Assignment 1

Ashish Jangid

Area of Triangle

Abstract—This document contains the solution to find the Area of a Triangle, given the coordinates of the vertices.

Download all python codes from

https://github.com/ashish-hk/Assignment1/blob/main/Assignment1.ipynb

Download latex-tikz codes from

https://github.com/ashish-hk/Assignment1/blob/main/main.tex

1 Problem

Solve: Problem set: Vector2, Example-2,1

Find the areas of the triangles the coordinates of whose angular points are respectively:

$$\mathbf{P} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} -7 \\ 6 \end{pmatrix} \text{ and } \mathbf{R} = \begin{pmatrix} 5 \\ -1 \end{pmatrix}$$

2 Solution

We will be using vectors for calculating the area of the triangle formed by above three points.

$$\mathbf{Q} - \mathbf{P} = \begin{pmatrix} -7 \\ 6 \end{pmatrix} - \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$
$$= \begin{pmatrix} -8 \\ 3 \end{pmatrix} \tag{2.0.1}$$

$$\mathbf{R} - \mathbf{P} = \begin{pmatrix} 5 \\ -1 \end{pmatrix} - \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$
$$= \begin{pmatrix} 4 \\ -4 \end{pmatrix} \tag{2.0.2}$$

: Area of the Triangle =
$$\frac{1}{2} ||(\mathbf{Q} - \mathbf{P}) \times (\mathbf{R} - \mathbf{P})||$$

As the vector cross product of two vectors can also be expressed as the product of a skew-symmetric matrix and a vector.

$$\mathbf{A} \times \mathbf{B} = \begin{pmatrix} 0 & -a_3 & a_2 \\ a_3 & 0 & -a_1 \\ -a_2 & a_1 & 0 \end{pmatrix} \times \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$
 (2.0.4)

Substituting values from equation 2.0.1 and 2.0.2 in above equation 2.0.4, we'll get:

$$(\mathbf{Q} - \mathbf{P}) \times (\mathbf{R} - \mathbf{P}) = \begin{pmatrix} 0 & 0 & 3 \\ 0 & 0 & 8 \\ -3 & -8 & 0 \end{pmatrix} \times \begin{pmatrix} 4 \\ -4 \\ 0 \end{pmatrix}$$

$$= \begin{pmatrix} 0 \\ 0 \\ 20 \end{pmatrix}$$
(2.0.5)

(2.0.6)

Substituting value from equation 2.0.6 in equation 2.0.3, we'll get area of triangle:

$$\implies \frac{1}{2}(20) = 10units^2$$

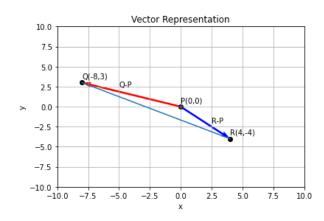


Fig. 1: Plot obtained from Python code