground state and $N_e$ atoms in the excited state, such that $N_g + N_e = N$ .	This collection	of t	wo-level
	atoms will have the following population distribution:	(GAT	ΈP	H 2010)

a)  $N_g \ll N_e$  b)  $N_g \gg N_e$  c)  $N_g \approx N_e = N/2$  d)  $N_g - N_e \approx N/2$ 

- 16) Two states of an atom have definite parities. An electric dipole transition between these states is (GATE PH 2010)
  - a) Allowed if both the states have even parity
  - b) Allowed if both the states have odd parity
  - c) Allowed if the two states have opposite parities
  - d) Not allowed unless a static electric field is applied
- 17) The spectrum of radiation emitted by a black body at a temperature 1000 K peaks in the (GATE PH 2010)

a) Visible range of frequencies

c) Ultraviolet range of frequencies

b) Infrared range of frequencies

d) Microwave range of frequencies

18) An insulating sphere of radius a carries a charge density  $\rho(\mathbf{r}) = \rho_0(a^2 - r^2)\cos\theta$ ; r < a. The leading order term for the electric field at a distance d, far away from the charge distribution, is proportional (GATE PH 2010) to

a)  $d^{-1}$ 

b)  $d^{-2}$ 

c)  $d^{-3}$ 

d)  $d^{-4}$ 

19) The voltage resolution of a 12-bit digital to analog converter (DAC), whose output varies from -10 V to +10 V is, approximately (GATE PH 2010)

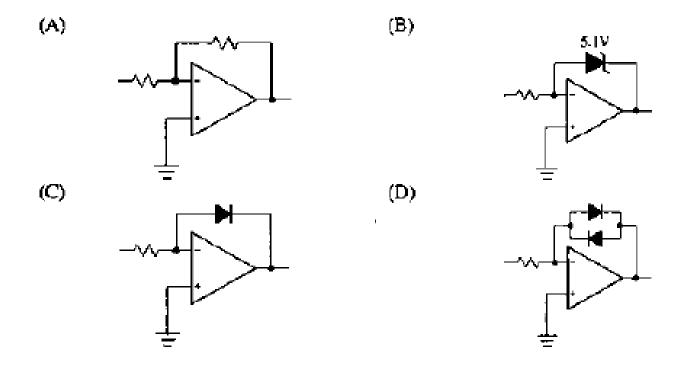
a) 1 mV

b) 5 mV

c) 20 mV

d) 100 mV

20) In one of the following circuits, negative feedback does not operate for a negative input. Which one is it? The opamps are running from  $\pm 15$  V supplies. (GATE PH 2010)



