METALLURGY ENGINEERING

GATE 2021 EE25BTECH11027-INDHIRESH S

GENERAL APTITUDE

Q1 - Q5 carry one mark each (for each wrong answer: - 1/3)
1) Five persons P, Q, R, S and T are to be seated in a row, all facing the same direction,
but not necessarily in the same order. P and T cannot be seated at either end of the

b) 3

2) Consider the following sentences:

is:

a) 2

row. P should not be seated adjacent to S. R is to be seated at the second position from the left end of the row. The number of distinct seating arrangements possible

P) The number of candidates who appear for the GATE examination is staggering.

Q) A number of candidates from my class are appearing for the GATE examination.

R) The number of candidates who appear for the GATE examination are staggering.

S) A number of candidates from my class is appearing for the GATE examination.

c) 4

(GATE MT 2021)

(GATE MT 2021)

d) 5

	Which of the above	sentences are gramm	atically CORRECT?	
	a) (P) and (Q)	b) (P) and (R)	c) (Q) and (R)	d) (R) and (S)
3)	•	peeps every 30 second or at 10 AM. The immo		•
	a) 10.08 AM	b) 10.42 AM	c) 11.00 AM	d) 10.00 PM
4)	If $\oplus \div \odot = 2$; $\oplus \div 4$ (GATE MT 2021)	$A = 3; \ 2 \times \oplus = 6; \ \Delta > 0$	$\langle \otimes = 10. \text{ Then, the } \rangle$	value of $(\otimes - \oplus)^2$, is:
	a) 0	b) 1	c) 4	d) 16
5)	straight from the bathen turns to his rig	Ir. X's house faces Eack door that is situated that, walks for another and at with respect to the	ed directly opposite t 50 m and stops. The	to the front door. He direction of the point

a) South-East	b) North-East	c) West	d) North-West
Q6 - Q10 carry two	o marks each (for e	ach wrong answei	r: - 2/3).
(GATE MT 2021) Statement 1: All er Statement 2: All w Conclusion I: All r Conclusion II: Only	ntrepreneurs are wea ealthy are risk seeke isk seekers are weal y some entrepreneur	ulthy. ers. lthy. s are risk seekers.	vo conclusions I and II. ne of the following options
is CORRECT?		vinonono, vinion o	no or une renewing opinions
a) Only conclusionb) Only conclusionc) Neither conclusiond) Both conclusions	II is correct on I nor II is correc		
without replacemen		f an outcome in v	valls are selected randomly, which the first selected is a (GATE MT 2021)
a) $\frac{3}{16}$	b) $\frac{45}{236}$	c) $\frac{1}{4}$	d) $\frac{3}{4}$
8) The ratio of the arc of an equilateral tri		circle to the area	of the circumscribed circle (GATE MT 2021)
	A	\mathcal{C}	



Fig. 8.

CIRCLE

a) $\frac{1}{8}$ b) $\frac{1}{6}$ c) $\frac{1}{4}$ d) $\frac{1}{2}$

- 9) Consider a square sheet of side 1 unit. The sheet is first folded along the main diagonal. This is followed by a fold along its line of symmetry. The resulting folded shape is again folded along its line of symmetry. The area of each face of the final folded shape, in square units, equal to

 (GATE MT 2021)
 - a) $\frac{1}{4}$ b) $\frac{1}{8}$ c) $\frac{1}{16}$ d) $\frac{1}{32}$
- 10) The world is going through the worst pandemic in the past hundred years. The air travel industry is facing a crisis, as the resulting quarantine requirement for travelers

led to weak demand. In relation to the first sentence above, what does the second sentence do? (GATE MT 2021)

- a) Restates an idea from the first sentence.
- b) Second sentence entirely contradicts the first sentence.
- c) The two statements are unrelated.
- d) States an effect of the first sentence.

