VECTORS

12^{th} Maths - EXERCISE-10.3

1. Find the angle between two vectors \overrightarrow{a} and \overrightarrow{b} with magnitudes $\sqrt{3}$ and 2 respectively having $\overrightarrow{a} \cdot \overrightarrow{b} = \sqrt{6}$.

Solution: Given points are

$$\|\mathbf{a}\| = \sqrt{3} \tag{1}$$

$$\|\mathbf{b}\| = 2 \tag{2}$$

$$\mathbf{a}^{\top}\mathbf{b} = \sqrt{6} \tag{3}$$

$$\cos \theta = \frac{\mathbf{a}^{\top} \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|}$$

$$= \frac{\sqrt{6}}{\sqrt{3} \times 2}$$

$$= \frac{1}{\sqrt{2}}$$
(6)

$$=\frac{\sqrt{6}}{\sqrt{3}\times 2}\tag{5}$$

$$=\frac{1}{\sqrt{2}}\tag{6}$$

$$\implies \theta = 45^{\circ} \tag{7}$$