21)	•	racting classical point par e internal energy of the s			ve on	the two-dimensional (GATE PH 2010)	
	a) $\frac{3}{2}Nk_BT$	b) $\frac{1}{2}Nk_BT$	c)	$Nk_BT$	d) $\frac{5}{2}\Lambda$	$Vk_BT$	
22)	Which of the following	atoms cannot exhibit Bose	se-Ei	nstein condensation, ev	en in	principle?(GATE PH 2010)	
	a) ${}^{1}H_{1}$	b) <sup>4</sup> <i>He</i> <sub>2</sub>	c)	$^{23}Na_{11}$	d) <sup>40</sup> <i>I</i>	$X_{19}$	
	<ul> <li>) For the set of all Lorentz transformations with velocities along the x-axis, consider the two statements given below:</li> <li>P: If L is a Lorentz transformation then, L<sup>-1</sup> is also a Lorentz transformation.</li> <li>Q: If L<sub>1</sub> and L<sub>2</sub> are Lorentz transformations then, L<sub>1</sub>L<sub>2</sub> is necessarily a Lorentz transformation.</li> <li>Choose the correct option. (GATE PH 2010)</li> </ul>						
	<ul><li>a) P is true and Q is fa</li><li>b) Both P and Q are true</li></ul>			Both P and Q are fals P is false and Q is tru			
24)	Which of the following and $\alpha, \beta > 0$ .	g is an allowed wavefunc	ction	for a particle in a box	ınd st	ate? N is a constant (GATE PH 2010)	
	a) $\psi = N \frac{e^{-\alpha r}}{r^3}$ b) $\psi = N(1 - e^{-\alpha r})$ c) $\psi = Ne^{-\alpha x} e^{-\beta(x^2 + y^2 + z^2)}$		d)	$\psi = \begin{cases} \text{non-zero constant} \\ 0 \end{cases}$	nt if if	r < R $r > R$	
25)	A particle is confined can be expected to be	within a spherical region about	of 1	radius one femtometer	$(10^{-1})$	(GATE PH 2010)	
	a) $20\frac{\text{keV}}{c}$	b) $200\frac{\text{keV}}{c}$	c)	$200 \frac{\text{MeV}}{c}$	d) 2 <sup>G</sup>	eV c	
	a) $z = 0$ is a branch post b) $z = 0$ is a pole of or c) $z = 0$ is a removable d) $z = 0$ is an essential	der one singularity singularity Gerential equation for $y(t)$	$(c) : \frac{d^2y}{dt^2}$				
28)	28) Given the recurrence relation for the Legendre polynomials						
$(2n+1)xP_n(x) = (n+1)P_{n+1}(x) + nP_{n-1}(x),$							
	which of the following	which of the following integrals has a non-zero value? (GATE PH 2010)					
	a) $\int_{-1}^{+1} x^2 P_n(x) P_{n+1}(x) dx$ b) $\int_{-1}^{+1} x P_n(x) P_{n+2}(x) dx$	¢	<ul><li>c)</li><li>d)</li></ul>	$\int_{-1}^{1} x [P_n(x)]^2 dx$ $\int_{-1}^{+1} x^2 P_n(x) P_{n+2}(x) dx$			
29)	For a two-dimensional by	free electron gas, the elect	troni	c density n, and the Fe	rmi eı	nergy $E_F$ , are related (GATE PH 2010)	

a) 
$$n = \frac{(2mE_F)^{3/2}}{3\pi^2\hbar^3}$$
  
b)  $n = \frac{mE_F}{3\pi^2\hbar^3}$ 

c) 
$$n = \frac{mE_F}{2\pi\hbar^2}$$
  
d)  $n = \frac{2^{3/2}(mE_F)^{1/2}}{\pi\hbar}$ 

- 30) Far away from any of the resonance frequencies of a medium, the real part of the dielectric permittivity (GATE PH 2010) is
  - a) Always independent of frequency
- c) Monotonically increasing with frequency
- b) Monotonically decreasing with frequency
- d) A non-monotonic function of frequency
- 31) The ground state wavefunction of deuteron is in a superposition of s and d states. Which of the following is NOT true as a consequence? (GATE PH 2010)
  - a) It has a non-zero quadruple moment
  - b) The neutron-proton potential is non-central
  - c) The orbital wavefunction is not spherically symmetric
  - d) The Hamiltonian does not conserve the total angular momentum
- 32) The first three energy levels of  $^{228}Th_{90}$  are shown below

The expected spin-parity and energy of the next level are given by

(GATE PH 2010)

- a) (6+; 400 keV)
- b) (6<sup>+</sup>; 300 keV) c) (2<sup>+</sup>; 400 keV) d) (4<sup>+</sup>; 300 keV)
- 33) The quark content of  $\Sigma^+$ ,  $K^-$ ,  $\pi^-$  and p is indicated:  $|\Sigma^+\rangle = |uus\rangle$ ;  $|K^-\rangle = |s\bar{u}\rangle$ ;  $|\pi^-\rangle = |\bar{u}d\rangle$ ;  $|p\rangle = |uud\rangle$ . In the process,  $\pi^- + p \rightarrow K^- + \Sigma^+$ , considering strong interactions only, which of the following statements is true? (GATE PH 2010)
  - a) The process is allowed because  $\Delta S = 0$
  - b) The process is allowed because  $\Delta I_3 = 0$
  - c) The process is not allowed because  $\Delta S \neq 0$  and  $\Delta I_3 \neq 0$
  - d) The process is not allowed because the baryon number is violated
- 34) The three principal moments of inertia of a methanol (CH<sub>3</sub>OH) molecule have the property  $I_x = I_y = I$ and  $I_z \neq I$ . The rotational energy eigenvalues are (GATE PH 2010)