METALLURGICAL ENGINEERING

Q1 - Q13 carry one mark each

1) For the matrix given below, the eigenvalues are: (GATE MT 2021)

$$\begin{pmatrix} 1 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 1 \end{pmatrix} \tag{1}$$

- a) 0, 2, 2
- b) 1, 1, 2
- c) 0, 1, 2
- d) 0, 1, 3
- 2) Which one of the following is a homogeneous function of degree three? (GATE MT 2021)
 - a) $x^3 + 2x^2y^2$

c) $y^3 + 2x^2$ d) $xy^2 + 3xy$

b) $v^2x + 2vx^2$

- 3) The divergence of a vector field V(x, y, z), where its three components (V_x, V_y, V_z) are functions of x, y, z, is: (GATE MT 2021)
 - a) $\frac{\partial V_x}{\partial x} + \frac{\partial V_y}{\partial y} + \frac{\partial V_z}{\partial z}$ c) $\frac{\partial V_x}{\partial x} i + \frac{\partial V_y}{\partial y} j + \frac{\partial V_z}{\partial z} k$ b) $(\frac{\partial V_z}{\partial y} \frac{\partial V_y}{\partial z})i + (\frac{\partial V_x}{\partial z} \frac{\partial V_z}{\partial x})j + (\frac{\partial V_y}{\partial x} \frac{\partial V_x}{\partial y})k$ d) $\frac{\partial^2 V_x}{\partial z^2} + \frac{\partial^2 V_y}{\partial z^2} + \frac{\partial^2 V_z}{\partial z^2}$
- 4) Which one of the following is 'center split' defect in rolling operation? (GATE MT 2021)

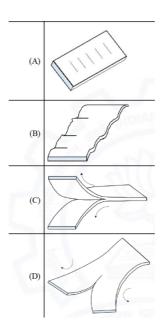


Fig. 4.

ROLLING OPERATION

- 5) Single crystal turbine blades of nickel-based superalloys for aero-engines are manufactured using: (GATE MT 2021)
 - a) Investment casting
 - b) Die casting

- c) Squeeze casting
- d) Directional solidification
- 6) Elements A and B have the same crystal structure. For a dilute solution of B in A, which one of the following is true? (GATE MT 2021)

(Given: ΔH_{mix} - Mixing enthalpy, a_B - Activity of B and X_B - Mole fraction of B)

- a) If $\Delta H_{mix} = 0$ then $a_B < X_B$
- c) If $\Delta H_{mix} > 0$, then $a_B > X_B$ d) If $\Delta H_{mix} < 0$, then $a_B < X_B$
- b) If $\Delta H_{mix} = 0$ then $a_B > X_B$
- 7) For uniaxial tensile stress-strain behaviour of polycrystalline aluminium, which one of the following statements is FALSE? (GATE MT 2021)
 - a) True stress is always higher than the engineering stress.
 - b) At the ultimate tensile stress point on the true stress strain curve, $\frac{d\sigma}{d\epsilon} = 0$
 - c) Resilience is the area under the elastic region of the engineering stress strain curve.
 - d) Maximum true stress does not correspond to the maximum load.
- 8) Which one of the following is FALSE for creep deformation? (GATE MT 2021)
 - a) The minimum creep rate is obtained in the primary stage (stage I).

(c) Coble creep occu	decreases with decre ars via grain boundar creep occurs via latt	y diffusion.	
	Which one of the (GATE MT 2021)	following elements	alloyed with iron is	a ferrite stabilizer?
í	a) Nickel	b) Manganese	c) Carbon	d) Silicon
		ollowing is the correct in heat treatment of	ct decreasing sequence f steels?	of Quenching Power (GATE MT 2021)
	a) Oil > Water > Ba b) Brine > Oil > Water		c) Brine > Water >d) Water > Brine >	
	For a zeroth order (GATE MT 2021)	chemical reaction,	which one of the f	following is FALSE?
ł	i) Increase in conceii) Half-life depends		species increases the rantration and zero-order	
	Which one of the process?	following elements of	oxidizes first in basic	oxygen steel making (GATE MT 2021)
í	a) Silicon	b) Carbon	c) Manganese	d) Phosphorus
13)	Which one of the fo	ollowing is a hydrom	netallurgical operation?	(GATE MT 2021)
á	a) Roasting	b) Leaching	c) Zone refining	d) Smelting
).carry ONE mark each	_
	The value of lim (GATE MT 2021)	$\lim_{x\to 0} \frac{\sin^2 5x}{\sin^2 4x}$ is:	(round off	to nearest integer).
15)	The grain size (X) a mean (μ) of 5 μ specimens with gra (round off to neares Given: For the s $(GATE\ MT\ 2021)$	m and a standard do in size in the range s st integer). ymmetric distribution	nens follows a symmer eviation (σ) of 0.5 μ r 5 to 6 μ m is expected on: Probability P(X \le 1)	n. The percentage of to be: $\mu + 2\sigma = 0.98$
16)	If $E_{Ni^{2+}/Ni}^{\theta} = -0.25$ (round off to neares	V, the value of μ_{Ni}^{θ} st integer).	$_{2+}$ (in J mol ⁻¹) at 298	8 K is:
17)	Given: F=96500 C Melting point of Cu	mol^{-1} is $1358K$ and its ent	chalpy of melting is 13- liquid to solid transfo	

