## 1

## **ASSIGNMENT**

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## 1 PROBLEM

1.If **E**, **F**, **G**, **H** are respectively the mid-points of the sides of a Parallelogram ABCD, show that area of Area of Parallelogram EFGH =  $\frac{1}{2}$  Area of Parallelogram ABCD.

SOLUTION: Let,

$$\mathbf{A} = \begin{pmatrix} 0 \\ -4 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 2 \\ -4 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 2 \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad (1.0.1)$$

: mid-points will be,

$$\mathbf{E} = \frac{\mathbf{A} + \mathbf{B}}{2} \tag{1.0.2}$$

$$=\frac{\binom{0}{-4}+\binom{2}{-4}}{2} \tag{1.0.3}$$

$$= \begin{pmatrix} 1 \\ -4 \end{pmatrix} \tag{1.0.4}$$

$$\mathbf{F} = \frac{\mathbf{B} + \mathbf{C}}{2} \tag{1.0.5}$$

$$= \frac{\binom{2}{-4} + \binom{2}{0}}{2} \tag{1.0.6}$$

$$= \begin{pmatrix} 2 \\ -2 \end{pmatrix} \tag{1.0.7}$$

$$\mathbf{G} = \frac{\mathbf{D} + \mathbf{C}}{2} \tag{1.0.8}$$

$$=\frac{\binom{0}{0}+\binom{2}{0}}{2}\tag{1.0.9}$$

$$= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \tag{1.0.10}$$

$$\mathbf{H} = \frac{\mathbf{D} + \mathbf{A}}{2} \tag{1.0.11}$$

$$=\frac{\binom{0}{0}+\binom{0}{-4}}{2} \tag{1.0.12}$$

$$= \begin{pmatrix} 0 \\ -2 \end{pmatrix} \tag{1.0.13}$$

Thus, Area of Parallelogram ABCD is given by,

$$= (\mathbf{D} - \mathbf{A}) \times (\mathbf{D} - \mathbf{C}) \tag{1.0.14}$$

$$= \begin{vmatrix} 0 & -2 \\ 4 & 0 \end{vmatrix} \tag{1.0.15}$$

$$= 8$$
 (1.0.16)

And, Area of Parallelogram EFGH is given by,

$$= (\mathbf{G} - \mathbf{H}) \times (\mathbf{G} - \mathbf{F}) \tag{1.0.17}$$

$$= \begin{vmatrix} 1 & -1 \\ 2 & 2 \end{vmatrix} \tag{1.0.18}$$

$$=4$$
 (1.0.19)

$$= \frac{1}{2} \text{Area of Parallelogram ABCD} \qquad (1.0.20)$$

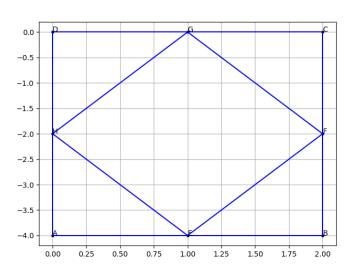


Fig. 0: Paralleogram according to the given vectors