1.5.31

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August 29,2025

Question

Problem

Find the coordinates of a point **P**, which lies on the line segment joining the points **A** (-2,2) and **B** (2,-4) such that $AP = \frac{3}{7}AB$.

Solution Process

Given:

$$\mathbf{A} = \begin{bmatrix} -2 \\ 2 \end{bmatrix}, \quad \mathbf{B} = \begin{bmatrix} 2 \\ -4 \end{bmatrix}, \quad AP = \frac{3}{7}AB$$

Step 1: Section formula

$$\mathbf{P} = \mathbf{A} + \frac{AP}{AB}(\mathbf{B} - \mathbf{A})$$

Step 2: Substitution

$$\mathbf{P} = \mathbf{A} + \frac{3}{7}(\mathbf{B} - \mathbf{A})$$

$$\mathbf{B} - \mathbf{A} = \begin{bmatrix} 2 \\ -4 \end{bmatrix} - \begin{bmatrix} -2 \\ 2 \end{bmatrix} = \begin{bmatrix} 4 \\ -6 \end{bmatrix}$$
$$\frac{3}{7}(\mathbf{B} - \mathbf{A}) = \begin{bmatrix} \frac{12}{7} \\ -\frac{18}{7} \end{bmatrix}$$

Final Answer

$$\mathbf{P} = \begin{bmatrix} -2\\2 \end{bmatrix} + \begin{bmatrix} \frac{12}{7}\\-\frac{18}{7} \end{bmatrix} = \begin{bmatrix} -\frac{2}{7}\\-\frac{4}{7} \end{bmatrix}$$

$$\mathbf{P} = \begin{bmatrix} -\frac{2}{7}\\-\frac{4}{7} \end{bmatrix} \quad \Rightarrow \quad \mathbf{P} \left(-\frac{2}{7}, -\frac{4}{7} \right)$$

C Code

Python Code (1/2)

```
import ctypes
# Load shared library
lib = ctypes.CDLL('./libsection_formula.so')
lib.find_section_point.argtypes = [
    ctypes.c_double, ctypes.c_double, ctypes.c_double,
    ctypes.c_double, ctypes.c_double, ctypes.c_double,
    ctypes.POINTER(ctypes.c_double), ctypes.POINTER(ctypes.c_double)
lib.find section point.restype = None
def find_section_point(x1, y1, x2, y2, m, n):
   x = ctypes.c double()
   y = ctypes.c double()
   lib.find_section_point(x1, y1, x2, y2, m, n, ctypes.byref
   return (x.value, y.value)
```

Python Code (2/2)

```
# Given points
A = (-2, 2)
B = (2, -4)

# Find P such that AP:PB = 3:4
P = find_section_point(A[0], A[1], B[0], B[1], 3, 4)
P_formatted = (round(P[0], 2), round(P[1], 2))
print(f"P: {P_formatted}")
```

Plot of Line Segment AB and Point P