Assume: $C_p^{liquid} = C_p^{solid}$ (GATE MT 2021)

18) A body is subjected to a state of stress given by the following stress tensor: (GATE MT 2021)

$$\begin{pmatrix}
50 & 0 & -0 \\
0 & 200 & 0 \\
0 & 0 & 100
\end{pmatrix}
\tag{2}$$

If yielding is predicted by the Tresca Criterion, the uniaxial tensile yield stress (in MPa) of the body should be less than or equal to: (round off to nearest (GATE MT 2021) integer).

- 19) Consider homogeneous nucleation of a spherical solid in liquid. For a given undercooling, if surface energy of a nucleus increases by 20%, the corresponding increase (in percent) in the critical radius of the nucleus is: _____ (round off (GATE MT 2021) to nearest integer).
- 20) If saturation magnetization of iron at room temperature is $1700kAm^{-1}$, the magnetic moment (in A m^2) per iron atom in the crystal is: _____ x 10^{-23} (round off to 1 decimal place).
 - (Given: Lattice parameter of iron at room temperature = 0.287 nm) (GATE MT 2021)
- 21) In the X-ray diffraction pattern of a FCC crystal, the first reflection occurs at a Bragg angle (θ) of 30°. The Bragg angle (in degree) for the second reflection will be: (round off to 1 decimal place). (GATE MT 2021)
- 22) A 0.6wt.%C steel sample is slowly cooled from 900°C to room temperature. The fraction of proeutectoid ferrite in the microstructure is: _____ (round off to 2 decimal places).

Given: Eutectoid composition: 0.8wt.%C

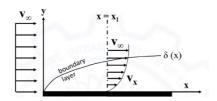
Maximum solubility of carbon in α -Fe: 0.025wt.%C

(GATE MT 2021)

- 23) If the degree of polymerization of polyethylene is 30000, the average molecular weight $(in \ g \ mol^{-1})$ is: (round off to nearest integer). (Given: Atomic weights of carbon and hydrogen are 12 and 1, respectively) (GATE MT 2021)
- 24) Water flows over a plate of finite length. At $x = x_1$ from the leading edge, the velocity of the flow is $V_x = 0.5y - 0.5y^3$. The thickness, δ (in meter) of the boundary layer at $x = x_1$ is: _____ (round off to 2 decimal places).

Given: V_{∞} is the free stream velocity.

(GATE MT 2021)



25) The vacancy concentration in a crystal doubles upon increasing the temperature from 27°C to 127°C. The enthalpy (in $kJmol^{-1}$) of vacancy formation is: _____ (round off to 2 decimal places).

Given: $R = 8.314 \text{ J} \ mol^{-1} K^{-1}$ (GATE MT 2021)

Q36 - Q65 Multipe choice question carry two marks each (for each wrong answer: - 2/3)

- 26) The minimum value of y for the equation $y = x^2 2x + 4$ is (GATE MT 2021)
 - a) 3 b) 1 c) 4
- d) 6
- 27) Match the forming process (in Column I) with its name (in Column II): (GATE MT 2021)

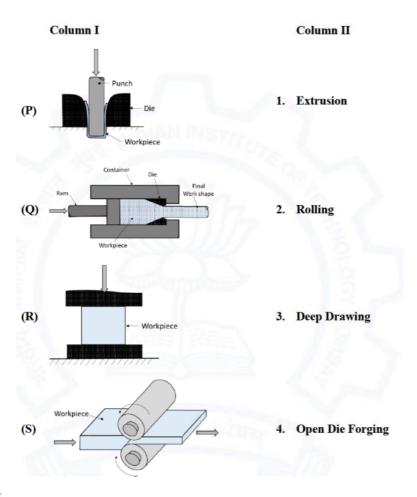


Fig. 27.

a)
$$P-1, Q-2, R-3, S-4$$

b)
$$P-3, \tilde{Q}-1, R-4, S-2$$

c)
$$P-3$$
, $Q-4$, $R-1$, $S-2$
d) $P-1$, $Q-4$, $R-3$, $S-2$

d)
$$P-1, Q-4, R-3, S-2$$

28) Match the nondestructive technique (in Column I) with its underlying phenomenon (in Column II): (GATE MT 2021)

