

GATE-IN-2020

EE25BTECH11002 - Achat Parth Kalpesh

Q.1-Q.5 CARRY ONE MARK EACH.

- 1) He is known for his unscrupulous ways. He always sheds _____ tears to deceive people.
(GATE IN 2020)
a) fox's b) crocodile's c) crocodile d) fox
- 2) Jofra Archer, the England fast bowler, is _____ than accurate.
(GATE IN 2020)
a) more fast b) faster c) less fast d) more faster
- 3) Select the word that fits the analogy:
Build : Building :: Grow : _____
(GATE IN 2020)
a) Grown
b) Grew
c) Growth
d) Grewed
- 4) I do not think you know the case well enough to have opinions. Having said that, I agree with your other point. What does the phrase "having said that" mean in the given text?
(GATE IN 2020)
a) as opposed to what I have said
b) despite what I have said
c) in addition to what I have said
d) contrary to what I have said
- 5) Define $[x]$ as the greatest integer less than or equal to x , for each $x \in (-\infty, \infty)$. If $y = [x]$, then area under y for $x \in [1, 4]$ is _____.
(GATE IN 2020)
a) 1 b) 3 c) 4 d) 6

Q.6 - Q.10 carry two marks each.

- 6) Crowd funding deals with mobilisation of funds for a project from a large number of people, who would be willing to invest smaller amounts through web-based platforms in the project.
Based on the above paragraph, which of the following is correct about crowd funding?
(GATE IN 2020)
a) Funds raised through unwilling contributions on web-based platforms.
b) Funds raised through large contributions on web-based platforms.
c) Funds raised through coerced contributions on web-based platforms.
d) Funds raised through voluntary contributions on web-based platforms.
- 7) P, Q, R and S are to be uniquely coded using α and β . If P is coded as $\alpha\alpha$ and Q as $\alpha\beta$, then R and S, respectively, can be coded as _____
(GATE IN 2020)

- a) $\beta\alpha$ and $\alpha\beta$
b) $\beta\beta$ and $\alpha\alpha$

- c) $\alpha\beta$ and $\beta\beta$
d) $\beta\alpha$ and $\beta\beta$

8) The sum of the first n terms in the sequence 8, 88, 888, 8888, ... is _____

(GATE IN 2020)

- a) $\frac{81}{80}(10^n - 1) + \frac{9}{8}n$
b) $\frac{81}{80}(10^n - 1) - \frac{9}{8}n$

- c) $\frac{80}{81}(10^n - 1) + \frac{8}{9}n$
d) $\frac{80}{81}(10^n - 1) - \frac{8}{9}n$

9) Select the graph that schematically represents BOTH $y = x^m$ and $y = x^{1/m}$ properly in the interval $0 \leq x \leq 1$, for integer values of m , where $m > 1$.

(GATE IN 2020)

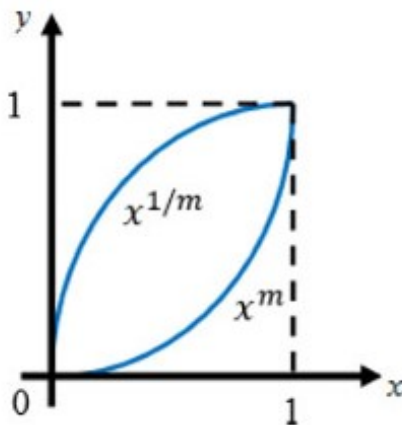


Fig. 1. *

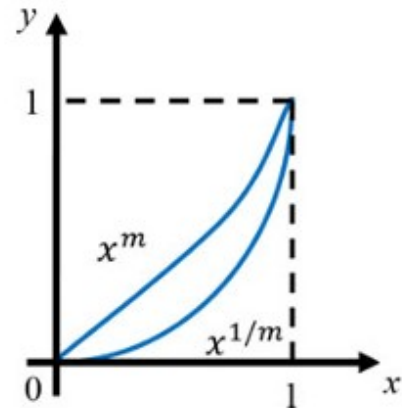


Fig. 3. *

a)

c)

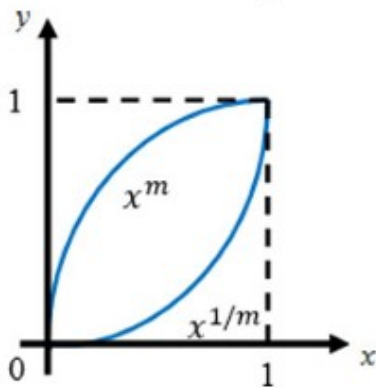


Fig. 2. *

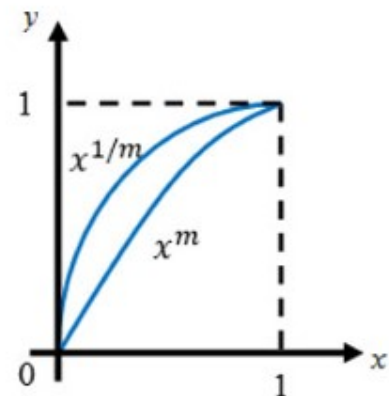


Fig. 4. *

b)

10) The bar graph Fig. 5 shows the data of the students who appeared and passed in an examination for four schools P, Q, R and S. The average of success rates (in percentage) of these four schools is _____

