GATE CS 2018

EE25BTECH11052 - Shriyansh Chawda

Q.1 to Q.5 Carry one mark each.

1) "From where are they bringing their books? _____ bringing _____ books from _____."
The words that best fill the blanks in the above sentence are (GATE CS 2018)

a) Their, they're, there
b) They're, their, there
c) There, their, they're
d) They're, there, there

2) "A _____ investigation can sometimes yield new facts, but typically organized ones are more successful."
The word that best fills the blank in the above sentence is (GATE CS 2018)

a) meandering b) timely c) consistent d) systematic

3) The area of a square is d. What is the area of the circle which has the diagonal of the square as its diameter? (GATE CS 2018)

a) πd b) πd^2 c) $\frac{1}{4}\pi d^2$ d) $\frac{1}{2}\pi d$

4) What would be the smallest natural number which when divided either by 20 or by 42 or by 76 leaves a remainder of 7 in each case? (GATE CS 2018)

a) 3047 b) 6047 c) 7987 d) 63847

5) What is the missing number in the following sequence?
2, 12, 60, 240, 720, 1440, _____, 0 (GATE CS 2018)

a) 2880 b) 1440 c) 720 d) 0

Q.6 to Q.10 Carry two mark each.

6) In appreciation of the social improvements completed in a town, a wealthy philanthropist decided to gift Rs 750 to each male senior citizen in the town and Rs 1000 to each female senior citizen. Altogether, there were 300 senior citizens eligible for this gift. However, only $8/9^{\text{th}}$ of the eligible men and $2/3^{\text{rd}}$ of the eligible women claimed the gift. How much money (in Rupees) did the philanthropist give away in total? (GATE CS 2018)

a) $1,50,000$
b) $2,00,000$
c) $1,75,000$
d) $1,51,000$

7) If $pqr \neq 0$ and $p^{-x} = \frac{1}{q}$, $q^{-y} = \frac{1}{r}$, $r^{-z} = \frac{1}{p}$, what is the value of the product xyz? (GATE CS 2018)

a) -1 b) $\frac{1}{pqr}$ c) 1 d) pqr

8) In a party, 60% of the invited guests are male and 40% are female. If 80% of the invited guests attended the party and if all the invited female guests attended, what would be the ratio of males to females among the attendees in the party? (GATE CS 2018)

a) 2 : 3 b) 1 : 1 c) 3 : 2 d) 2 : 1

9) In the figure below, $\angle DEC + \angle BFC$ is equal to _____. (GATE CS 2018)

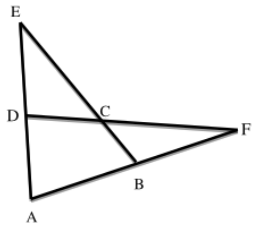

Fig. 1

a) $\angle BCD - \angle BAD$ b) $\angle BAD + \angle BCF$ c) $\angle BAD + \angle BCD$ d) $\angle CBA + \angle ADC$

10) A six sided unbiased die with four green faces and two red faces is rolled seven times. Which of the following combinations is the most likely outcome of the experiment? (GATE CS 2018)

a) Three green faces and four red faces.
b) Four green faces and three red faces.
c) Five green faces and two red faces.
d) Six green faces and one red face.

Q.1 to Q.25 Carry one mark each.

1) Which one of the following is a closed form expression for the generating function of the sequence $\{a_n\}$, where $a_n = 2n + 3$ for all $n = 0, 1, 2, \ldots$?

(GATE CS 2018)

a) $\frac{3}{(1-x)^2}$ b) $\frac{3x}{(1-x)^2}$ c) $\frac{2-x}{(1-x)^2}$ d) $\frac{3-x}{(1-x)^2}$

2) Consider the following C program.

```
#include<stdio.h>
struct Ournode{
 char x,y,z;
};

int main(){
 struct Ournode p = {'1', '0', 'a'+2};
 struct Ournode *q = &p;
 printf ("%c, %c", *((char*)q+1), *((char*)q+2));
 return 0;
}
```

The output of this program is:

(GATE CS 2018)

a) 0, c b) 0, a+2 c) '0', 'a'+2' d) '0', 'c'

3) A queue is implemented using a non-circular singly linked list. The queue has a head pointer and a tail pointer, as shown in the figure. Let n denote the number of nodes in the queue. Let `enqueue` be implemented by inserting a new node at the head, and `dequeue` be implemented by deletion of a node from the tail. Which one of the following is the time complexity of the most time-efficient implementation of `enqueue` and `dequeue`, respectively, for this data structure?