C_{Λ}	umn	1
COL	umn	

- (P) Dye penetrant test
- (Q) Radiography
- (R) Eddy current test
- (S) Ultrasonic inspection

Column II

- 1. X-ray absorption
- 2. Capillary action
- 3. Elastic waves reflection
- 4. Electromagnetic induction

a)
$$P-4, Q-3, R-2, S-1$$

c)
$$P-2, Q-1, R-4, S-3$$

b)
$$P-2$$
, $Q-1$, $R-3$, $S-4$

d)
$$P-3$$
, $Q-2$, $R-1$, $S-4$

29) Number of degrees of freedom for the following reacting system is: (GATE MT 2021)

$$M(s) + CO_2(g) = MO(s) + CO(g)$$
(3)

a) 0

b) 1

c) 2

d) 3

30) The condition for getting the binary phase diagram of A-B (shown below) is: (GATE MT 2021)

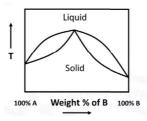


Fig. 30.

BINARY PHASE DIAGRAM

Given: ΔH_{mix}^{solid} - Enthalpy of mixing of solid ΔH_{mix}^{liquid} - Enthalpy of mixing of liquid

- a) $\Delta H_{mix}^{solid} = 0$ and $\Delta H_{mix}^{liquid} = 0$ c) $\Delta H_{mix}^{solid} > 0$ and $\Delta H_{mix}^{liquid} = 0$ b) $\Delta H_{mix}^{solid} < 0$ and $\Delta H_{mix}^{liquid} = 0$ d) $\Delta H_{mix}^{solid} = 0$ and $\Delta H_{mix}^{liquid} < < 0$

- 31) In the absence of any external stress, which one of the following statements related to the interaction of point defect and a dislocation is FALSE: (GATE MT 2021)
 - a) An oversized solute atom would preferentially migrate below the slip plane of an edge dislocation

- b) A spherically symmetric point defect can interact with both the hydrostatic and shear stress fields of a dislocation.
- c) A point defect can locally modify the elastic modulus and thereby can change the interaction energy
- d) Vacancies are attracted towards the compressive region of dislocation.
- 32) A single crystal aluminium sample is subjected to uniaxial tension along [112] direction. If the applied tensile stress is 100 MPa and the critical resolved shear stress (CRSS) is 25 MPa, which one of the following slip systems will be activated?

 (GATE MT 2021)
 - a) [101](111) b) [110](111) c) [101](111) d) [011](111)
- 33) One-dimensional steady-state temperature distribution in two adjacent refractory blocks (with thermal conductivities, k1 and k2) of unit cross- sectional area are shown below. The temperature T1 and thermal contact resistance of the interface, respectively, are:

 (GATE MT 2021)

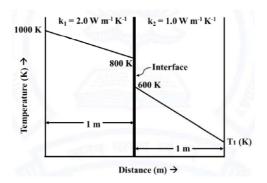


Fig. 33.

ADJACENT REFRACTORY BLOCKS

a) 200K, $0.5KW^{-1}$

c) 200K, $0.25KW^{-1}$

b) 400K, $1KW^{-1}$

- d) 500K, $0.5KW^{-1}$
- 34) For a fully developed 1-D flow of a Newtonian fluid through a horizontal pipe of radius R (see figure), the axial velocity (V_z) is given by:

$$V_z = \left[\frac{\Delta P}{L}\right] \left(\frac{R^2 - r^2}{4\mu}\right),\tag{4}$$

where, ΔP is the pressure difference (P1 - P2), μ is the viscosity, r is the radial distance from the axis and L is the length of the tube. The shear stress exerted by the fluid on the tube wall is:

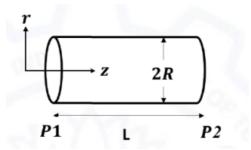


Fig. 34.

