GATE 2018

1

EE25BTECH11060 - Namaswi Vajjala

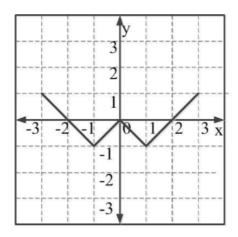
school	e involved	_ that many hands all the students in the the above sentence is	make light work, the task"
a) principle, principal, principal, principal	-	c) principle, prind) principal, prin	
			(GATE ME 2018)
to assist those of	on need."	be confused with miser the above sentence is	liness; she is ever willing
a) cleanliness	b) punctuality	c) frugality	d) greatness
			(GATE ME 2018)
		ake 7 identical toys. At ines to make 100 toys?	the same rate, how many
a) 1	b) 7	c) 100	d) 700
			(GATE ME 2018)
5 m, respective		ss, the rectangle loses	are reduced by 10 m and $650 m^2$ of area. What is
a) 1125	b) 2250	c) 2924	d) 4500
			(GATE ME 2018)

5) A number consists of two digits. The sum of digits is 9. If 45 is subtracted from the

number, its digits are interchanged. What is the number?

a) 6	3	b) 72	c) 81	d) 90		
				(GATE ME 2018)		
Q. 6 - Q. 10 carry one mark each.						
6) For integers a, b and c, what would be the minimum and maximum values respectively of $a + b + c$ if $\log a + \log b + \log c = 0$?						
a) –	3 and 3	b) -1 and 1	c) -1 and 3	d) 1 and 3		
				(GATE ME 2018)		
7) Given that a and b are integers and $a + a^2b^3$ is odd, which one of the following statements is correct?						
a) a and b are both oddb) a and b are both even		c) a is even and b is d) a is odd and b is				
				(GATE ME 2018)		
8) From the time the front of a train enters a platform, it takes 25 seconds for the back of the train to leave the platform, while traveling at a constant speed of 54 km/h. At the same speed, it takes 14 seconds to pass a man running at 9 km/h in the same direction as the train. What is the length of the train and that of the platform in meters, respectively?						
	10 and 140 62.5 and 187.5		c) 245 and 130 d) 175 and 200			

9) Which of the following functions describe the graph shown in the below figure?



a)
$$y = ||x| + 1| - 2$$

c)
$$y = ||x| + 1| - 1|$$

b)
$$y = ||x| - 1| - 1$$

d)
$$y = ||x - 1| - 1|$$

- 10) Consider the following three statements:
 - (i) Some roses are red.
 - (ii) All red flowers fade quickly.
 - (iii) Some roses fade quickly.

Which of the following statement can be logically inferred from the above statements?

- a) If (i) is true and (ii) is false, then (iii) is false.
- b) If (i) is true and (ii) is false, then (iii) is true.
- c) If (i) and (ii) are true, then (iii) is true.
- d) If (i) and (ii) are false, then (iii) is false.

(GATE ME 2018)

END OF THE QUESTION PAPER

O. 1 - O.55 carry one mark each.

- 1) Four red balls, four green balls and four blue balls are put in a box. Three balls are pulled out of the box at random one after another without replacement. The probability that all the three balls are red is (GATE ME 2018)
 - a) $\frac{1}{72}$

b) $\frac{1}{55}$

c) $\frac{1}{36}$

d) $\frac{1}{27}$

2) The rank of matrix

$$\begin{bmatrix} -4 & 1 & -1 \\ -1 & -1 & -1 \\ 7 & -3 & 1 \end{bmatrix}$$
 (2.1)

(GATE ME 2018)

a) 1

b) 2

c) 3

- d) 4
- 3) According to the Mean Value Theorem, for a continuous function f(x) in the interval (a,b), there exists a value ξ in this interval such that $\int_a^b f(x) dx =$ (GATE ME 2018)
 - a) $f(\xi)(b-a)$

c) $f(a)(b - \xi)$ d) 0

b) $f(b)(\xi - a)$

- 4) F(z) be a function of the complex variable z = x + iy given by:

$$F(z) = iz + k \operatorname{Re}(z) + i \operatorname{Im}(z)$$

For what value of k will F(z) satisfy the Cauchy-Riemann equations?