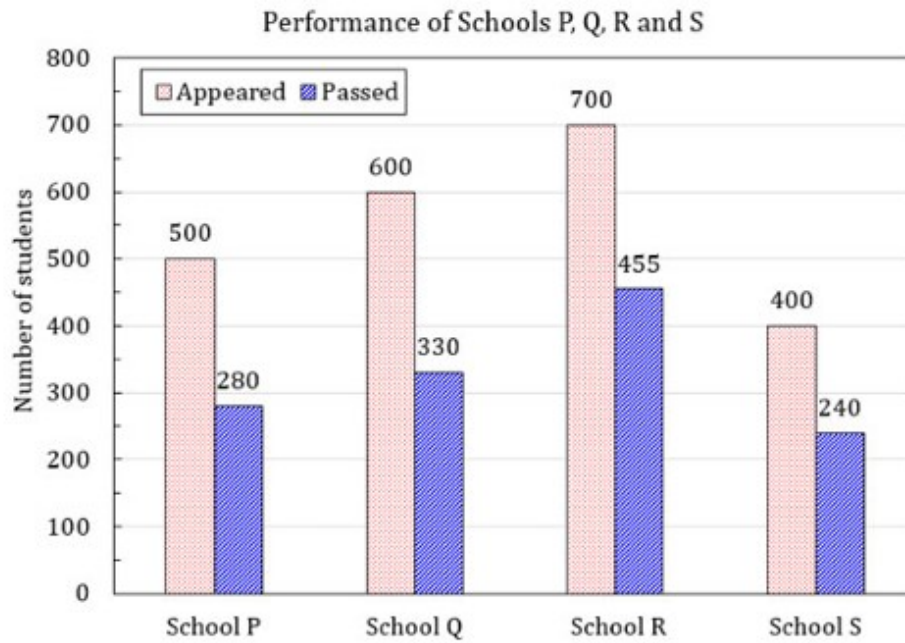


Fig. 5. *

(GATE IN 2020)

- a) 58.5 % b) 58.8 % c) 59.0 % d) 59.3 %

INSTRUMENTATION ENGINEERING

Q1 - Q25 carry one mark each.

- 1) The unit vectors along the mutually perpendicular x, y and z axes are \hat{i}, \hat{j} and \hat{k} respectively. Consider the plane $z = 0$ and two vectors \mathbf{a} and \mathbf{b} on that plane such that $\mathbf{a} \neq \alpha \mathbf{b}$ for any scalar α . A vector perpendicular to both \mathbf{a} and \mathbf{b} is _____

(GATE IN 2020)

- a) \hat{k} b) $\hat{i} - \hat{j}$ c) $-\hat{j}$ d) \hat{i}

- 2) Consider the recursive equation $X_{n+1} = X_n - h(F(X_n) - X_n)$, with initial condition $X_0 = 1$ and $h > 0$ being a very small valued scalar. This recursion numerically solves the ordinary differential equation _____

(GATE IN 2020)

- a) $\dot{X} = -F(X), X(0) = 1$ c) $\dot{X} = F(X), X(0) = 1$
 b) $\dot{X} = -F(X) + X, X(0) = 1$ d) $\dot{X} = F(X) + X, X(0) = 1$

- 3) A set of linear equations is given in the form $Ax = b$, where A is a 2×4 matrix with real number entries and $b \neq 0$. Will it be possible to solve for x and obtain a unique solution by multiplying both left and right sides of the equation by A^T (the super script T denotes the transpose) and inverting the matrix $A^T A$? Answer is _____

(GATE IN 2020)

- a) Yes, it is always possible to get a unique solution for any 2×4 matrix A .
 b) No, it is not possible to get a unique solution for any 2×4 matrix A .
 c) Yes, can obtain a unique solution provided the matrix $A^T A$ is well conditioned

- d) Yes, can obtain a unique solution provided the matrix A is well conditioned
- 4) In the circuit shown below, Fig. 6 the safe maximum value for the current I is _____

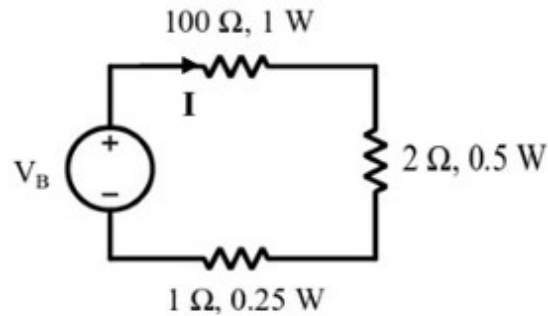


Fig. 6. *

(GATE IN 2020)

- a) 1.0 A b) 0.5 A c) 0.1 A d) 0.05 A
- 5) A differentiator has a transfer function whose _____
- (GATE IN 2020)
- a) phase increases linearly with frequency
 b) magnitude remains constant
 c) magnitude increases linearly with frequency
 d) magnitude decreases linearly with frequency
- 6) A phase lead network has the transfer function $G(s) = \frac{1+0.2s}{1+0.05s}$. The angular frequency at which the maximum phase shift for the network occurs is _____
- (GATE IN 2020)
- a) 10 rad/s b) 20 rad/s c) 100 rad/s d) 200 rad/s
- 7) If the diodes in the circuit shown Fig. 7 are ideal and the breakdown voltage V_z of the Zener diode is 5 V, the power dissipated in the 100 Ω resistor (in watts) is _____