HORIZONTAL PIPE

(GATE MT 2021)

- a) $\frac{\Delta PR}{2I}$
- b) $\frac{\Delta PR}{I}$
- c) $\frac{3\Delta PR}{2L}$
- d) $\frac{2\Delta PR}{I}$
- 35) Match the terms (in Column I) with the unit process (in Column II) (GATE MT 2021)

Column I

(P) Submerged Entry Nozzle

- (Q) Electric Heating
- (R) Raceway Zone
- (S) Oxygen Lancing
- in Column II
- 1. Ladle Furnace
- 2. Continuous Casting
- 3. LD Converter
- 4. Blast Furnace

a)
$$P-2, Q-1, R-4, S-3$$

c)
$$P-4, Q-3, R-1, S-2$$

b)
$$P-4, Q-1, R-2, S-3$$

d)
$$P-2, \widetilde{Q}-3, R-4, S-1$$

36) A blast furnace uses hematite ore with 80% Fe_2O_3 and 20% gangue materials. It uses 600 kg coke per ton of hot metal. The coke contains 85% C and 15% ash. The composition of hot metal is 95.5% Fe and 4.5%C. The weight of iron ore used and slag produced per ton of hot metal respectively, are:

Assume that the gangue materials of the ore and ash content of coke form slag while Fe2O3 in the ore is consumed in making hot metal. (GATE MT 2021)

a) 1705kg, 431kg

c) 1705kg, 331kg

b) 2131kg, 546kg

d) 1500kg, 431kg

Q.37-Q.55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).

- 37) Consider the function $f(x) = x \cos x$. Using Newton-Raphson method, the estimated root of f(x) after the first iteration is: _______. (round off to 3 decimal places). Assume: Initial guess of the root = 0.5 radians (GATE MT 2021)
- 38) The work done by a force $\mathbf{F} = 2x\mathbf{i} + 3y\mathbf{j}$ along a straight line from point (0,0) to (1,2) is: ______ . (GATE MT 2021)

39) A coin is tossed three times. Given that there are more heads than tails, the probability of getting exactly one tail is: _______. (round off to 2 decimal places). (GATE MT 2021)

40) A continuous fillet weld is made using a 3000W welding machine. At a travel speed of $6 \text{ } mms^{-1}$, the cross-sectional area ($in \text{ } mm^2$) of the weld is: ______. (round off to nearest integer).

Given: The unit energy required to melt the metal is 6 Jmm^{-3} .

Heat transfer factor = 0.6

Melting factor = 0.5

(GATE MT 2021)

- 41) Liquid iron is cast into a spherical sand mold (6 cm radius) and a cubical sand mold (12 cm edge length). If solidification time is 60 minutes in the spherical casting, the time (in minutes) required to solidify in the cubical casting is: ______. (round off to nearest integer). (GATE MT 2021)
- 42) True strain for 60% height reduction of a sample subjected to hot forging is:______. (round off to 2 decimal places). (GATE MT 2021)
- 43) For the equilibrium reaction: $2Cu(s) + SO_2(g) = Cu_2S(s) + O_2(g)$, the value of $\ln \frac{Po_2}{P_{SO_2}}$ at 973 K is _____. (round off to 2 decimal places). Given: $2Cu(s) + 0.5SO_2(g) = Cu_2S(s) \Delta G^{\circ}$ at 973 K = -100kJ

 $SO_2(g) = 0.5S_2 + O_2(g) \Delta G^{\circ}$ at 973 K = 292kJ

 $R = 8.314 J mol^{-1} K^{-1}$

Assume: Cu and Cu_2S are pure solids.

(GATE MT 2021)

- 44) One mole of an ideal gas at 10 atm. and 300 K undergoes reversible adiabatic expansion to a pressure of one atm. The work done (in Joule) by the gas is:

 . (round off to nearest integer). (GATE MT 2021)
- 45) The figure shows the entropy versus temperature (S-T) plot of a reversible cycle of an engine. If $T_1 = 200K$ and $T_2 = 600K$, the efficiency of the engine (in percent) is:

 . (round off to nearest integer). (GATE MT 2021)

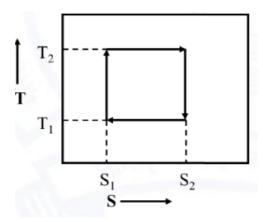


Fig. 45.

46) Two dislocation lines parallel to z - axis lying in the x - z plane are shown in the figure. The glide force (in Newton) exerted by the edge dislocation on the screw dislocation is:

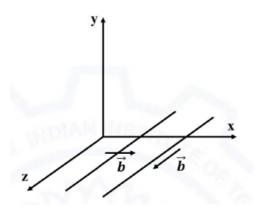


Fig. 46.