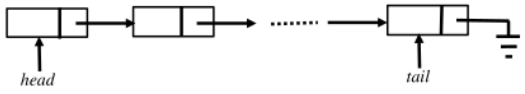

Fig. 2

(GATE CS 2018)

a) $\theta(1), \theta(1)$ b) $\theta(1), \theta(n)$ c) $\theta(n), \theta(1)$ d) $\theta(n), \theta(n)$

4) Let $\oplus$ and $\odot$ denote the Exclusive OR and Exclusive NOR operations, respectively. Which one of the following is NOT CORRECT?

(GATE CS 2018)

a) $\overline{P \oplus Q} = P \odot Q$
b) $\overline{P} \oplus Q = P \odot Q$
c) $\overline{P} \oplus \overline{Q} = P \oplus Q$
d) $\left(P \oplus \overline{P}\right) \oplus Q = \left(P \odot \overline{P}\right) \odot \overline{Q}$

5) Consider the following processor design characteristics.

I. Register-to-register arithmetic operations only

II. Fixed-length instruction format
III. Hardwired control unit

Which of the characteristics above are used in the design of a RISC processor?

(GATE CS 2018)

a) I and II only b) II and III only c) I and III only d) I, II and III

6) Let N be an NFA with n states. Let k be the number of states of a minimal DFA which is equivalent to N. Which one of the following is necessarily true?

(GATE CS 2018)

a) $k \geq 2^n$ b) $k \geq n$ c) $k \leq n^2$ d) $k \leq 2^n$

7) The set of all recursively enumerable languages is

(GATE CS 2018)

a) closed under complementation.
b) closed under intersection.
c) a subset of the set of all recursive languages.
d) an uncountable set.

8) Which one of the following statements is FALSE?

(GATE CS 2018)

a) Context-free grammar can be used to specify both lexical and syntax rules.
b) Type checking is done before parsing.
c) High-level language programs can be translated to different Intermediate Representations.
d) Arguments to a function can be passed using the program stack.

9) The following are some events that occur after a device controller issues an interrupt while process L is under execution.

(P) The processor pushes the process status of L onto the control stack.
(Q) The processor finishes the execution of the current instruction.
(R) The processor executes the interrupt service routine.
(S) The processor pops the process status of L from the control stack.
(T) The processor loads the new PC value based on the interrupt.

Which one of the following is the correct order in which the events above occur?

(GATE CS 2018)

a) QPTRS b) PTRSQ c) TRPQS d) QTPRS

10) Consider a process executing on an operating system that uses demand paging. The average time for a memory access in the system is M units if the corresponding memory page is available in memory, and D units if the memory access causes a page fault. It has been experimentally measured that the average time taken for a memory access in the process is X units. Which one of the following is the correct expression for the page fault rate experienced by the process?

(GATE CS 2018)

a) $(D - M) / (X - M)$
b) $(X - M) / (D - M)$
c) $(D - X) / (D - M)$
d) $(X - M) / (D - X)$

11) In an Entity-Relationship (ER) model, suppose R is a many-to-one relationship from entity set E1 to entity set E2. Assume that E1 and E2 participate totally in R and that the cardinality of E1 is greater than the cardinality of E2. Which one of the following is true about R?

(GATE CS 2018)

a) Every entity in E1 is associated with exactly one entity in E2.
b) Some entity in E1 is associated with more than one entity in E2.
c) Every entity in E2 is associated with exactly one entity in E1.
d) Every entity in E2 is associated with at most one entity in E1.

