

## 1.2.23 – Matgeo Assignment

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## Question

Represent graphically a displacement of 40 km,  $30^\circ$  west of south.

# Coordinate Convention

We choose the coordinate axes as:

$$\text{East} \equiv +x, \quad \text{West} \equiv -x, \quad \text{North} \equiv +y, \quad \text{South} \equiv -y.$$

The unit column for South is

$$\mathbf{s} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}.$$

## Rotation Matrix

For rotation by angle  $\theta$  anti clockwise,

$$R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}.$$

Since “30° west of south” means clockwise rotation of 30° or anti-clockwise rotation of 330°, we apply

$$\mathbf{u} = R(330^\circ)\mathbf{s}.$$

## Direction Column

$$\mathbf{u} = \begin{bmatrix} \cos 330^\circ & -\sin 330^\circ \\ \sin 330^\circ & \cos 330^\circ \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix} = \begin{bmatrix} -\frac{1}{2} \\ -\frac{\sqrt{3}}{2} \end{bmatrix}.$$

## Displacement Column

With magnitude 40 km:

$$\mathbf{d} = 40\mathbf{u} = 40 \begin{bmatrix} -\frac{1}{2} \\ -\frac{\sqrt{3}}{2} \end{bmatrix} = \begin{bmatrix} -20 \\ -20\sqrt{3} \end{bmatrix} \text{ km.}$$

Endpoint:

$$(x, y) = (-20, -20\sqrt{3}) \text{ km.}$$

# Graphical Representation

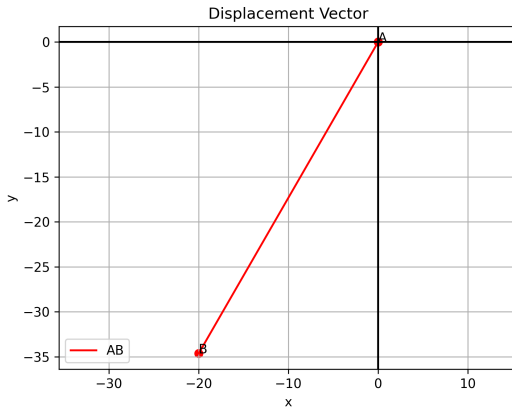


Figure: Displacement vector: 40 km,  $30^\circ$  west of south