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(12)



Assignment - 12.10.3.5

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II **Solution**

Problem

I

 $= \sqrt{\begin{pmatrix} \frac{6}{7} & \frac{2}{7} & -\frac{3}{7} \end{pmatrix} \begin{pmatrix} \frac{6}{7} \\ \frac{2}{7} \\ -\frac{3}{2} \end{pmatrix}}$ (13)

I. PROBLEM

 $=\sqrt{\frac{36}{40}+\frac{4}{40}+\frac{9}{40}}$ (14)

Show that each of the given three vectors is a unit vector: $\frac{1}{7} (2\hat{i} + 3\hat{j} + 6\hat{k})$, $\frac{1}{7} (3\hat{i} - 6\hat{j} + 2\hat{k})$, $\frac{1}{7} (6\hat{i} + 2\hat{j} - 3\hat{k})$ Also, Show that they are mutually perpendicular to eatch other.

(15)(16)

II. SOLUTION

Now, we need to show that they are mutually perpridicular to eatch other.

 $\|\mathbf{C}\| = \mathbf{C}^{\mathsf{T}}\mathbf{C}$

Given

$$\mathbf{A} = \begin{pmatrix} \frac{2}{7} \\ \frac{3}{7} \\ \frac{6}{7} \end{pmatrix}, \mathbf{B} = \begin{pmatrix} \frac{3}{7} \\ -\frac{6}{7} \\ \frac{2}{7} \end{pmatrix}, \mathbf{C} = \begin{pmatrix} \frac{6}{7} \\ \frac{2}{7} \\ -\frac{3}{7} \end{pmatrix}$$
(1)

$$\mathbf{A}^{\top}\mathbf{B} = \begin{pmatrix} \frac{2}{7} & \frac{3}{7} & \frac{6}{7} \end{pmatrix} \begin{pmatrix} \frac{3}{7} \\ -\frac{6}{7} \\ \frac{2}{7} \end{pmatrix}$$
 (17)

$$||\mathbf{A}|| = \mathbf{A}^{\mathsf{T}} \mathbf{A}$$
 (2)

$$= \frac{6}{49} - \frac{18}{49} + \frac{12}{49}$$

$$= 0 (18)$$

$$\|\mathbf{A}\| = \mathbf{A}^{\top} \mathbf{A}$$

$$= \sqrt{\begin{pmatrix} \frac{2}{7} & \frac{3}{7} & \frac{6}{7} \end{pmatrix} \begin{pmatrix} \frac{2}{7} \\ \frac{3}{7} \\ \frac{6}{7} \end{pmatrix}}$$
(2)

$$\mathbf{B}^{\mathsf{T}}\mathbf{C} = \begin{pmatrix} \frac{3}{7} & -\frac{6}{7} & \frac{2}{7} \end{pmatrix} \begin{pmatrix} \frac{6}{7} \\ \frac{2}{7} \\ -\frac{3}{7} \end{pmatrix}$$
 (20)

$$=\sqrt{\frac{4}{49} + \frac{9}{49} + \frac{36}{49}}\tag{4}$$

$$=\frac{18}{49} - \frac{12}{49} - \frac{6}{49} \tag{21}$$

$$= \sqrt{\frac{49}{49}}$$
 49 49 (5)

$$=0$$
 (22)

$$= 1 \tag{6}$$

$$\mathbf{C}^{\top}\mathbf{A} = \begin{pmatrix} \frac{6}{7} & \frac{2}{7} & -\frac{3}{7} \end{pmatrix} \begin{pmatrix} \frac{2}{7} \\ \frac{3}{7} \\ \frac{6}{7} \end{pmatrix}$$
 (23)

$$\|\mathbf{B}\| = \mathbf{B}^{\mathsf{T}}\mathbf{B} \tag{7}$$

$$= \frac{12}{49} + \frac{6}{49} - \frac{18}{49}$$

$$= 0 \tag{24}$$

$$= \sqrt{ \begin{pmatrix} \frac{3}{7} & -\frac{6}{7} & \frac{2}{7} \end{pmatrix} \begin{pmatrix} \frac{3}{7} \\ -\frac{6}{7} \\ \frac{2}{7} \end{pmatrix} }$$

= 1

$$\mathbf{A}^{\mathsf{T}}\mathbf{B} = \mathbf{B}^{\mathsf{T}}\mathbf{C} = \mathbf{C}^{\mathsf{T}}\mathbf{A} = 0 \tag{26}$$

$$= \sqrt{\frac{9}{49} + \frac{36}{49} + \frac{4}{49}}$$

$$= \sqrt{\frac{49}{49}}$$
(10)

Thus, they are mutully perpendiculars to eatch other https://github.com/sssurajit/fwc/blob/main/vectors /12.10.3.5/codes/code.py

Execute the code by using the command (11)python3 code.py