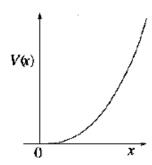
a) 
$$\frac{\hbar^2}{2I}l(l+1) + \frac{\hbar^2 m_l^2}{2}(\frac{1}{I_z} - \frac{1}{I}b) \frac{\hbar^2}{2I}l(l+1)$$

c) 
$$\frac{\hbar^2 m_l^2}{2} (\frac{1}{I_z} - \frac{1}{I})$$

c) 
$$\frac{\hbar^2 m_l^2}{2} (\frac{1}{I_z} - \frac{1}{I})$$
 d)  $\frac{\hbar^2}{2I} l(l+1) + \frac{\hbar^2 m_l^2}{2} (\frac{1}{I_z} + \frac{1}{I})$ 

35) A particle of mass m is confined in the potential  $V(x) = \begin{cases} \frac{1}{2}m\omega^2x^2 & \text{for } x > 0, \\ \infty & \text{for } x \le 0. \end{cases}$  Let the wavefunction of the particle be given by  $\psi(x) = -\frac{1}{\sqrt{5}}\psi_0 + \frac{2}{\sqrt{5}}\psi_1$ , where  $\psi_0$  and  $\psi_1$  are the eigenfunctions of the ground state and the first excited state quantities.

state and the first excited state respectively. The expectation value of the energy is(GATE PH 2010)



a) 
$$\frac{31}{10}\hbar\omega$$

b) 
$$\frac{25}{10}\hbar\omega$$

c) 
$$\frac{13}{10}\hbar\omega$$

d) 
$$\frac{11}{10}\hbar\omega$$

36) Match the typical spectra of stable molecules with the corresponding wave-number range (GATE PH 2010)

a) Electronic Spectra

b) Rotational Spectra

c) Molecular dissociation

•  $10^6 cm^{-1}$  and above

• 
$$10^5 - 10^6 cm^{-1}$$

• 
$$10^0 - 10^2 cm^{-1}$$

37) Consider the operations  $P: \mathbf{r} \to -\mathbf{r}$  (parity) and  $T: t \to -t$  (time-reversal). For the electric and magnetic fields  $\mathbf{E}$  and  $\mathbf{B}$ , which of the following set of transformations is correct?(GATE PH 2010)

a) 
$$P : \mathbf{E} \to -\mathbf{E}, \mathbf{B} \to \mathbf{B};$$

$$T: \mathbf{E} \to \mathbf{E}, \mathbf{B} \to -\mathbf{B}$$

b) 
$$P: \mathbf{E} \to \mathbf{E}, \mathbf{B} \to -\mathbf{B};$$

$$T: \mathbf{E} \to \mathbf{E}, \mathbf{B} \to \mathbf{B}$$

c) 
$$P: \mathbf{E} \to -\mathbf{E}, \mathbf{B} \to \mathbf{B};$$

$$T: \mathbf{E} \to -\mathbf{E}, \mathbf{B} \to -\mathbf{B}$$

d) 
$$P : \mathbf{E} \to \mathbf{E}, \mathbf{B} \to -\mathbf{B};$$

$$T: \mathbf{E} \to -\mathbf{E}, \mathbf{B} \to \mathbf{B}$$

38) Two magnetic dipoles of magnitude m each are placed in a plane as shown. The energy of interaction is given by (GATE PH 2010)