12) Consider the following two tables and four queries in SQL.

```
Book (isbn, bname), Stock (isbn, copies)
```

Query 1:

```
SELECT B.isbn, S.copies
 FROM Book B INNER JOIN Stock S
 ON B.isbn = S.isbn;
```

Query 2:

```
SELECT B.isbn, S.copies
  FROM Book B LEFT OUTER JOIN Stock S
  ON B.isbn = S.isbn;
```

Query 3:

```
SELECT B.isbn, S.copies
  FROM Book B RIGHT OUTER JOIN Stock S
  ON B.isbn = S.isbn;
```

Query 4:

```
SELECT B.isbn, S.copies
 FROM Book B FULL OUTER JOIN Stock S
 ON B.isbn = S.isbn;
```

Which one of the queries above is certain to have an output that is a superset of the outputs of the other three queries?

(GATE CS 2018)

a) Query 1 b) Query 2 c) Query 3 d) Query 4

13) Match the following:

Field	**Length in bits**
P. UDP Header's Port Number	I. 48
Q. Ethernet MAC Address	II. 8
R. IPv6 Next Header	III. 32
S. TCP Header's Sequence Number	IV. 16

(GATE CS 2018)

a) P-III, Q-IV, R-II, S-I
b) P-II, Q-I, R-IV, S-III
c) P-IV, Q-I, R-II, S-III
d) P-IV, Q-I, R-III, S-II

14) Consider the following statements regarding the slow start phase of the TCP congestion control algorithm. Note that *cwnd* stands for the TCP congestion window and MSS denotes the Maximum Segment Size.

(*i*) The *cwnd* increases by 2 MSS on every successful acknowledgment.
(*ii*) The *cwnd* approximately doubles on every successful acknowledgement.
(*iii*) The *cwnd* increases by 1 MSS every round trip time.
(*iv*) The *cwnd* approximately doubles every round trip time.

Which one of the following is correct?

(GATE CS 2018)

a) Only (*ii*) and (*iii*) are true
b) Only (*i*) and (*iii*) are true
c) Only (*iv*) is true
d) Only (*i*) and (*iv*) are true

15) Two people, P and Q, decide to independently roll two identical dice, each with 6 faces, numbered 1 to 6. The person with the lower number wins. In case of a tie, they roll the dice repeatedly until there is no tie. Define a trial as a throw of the dice by P and Q. Assume that all 6 numbers on each dice are equi-probable and that all trials are independent. The probability (rounded to 3 decimal places) that one of them wins on the third trial is _____. (GATE CS 2018)

16) The value of $\int_0^{\pi/4} x\cos\left(x^2\right)dx$ correct to three decimal places $(assumingthat)\ \pi = 3.14$ is _____.

(GATE CS 2018)

17) Consider a matrix $A = uv^T$ where $u = \begin{pmatrix}1\\2\end{pmatrix}, v = \begin{pmatrix}1\\1\end{pmatrix}$. Note that v^T denotes the transpose of v. The largest eigenvalue of A is _____. (GATE CS 2018)

18) The chromatic number of the following graph is _____. (GATE CS 2018)

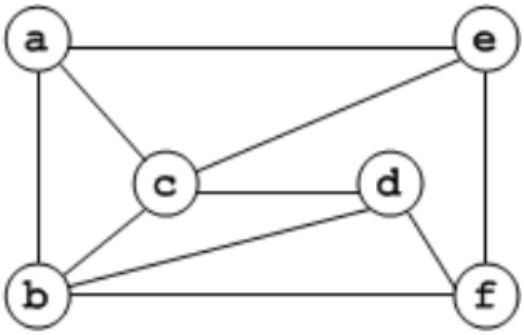

Fig. 3

19) Let G be a finite group on 84 elements. The size of a largest possible proper subgroup of G is _____.

(GATE CS 2018)

20) The postorder traversal of a binary tree is $8, 9, 6, 7, 4, 5, 2, 3, 1$. The inorder traversal of the same tree is $8, 6, 9, 4, 7, 2, 5, 1, 3$. The height of a tree is the length of the longest path from the root to any leaf. The height of the binary tree above is _____.

