GATE(2023)

Aerospace Engineering (AE)

Q.1 - Q.5 carry one mark each.

1) A student is required to demonstrate a high level of *comprehension* of the subject, especially in the social sciences.
The word closest in meaning to *comprehension* is
a) understanding
b) meaning
c) concentration
d) stability

(GATE AE 2014)

2) Choose the most appropriate word from the options given below to complete the following sentence.
One of his biggest _____ was his ability to forgive.
a) vice
b) virtues
c) choices
d) strength

(GATE AE 2014)

3) Rajan was not happy that Sajan decided to do the project on his own. On observing his unhappiness, Sajan explained to Rajan that he preferred to work independently. Which one of the statements below is logically valid and can be inferred from the above sentences?
a) Rajan has decided to work only in a group.
b) Rajan and Sajan were formed into a group against their wishes.
c) Sajan had decided to give in to Rajan's request to work with him.
d) Rajan had believed that Sajan and he would be working together.

(GATE AE 2014)

4) If $y = 5x^2 + 3$, then the tangent at $x = 0, y = 3$
a) passes through $x = 0, y = 0$
b) has a slope of $+1$
c) is parallel to the x-axis
d) has a slope of -1

(GATE AE 2014)

5) A foundry has a fixed daily cost of Rs 50,000 whenever it operates and a variable cost of Rs $800Q$, where Q is the daily production in tonnes. What is the cost of production in Rs per tonne for a daily production of 100 tonnes?

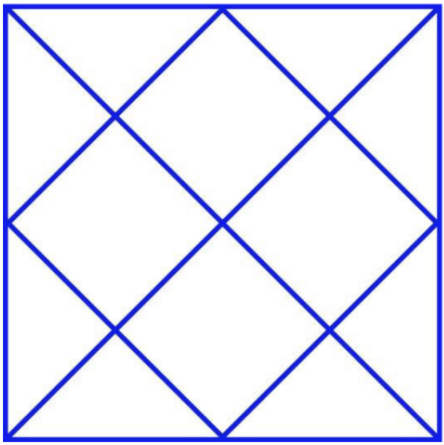

Fig. 1

Q.6 - Q.10carry two mark each.

6) Find the odd one in the following group:

ALRVX, EPVZB, ITZDF, OYEIK

a) ALRVX
b) EPVZB
c) ITZDF
d) OYEIK

(GATE AE 2014)

7) Anuj, Bhola, Chandan, Dilip, Eswar and Faisal live on different floors in a six-storeyed building (the ground floor is numbered 1, the floor above it 2, and so on). Anuj lives on an even-numbered floor. Bhola does not live on an odd numbered floor. Chandan does not live on any of the floors below Faisal's floor. Dilip does not live on floor number 2. Eswar does not live on a floor immediately above or immediately below Bhola. Faisal lives three floors above Dilip. Which of the following floor-person combinations is correct?

	Anuj	Bhola	Chandan	Dilip	Eswar	Faisal
(A)	6	2	5	1	3	4
(B)	2	6	5	1	3	4
(C)	4	2	6	3	1	5
(D)	2	4	6	1	3	5

(GATE AE 2014)

8) The smallest angle of a triangle is equal to two thirds of the smallest angle of a quadrilateral. The ratio between the angles of the quadrilateral is 3 : 4 : 5 : 6. The largest angle of the triangle is twice its smallest angle. What is the sum, in degrees, of the second largest angle of the triangle and the largest angle of the quadrilateral?

(GATE AE 2014)

9) One percent of the people of country X are taller than 6 ft. Two percent of the people of country Y are taller than 6 ft. There are thrice as many people in country X as in country Y. Taking both countries together, what is the percentage of people taller than 6 ft?

a) 3.0
b) 2.5
c) 1.5
d) 1.25

(GATE AE 2014)

10) The monthly rainfall chart based on 50 years of rainfall in Agra is shown in the following figure. Which of the following are true? (k percentile is the value such that k percent of the data fall below that value)