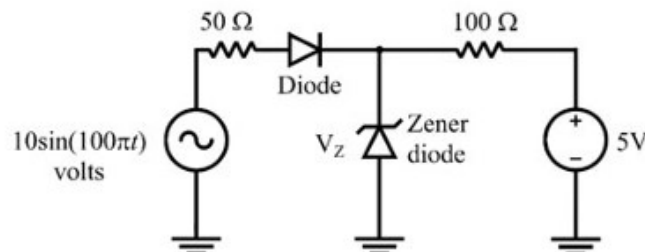


Fig. 7. *

(GATE IN 2020)

- a) 0 b) 1 c) 25/100 d) 225/100

8) Given $f(A, B, C, D) = \sum m(0, 1, 2, 6, 8, 9, 10, 11) + \sum d(3, 7, 14, 15)$ is a Boolean function, where m represents min-terms and d represents don't-cares. The minimal sum of products expression for f is _____

(GATE IN 2020)

- a) $f = \bar{A}\bar{B} + C\bar{B}$ c) $f = \bar{D} + A$
 b) $f = \bar{B} + C$ d) $f = A\bar{B} + C\bar{D}$

9) A Q meter is best suited for the measurement of the _____

(GATE IN 2020)

- a) Quality factor of a capacitance.
 b) Distributed capacitance of a coil.
 c) Quality factor of piezoelectric sensor.
 d) Turns-ratio of a transformer

10) If I is the current flowing through a Hall effect sensor and B is the magnetic flux density perpendicular to the direction of the current (in the plane of the Hall effect sensor), the Hall voltage generated is _____

(GATE IN 2020)

- a) Directly proportional to I and inversely proportional to B
 b) Directly proportional to both I and B
 c) Inversely proportional to both I and B
 d) Inversely proportional to I and directly proportional to B

11) The Boolean expression for the shaded regions as shown in the figure Fig. 8 is _____

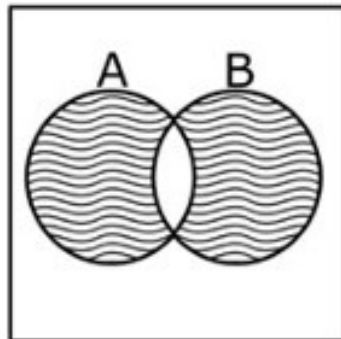


Fig. 8. *

(GATE IN 2020)

- a) $(A + B) \cdot (\bar{A} + \bar{B})$ c) $(\bar{A} + \bar{B}) \cdot (A + B)$
 b) $(\bar{A} + B) \cdot (A + \bar{B})$ d) $(A + \bar{B}) \cdot (A + B)$

12) The Boolean operation performed by the following circuit Fig. 9 at the output O is _____

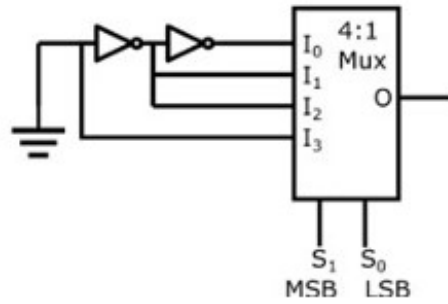


Fig. 9. *

(GATE IN 2020)

a) $O = S_1 \oplus S_0$
 b) $O = S_1 \cdot S_0$

c) $O = S_1 + S_0$
 d) $O = S_0 \cdot S_1$

- 13) Consider the Signal $x[n] = \sin(2\pi n)u[n]$, where $u[n] = \begin{cases} 1 & n = 0, 1, 2, 3, \dots \\ 0 & \text{otherwise} \end{cases}$. The period of this signal $x[n]$ is _____

(GATE IN 2020)

- a) 4 b) 3 c) 2 d) 1

- 14) The closed loop transfer function of a control system is given by $\frac{C(s)}{R(s)} = \frac{1}{s+1}$. For the input $r(t) = \sin t$, the steady state response $c(t)$ is _____

(GATE IN 2020)

a) 1 c) $\frac{1}{\sqrt{2}} \sin\left(t + \frac{\pi}{4}\right)$
 b) $\frac{1}{\sqrt{2}} \cos t$ d) $\frac{1}{\sqrt{2}} \sin\left(t - \frac{\pi}{4}\right)$

- 15) Let $f(z) = \frac{1}{z+a}$, $a > 0$. The value of the integral $\oint_C f(z) dz$ over a circle C with center $(-a, 0)$ and radius $R > 0$ evaluated in the anti-clockwise direction is _____

(GATE IN 2020)

- a) 0 b) $2\pi i$ c) $-2\pi i$ d) $4\pi i$

- 16) A player throws a ball at a basket kept at a distance. The probability that the ball falls into the basket in a single attempt is 0.1. The player attempts to throw the ball twice. Considering each attempt to be independent, the probability that this player puts the ball into the basket only in the second attempt (rounded off to two decimal places) is _____

(GATE IN 2020)

- 17) Assuming ideal opamps, the output voltage at V_1 in the figure shown Fig. ?? (in volts) is _____