(GATE CS 2018)

21) Consider the following C program:

```
#include <stdio.h>

int counter = 0;

int calc(int a, int b) {
 int c;
 counter++;
 if (b==3) return (a*a*a);
 else {
  c = calc(a, b/3);
```

```
  return (c*c*c);
 }
}

int main() {
 calc(4, 81);
 printf("%d", counter);
}
```

The output of this program is _____.

(GATE CS 2018)

22) Consider the sequential circuit shown in the figure, where both flip-flops used are positive edge-triggered D flip-flops.

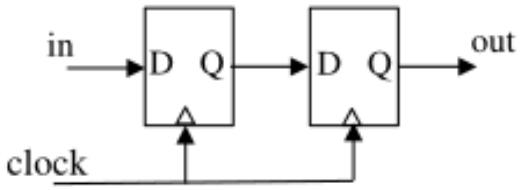

Fig. 4

The number of states in the state transition diagram of this circuit that have a transition back to the same state on some value of "in" is _____.

(GATE CS 2018)

23) A 32-bit wide main memory unit with a capacity of 1 GB is built using 256M $\times$ 4-bit DRAM chips. The number of rows of memory cells in the DRAM chip is 2^{14}. The time taken to perform one refresh operation is 50 nanoseconds. The refresh period is 2 milliseconds. The percentage (rounded to the closest integer) of the time available for performing the memory read/write operations in the main memory unit is _____.

(GATE CS 2018)

24) Consider a system with 3 processes that share 4 instances of the same resource type. Each process can request a maximum of K instances. Resource instances can be requested and released only one at a time. The largest value of K that will always avoid deadlock is _____.

(GATE CS 2018)

25) Consider a long-lived TCP session with an end-to-end bandwidth of 1 Gbps (= 10^9 bits-per-second). The session starts with a sequence number of 1234. The minimum time (*inseconds*, *roundedtotheclosestinteger*) before this sequence number can be used again is _____.
(GATE CS 2018)

Q.26 to Q.55 Carry one mark each.

26) Consider a matrix P whose only eigenvectors are the multiples of $\begin{pmatrix}1\\4\end{pmatrix}$. Consider the following statements.

(I) P does not have an inverse
(II) P has a repeated eigenvalue
(III) P cannot be diagonalized

Which one of the following options is correct?

(GATE CS 2018)

a) Only I and III are necessarily true
b) Only II is necessarily true
c) Only I and II are necessarily true
d) Only II and III are necessarily true

27) Let N be the set of natural numbers. Consider the following sets.

P: Set of Rational numbers (*positiveandnegative*)
Q: Set of functions from $\{0, 1\}$ to N
R: Set of functions from N to $\{0, 1\}$
S: Set of finite subsets of N.

Which of the sets above are countable?

(GATE CS 2018)

a) Q and S only
b) P and S only
c) P and R only
d) P, Q and S only

28) Consider the first-order logic sentence

$$\varphi \equiv \exists s \exists t \exists u \forall v \forall w \forall x \forall y \; \psi(s, t, u, v, w, x, y)$$

where $\psi(s, t, u, v, w, x, y)$ is a quantifier-free first-order logic formula using only predicate symbols, and possibly equality, but no function symbols. Suppose φ has a model with a universe containing 7 elements. Which one of the following statements is necessarily true?

(GATE CS 2018)

a) There exists at least one model of φ with universe of size less than or equal to 3.
b) There exists no model of φ with universe of size less than or equal to 3.
c) There exists no model of φ with universe of size greater than 7.
d) Every model of φ has a universe of size equal to 7.

29) Consider the following C program:

```
#include<stdio.h>

void fun1(char *s1, char *s2) {
 char *tmp;
 tmp = s1;
 s1 = s2;
 s2 = tmp;
}

void fun2(char **s1, char **s2) {
 char *tmp;
 tmp = *s1;
 *s1 = *s2;
 *s2 = tmp;
}

int main() {
 char *str1 = "Hi", *str2 = "Bye";
 fun1(str1, str2); printf("%s %s ", str1, str2);
 fun2(&str1, &str2); printf("%s %s", str1, str2);
 return 0;
}
```

The output of the program above is

(GATE CS 2018)

a) Hi Bye Bye Hi b) Hi Bye Hi Bye c) Bye Hi Hi Bye d) Bye Hi Bye Hi

30) Let G be a simple undirected graph. Let T_D be a depth first search tree of G. Let T_B be a breadth first search tree of G. Consider the following statements.

