

# Assignment 1

Jaswanth Chowdary Madala

- 1) Consider the following population and year graph, Find the slope of the line AB and using it, find what will be the population in the year 2010?

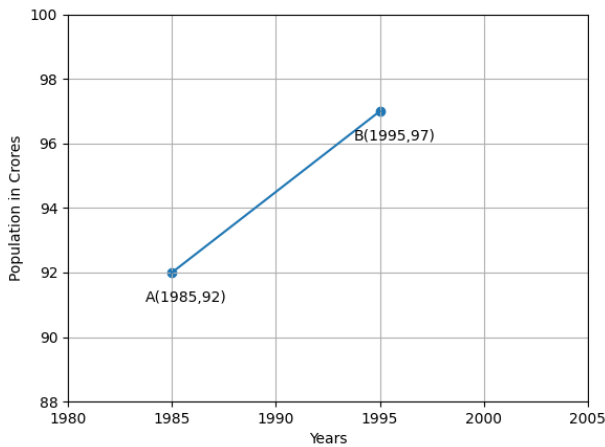


Fig. 1: Graph

**Solution:** Given the points

$$\mathbf{A} \begin{pmatrix} 1985 \\ 92 \end{pmatrix}, \mathbf{B} \begin{pmatrix} 1995 \\ 97 \end{pmatrix} \quad (0.0.1)$$

The direction vector is given by,

$$\mathbf{m} = \mathbf{B} - \mathbf{A} \quad (0.0.2)$$

$$\mathbf{m} = \begin{pmatrix} 1995 \\ 97 \end{pmatrix} - \begin{pmatrix} 1985 \\ 92 \end{pmatrix} \quad (0.0.3)$$

$$\mathbf{m} = \begin{pmatrix} 10 \\ 5 \end{pmatrix} \quad (0.0.4)$$

Direction vector,

$$\mathbf{m} = \frac{1}{5} \begin{pmatrix} 10 \\ 5 \end{pmatrix} \quad (0.0.5)$$

$$\mathbf{m} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \quad (0.0.6)$$

The slope of the line,  $m$  can be found by expressing the direction vector  $\mathbf{m}$  in the following

form

$$\mathbf{m} = \begin{pmatrix} 1 \\ m \end{pmatrix} \quad (0.0.7)$$

$$\mathbf{m} = \begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} \quad (0.0.8)$$

$$m = \frac{1}{2} \quad (0.0.9)$$

The normal of the line  $\mathbf{n}$  is given by,

$$\mathbf{n} = \begin{pmatrix} 1 \\ -2 \end{pmatrix} \quad (0.0.10)$$

Any point,  $\mathbf{x}$  on the line can be written as

$$\mathbf{n}^T(\mathbf{x} - \mathbf{A}) = 0 \quad (0.0.11)$$

$$\mathbf{n}^T \mathbf{x} = \mathbf{n}^T \mathbf{A} \quad (0.0.12)$$

$$\begin{pmatrix} 1 & -2 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 1 & -2 \end{pmatrix} \begin{pmatrix} 1985 \\ 92 \end{pmatrix} \quad (0.0.13)$$

$$\begin{pmatrix} 1 & -2 \end{pmatrix} \mathbf{x} = (1 \times 1985) + (-2 \times 92) \quad (0.0.14)$$

$$\begin{pmatrix} 1 & -2 \end{pmatrix} \mathbf{x} = 1801 \quad (0.0.15)$$

We need to find the population in the year 2010

$$\mathbf{x} = \begin{pmatrix} 2010 \\ y \end{pmatrix} \quad (0.0.16)$$

$$\begin{pmatrix} 1 & -2 \end{pmatrix} \begin{pmatrix} 2010 \\ y \end{pmatrix} = 1801 \quad (0.0.17)$$

$$(1 \times 2010) + (-2 \times y) = 1801 \quad (0.0.18)$$

$$2y = 209 \quad (0.0.19)$$

$$y = \frac{209}{2} \quad (0.0.20)$$

Hence the population in the year 2010 is 104.5 crores.