## Straight Lines

## $12^{th}$ Maths - Chapter 10

This is Problem-12 from Exercise 10.2

1. Find the direction cosines of the vector  $\hat{i} + 2\hat{j} + 3\hat{k}$ .

**Solution:** The direction cosines are the cosines of the angles formed by the given vector with the respective axes, let  $\mathbf{A}$  be the given vector

$$\mathbf{A} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \tag{1}$$

The Directional vectors of x, y and z axes are given respectively

$$\mathbf{e_1} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \mathbf{e_2} = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \mathbf{e_3} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \tag{2}$$

The magnitudes for A and directional vectors  $e_1, e_2, e_3$  are

$$\|\mathbf{A}\| = \sqrt{14}, \|\mathbf{e_1}\| = \sqrt{1}, \|\mathbf{e_1}\| = \sqrt{1}, \|\mathbf{e_1}\| = \sqrt{1}$$
 (3)

Let

$$\cos \theta_i = 1, 2, 3 \tag{4}$$

So for different values of  $\cos \theta_i$  the direction cosines of vector  ${\bf A}$  are

$$\cos \theta_1 = \frac{\begin{pmatrix} 1 & 2 & 3 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}}{\sqrt{14}} = \frac{1}{\sqrt{14}} \tag{5}$$

$$\cos \theta_2 = \frac{\begin{pmatrix} 1 & 2 & 3 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}}{\sqrt{14}} = \frac{2}{\sqrt{14}} \tag{6}$$

$$\cos \theta_3 = \frac{\begin{pmatrix} 1 & 2 & 3 \end{pmatrix} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}}{\sqrt{14}} = \frac{3}{\sqrt{14}} \tag{7}$$