(I) No edge of G is a cross edge with respect to T_D. (A cross edge in G is between two nodes neither of which i

(II) For every edge (u, v) of G, if u is at depth i and v is at depth j in T_B, then $|i - j| = 1$.

Which of the statements above must necessarily be true?

(GATE CS 2018)

a) I only b) II only c) Both I and II d) Neither I nor II

31) Assume that multiplying a matrix G_1 of dimension $p \times q$ with another matrix G_2 of dimension $q \times r$ requires pqr scalar multiplications. Computing the product of n matrices $G_1G_2G_3 \ldots G_n$ can be done by parenthesizing in different ways. Define G_iG_{i+1} as an **explicitly computed pair** for a given parenthesization if they are directly multiplied. For example, in the matrix multiplication chain $G_1G_2G_3G_4G_5G_6$ using parenthesization $(G_1\,(G_2G_3))\,(G_4\,(G_5G_6))$, G_2G_3 and G_5G_6 are the only explicitly computed pairs.

Consider a matrix multiplication chain $F_1F_2F_3F_4F_5$, where matrices F_1, F_2, F_3, F_4 and F_5 are of dimensions 2×25, 25×3, 3×16, 16×1 and 1×1000, respectively. In the parenthesization of $F_1F_2F_3F_4F_5$ that minimizes the total number of scalar multiplications, the explicitly computed pairs is/are

(GATE CS 2018)

a) F_1F_2 and F_3F_4 only
b) F_2F_3 only
c) F_3F_4 only
d) F_1F_2 and F_4F_5 only

32) Consider the following C code. Assume that unsigned long int type length is 64 bits.

```
unsigned long int fun(unsigned long int n) {
 unsigned long int i, j = 0, sum = 0;
 for (i = n; i > 1; i = i/2) j++;
 for ( ; j > 1; j = j/2) sum++;
 return(sum);
}
```

The value returned when we call `fun` with the input 2^{40} is

(GATE CS 2018)

a) 4 b) 5 c) 6 d) 40

33) Consider the unsigned 8-bit fixed point binary number representation below,

$$b_7\ b_6\ b_5\ b_4\ b_3 \cdot b_2\ b_1\ b_0$$

where the position of the binary point is between b_3 and b_2. Assume b_7 is the most significant bit. Some of the decimal numbers listed below **cannot** be represented **exactly** in the above representation:

(i) 31.500
(ii) 0.875
(iii) 12.100
(iv) 3.001

Which one of the following statements is true?

(GATE CS 2018)

a) None of (i), (ii), (iii), (iv) can be exactly represented

b) Only (ii) cannot be exactly represented
c) Only (iii) and (iv) cannot be exactly represented
d) Only (i) and (ii) cannot be exactly represented

34) The size of the physical address space of a processor is 2^P bytes. The word length is 2^W bytes. The capacity of cache memory is 2^N bytes. The size of each cache block is 2^M words. For a K-way set-associative cache memory, the length (in number of bits) of the tag field is

(GATE CS 2018)

a) $P - N - \log_2 K$
b) $P - N + \log_2 K$
c) $P - N - M - W - \log_2 K$
d) $P - N - M - W + \log_2 K$

35) Consider the following languages:

I. $\{a^m b^n c^p d^q \mid m + p = n + q, \text{ where } m, n, p, q \geq 0\}$
II. $\{a^m b^n c^p d^q \mid m = n \text{ and } p = q, \text{ where } m, n, p, q \geq 0\}$
III. $\{a^m b^n c^p d^q \mid m = n = p \text{ and } p \neq q, \text{ where } m, n, p, q \geq 0\}$
IV. $\{a^m b^n c^p d^q \mid mn = p + q, \text{ where } m, n, p, q \geq 0\}$

Which of the languages above are context-free?

(GATE CS 2018)

a) I and IV only
b) I and II only
c) II and III only
d) II and IV only

36) Consider the following problems. $L(G)$ denotes the language generated by a grammar G. $L(M)$ denotes the language accepted by a machine M.