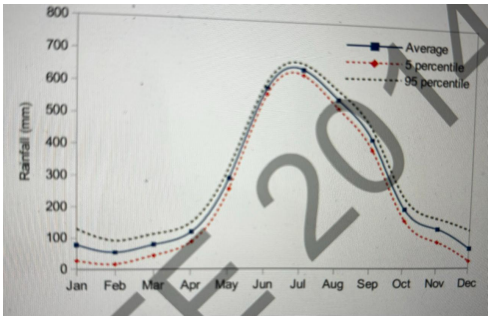

Fig. 2

a) On average, it rains more in July than in December
b) Every year, the amount of rainfall in August is more than that in January
c) July rainfall can be estimated with better confidence than February rainfall
d) In August, there is at least 500 mm of rainfall

a) (i) and (ii)
b) (i) and (iii)
c) (ii) and (iii)
d) (iii) and (iv)

(GATE AE 2014)

Q.1 – Q.25 CARRY ONE MARK EACH

11) For a real symmetric matrix $[A]$, which of the following statements is true?

a) The matrix is always diagonalizable and invertible.

b) The matrix is always invertible but not necessarily diagonalizable.
c) The matrix is always diagonalizable but not necessarily invertible.
d) The matrix is always neither diagonalizable nor invertible.

(GATE AE 2014)

12) The series

$$s = \sum_{m=1}^{\infty} \frac{m^2}{3^m}(x-2)^m$$

converges for all x with $|x-2| \le R$ given by

a) $R = 0$
b) $R = 3$
c) $R = \infty$
d) $R = \frac{1}{3}$

(GATE AE 2014)

13) The function given by

$$f(x) = \begin{cases} \sin\left(\frac{1}{x}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$$

is

a) Unbounded everywhere
b) Bounded and continuous everywhere
c) Bounded but not continuous at $x = 0$
d) Continuous and differentiable everywhere

(GATE AE 2014)

14) Given the boundary-value problem

$$\frac{d}{dx}\left(\frac{dy}{dx}\right) + ky = 0, \quad 0 < x < 1, \quad \text{with } y(0) = y(1) = 0.$$

Then the solutions of the boundary-value problem for $k = 1$ (given by y_1) and $k = 5$ (given by y_5) satisfy:

a) $\int_0^1 y_1 y_5 \, dx = 0$
b) $\int_0^1 \frac{dy_1}{dx}\frac{dy_5}{dx} \, dx = 0$
c) $\int_0^1 y_1 y_5 \, dx \neq 0$
d) $\int_0^1 \left(y_1 y_5 + \frac{dy_1}{dx}\frac{dy_5}{dx}\right) dx = 0$

(GATE AE 2014)

15) The value of

$$I = \int_0^1 1000x^4 \, dx$$

obtained by using Simpson's rule with 2 equally spaced intervals is,

a) 200

b) 400
c) 180
d) 208

(GATE AE 2014)

16) For a *NACA* 5-digit airfoil of chord c, the designed lift coefficient and location of maximum camber along the chord from the leading edge are denoted by C_L and X_m respectively. For *NACA12018* airfoil, which combination of C_L and X_m given below are correct?

a) $C_L = 0.15$ and $X_m = 0.1c$
b) $C_L = 0.12$ and $X_m = 0.2c$
c) $C_L = 0.12$ and $X_m = 0.18c$
d) $C_L = 0.15$ and $X_m = 0.2c$

(GATE AE 2014)

17) For inviscid, supersonic flow over a diamond shaped airfoil, shown in the figure, which statement is correct among the following?

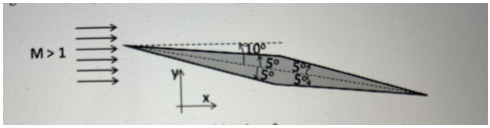

Fig. 3

a) The airfoil will experience zero lift and positive drag force
b) The airfoil will experience positive lift and zero drag force
c) The airfoil will experience negative lift and zero drag force
d) The airfoil will experience positive lift and positive drag force

(GATE AE 2014)

18) Consider supersonic flow near a corner (at an angle θ from the horizontal) with an attached oblique shock (at an angle β with horizontal) as shown in figure. If Mach number M decreases gradually from a high supersonic value, which of the following statements is correct?