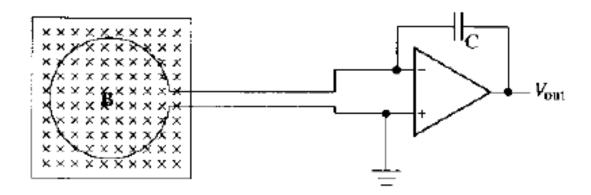
a) Zero

b)  $\frac{\mu_0}{4\pi} \frac{m^2}{d^3}$ 

c)  $\frac{3\mu_0}{2\pi} \frac{m^2}{d^3}$ 

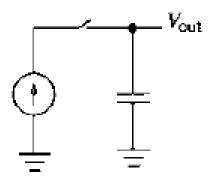
d) 
$$-\frac{3\mu_0}{8\pi}\frac{m^2}{d^3}$$

39) Consider a conducting loop of radius a and total loop resistance R placed in a region with a magnetic field B thereby enclosing a flux  $\phi_0$ . The loop is connected to an electronic circuit as shown, the capacitor being initially uncharged.

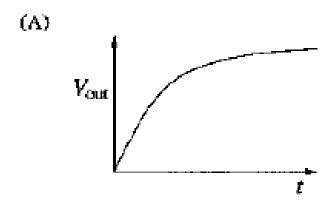


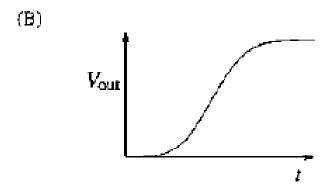
If the loop is pulled out of the region of the magnetic field at a constant speed u, the final output voltage  $V_{out}$  is independent of (GATE PH 2010)

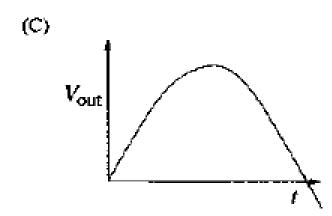
- a)  $\phi_0$  b) u c) R d) C
- 40) The figure shows a constant current source charging a capacitor that is initially uncharged.

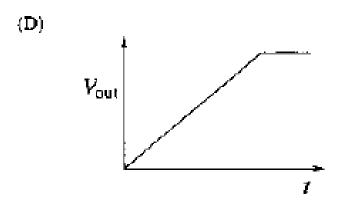


If the switch is closed at t = 0, which of the following plots depicts correctly the output voltage of the circuit as a function of time? (GATE PH 2010)

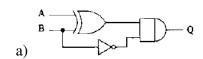


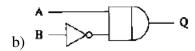


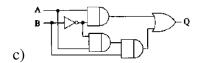


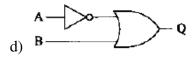


41) For any set of inputs, A and B, the following circuits give the same output, Q, except one. Which one is it? (GATE PH 2010)









- 42) CO<sub>2</sub> molecule has the first few energy levels uniformly separated by approximately 2.5 meV. At a temperature of 300 K, the ratio of the number of molecules in the 4th excited state to the number in the 2<sup>nd</sup> excited state is about (GATE PH 2010)
  - a) 0.5

b) 0.6

c) 0.8

- d) 0.9
- 43) Which among the following sets of Maxwell relations is correct? (U- internal energy, H- enthalpy, A- Helmholtz free energy and G- Gibbs free energy) (GATE PH 2010)

a) 
$$T = \left(\frac{\partial U}{\partial V}\right)_S$$
 and  $P = -\left(\frac{\partial U}{\partial S}\right)_V$   
b)  $V = \left(\frac{\partial H}{\partial P}\right)_S$  and  $T = \left(\frac{\partial H}{\partial S}\right)_P$ 

c) 
$$P = -\left(\frac{\partial G}{\partial V}\right)_T$$
 and  $V = -\left(\frac{\partial G}{\partial P}\right)_S$   
d)  $P = -\left(\frac{\partial A}{\partial S}\right)_T$  and  $S = -\left(\frac{\partial A}{\partial P}\right)_V$ 

$$V = \left(\frac{\partial H}{\partial P}\right)_S$$
 and  $T = \left(\frac{\partial H}{\partial S}\right)_P$  d)  $P = -\left(\frac{\partial A}{\partial S}\right)_T$  and  $S = -\left(\frac{\partial A}{\partial P}\right)_V$ 