(I) For an unrestricted grammar G and a string w, whether $w \in L(G)$
(II) Given a Turing machine M, whether $L(M)$ is regular
(III) Given two grammars G_1 and G_2, whether $L(G_1) = L(G_2)$
(IV) Given an NFA N, whether there is a deterministic PDA P such that N and P accept the same language.

Which one of the following statements is correct?

(GATE CS 2018)

a) Only I and II are undecidable
b) Only III is undecidable
c) Only II and IV are undecidable
d) Only I, II and III are undecidable

37) A lexical analyzer uses the following patterns to recognize three tokens T_1, T_2, and T_3 over the alphabet $\{a, b, c\}$.

$$T_1: \quad a?\,(b|c)^*\,a$$
$$T_2: \quad b?\,(a|c)^*\,b$$
$$T_3: \quad c?\,(b|a)^*\,c$$

Note that 'x?' means 0 or 1 occurrence of the symbol x. Note also that the analyzer outputs the token that matches the longest possible prefix.

If the string `bbaacabc` is processed by the analyzer, which one of the following is the sequence of tokens it outputs?

(GATE CS 2018)

a) $T_1T_2T_3$
b) $T_1T_1T_3$
c) $T_2T_1T_3$
d) T_3T_3

38) Consider the following parse tree for the expression `a#b$c$d#e#f`, involving two binary operators $ and #.Which one of the following is correct for the given parse tree?

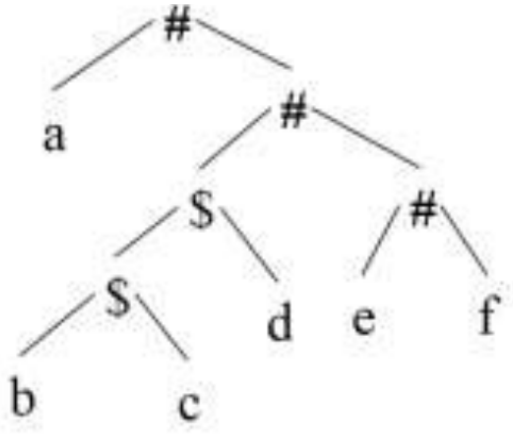

Fig. 5

a) $ has higher precedence and is left associative; # is right associative
b) # has higher precedence and is left associative; $ is right associative
c) $ has higher precedence and is left associative; # is left associative
d) # has higher precedence and is right associative; $ is left associative

39) In a system, there are three types of resources: E, F and G. Four processes P_0, P_1, P_2 and P_3 execute concurrently. At the outset, the processes have declared their maximum resource requirements using a matrix named Max as given below. For example, Max$[P_2, F]$ is the maximum number of instances of F that P_2 would require. The number of instances of the resources allocated to the various processes at any given state is given by a matrix named Allocation.
Consider a state of the system with the Allocation matrix as shown below, and in which 3 instances of E and 3 instances of F are the only resources available.

	E	F	G
P_0	1	0	1
P_1	1	1	2
P_2	1	0	3
P_3	2	0	0

Allocation

	E	F	G
P_0	4	3	1
P_1	2	1	4
P_2	1	3	3
P_3	5	4	1

Max

From the perspective of deadlock avoidance, which one of the following is true?

(GATE CS 2018)

a) The system is in *safe* state.
b) The system is not in *safe* state, but would be *safe* if one more instance of E were available
c) The system is not in *safe* state, but would be *safe* if one more instance of F were available
d) The system is not in *safe* state, but would be *safe* if one more instance of G were available

40) Consider the following solution to the producer-consumer synchronization problem. The shared buffer size is N. Three semaphores *empty*, *full* and *mutex* are defined with respective initial values of 0, N and 1. Semaphore *empty* denotes the number of available slots in the buffer, for the consumer to read from. Semaphore *full* denotes the number of available slots in the buffer, for the producer to write to. The placeholder variables, denoted by P, Q, R, and S, in the code below can be assigned either *empty* or *full*. The valid semaphore operations are: `wait()` and `signal()`.