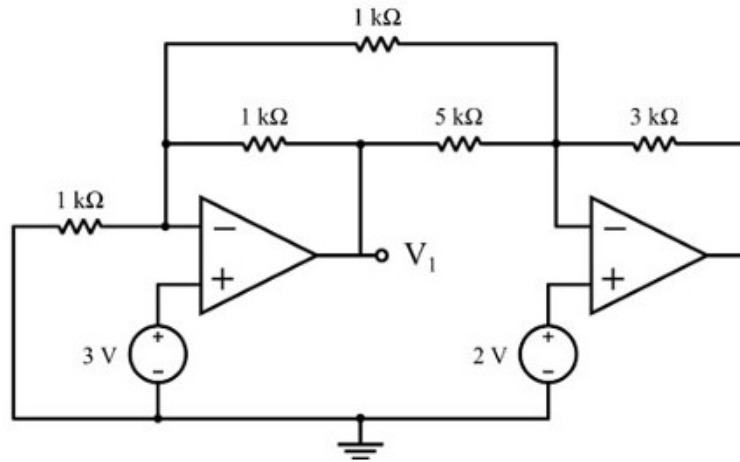


Fig. 10. *

(GATE IN 2020)

- 18) Three $400\ \Omega$ resistors are connected in delta and powered by a $400\ \text{V}$ (rms), $50\ \text{Hz}$, balanced, symmetrical R-Y-B sequence, three-phase three-wire mains. The rms value of the line current is _____ (in amperes, rounded off to one decimal place)

(GATE IN 2020)

- 19) Consider the signal $x(t) = e^{-|t|}$. Let $X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$ be the Fourier transform of $x(t)$. The value of $X(j0)$ is _____

(GATE IN 2020)

- 20) A second order system has closed loop poles located at $s = -3 \pm j4$. The time t at which the maximum value of the step response occurs (in seconds, rounded off to two decimal places) is _____

(GATE IN 2020)

- 21) Assume that the opamp in the circuit shown Fig. 11 is ideal. The value of $\frac{V_x}{I_x}$ (in $\text{k}\Omega$) is _____

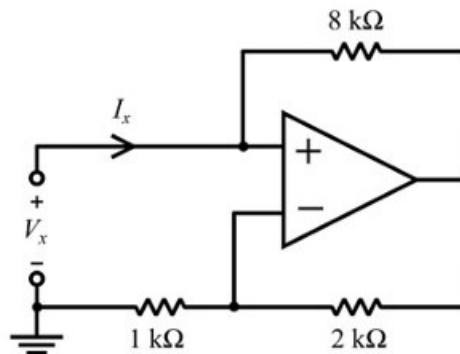


Fig. 11. *

(GATE IN 2020)

- 22) A sinusoid of $10\ \text{kHz}$ is sampled at $15\ \text{k samples/s}$. The resulting signal is passed through an ideal low pass filter (LPF) with cut-off frequency of $25\ \text{kHz}$. The maximum frequency component at the output of the LPF (in kHz) is _____

(GATE IN 2020)

- 23) A $200\ \text{mV}$ full-scale dual-slope analog to digital converter (DS-ADC) has a reference voltage of $100\ \text{mV}$. The first integration time is set as $100\ \text{ms}$. The DS-ADC is operated in the contin-

uous conversion mode. The conversion time of the DS-ADC for an input voltage of 123.4 mV (in ms, rounded off to one decimal place) is _____

(GATE IN 2020)

- 24) The capacitance C_x of a capacitive type sensor is $(1000x)$ pF, where x is the input to the sensor. As shown in the figure, Fig. 12 the sensor is excited by a voltage $10 \sin(100\pi t)$ V. The other terminal of the sensor is tied to the input of a high input impedance amplifier through a shielded cable, with shield connected to ground. The cable capacitance is 100 pF. The peak of the voltage V_A at the input of the amplifier when $x = 0.1$ (in volts) is _____

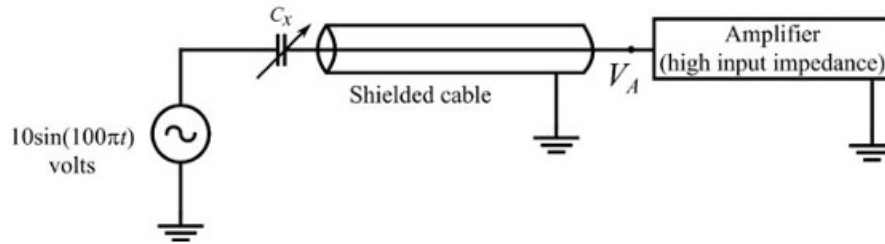


Fig. 12. *

(GATE IN 2020)

- 25) Two 100Ω resistors having tolerance 3% and 4% are connected in series. The effective tolerance of the series combination (in % ,rounded off to one decimal place) is _____

(GATE IN 2020)

- 26) Consider the matrix

$$M = \begin{pmatrix} 1 & -1 & 0 \\ 1 & -2 & 1 \\ 0 & -1 & 1 \end{pmatrix}.$$

One of the eigenvectors of M is

(GATE IN 2020)

a)

b)

c)

d)

$$\begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} -1 \\ -1 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