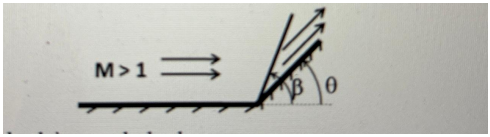

Fig. 4

a) β will decrease if the shock is a weak shock
b) β will decrease if the shock is a strong shock
c) β will increase for both weak and strong shocks
d) β remains unchanged for both weak and strong shocks

(GATE AE 2014)

19) The streamlines of a potential line vortex is concentric circles with respect to the vortex center as shown in figure. Velocity along these streamlines, outside the core of the vortex can be written as,

$$v_\theta = \frac{\Gamma}{2\pi r},$$

where strength of the vortex is Γ and r is radial direction. The value of circulation along the curve shown in the figure is:

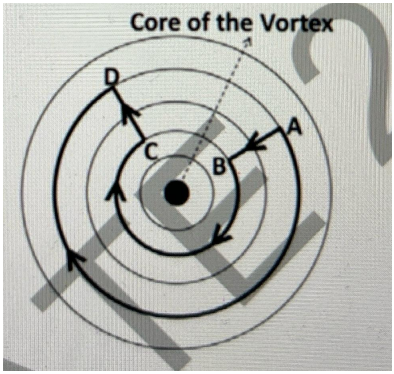

Fig. 5

a) Γ
b) -2Γ
c) 2Γ
d) 0

(GATE AE 2014)

20) To observe unsteady separated flow in a diverging channel, bubbles are injected at each 10 ms interval at point A as shown in figure. These bubbles act as tracer particles and follow the flow faithfully. The curved line AB shown at any instant represents:

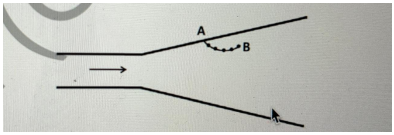

Fig. 6

a) Streamline, streakline and pathline
b) Streamline and pathline
c) Only a pathline
d) Only a streakline

(GATE AE 2014)

21) It is desired to measure the Young's modulus and the Poisson's ratio of a given homogeneous, isotropic material. A bar of length 20 cm and square cross-section

(10 mm × 10 mm) of this material is subjected to a tensile load of 40 kN. Under this load, length increases to 20.1 cm while the cross-section reduces to 9.98 mm × 9.98 mm. Young's modulus and Poisson's ratio of the material are:

a) 80 GPa & 0.4 respectively
b) 40 GPa & − 0.4 respectively
c) 80 GPa & − 0.2 respectively
d) 40 GPa & 0.2 respectively

(GATE AE 2014)

22) In general, for any given solid subjected to arbitrary loading, which of the following statements is *always* true:

a) Volume does not vary with loading
b) Mass does not vary with loading
c) Density does not vary with loading
d) Volume, mass and density vary with loading

(GATE AE 2014)

23) Which one of the following objects with inclined face at 45°, subjected to the given stresses, are in static equilibrium:

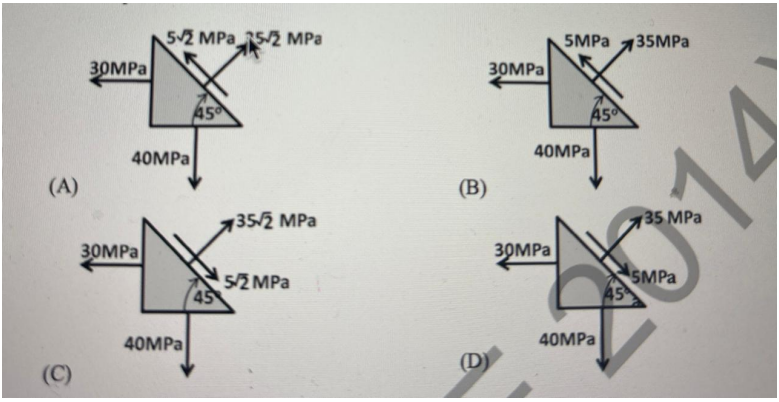

Fig. 7

(GATE AE 2014)

24) A damped single degree of freedom system whose undamped natural frequency, ω_n = 10 Hz, is subjected to sinusoidal external force. Power is half of the maximum for the two frequencies of 60.9469 rad/s and 64.168 rad/s. The damping factor associated with the vibrating system (in %) is:

25) The boundary conditions for a rod with circular cross-section, under torsional vibration, are changed from fixed-free to fixed-fixed. The fundamental natural frequency of the fixed-fixed rod is k times that of fixed-free rod. The value of k is:

a) 1.5
b) π

c) 2.0
d) 0.5

(GATE AE 2014)

26) Match the appropriate engine (in right column) with the corresponding aircraft (in left column) for most efficient performance of the engine.