Producer:	**Consumer:**

`do{`
`wait(P);`
`wait(mutex);`
`//Add item to buffer`
`signal(mutex);`
`signal(Q);`
`}while(1);`
	`do{`
	`wait(R);`
	`wait(mutex);`
	`//Consume item from buffer`
	`signal(mutex);`
	`signal(S);`
	`}while(1);`

Which one of the following assignments to P, Q, R and S will yield the correct solution?

(GATE CS 2018)

a) P: *full*, Q: *full*, R: *empty*, S: *empty*
b) P: *empty*, Q: *empty*, R: *full*, S: *full*
c) P: *full*, Q: *empty*, R: *empty*, S: *full*
d) P: *empty*, Q: *full*, R: *full*, S: *empty*

41) Consider the relations $r(A, B)$ and $s(B, C)$, where $s.B$ is a primary key and $r.B$ is a foreign key referencing $s.B$. Consider the query

$$\text{Q: } r \bowtie (\sigma_{B<5}(s))$$

Let *LOJ* denote the natural left outer-join operation. Assume that r and s contain no null values. Which one of the following queries is NOT equivalent to Q?

(GATE CS 2018)

a) $\sigma_{B<5}(r \bowtie s)$
b) $\sigma_{B<5}(r \text{ LOJ } s)$
c) $r \text{ LOJ } (\sigma_{B<5}(s))$
d) $\sigma_{B<5}(r) \text{ LOJ } s$

42) Consider the following four relational schemas. For each schema, all non-trivial functional dependencies are listed. The underlined attributes are the respective primary keys.
Schema I: *Registration*(<u>*rollno*</u>, *courses*)
Field '*courses*' is a set-valued attribute containing the set of courses a student has registered for.
Non-trivial functional dependency:
rollno → *courses*

Schema II: *Registration*(<u>*rollno*</u>, <u>*courseid*</u>, *email*)
Non-trivial functional dependencies:
rollno, courseid → *email*
email → *rollno*

Schema III: *Registration*(<u>*rollno*</u>, <u>*courseid*</u>, *marks, grade*)
Non-trivial functional dependencies:
rollno, courseid → *marks, grade*
marks → *grade*

Schema IV: *Registration*(<u>*rollno*</u>, <u>*courseid*</u>, *credit*)
Non-trivial functional dependencies:
rollno, courseid → *credit*
courseid → *credit*

Which one of the relational schemas above is in 3NF but not in BCNF?

(GATE CS 2018)

a) Schema I b) Schema II c) Schema III d) Schema IV

43) Let G be a graph with 100! vertices, with each vertex labelled by a distinct permutation of the numbers $1, 2, \ldots, 100$. There is an edge between vertices u and v if and only if the label of u can be obtained by swapping two adjacent numbers in the label of v. Let y denote the degree of a vertex in G, and z denote the number of connected components in G.
Then, $y + 10z =$ _____.

(GATE CS 2018)

44) Consider Guwahati (G) and Delhi (D) whose temperatures can be classified as high (H), medium (M) and low (L). Let $P(H_G)$ denote the probability that Guwahati has high temperature. Similarly, $P(M_G)$ and $P(L_G)$ denotes the probability of Guwahati having medium and low temperatures respectively. Similarly, we use $P(H_D), P(M_D)$ and $P(L_D)$ for Delhi.
The following table gives the conditional probabilities for Delhi's temperature given Guwahati's temperature.

	H_D	M_D	L_D
H_G	0.40	0.48	0.12
M_G	0.10	0.65	0.25
L_G	0.01	0.50	0.49

Consider the first row in the table above. The first entry denotes that if Guwahati has high temperature (H_G) then the probability of Delhi also having a high temperature (H_D) is 0.40; i.e., P($H_D|H_G$) = 0.40. Similarly, the next two entries are P($M_D|H_G$) = 0.48 and P($L_D|H_G$) = 0.12. Similarly for the other rows.
If it is known that $P(H_G) = 0.2$, $P(M_G) = 0.5$, and $P(L_G) = 0.3$, then the probability (correct to two decimal pla that Guwahati has high temperature given that Delhi has high temperature is _____.