- 27) Consider the differential equation $\frac{dx}{dt} = \sin(x)$, with the initial condition $x(0) = 0$. The solution to this ordinary differential equation is _____

(GATE IN 2020)

a) $x(t) = 0$

c) $x(t) = \cos(t)$

b) $x(t) = \sin(t)$

d) $x(t) = \sin(t) - \cos(t)$

- 28) A straight line drawn on an x-y plane intercepts the x-axis at -0.5 and the y-axis at 1 . The equation that describes this line is _____

(GATE IN 2020)

a) $y = -0.5x + 1$

c) $y = 0.5x - 1$

b) $y = x - 0.5$

d) $y = 2x + 1$

29) The loop transfer function of a negative feedback system is $G(s)H(s) = \frac{1}{s(s-2)}$. The Nyquist plot for the above system _____

(GATE IN 2020)

- a) encircles $(-1 + j0)$ point once in the clockwise direction
- b) encircles $(-1 + j0)$ point once in the counterclockwise direction
- c) does not encircle $(-1 + j0)$ point
- d) encircles $(-1 + j0)$ point twice in the counterclockwise direction

30) I_1, I_2 and I_3 in the figure below Fig. ?? are mesh currents. The correct set of mesh equations for these currents, in matrix form, is _____

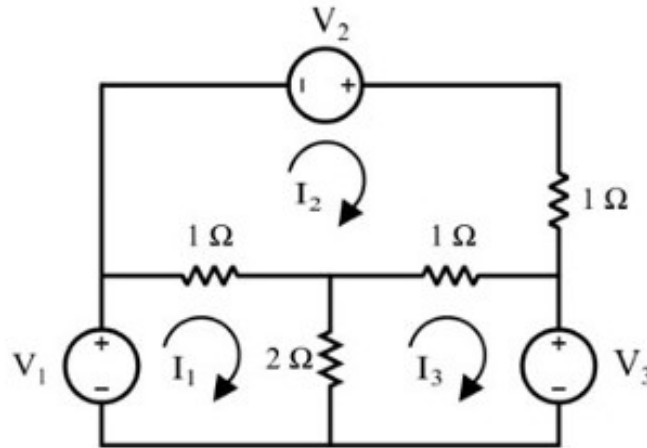


Fig. 13. *

(GATE IN 2020)

a)

$$\begin{pmatrix} 3 & -1 & -2 \\ -1 & 3 & -1 \\ -2 & -1 & 3 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} V_1 \\ V_2 \\ -V_3 \end{pmatrix}$$

c)

$$\begin{pmatrix} -3 & -1 & -2 \\ -1 & 3 & -1 \\ -2 & -1 & 3 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} V_1 \\ V_2 \\ -V_3 \end{pmatrix}$$

b)

$$\begin{pmatrix} 3 & -1 & -2 \\ -1 & 3 & -1 \\ -2 & -1 & -3 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} V_1 \\ V_2 \\ V_3 \end{pmatrix}$$

d)

$$\begin{pmatrix} 1 & -1 & -2 \\ -1 & 2 & -1 \\ -2 & -1 & 3 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} V_1 \\ V_2 \\ V_3 \end{pmatrix}$$

31) Consider the function $f(x, y) = x^2 + y^2$. The minimum value the function attains on the line $x + y = 1$ (rounded off to one decimal place) is _____

(GATE IN 2020)

32) Consider two identical bags B1 and B2 each containing 10 balls of identical shapes and sizes. Bag B1 contains 7 Red and 3 Green balls, while bag B2 contains 3 Red and 7 Green balls. A bag is picked at random and a ball is drawn from it, which was found to be Red. The probability that the Red ball came from bag B1 (rounded off to one decimal place) is _____

(GATE IN 2020)

33) The rms value of the phasor current I in the circuit shown Fig. 14 (in amperes) is _____

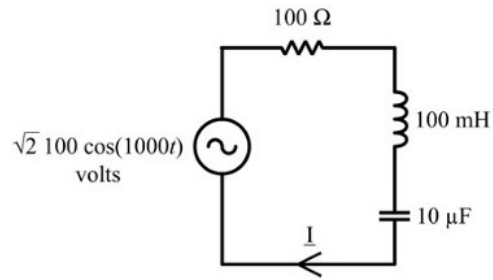


Fig. 14. *

(GATE IN 2020)

34) In the circuit shown, Fig. 15 the rms value of the voltage across the 100Ω resistor (in volts) is _____

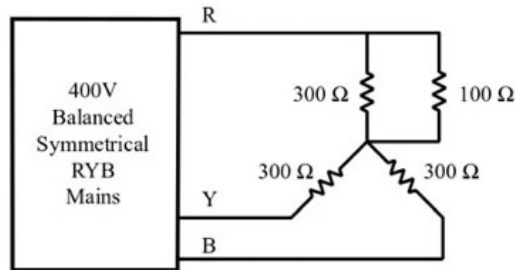


Fig. 15. *

(GATE IN 2020)

35) Let

$$g[n] = \begin{cases} 1 & n = 0 \\ 0 & n = \pm 1, \pm 2, \pm 3, \dots \end{cases} \text{ and } h[n] = \begin{cases} 1 & n = 0, 3, 6, 9, \dots \\ 0 & \text{otherwise} \end{cases}$$