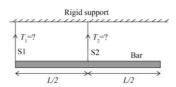
(GATE ME 2018)

a) 0

c) -1

b) 1

- d) v
- 5) A bar of uniform cross-section and weighing 100 N is held horizontally using two massless and inextensible strings S1 and S2 as shown below:



- a) T1=100 N and T2=0N
- b) T1=75 N and T2=25N
- c) T1=0 N and T2=100N
- d) T1=25 N and T2=75N
- 6) If σ_1 and σ_3 are the algebraically largest and smallest principal stresses respectively, the value of the maximum shear stress is

- a) $(\sigma_1 + \sigma_3)/2$ b) $(\sigma_1 \sigma_3)/2$ c) $\sqrt{(\sigma_1 + \sigma_3)/2}$ d) $\sqrt{(\sigma_1 \sigma_3)/2}$
- 7) The equation of motion for a spring-mass system excited by a harmonic force is Mx + $Kx = F \cos(\omega t)$ where M is the mass, K is the spring stiffness, F is the force amplitude and ω is the angular frequency of excitation. Resonance occurs when ω is equal to (GATE ME 2018)
 - a) $\sqrt{(M/K)}$
 - b) $\frac{1}{2\pi} \sqrt{(M/K)}$
 - c) $2\pi \sqrt{(M/K)}$
 - d) $\sqrt{(K/M)}$
- 8) For an Oldham coupling used between two shafts, which among the following statements are correct? I.Torsional load is transferred along shaft axis. II.A velocity ratio of 1:2 between shafts is obtained without using gears. III.Bending load is transferred transverse to shaft axis. IV.Rotation is transferred along shaft axis.

(GATE ME 2018)

- a) I and III
- b) I and IV
- c) II and III
- d) II and IV
- 9) For a two-dimensional incompressible flow field given by

$$\mathbf{u} = A(x\hat{i} - y\hat{j}), where A > 0,$$

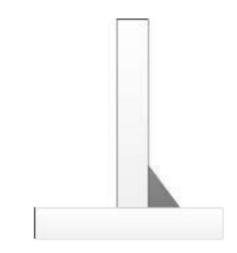
which one of the following statements is **FALSE**?

(GATE ME 2018)

- a) It satisfies continuity equation.
- b) It is unidirectional when $x \to 0$ and $y \to \infty$.
- c) Its streamlines are given by x = y.
- d) It is irrotational.
- 10) Which one of the following statements is correct for a superheated vapour?

- a) Its pressure is less than the saturation pressure at a given temperature.
- b) Its temperature is less than the saturation temperature at a given pressure.
- c) Its volume is less than the volume of the saturated vapour at a given temperature.
- d) Its enthalpy is less than the enthalpy of the saturated vapour at a given pressure.
- 11) In a linearly hardening plastic material, the true stress beyond initial yielding

- a) increases linearly with the true strain
- b) decreases linearly with the true strain
- c) first increases linearly and then decreases linearly with the true strain
- d) remains constant
- 12) The type of weld represented by shaded region in the figure is



(GATE ME 2018)

- a) groove
- b) spot
- c) fillet
- d) plug
- 13) Using the Taylor's tool life equation with exponent n = 0.5, if the cutting speed is reduced by 50%, the ratio of new tool life to original tool life is (GATE ME 2018)
 - a) 2

b) 4

c) 1

d) 0.5

14) A grinding ratio of 200 implies that the

(GATE ME 2018)

- a) grinding wheel wears 200 times the volume of the material removed
- b) grinding wheel wears 0.005 times the volume of the material removed
- c) aspect ratio of abrasive particles used in the grinding wheel is 200
- d) ratio of volume of abrasive particle to that of grinding wheel is 200
- 15) Interpolator in a CNC machine