3D PLANE

For the edge, the shear stress component is given by:

$$\tau_{xy} = \frac{Gb}{2\pi(1-\nu)} \frac{x(x^2 - y^2)}{(x^2 + y^2)^2}$$
 (5)

Given: Shear modulus, G = 28GPa

Poisson's ratio, v = 0.3

Burgers vector, b = 0.29nm

Distance between the two dislocations = 0.5 nm

- 47) In a material, a shear stress of 100*MPa* is required to bow a dislocation line between precipitates with a spacing of 0.2μ*m*. If the spacing between the precipitates is increased to 0.5μ*m*, the shear stress (in MPa) to bow the dislocation would be:

 . (round off to nearest integer). (GATE MT 2021)
- 48) A metal plate is in a state of plane strain ($\epsilon_{zz} = 0$) with $\sigma_{xx} = \sigma_{yy} \neq 0$ and $\tau_{xy} = \tau_{xz} = \tau_{yz}$ If the Poisson's ratio is 0.3, the ratio, σ_{zz}/σ_{xx} . (round off to 1 decimal places). (GATE MT 2021)
- 49) An infinite metal plate has a central through-thickness crack of length $\frac{80}{\pi}$ mm. The maximum applied stress (in MPa) that the plate can sustain in mode I is:
 ________. (round off to nearest integer).

Assume: Linear elastic fracture mechanics is valid

Given: Fracture toughness, $K_{IC} = 20MPa m^{1/2}$ (GATE MT 2021)

50) A hypothetical binary eutectic phase diagram of A-B is shown below. An alloy with 5wt.% B solidifies with no convection. Assuming steady state, the critical temperature gradient (in K mm⁻¹) required to maintain planar solidification front is: _______. (round off to nearest integer). (GATE MT 2021)

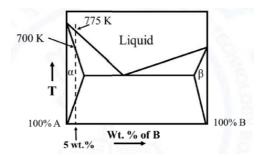


Fig. 50

(GATE MT 2021)

rig. J	PHASE DIAGRAM
51)	Given: Diffusivity of B in liquid = $10^{-9}m^2s^{-1}$ Velocity of solidification front = $4 \mu m s^{-1}$ A thick steel plate containing $0.1wt.\%C$ is carburized at $950^{\circ}C$. The plate's surface carbon concentration is maintained at $1.1wt.\%C$. After 9 hours, the depth (in mm) below the surface at which the carbon concentration is $0.6wt.\%C$ will be: (round off to 2 decimal places). (GATE MT 2021)
	Given: Diffusivity of carbon in $\gamma - Fe$ at $950^{\circ}C = 1.6 \times 10^{-11} m^2 s^{-1}$
	Error function table: z
52)	erf(z) 0.3794 0.4284 0.4755 0.5205 0.5633 0.6039 At 25° $^{\circ}C$, iron corrodes in a deaerated acid of pH 3 with a corrosion current density of $4\mu A\ cm^{-2}$. The corrosion potential (V) is: (round off to 2 decimal
	places). (GATE MT 2021)
	Given: $\beta_c = 0.1V$ per decade of current density
	Exchange current density of hydrogen on iron surface = $10^{-9} A cm^{-2}$ R = $8.314 Jmol^{-1} K^{-1}$, $F = 96500 Cmol^{-1}$
	All potentials are with reference to standard hydrogen electrode.
53)	The radius of an interstitial atom which just fits (without distorting the structure) inside an octahedral void of a bcc-iron crystal (in nm) is: (round off
	to 3 decimal places). Assume the radius of Fe atom to be 0.124 <i>nm</i> (GATE MT 2021)
54)	Assume the radius of Fe atom to be 0.124 <i>nm</i> (GATE MT 2021) Nickel undergoes isothermal oxidation at 800 <i>K</i> for a duration of 400 <i>s</i> resulting in a
54)	weight gain of 2 mg cm^{-2} . The weight gain (mg cm^{-2}) after a duration of 1600 s is:
	. (round off to nearest integer). (GATE MT 2021)
	Assume: Weight gain is proportional to square root of time
55)	A solid sphere $(0.5\ m\ radius)$ is enclosed within a larger hollow sphere $(1\ m\ radius)$,
	as shown in figure. The radiation exchange takes place between the outer surface
	(surface 1) of the small sphere and the inner surface (surface 2) of the bigger sphere.
	The value of the view factor, F_{22} is: (round off to 2 decimal places).

Given: View factor (F_{ij}) is the fraction of the radiation leaving surface i that is intercepted by surface j.

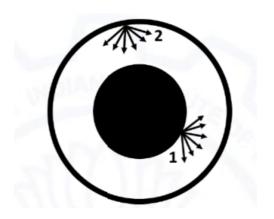


Fig. 55.

SOLID SPHERE

END OF THE QUESTION PAPER