Consider $y[n] = h[n] \otimes g[n]$, where \otimes denotes the convolution operator. The value of $y(2)$ is _____

(GATE IN 2020)

36) The loop transfer function of a negative feedback system is given by $G(s)H(s) = \frac{K}{s(s+2)(s+6)}$, where $K > 0$. The value of K at the breakaway point of the root locus for the above system (rounded off to one decimal) is _____

(GATE IN 2020)

37) The system shown in Fig. 16 in Fig. (a) has a time response $y(t)$ to an input $r(t) = 10u(t)$ as shown in Fig. (b), $u(t)$ being the unit step input. Both K, τ are positive. The gain K of the system is _____

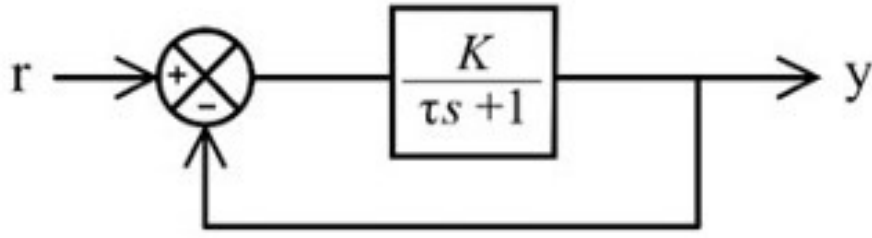


Fig. (a)

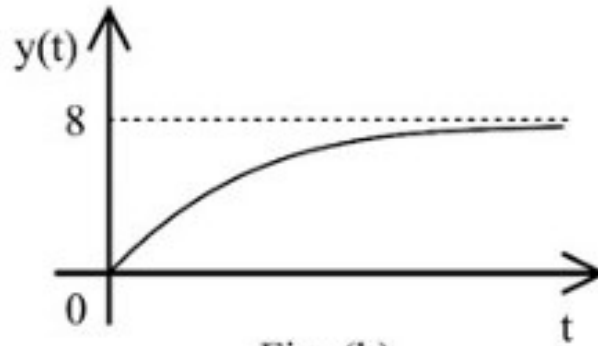


Fig. (b)

Fig. 16. *

(GATE IN 2020)

- 38) Assuming that the opamp used in the circuit shown Fig. 17 is ideal, the reading of the 1 Hz bandwidth, permanent magnet moving coil (PMMC) type voltmeter (in volts) is _____

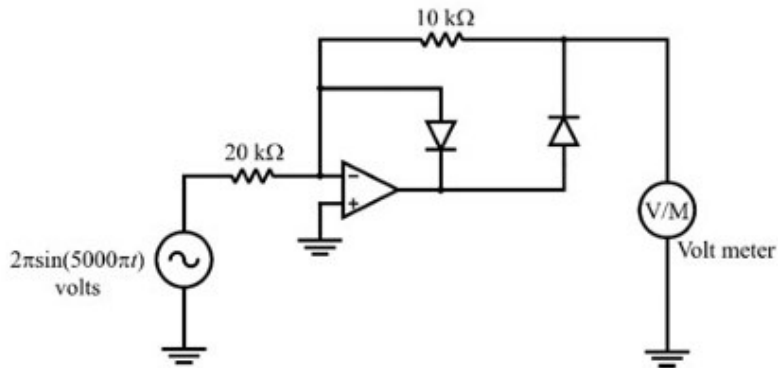


Fig. 17. *

(GATE IN 2020)

- 39) If the opamps in the circuit shown Fig. 18 are ideal and $V_x = 0.5$ mV, the steady state value of V_o (in volts, rounded off to two decimal places) is _____

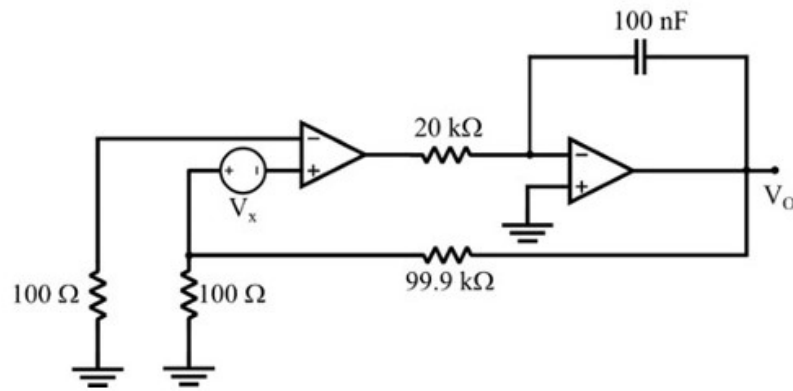


Fig. 18. *

(GATE IN 2020)

- 40) Two T-flip flops are interconnected as shown in the figure. Fig. 19 The present state of the flip flops are: $A = 1, B = 1$. The input x is given as 1, 0, 1 in the next three clock cycles. The decimal equivalent of $(AB_y)_2$ with A being the MSB and y being the LSB, after the 3rd clock cycle is _____