(GATE CS 2018)

45) Consider the following program written in pseudo-code. Assume that x and y are integers.

```
Count(x,y) {
 if (y != 1) {
  if (x != 1) {
   print("*");
   Count(x/2, y);
  }
  else {
   y = y-1;
   Count(1024, y);
  }
 }
}
```

The number of times that the `print` statement is executed by the call `Count(1024,1024)` is _____.

(GATE CS 2018)

46) The number of possible min-heaps containing each value from $\{1, 2, 3, 4, 5, 6, 7\}$ exactly once is _____.

(GATE CS 2018)

47) Consider the following undirected graph G:

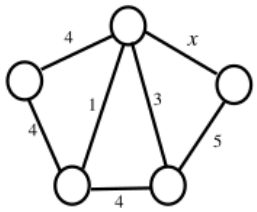

Fig. 6

Choose a value for x that will maximize the number of minimum weight spanning trees ($MWSTs$) of G. The number of MWSTs of G for this value of x is _____.

(GATE CS 2018)

48) Consider the weights and values of items listed below. Note that there is only one unit of each item. The task is to pick a subset of these items such that their total weight is no more than 11 Kgs and

Item number	Weight (in Kgs)	Value (in Rupees)
1	10	60
2	7	28
3	4	20
4	2	24

their total value is maximized. Moreover, no item may be split. The total value of items picked by an optimal algorithm is denoted by V_{opt}. A greedy algorithm sorts the items by their value-to-weight ratios in descending order and packs them greedily, starting from the first item in the ordered list. The total value of items picked by the greedy algorithm is denoted by V_{greedy}.
The value of $V_{opt} - V_{greedy}$ is _____.

(GATE CS 2018)

49) Consider the minterm list form of a Boolean function F given below.

$$F(P, Q, R, S) = \sum m(0, 2, 5, 7, 9, 11) + d(3, 8, 10, 12, 14)$$

Here, m denotes a minterm and d denotes a don't care term. The number of essential prime implicants of the function F is _____. (GATE CS 2018)

50) The instruction pipeline of a RISC processor has the following stages: Instruction Fetch (IF), Instruction Decode (ID), Operand Fetch (OF), Perform Operation (PO) and Writeback (WB). The IF, ID, OF and WB stages take 1 clock cycle each for every instruction. Consider a sequence of 100 instructions. In the PO stage, 40 instructions take 3 clock cycles each, 35 instructions take 2 clock cycles each, and the remaining 25 instructions take 1 clock cycle each. Assume that there are no data hazards and no control hazards.
The number of clock cycles required for completion of execution of the sequence of instructions is _____.

(GATE CS 2018)

51) A processor has 16 integer registers (R0, R1,..., R15) and 64 floating point registers ($F0, F1, ..., F63$). It uses a 2-byte instruction format. There are four categories of instructions: Type-1, Type-2, Type-3, and Type-4. Type-1 category consists of four instructions, each with 3 integer register operands (3Rs). Type-2 category consists of eight instructions, each with 2 floating point register operands (2Fs). Type-3 category consists of fourteen instructions, each with one integer register operand and one floating point register operand (1R+1F). Type-4 category consists of N instructions, each with a floating point register operand (1F).
The maximum value of N is _____.

(GATE CS 2018)

52) Given a language L, define L^i as follows:

$$L^0 = \{\varepsilon\}$$
$$L^i = L^{i-1} \cdot L \text{ for all } i > 0$$

The order of a language L is defined as the smallest k such that $L^k = L^{k+1}$. Consider the language L_1 (over alphabet 0) accepted by the following automaton.

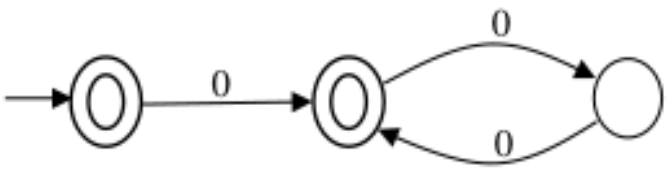

Fig. 7

The order of L_1 is _____.

(GATE CS 2018)