- a) controls spindle speed
- b) coordinates axes movements

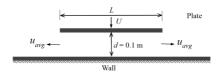
- c) operates tool changer
- d) commands canned cycle
- 16) The time series forecasting method that gives equal weightage to each of the m most recent observations is (GATE ME 2018)
 - a) Moving average method
 - b) Triple Exponential smoothing
 - c) Exponential smoothing with linear trend
 - d) Kalman Filter
- 17) The number of atoms per unit cell and the number of slip systems, respectively, for a face-centered cubic (FCC) crystal are (GATE ME 2018)
 - a) 3,3

- b) 3,12
- c) 4,12
- d) 4,48
- 18) A six-faced fair dice is rolled five times. The probability (in %) of obtaining "ONE" at least four times is (GATE ME 2018)
 - a) 33.3
- b) 3.33
- c) 0.33
- d) 0.0033
- 19) A steel column of rectangular cross-section $15 \,\mathrm{mm} \times 10 \,\mathrm{mm}$ and length $1.5 \,\mathrm{m}$ is simply supported. at both ends. Assuming modulus of elasticity, E = 200 GPa for steel, the critical axial load (inkN) is (correct to two decimal places). (GATE ME 2018)
- 20) A four bar mechanism is made up of links of length 100, 200, 300 and 350 mm. If the 350 mm link is fixed, the number of links that can rotate fully is (GATE ME 2018)
- 21) If the wire diameter of a compressive helical spring is increased by 2 %, the change in spring stiffness (in %) is

(correct to two decimal places).

(GATE ME 2018)

22) A flat plate of width L=1 m is pushed down with a velocity U=0.01 m/s towards a wall resulting in the drainage of the fluid between the plate and the wall as shown in the figure. The average velocity, Uavg of the fluid (in m/s) draining out at the instant shown in the figure is (correct to three decimal places).



(GATE ME 2018).

23) An ideal gas undergoes a process from state 1 (T= 300 K, P1 = 100 kPa) to state 2 $(T_2 = 600K, P_2 = 500kPa.)$ The specific heats of the ideal gas are : Cp= 1 kJ/kg-K

and Cv=0.7 kJ/kg-K. The change in specific entropy of the ideal gas from state 1 to state 2 (inkJ/kg-K) is

(GATE ME 2018)

24) For a Pelton wheel with a given water jet velocity, the maximum output power from the Pelton wheel is obtained when the ratio of the bucket speed to the water jet speed (correct to two decimal places), piece is

(GATE ME 2018)

25) The height (in mm) for a 125 mm sine bar to measure a taper of 27° 32' on a flat work (correct to three decimal places).

(GATE ME 2018)

Q.26-Q.50 carry 2 marks each

26) Let X1, X2 be two independent normal random variables with means $\mu_1\mu_2$ and standard $\mu_1 = \mu_2 = 1$ $\sigma_1 = 1\sigma_2 = 2$ deviations $\sigma_1\sigma_2$ respectively. Consider Y = X1-X2; Then,

(GATE ME 2018)

- a) Y is normally distributed with mean 0 and variance 1
- b) Y is normally distributed with mean 0 and variance 5
- c) Y has mean 0 and variance 5, but is NOT normally distributed
- d) Y has mean 0 and variance 1, but is NOT normally distributed
- 27) The value of the integral

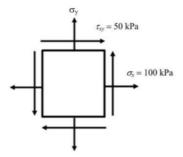
 $\iint_{S} \mathbf{r} \cdot \mathbf{n} \, dS$

over the closed surface S bounding a volume V, where

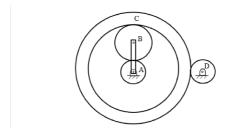
$$\hat{\mathbf{r}} = x\hat{\mathbf{i}} + y\hat{\mathbf{j}} + z\hat{\mathbf{k}} \tag{27.1}$$

is the position vector and n is the normal to the surface S, is (GATE ME 2018)