Left column:	**Right column:**
a) Low speed transport aircraft	a) Ramjet
b) High subsonic civilian aircraft	b) Turboprop
c) Supersonic fighter aircraft	c) Turbojet
d) Hypersonic aircraft	d) Turbofan

a) a – iv, b – iii, c – i, d – ii
b) a – ii, b – i, c – iii, d – iv
c) a – i, b – ii, c – iv, d – iii
d) a – ii, b – iv, c – iii, d – i

(GATE AE 2014)

27) For a given fuel flow rate and thermal efficiency, the take-off thrust for a gas turbine engine burning aviation turbine fuel (considering fuel-air ratio $f \ll 1$) is

a) Directly proportional to exhaust velocity
b) Inversely proportional to exhaust velocity
c) Independent of exhaust velocity
d) Directly proportional to the square of the exhaust velocity

(GATE AE 2014)

28) For a fifty percent reaction axial compressor stage, following statements are given: I. Velocity triangles at the entry and exit of the rotor are symmetrical II. The whirl or swirl component of absolute velocity at the entry of rotor and entry of stator are same.
Which of the following options are correct?

a) Both I and II are correct statements
b) I is correct but II is incorrect
c) I is incorrect but II is correct
d) Both I and II are incorrect

(GATE AE 2014)

29) A small rocket having a specific impulse of $200\,s$ produces a total thrust of $98\,kN$, out of which $10\,kN$ is the pressure thrust. Considering the acceleration due to gravity to be $9.8\,m/s^2$, the propellant mass flow rate in kg/s is

a) 55.1
b) 44.9
c) 50
d) 60.2

(GATE AE 2014)

30) The thrust produced by a turbojet engine

a) Increases with increasing compressor pressure ratio
b) Decreases with increasing compressor pressure ratio
c) Remains constant with increasing compressor pressure ratio
d) First increases and then decreases with increasing compressor pressure ratio

(GATE AE 2014)

31) The moment coefficient measured about the centre of gravity and about aerodynamic centre of a given wing-body combination are 0.0065 and 0.0235 respectively. The aerodynamic centre lies 0.06 chord lengths ahead of the centre of gravity. The lift coefficient for this wing-body is _____.

(GATE AE 2014)

32) The vertical ground load factor on a stationary aircraft parked in its hangar is:
a) 0
b) -1
c) Not defined
d) 1

(GATE AE 2014)

33) Under what condition should a glider be operated to ensure minimum sink rate?
a) Maximum C_L/C_D
b) Minimum C_L/C_D
c) Maximum $C_L/C_D^{3/2}$
d) Minimum $C_L/C_D^{3/2}$

34) In most airplanes, the Dutch roll mode can be excited by applying
a) A step input to the elevators
b) A step input to the rudder
c) A sinusoidal input to the aileron
d) An impulse input to the elevators

(GATE AE 2014)

35) Considering R as the radius of the moon, the ratio of the velocities of two spacecraft orbiting moon in circular orbit at altitudes R and $2R$ above the surface of the moon is _____.

(GATE AE 2014)

Q.26 - Q.55 carry two mark each

36) If

$$A = \begin{pmatrix} 3 & -3 \\ -3 & 4 \end{pmatrix}$$

Then

$$\det\left(-[A]^2 + 7[A] - 3[I]\right) \text{ is}$$

a) 0
b) -324
c) 324
d) 6

(GATE AE 2014)

37) For the periodic function given by

$$f(x) = \begin{cases} -2, & -\pi < x < 0 \\ 2, & 0 < x < \pi \end{cases}$$

with $f(x + 2\pi) = f(x)$, using Fourier series, the sum

$$S = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \cdots$$

converges to

a) 1
b) $\frac{\pi}{3}$
c) $\frac{\pi}{4}$
d) $\frac{\pi}{5}$

(GATE AE 2014)

38) Let Γ be the boundary of the closed circular region A given by $x^2 + y^2 \leq 1$. Then

$$\oint_{\Gamma} (3x - 5y^3)\, dx$$

(where ds means integration along the bounding curve) is

a) π
b) $-\pi$
c) 1
d) 0

(GATE AE 2014)