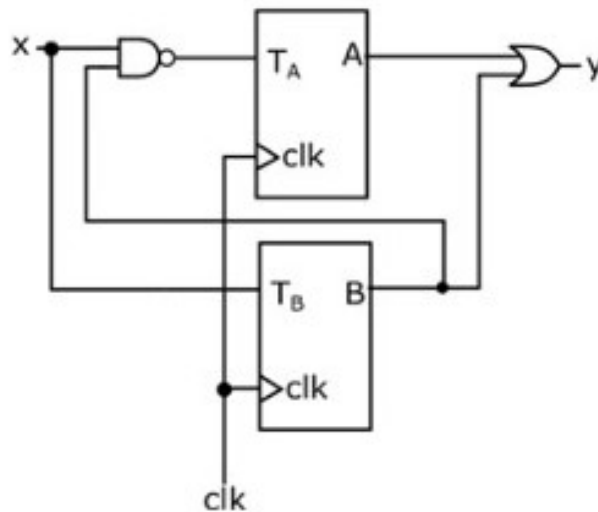


Fig. 19. *

(GATE IN 2020)

- 41) The address lines $A_9 \dots A_2$ of a 10 bit, 1.023 V full-scale digital to analog converter (DAC) is connected to the data lines D_7 to D_0 of an 8-bit microprocessor, with A_1 and A_0 of the DAC grounded. Now, $D_7 \dots D_0$ is changed from 1010 1010 to 1010 1011. The corresponding change in the output of the DAC (in mV, rounded off to one decimal place) is _____

(GATE IN 2020)

- 42) The real power drawn by a balanced load connected to a 400 V, 50 Hz, balanced, symmetrical 3-phase, 3-wire, RYB sequence mains is measured using the two-wattmeter method. Wattmeter W_1 is connected in the R line and wattmeter W_2 is connected in the B line. The line current is measured as $\frac{1}{\sqrt{3}}$ A. If the wattmeter W_1 reads zero, the reading on W_2 (in watts) is _____

(GATE IN 2020)

- 43) A $6\frac{1}{2}$ digit timer-counter is set in the 'time period' mode of operation and the range is set as 'ns'. For an input signal, the timer-counter displays 1000000. With the same input signal, the timer-counter is

changed to 'frequency' mode of operation and the range is set as 'Hz'. The display will show the number _____

(GATE IN 2020)

- 44) The circuit shown in Fig. 20 uses an ideal opamp powered from a supply $V_{CC} = 5$ V. If the charge q_p generated by the piezoelectric sensor is of the form $q_p = 0.1 \sin(10000\pi t) \mu C$, the peak detector output after 10 cycles of q_p (in volts, rounded off to one decimal place) is _____

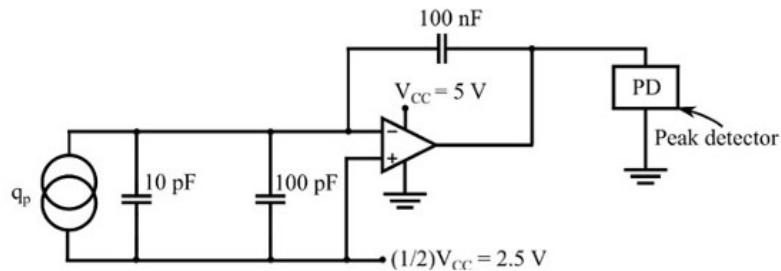


Fig. 20. *

(GATE IN 2020)

- 45) A metallic strain gauge of resistance R_x with a gauge factor of 2 is bonded to a structure made of a metal with modulus of elasticity of 200 GN/m^2 . The value of R_x is $1 \text{ k}\Omega$ when no stress is applied. R_x is a part of a quarter bridge with three identical fixed resistors of $1 \text{ k}\Omega$ each. The bridge is excited from a DC voltage of 4 V . The structure is subjected to a stress of 100 MN/m^2 . Magnitude of the output of the bridge (in mV, rounded off to two decimal places) is _____

(GATE IN 2020)

- 46) A laser beam of 10 mm beam diameter is focused onto an optical fibre using a thin biconvex lens as shown in the figure in Fig. 21. The refractive index of the lens is 1.5 . The refractive indices of the core and cladding of the fibre are 1.55 and 1.54 respectively. The minimum value of the focal length of the lens to attain the maximum coupling to the fibre (in mm, rounded off to one decimal place) is _____

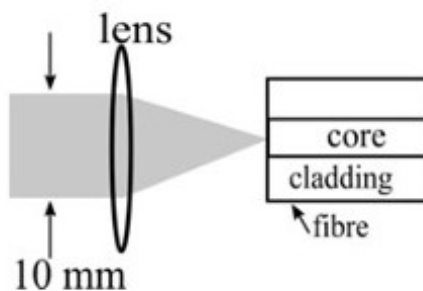


Fig. 21. *

(GATE IN 2020)

- 47) As shown in the figure in Fig. 22, a slab of finite thickness t with refractive index $n_2 = 1.5$, has air ($n_1 = 1$) above and below it. Light of free space wavelength 600 nm is incident normally from air as shown. For a destructive interference to be observed at R, the minimum value of thickness of the slab t (in nm) is _____

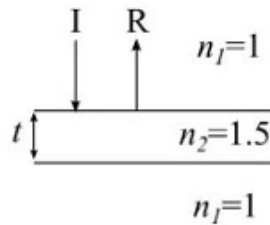


Fig. 22. *

(GATE IN 2020)