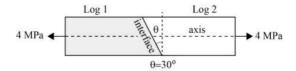
- a) V
- b) 2V
- c) 3V
- d) 4V
- 28) A point mass is shot vertically up from ground level with a velocity of 4 m/s at time, t=0. It loses 20 % of its impact velocity after each collision with the ground. Assuming that the acceleration due to gravity is 10 m/s^2 and that air resistance is negligible, the mass stops bouncing and comes to complete rest on the ground after a total time (*inseconds*) of (GATE ME 2018)
 - a) 1
 - b) 2
 - c) 4
 - d) ∞
- 29) The state of stress at a point, for a body in plane stress, is shown in the figure below. If the minimum principal stress is 10 kPa, then the normal stress σ_y (inKPa) is (GATE ME 2018)



- a) 9.45
- b) 18.88
- c) 37.78
- d) 75.50
- 30) An epicyclic gear train is shown in the figure below. The number of teeth on the gears A, B and D are 20, 30 and 20, respectively. Gear C has 80 teeth on the inner surface and 100 teeth on the outer surface. If the carrier arm AB is fixed and the sun gear A rotates at 300 rpm in the clockwise direction, then the rpm of D in the clockwise direction is

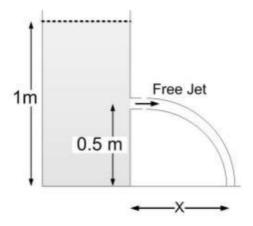


- a) 240
- b) -240
- c) 375
- d) -375
- 31) A carpenter glues a pair of cylindrical wooden logs by bonding their end faces at an angle of $\theta = 30^{\circ}$ as shown in the figure.



The glue used at the interface fails if Criterion 1: the maximum normal stress exceeds 2.5 MPa. Criterion 2: the maximum shear stress exceeds 1.5 MPa. Assume that the interface fails before the logs fail. When a uniform tensile stress of 4 MPa is applied, the interface (GATE ME 2018)

- a) fails only because of criterion 1
- b) fails only because of criterion 2
- c) fails because of both criteria 1 and 2
- d) does not fail
- 32) A self-aligning ball bearing has a basic dynamic load rating (C10, for106revolutions) of 35 kN. If the equivalent radial load on the bearing is 45 kN, the expected life (in106revolutions) is (GATE ME 2018)
 - a) below 0.5
 - b) 0.5 to 0.8
 - c) 0.8 to 1.0
 - d) above 1.0
- 33) A tank open at the top with a water level of 1 m, as shown in the figure, has a hole at a height of 0.5 m. A free jet leaves horizontally from the smooth hole. The distance X (*im m*) where the jet strikes the floor is



- a) 0.5
- b) 1
- c) 2
- d) 4
- 34) In a Lagrangian system, the position of a fluid particle in a flow is described as $x = x_0 e^{-kt}$ and $y = y_0 e^{kt}$ where t is the time while x_0, y_0, y_0 and k are constants. The flow is (GATE ME 2018)
 - a) unsteady and one-dimensional c) steady and one-dimensional
 - b) steady and two-dimensional
- d) unsteady and two-dimensional
- 35) The maximum reduction in cross-sectional area per pass (R) of a cold wire drawing process is

$$R = 1 - e^{-(n+1)}.$$

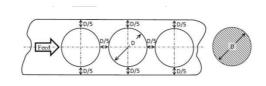
where n represents the strain hardening coefficient. For the case of a perfectly plastic material. R is (GATE ME 2018)

a) 0.865

c) 0.777

b) 0.826

- d) 0.632
- 36) The percentage scrap in a sheet metal blanking operation of a continuous strip of sheet metal (correct to two decimal places). as shown in the figure is



(GATE ME 2018)

37) An explicit forward Euler method is used to numerically integrate the differential equation

$$\frac{dy}{dt} = y$$

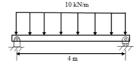
using a time step of 0.1. With the initial condition y(0) = 1, the value of y(1)computed by this method is (correct to two decimal places). (GATE ME 2018)

38) F(s) is the Laplace transform of the function

$$f(t) = 2t^2 e^{-t}$$

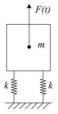
F(1) is (correct to two decimal places).