44) For a spin-s particle, in the eigen basis of  $\hat{S}^2$ , S, the expectation value  $\langle sm|S_x^2|sm\rangle$  is(GATE PH 2010)

a) 
$$\frac{\hbar^2[s(s+1)-m^2]}{2}$$
  
b)  $\hbar^2[s(s+1)-2m^2]$ 

c) 
$$\hbar^2 [s(s+1) - m^2]$$
  
d)  $\hbar^2 m^2$ 

b) 
$$\hbar^2[s(s+1)-2m^2]$$

d) 
$$\hbar^2 m^2$$

- 45) A particle is placed in a region with the potential  $V(x) = \frac{1}{2}kx^2 \frac{1}{4}\lambda x^3$ , where  $k, \lambda > 0$ . Then, (GATE PH 2010)
  - a) x = 0 and  $x = \pm \sqrt{\frac{k}{\lambda}}$  are points of stable equilibrium
  - b) x = 0 is a point of stable equilibrium and  $x = \pm \sqrt{\frac{k}{\lambda}}$  is a point of unstable equilibrium
  - c) x = 0 and  $x = \pm \sqrt{\frac{k}{\lambda}}$  are points of unstable equilibrium d) There are no points of stable or unstable equilibrium
- 46) A  $\pi^0$  meson at rest decays into two photons, which move along the x-axis. They are both detected simultaneously after a time, t = 10 s. In an inertial frame moving with a velocity V = 0.6c in the direction of one of the photons, the time interval between the two detections is (GATE PH 2010)
  - a) 15 s

b) 0 s

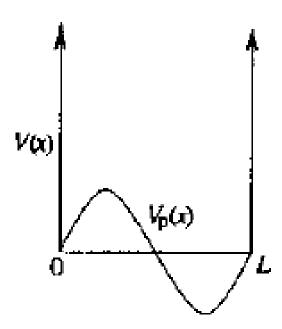
c) 10 s

d) 20 s

47) A particle of mass m is confined in an infinite potential well:

$$V(x) = \begin{cases} 0 & \text{if } 0 < x < L, \\ \infty & \text{otherwise} \end{cases}$$

. It is subjected to a perturbing potential  $V_p(x) = V_0 \sin\left(\frac{2\pi x}{L}\right)$  within the well. Let  $E^{(1)}$  and  $E^{(2)}$  be the corrections to the ground state energy in the first and second order in  $V_0$ , respectively. Which of the (GATE PH 2010) following are true?



a) 
$$E^{(1)} = 0$$
;  $E^{(2)} < 0$ 

c) 
$$E^{(1)} = 0$$
;

c)  $E^{(1)}=0$ ;  $E^{(2)}$  depends on the sign of  $V_0$  d)  $E^{(1)}<0$ ;  $E^{(2)}<0$ 

b) 
$$E^{(1)} > 0$$
:  $E^{(2)} = 0$ 

d) 
$$F(1) < 0$$
:  $F(2) < 0$ 

In the presence of a weak magnetic field, atomic hydrogen undergoes the transition:

$${}^{2}P_{3/2} \rightarrow {}^{2}S_{1/2}$$

by emission of radiation.