- 48) Consider the finite sequence $X = (1, 1, 1)$. The Inverse Discrete Fourier Transform (*IDFT*) of X is given as $(x(0), x(1), x(2))$. The value of $x(2)$ is _____

(GATE IN 2020)

- 49) A circuit consisting of capacitors, DC voltage source and an amplifier having a voltage gain $G = -5$ is shown in the figure. Fig. 23 The effective capacitance across the nodes A and B is _____ (in μF , rounded off to one decimal place)

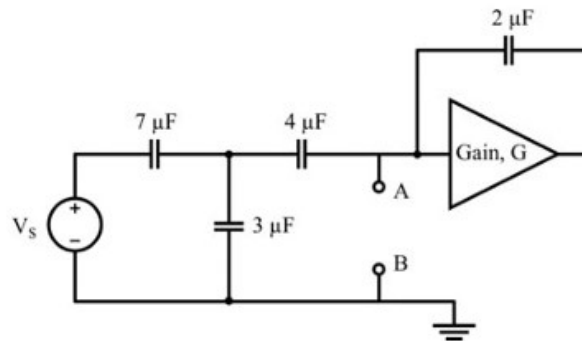


Fig. 23. *

(GATE IN 2020)

- 50) Consider the following state variable equations:

$$\dot{x}_1(t) = x_2(t)$$

$$\dot{x}_2(t) = -6x_1(t) - 5x_2(t)$$

The initial conditions are $x_1(0) = 0$ and $x_2(0) = 1$. At $t = 1$ second, the value of $x_2(1)$ is _____ (rounded off to two decimal places)

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- 51) Assume the diodes in the circuit shown Fig. 24 are ideal. The current I_x flowing through the $3 \text{ k}\Omega$ resistor (in mA, rounded off to one decimal place) is _____

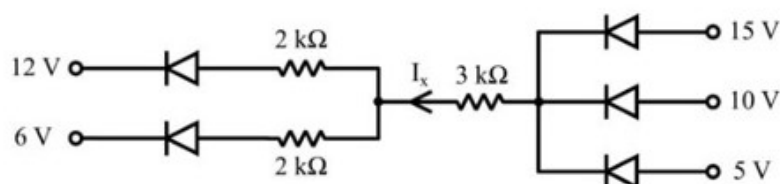


Fig. 24. *

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- 52) A 1000/1 A, 5 VA, UPF bar-primary measuring current transformer has 1000 secondary turns. The current transformer exhibits a ratio error of -0.1% and a phase error of 3.438 minutes when the primary current is 1000 A. At this operating condition, the rms value of the magnetization current of the current transformer (in amperes, rounded off to two decimal places) is _____

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- 53) The mutual inductances between the primary coil and the secondary coils of a linear variable differential transformer (LVDT) shown in the figure Fig. 25 are M_1 and M_2 . Assume that the self-inductances L_{s1} and L_{s2} remain constant and are independent of x . When $x = 0$, $M_1 = M_2 = M_0$. When x is in the range ± 10 mm, M_1 and M_2 change linearly with x . At $x = +10$ mm or -10 mm, the change in the magnitudes of M_1 and M_2 is $0.25M_0$. For a particular displacement $x = D$, the voltage across the detector becomes zero when $|V_2| = 1.25|V_1|$. The value of D (in mm, rounded off to one decimal place) is _____

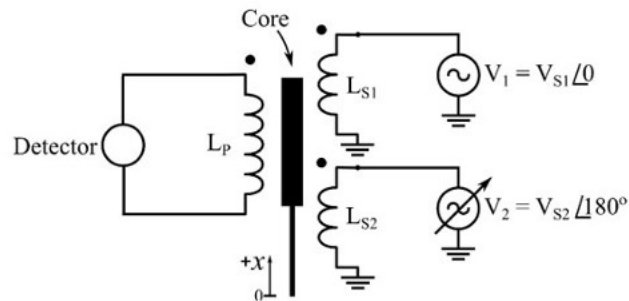


Fig. 25. *

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- 54) In the Maxwell-Wien bridge shown, Fig. 26 the detector D reads zero when $C_1 = 100$ nF and $R_1 = 100$ k Ω . The Q factor of the coil is _____

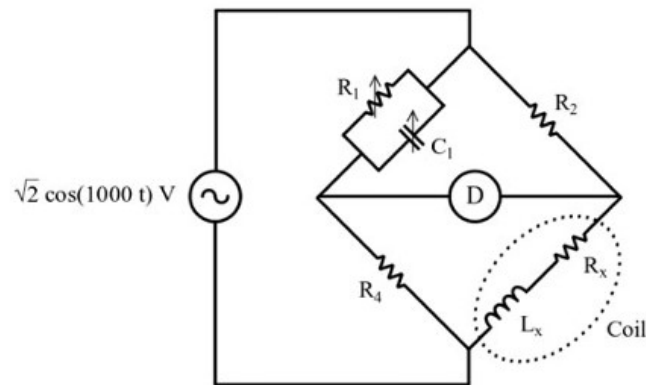


Fig. 26. *

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- 55) The loop transfer function of a negative feedback system is $G(s)H(s) = \frac{2(s+1)}{s^2}$. The phase margin of the system (in degrees, rounded off to one decimal place) is _____

(GATE IN 2020)