39) A simply supported beam of width 100 mm, height 200 mm and length 4 m is carrying a uniformly distributed load of intensity 10 kN/m. The maximum bending stress (in MPa) in the beam is (correct to one decimal place).



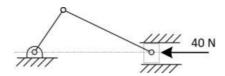
(GATE ME 2018)

40) A machine of mass m = 200 kg is supported on two mounts, each of stiffness k = 10 kN/m. The machine is subjected to an external force (in N) F(t) = 50 cos 5t. Assuming only vertical translatory motion, the magnitude of the dynamic force (in N) transmitted from each mount to the ground is (correct to two decimal places).

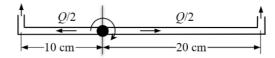


(GATE ME 2018)

41) A slider crank mechanism is shown in the figure. At some instant, the crank angle is $45 \hat{A}^{\circ}$ and a force of 40 N is acting towards the left on the slider. The length of the crank is 30 mm and the connecting rod is 70 mm. Ignoring the effect of gravity, friction and inertial forces, the magnitude of the crankshaft torque (in Nm) needed to keep the mechanism in equilibrium is (correct to two decimal places). (GATE ME 2018)

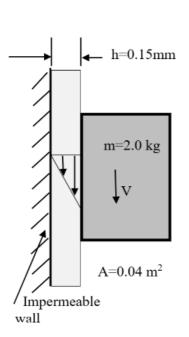


42) A sprinkler shown in the figure rotates about its hinge point in a horizontal plane due to water flow discharged through its two exit nozzles. (GATE ME 2018)



The total flow rate Q through the sprinkler is 1 litre/sec and the cross-sectional area of each exit nozzle is 1 cm^2 . Assuming equal flow rate through both arms and a frictionless hinge, the steady state angular speed of rotation (inrad/s) of the sprinkler is (correct to two decimal places).

43) A solid block of 2.0 kg mass slides steadily at a velocity V along a vertical wall as shown in the figure below. A thin oil film of thickness h=0.15 mm provides lubrication between the block and the wall. The surface area of the face of the block in contact with the oil film is 0.04 m2. The velocity distribution within the oil film gap is linear as shown in the figure. Take dynamic viscosity of oil as $7x10^{-3}$ Pas and acceleration due to gravity as $10m/s^2$. Neglect weight of the oil. The terminal velocity V (in m/s) of the block is



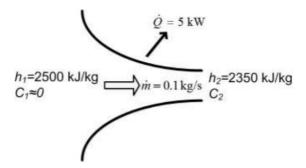
44) A tank of volume 0.05 m³ contains a mixture of saturated water and saturated steam at 200°C. The mass of the liquid present is 8 kg. The entropy (in kJ/kg K) of the mixture is ______ (correct to two decimal places). Property data for saturated steam and water are:

At 200°C,
$$p_{\text{sat}} = 1.5538 \text{ MPa}$$

 $v_f = 0.001157 \text{ m}^3/\text{kg}$, $v_g = 0.12736 \text{ m}^3/\text{kg}$
 $s_{fg} = 4.1014 \text{ kJ/kg K}$, $s_f = 2.3309 \text{ kJ/kg K}$

(GATE ME 2018)

45) Steam flows through a nozzle at a mass flow rate of $\dot{m}0.1$ kg/s with a heat loss of 5 kW. The enthalpies at inlet and exit are 2500 kJ/kg and 2350 kJ/kg, respectively. Assuming negligible velocity at inlet $C_1 \approx 0$, the velocity C_2 steam (inm/s) at the nozzle exit is (correct to two decimal places).