48) The number of distinct spectral lines that are observed in the resultant Zeeman spectrum is (GATE PH 2010)

49) The spectral line corresponding to the transition

$${}^{2}P_{3/2}\left(m_{j}=+\frac{1}{2}\right) \rightarrow {}^{2}S_{1/2}\left(m_{j}=-\frac{1}{2}\right)$$

is observed along the direction of the applied magnetic field. The emitted electromagnetic field is: (GATE PH 2010)

a) Circularly polarized

c) Unpolarized

b) Linearly polarized

d) Not emitted along the magnetic field direction

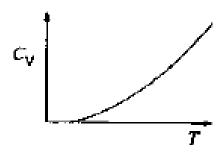
## Common Data for Questions 50 and 51:

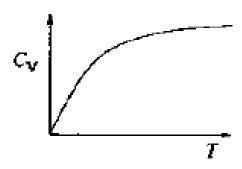
The partition function for a gas of photons is given by

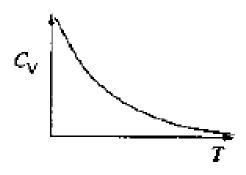
$$\ln Z = \frac{\pi^2 V (k_B T)^3}{45\hbar^3 c^3}$$

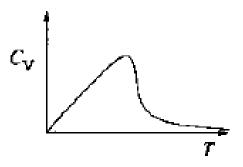
50) The specific heat of the photon gas varies with temperature as

(GATE PH 2010)









51) The pressure of the photon gas is

(GATE PH 2010)

a) 
$$\frac{\pi^2 (k_B T)^4}{15\hbar^3 c^3}$$

b) 
$$\frac{\pi^2 (k_B T)^4}{8\hbar^3 c^3}$$

c) 
$$\frac{\pi^2 (k_B T)^4}{45\hbar^3 c^3}$$

d) 
$$\frac{\pi (k_B T)^4}{45\hbar^3 c^3}$$

Consider the propagation of electromagnetic waves in a linear, homogeneous and isotropic material medium with electric permittivity  $\epsilon$  and magnetic permeability  $\mu$ .

- 52) For a plane wave of angular frequency  $\omega$  and propagation vector **k** propagating in the medium (GATE PH 2010) Maxwell's equations reduce to
  - a)  $\mathbf{k} \cdot \mathbf{E} = 0$ ;  $\mathbf{k} \cdot \mathbf{H} = 0$ ;  $\mathbf{k} \times \mathbf{E} = \omega \epsilon \mathbf{H}$ ;  $\mathbf{k} \times \mathbf{H} = -\omega \mu \mathbf{E}$
  - b)  $\mathbf{k} \cdot \mathbf{E} = 0$ ;  $\mathbf{k} \cdot \mathbf{H} = 0$ ;  $\mathbf{k} \times \mathbf{E} = -\omega \epsilon \mathbf{H}$ ;  $\mathbf{k} \times \mathbf{H} = \omega \mu \mathbf{E}$
  - c)  $\mathbf{k} \cdot \mathbf{E} = 0$ ;  $\mathbf{k} \cdot \mathbf{H} = 0$ ;  $\mathbf{k} \times \mathbf{E} = -\omega \mu \mathbf{H}$ ;  $\mathbf{k} \times \mathbf{H} = \omega \epsilon \mathbf{E}$
  - d)  $\mathbf{k} \cdot \mathbf{E} = 0$ ;  $\mathbf{k} \cdot \mathbf{H} = 0$ ;  $\mathbf{k} \times \mathbf{E} = \omega \mu \mathbf{H}$ ;  $\mathbf{k} \times \mathbf{H} = -\omega \epsilon \mathbf{E}$
- 53) If  $\epsilon$  and  $\mu$  assume negative values in a certain frequency range, then the directions of the propagation vector **k** and the Poynting vector **S** in that frequency range are related as (GATE PH 2010)
  - a) k and S are parallel
  - b) k and S are anti-parallel
  - c) k and S are perpendicular to each other
  - d) **k** and **S** make an angle that depends on the magnitude of  $|\epsilon|$  and  $|\mu|$