39) Solution to the boundary-value problem

$$\frac{d^2u}{dx^2} + u = 5x, \quad 0 < x < 3, \quad u(0) = 0, \quad \frac{du}{dx}(x = 3) = 0$$

is

a) $u(x) = \frac{-15e}{1+e^3} e^{x-3} + \frac{15e}{1+e^3} e^{-x} + 5x$
b) $u(x) = \frac{15e}{1+e^3} e^{x} + \frac{-15e}{1+e^3} e^{3-x} + 5x$
c) $u(x) = \frac{-15 \sin(x/3)}{\cos(1)} + 5x$
d) $u(x) = \frac{-15 \sin(x/3)}{\cos(1)} + \frac{5}{54} x^3$

(GATE AE 2014)

40) The Laplace transform $L(u(t)) = U(s)$, for the solution $u(t)$ of the problem

$$\frac{d^2u}{dt^2} + 2\frac{du}{dt} = 1, \quad t > 0$$

with initial conditions $u(0) = 0$, $\frac{du}{dt}(0) = 5$ is given by:

a) $\frac{6}{(s+1)^2}$
b) $\frac{5s+1}{(s+1)^2}$
c) $\frac{1-5s}{s(s+1)^2}$
d) $\frac{5s^2+1}{s(s+1)^2}$

(GATE AE 2014)

41) For a steady, incompressible two-dimensional flow, represented in Cartesian coordinates (x, y), a student correctly writes the equation of pathline of any arbitrary particle as

$$\frac{dx}{ax} = \frac{dy}{by}$$

where a and b are constants having unit of (sec^{-1}). If value of a is 5, the value of b is _____.

(GATE AE 2014)

42) Figures (a)-(d) below show four objects. Dimensions and surface conditions of the objects are shown in the respective figures. All four objects are placed independently in a steady, uniform flow of same velocity and the direction of flow is from left to right as shown in (a). The flow field can be considered as 2-D, viscous and incompressible. Following statements are made regarding the drag that these objects experience.

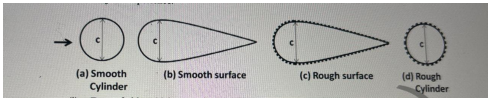

Fig. 8

(i) Drag of object (a) is more than the drag of object (d)
(ii) Drag of object (a) is less than the drag of object (d)
(iii) Drag of object (b) is more than the drag of object (c)
(iv) Drag of object (c) is more than the drag of object (b)
(v) Drag of object (a) is more than the drag of object (b)

Choose the correct combination of statements from the options given above:

a) (i), (iii), (v)
b) (ii), (iv), (v)
c) (i), (iv), (v)
d) (i), (iii)

(GATE AE 2014)

43) A student needs to find velocity across a stationary normal shock. He measures density and pressure across the shock as shown in the figure below. (No shock table is needed for the calculations.) The value of u_1 in m/s is

$$P_1 = 1 \text{ bar} \quad \rho_1 = 1.2 \text{ kg/m}^3 \quad \longrightarrow$$
$$\text{Shock}$$
$$P_2 = 29 \text{ bar} \quad \rho_2 = 6 \text{ kg/m}^3 \quad u_2$$

(GATE AE 2014)

44) For inviscid, compressible flow past a thin airfoil, shown in the figure, free-stream Mach number and pressure are denoted by M_∞ and p_∞ respectively. Ratio of pressure at point A and p_∞ is 0.8 and specific heat ratio is 1.4. If the Mach number at point A is 1.0 and rest of the flow field is subsonic, the value of M_∞ is:

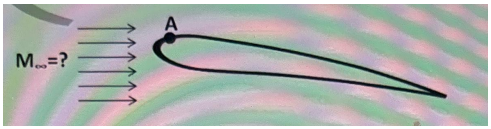

Fig. 9

a) 2.95
b) 0.79
c) 1.18
d) 0.64

(GATE AE 2014)

45) A student can measure free-stream velocity of a low-speed wind tunnel using a:

(i) Pitot tube alone aligned with the flow direction.
(ii) Pitot tube aligned with the flow direction with static pressure measurement at an appropriate position on the tunnel wall.
(iii) Pitot tube aligned with the flow direction along with barometer pressure reading of the outside ambient.
(iv) Pitot static tube alone aligned with the flow direction.