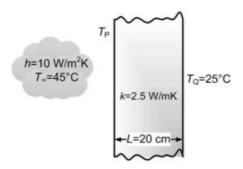
46) An engine working on air standard Otto cycle is supplied with air at 0.1 MPa and 35°C. The compression ratio is 8. The heat supplied is 500 kJ/kg. Property data for air:

$$c_p = 1.005~\mathrm{kJ/kg}~\mathrm{K}, \quad c_v = 0.718~\mathrm{kJ/kg}~\mathrm{K}, \quad R = 0.287~\mathrm{kJ/kg}~\mathrm{K}$$

The maximum temperature (in K) of the cycle is _____ (correct to one decimal place).

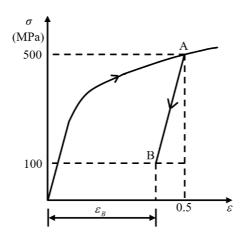
(GATE ME 2018)

47) A plane slab of thickness L and thermal conductivity k is heated with a fluid on one side (P), and the other side (Q) is maintained at a constant temperature, T_Q of 25°C, as shown in the figure.



The fluid is at 45°C and the surface heat transfer coefficient, h, is 10 W/m²K. The steady state temperature, T_P (in °C), of the side which is exposed to the fluid is (correct to two decimal places).

48) The true stress σ - true strain ϵ diagram of a strain hardening material is shown in figure. First, there is loading up to point A, i.e., up to stress of 500 MPa and strain of 0.5. Then from point A, there is unloading up to point B, i.e., to stress of 100 MPa. Given that the Young's modulus E = 200 GPa, the natural strain at point B (ϵ_B) is (GATE ME 2018)



49) An orthogonal cutting operation is being carried out in which uncut thickness is 0.010 mm, cutting speed is 130 m/min, rake angle is 15° and width of cut is 6 mm. It is observed that the chip thickness is 0.015 mm, the cutting force is 60 N and the thrust force is 25 N. The ratio of friction energy to total energy is

(correcttotwodecimalplaces)

(GATE ME 2018)

50) A bar is compressed to half of its original length. The magnitude of true strain produced in the deformed bar is (GATE ME 2018)

51) The minimum value of 3x + 5y is such that:

$$3x + 5y \le 15$$

$$4x + 9y \le 8$$

$$13x + 2y \le 2$$

$$x \ge 0, \quad y \ge 0$$

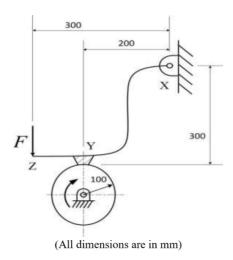
(GATE ME 2018)

52) Processing times (including setup times) and due dates for six jobs waiting to be processed at a work centre are given in the table. The average tardiness (in days) using shortest processing time rule is

Job	Processing time (days)	Due date (days)
A	3	8
В	7	16
C	4	4
D	9	18
Е	5	17
F	13	19

(GATE ME 2018)

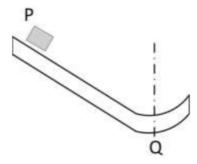
53) The schematic of an external drum rotating clockwise engaging with a short shoe is shown in the figure. The shoe is mounted at point Y on a rigid lever XYZ hinged at point X. A force F = 100 N is applied at the free end of the lever as shown. Given that the coefficient of friction between the shoe and the drum is 0.3, the braking torque (in Nm) applied on the drum is (correct to two decimal places).



54) Block P of mass 2 kg slides down the surface and has a speed 20 m/s at the lowest point, Q, where the local radius of curvature is 2 m as shown in the figure.

Assuming g = 10 m/s2, the normal force (in N) at Q is (correct to two decimal places).

(GATE ME 2018)



55) An electrochemical machining (ECM) is to be used to cut a through hole into a 12 mm thick aluminum plate. The hole has a rectangular cross-section, 10 mm x 30 mm. The ECM operation will be accomplished in 2 minutes, with efficiency of 90%. Assuming specific removal rate for aluminum as $3.44 \times 10^{(1)} - 20 \text{mm}^3/(As)$,

the current (inA) required is (correct to two decimal places).