The Lagrangian for a simple pendulum is given by:

$$L = \frac{1}{2}ml^2\dot{\theta}^2 - mgl(1 - \cos\theta)$$

54) Hamilton's equations are then given by

(GATE PH 2010)

a) 
$$p_{\theta} = -mgl\sin\theta$$
;  $\dot{\theta} = \frac{p_{\theta}}{ml^2}$   
b)  $p_{\theta} = mgl\sin\theta$ ;  $\dot{\theta} = \frac{p_{\theta}}{ml^2}$ 

c) 
$$p_{\theta} = -m\ddot{\theta}; \quad \dot{\theta} = \frac{p_{\theta}}{m}$$

b) 
$$p_{\theta} = mgl\sin\theta$$
;  $\dot{\theta} = \frac{p_{\theta}^{ml}}{ml^2}$ 

c) 
$$p_{\theta} = -m\ddot{\theta}; \quad \dot{\theta} = \frac{p_{\theta}}{m}$$
  
d)  $\dot{p}_{\theta} = -\left(\frac{g}{l}\right)\theta; \quad \dot{\theta} = \frac{p_{\theta}}{ml}$ 

55) The Poisson bracket between  $\theta$  and  $\dot{\theta}$  is

(GATE PH 2010)

a) 
$$\{\theta, \dot{\theta}\} = 1$$

a) 
$$\{\theta, \dot{\theta}\} = 1$$
 b)  $\{\theta, \dot{\theta}\} = \frac{1}{ml^2}$  c)  $\{\theta, \dot{\theta}\} = \frac{1}{m}$  d)  $\{\theta, \dot{\theta}\} = \frac{g}{l}$ 

c) 
$$\{\theta, \dot{\theta}\} = \frac{1}{m}$$

d) 
$$\{\theta, \dot{\theta}\} = \frac{g}{l}$$

	(GATE PH 2010) His rather casual ren	narks on politics	his lack of serious	ness about the subject.
	a) masked	b) belied	c) betrayed	d) suppressed
57)	Which of the following Circuitous	g options is the closest in	meaning to the word be	low: (GATE PH 2010)
	a) cyclic	b) indirect	c) confusing	d) crooked
58)	(GATE PH 2010)			lete the following sentence: e a better planet for our
	a) uphold	b) restrain	c) cherish	d) conserve
59)	<u> </u>	± •		football and 10 of them leither hockey nor football (GATE PH 2010)
	a) 2	b) 17	c) 13	d) 3
60)	-	s the relation in the origi	• •	pairs of words. Select the (GATE PH 2010)
	a) fallow : land	b) unaware : sleeper	c) wit : jester	d) renovated : house
61)	If $137 + 276 = 435$ how	w much is 731 + 672?		(GATE PH 2010)
	a) 534	b) 1403	c) 1623	d) 1513
	1 <sup>st</sup> January. The age di is less than 3 years. Gi a) Hari's age + Gita's a	ifference between any two iven the following facts: age > Irfan's age + Saira	o successive siblings (that a's age.	sisters). All were born on t is born one after another) not the oldest and Saira is
	In what order were the	ey born (oldest first)?		(GATE PH 2010)
	a) HSIG	b) SGHI	c) IGSH	d) IHSG
63)	populations. Chemica	l agents that do their w	ork silently appear to b	to suppression of civilian be suited to such warfare; a that chemical agents are

Which of the following statements best sums up the meaning of the above passage:(GATE PH 2010)

a) Modern warfare has resulted in civil strife.

useful tools for their cause.

b) Chemical agents are useful in modern warfare.

- c) Use of chemical agents in warfare would be undesirable.
- d) People in military establishments like to use chemical agents in war.
- 64) 5 skilled workers can build a wall in 20 days; 8 semi-skilled workers can build a wall in 25 days; 10 unskilled workers can build a wall in 30 days. If a team has 2 skilled, 6 semi-skilled and 5 unskilled workers, how long will it take to build the wall? (GATE PH 2010)
  - a) 20 days
- b) 18 days
- c) 16 days
- d) 15 days
- 65) Given digits 2, 2, 3, 3, 4, 4, 4, 4 how many distinct 4 digit numbers greater than 3000 can be formed? (GATE PH 2010)
  - a) 50

b) 51

c) 52

d) 54

### END OF THE QUESTION PAPER