Considering the above statements, which of the following options is correct?

a) (i) only
b) (i) & (ii)
c) (ii) & (iv)
d) (i), (iii) & (iv)

(GATE AE 2014)

46) Induced velocity w at a point $z = z_1$ along the lifting line can be calculated using the formula

$$w(z_1) = -\frac{1}{4\pi}\int_{-S}^{S} \frac{d\Gamma/dz}{z_1 - z}\, dz$$

Given

$$\frac{r^2}{T_0^2} + \frac{z^2}{S^2} = 1$$

where r, T_0 and S are given in the figure below.
For the above semi-elliptic distribution of circulation,

$$\Gamma = \frac{\Gamma_0}{4\pi S}\int_{-S}^{S} \frac{\sqrt{S^2 - z^2}}{z_1 - z}\, dz$$

the downwash velocity at any point z_1 for symmetric flight can be obtained as,

$$w(z_1) = \frac{\Gamma_0}{4\pi S}\left[\pi r + z_1 I_1\right], \quad I_1 = \int_{-S}^{S} \frac{\sqrt{S^2 - z^2}}{z_1 - z}\, dz$$

The induced drag is

$$D_i = \frac{\rho U_\infty}{S}\int_{-S}^{S} \sqrt{1 - \frac{z^2}{S^2}}\, dz = \frac{\pi S}{2}$$

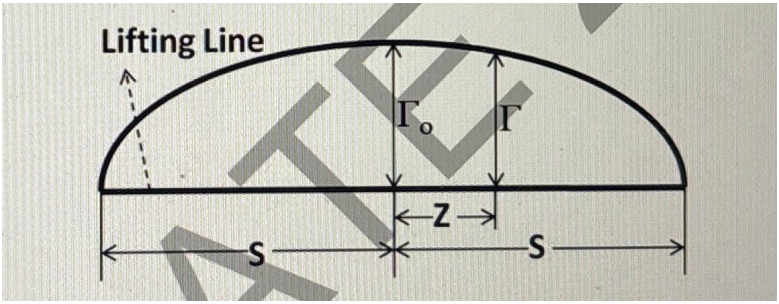

Fig. 10

Which of the following options is correct if the induced drag is D_i (given S)?

a) $l = 0$ and $D_i = \frac{8\rho\Gamma_0^2}{\pi}$
b) $l = l$ and $D_i = \frac{8\rho\Gamma_0^2}{\pi}$
c) $l = 0$ and $D_i = \frac{\pi\rho\Gamma_0^2}{8}$
d) $l = l$ and $D_i = \frac{\pi\rho\Gamma_0^2}{8}$

(GATE AE 2014)

47) Two overflowing water reservoirs are connected with a 100 m long pipe of circular cross-section (of radius $R = 0.02$ m), such that the height difference h remains constant as shown in the figure below.

The centerline velocity in the pipe is 10 m/s. The velocity profile inside the pipe over the entire length is given as

$$u_z(r) = \frac{R^2}{4\mu}\frac{dp}{dx}\left[1 - \frac{r^2}{R^2}\right]$$

where $\frac{dp}{dx}$ is a constant pressure gradient along the pipe length, x is measured from the left end of the pipe along its central axis and r is radial location inside the pipe with respect to its axis.

Given: density and kinematic viscosity of water are 1000 kg/m^3 and 1×10^{-6} m^2/s respectively, acceleration due to gravity is 10 m/s^2.

If all other losses except the frictional losses at the pipe wall are neglected, the value of h in meters is:

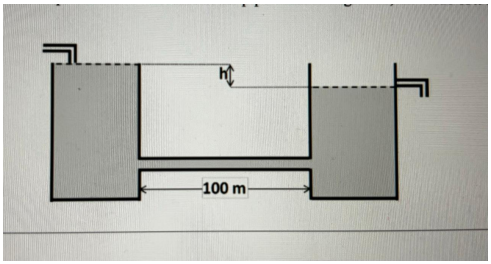

Fig. 11

(GATE AE 2014)

48) A 1.8 m long steel beam of rectangular cross section (10 mm $\times$ 6 mm) is simply supported with a length of 1.2 m between the supports and an overhang of 0.3 m on either side. Young's modulus for the material of the beam is 200 GPa. For a 50 N load applied at the center of the beam, magnitude of the slope of the beam at tip S is:

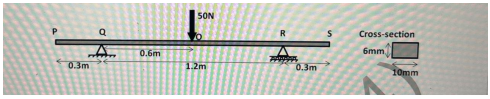

Fig. 12

(GATE AE 2014)

49) There are 2 designs proposed for a shaft of length l, with a torque carrying capacity of T. *Design I* is a solid circular cross-section shaft of diameter 30 mm. *Design II* is a thin-walled circular shaft of average diameter 40 mm. Thickness of the wall in *Design II* has to be determined such that maximum shear stress is the same in both designs for the given torque T. The same material can be used for manufacturing both the shafts. Ratio of mass of shaft using *Design I* to the mass of shaft using *Design II* is:

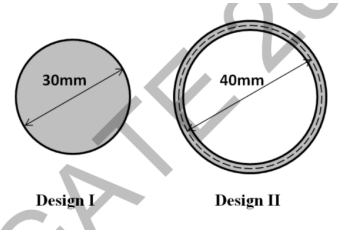

Fig. 13: Caption

a) 2.68
b) 3.56
c) 1.79
d) 3.58

(GATE AE 2014)

50) A structural member of rectangular cross-section (10 mm $\times$ 6 mm) and length 1 m is made of steel (Young's modulus is 200 GPa and coefficient of thermal expansion is $12 \times 10^{-6}/^{\circ}$C). It is rigidly fixed at both the ends and then subjected to a gradual increase in temperature. Ignoring the three dimensional effects, the structural member will buckle if the temperature is increased by ΔT°C which is:

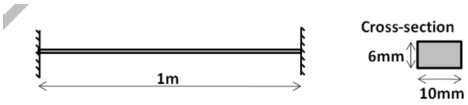

Fig. 14: Caption

a) 19.74
b) 9.87
c) 78.96
d) 39.48

(GATE AE 2014)

51) A gas cylinder (closed thin-walled cylindrical pressure vessel) of diameter 30 cm and wall thickness 1 mm is subjected to a design maximum internal pressure of 5 bar (0.5 MPa). The material used for manufacturing this cylinder has a failure stress of 260 MPa. Assuming von Mises failure criterion, the factor of safety (with respect to maximum allowable stress) for this cylinder is:

a) 2.8
b) 2.0
c) 6.9
d) 4.0

(GATE AE 2014)

52) A cantilevered beam is subjected to a parabolic distribution of shear traction at the right edge while the top and bottom surfaces are traction free. To solve this problem, following Airy's stress function is proposed:

$$\phi = C_1xy + C_2x^3y + C_3x^2y^2 + C_4xy^3$$

This is an admissible Airys function that would satisfy the bi-harmonic equation as well as the boundary conditions if and only if

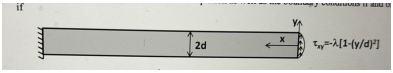

Fig. 15

a) $C_1 = 0,\ C_2 = \lambda,\ C_3 = 0,\ C_4 = \frac{\lambda}{3d^2}$
b) $C_1 = \lambda,\ C_2 = \frac{\lambda}{3d^2},\ C_3 = 0,\ C_4 = 0$
c) $C_1 = 0,\ C_2 = 0,\ C_3 = \lambda,\ C_4 = -\frac{\lambda}{3d^2}$
d) $C_1 = \lambda,\ C_2 = -\frac{\lambda}{3d^2},\ C_3 = 0,\ C_4 = 0$

(GATE AE 2014)

53) 1 kg mass is hanging from a spring of stiffness 500 N/m attached to a massless, symmetric beam of length 0.6 m, moment of inertia about the bending axis $I = 8.33 \times 10^{-10}$ m^4 and Young's modulus $E = 210$ GPa as shown in the figure. The fundamental natural frequency (in rad/s) of the system is:

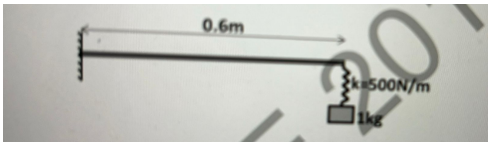

Fig. 16

a) 3.24
b) 20.36
c) 22.36
d) 3.56

(GATE AE 2014)

54) A single degree of freedom system is vibrating with initial (first cycle) amplitude of 5 cm. The viscous damping factor associated with the vibrating system is 2%. Vibration amplitude of the fifth cycle (in cm) is:

a) 1.65
b) 4.41
c) 2.67
d) 3.02

(GATE AE 2014)

55) A cruise missile with an *ideal* ramjet engine is flying at Mach 4.0 at an altitude where the ambient temperature is 100 K. Considering specific heat ratio $\gamma = 1.4$ and specific gas constant $R = 287$ J/kg · K. If the stagnation temperature in the combustion chamber is equal to 2310 K, the speed of the exhaust gases (in m/s) is:

(GATE AE 2014)

56) A gas turbine engine is operating under the following conditions:

Stagnation temperature at turbine inlet	1350 K
Stagnation pressure at the turbine inlet	10 bar
Static temperature at turbine exit	800 K
Velocity at turbine exit	200 m/s
Total-to-total efficiency of turbine	0.96
γ (ratio of specific heats)	1.33
C_p (specific heat at constant pressure)	1.147 kJ/kgK

The stagnation pressure (in bar) in the nozzle (considering isentropic nozzle) is equal to _____.

(GATE AE 2014)

57) Air at a stagnation temperature of 300 K (ratio of specific heats, $\gamma = 1.4$ and specific gas constant $R = 287$ J/kgK) enters the impeller of a centrifugal compressor in axial direction. The stagnation pressure ratio between the diffuser outlet and impeller inlet is 4.0. The impeller blade radius is 0.3 m and it is rotating at 15000 rev/min. If the slip factor σ_s (Ratio of tangential component of air velocity at the blade tip to the blade tip speed) is 0.88, the overall efficiency (total-to-total) of the compressor (in %) is _____.

(GATE AE 2014)

58) A stationary two stage rocket with initial mass of 16000 kg, carrying a payload of 1000 kg, is fired in a vertical trajectory from the surface of the earth. Both the

stages of the rocket have same specific impulse, I_{sp}, of 300 s and same structural coefficient of 0.14. The acceleration due to gravity is 9.8 m/s^2. Neglecting drag and gravity effects and considering both the stages with same payload ratio, the terminal velocity attained by the payload in m/s is _____.

(GATE AE 2014)

59) An aircraft is flying at Mach 3.0 at an altitude where the ambient pressure and temperature are 50 kPa and 200 K respectively. If the converging-diverging diffuser of the engine (considered isentropic with ratio of specific heats, $\gamma = 1.4$ and specific gas constant $R = 287$ J/kgK) has a throat area of 0.05 m^2, the mass flow rate through the engine in kg/s is

a) 197
b) 232
c) 790
d) 157

(GATE AE 2014)

60) A cryogenic rocket has a specific impulse of 455 s and characteristic velocity of 2386 m/s. The value of thrust coefficient for this rocket is

a) 1.78
b) 1.73
c) 1.87
d) 1.95

(GATE AE 2014)

61) For a given airplane with a given wing loading executing a turn in the vertical plane, under what conditions will the turn radius be minimum and the turn rate be maximum?

a) Highest possible C_L and lowest possible load factor
b) Lowest possible C_L and lowest possible load factor
c) Lowest possible C_L and highest possible load factor
d) Highest possible C_L and highest possible load factor

(GATE AE 2014)

62) Lift-off distance for a given aircraft of weight W is S_{L0}. If the take-off weight is reduced by 10%, then the magnitude of percentage change in the lift-off distance (assume all other parameters to remain constant) is _____. (GATE AE 2014)

63) Which of the following design parameters influence the maximum rate-of-climb for a jet-propelled airplane? P. Wing loading
Q. Maximum thrust-to-weight ratio
R. Zero-lift drag coefficient
S. Maximum lift-to-drag ratio

a) P and Q alone
b) P, Q, R and S
c) P, Q and S alone
d) Q, R and S alone

(GATE AE 2014)

64) Consider the following four statements regarding aircraft longitudinal stability:

P. $C_{M_{ac}}$ at zero lift must be positive
Q. $\frac{\partial C_{M_{ac}}}{\partial \alpha}$ must be negative (α is absolute angle of attack)
R. $C_{M_{ac}}$ at zero lift must be negative
S. Slope of C_L versus α must be negative

Which of the following combination is the necessary criterion for stick fixed longitudinal balance and static stability?

a) Q and R only
b) Q, R and S only
c) P and Q only
d) Q and S only

(GATE AE 2014)

65) Data for a light, single-engine, propeller driven aircraft in steady level flight at sea-level is as follows: velocity $V_\infty = 40\,\text{m/s}$, weight $W = 13000\,\text{N}$, lift coefficient $C_L = 0.65$, drag coefficient $C_D = 0.025 + 0.04C_L^2$ and power available $P_a = 100{,}000\,\text{W}$. The rate of climb possible for this aircraft under the given conditions (in m/s) is _____.

a) 7.20
b) 5.11
c) 6.32
d) 4.23

(GATE AE 2014)