

# Math Document Template

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**Abstract**—This is a document explaining for a question on the concept of triangles.

Download all python codes from

```
svn co https://github.com/Ashuwin/Summer_2020/trunk/triangle/codes
```

and latex-tikz codes from

```
svn co https://github.com/Ashuwin/Summer_2020/trunk/triangle/figs
```

Design Parameters	
Parameters	Value
PQ	4
PR	5
QR	6

TABLE 2.2: Triangle  $PQR$

## 1 PROBLEM

In  $\triangle PQR$ ,  $PR > PQ$  and  $PS$  bisects  $\angle QPR$ . Prove that  $\angle PSR > \angle PSQ$

## 2 CONSTRUCTION

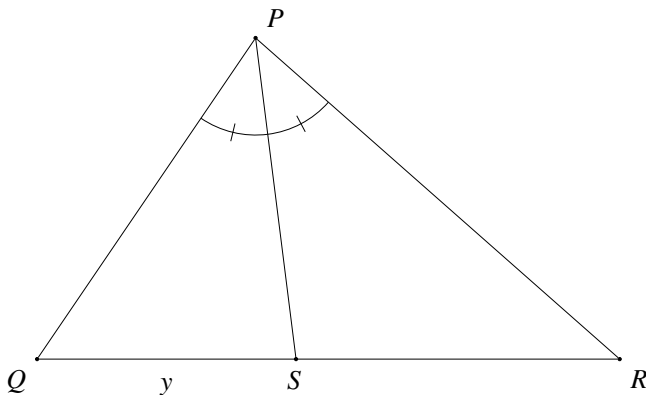


Fig. 2.0: Triangle by Latex-Tikz

2.1. The figure obtained looks like Fig. 2.0.  $PR > PQ$ ,  $\angle QPS = \angle SPR = x$

2.2. The design parameters used for construction

**Solution:** See Table. 2.2.

2.3. Find the coordinates of various points:

**Solution:** From the given information,

$$\mathbf{P} = \begin{pmatrix} a \\ b \end{pmatrix} \quad (2.3.1)$$

$$\mathbf{Q} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \quad (2.3.2)$$

$$\mathbf{R} = \begin{pmatrix} p \\ 0 \end{pmatrix} \quad (2.3.3)$$

$$\mathbf{S} = \begin{pmatrix} y \\ 0 \end{pmatrix} \quad (2.3.4)$$

where

$$a = (p^2 + r^2 - q^2)/2p$$

$$b = \sqrt{r^2 - a^2}$$

2.4. Point  $S$  can be found by Triangle angle bisector theorem.

$$\frac{\|QS\|}{\|PQ\|} = \frac{\|SR\|}{\|PR\|}$$

$$\frac{y}{4} = \frac{6-y}{5}$$

$$5y = 24 - 4y$$

$$9y = 24$$

$$y = \frac{8}{3}$$

2.5. The derived parameters used for construction

**Solution:** From the given information, The values are listed in 2.5

2.6. Draw fig. 2.6.

**Solution:** The following Python code generates

Derived values	
Parameter	values
<b>P</b>	$\begin{pmatrix} 2.25 \\ 3.3072 \end{pmatrix}$
<b>S</b>	$\begin{pmatrix} 8/3 \\ 0 \end{pmatrix}$

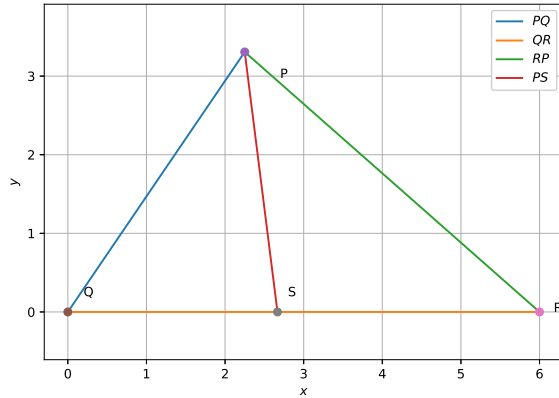
TABLE 2.5: *TrianglePQR*

Fig. 2.6: Triangle generated using python

Fig. 2.6

```
codes/tri.py
```

and the equivalent latex-tikz code generating Fig. 2.6 is

```
figs/triangle.tex
```

### 3 SOLUTION

$\angle PSQ$  is the angle between **SP** and **SQ**

$\angle PSR$  is the angle between **SP** and **SR**

Finding the Scalar Products:

$$(\mathbf{P} - \mathbf{S})^T(\mathbf{Q} - \mathbf{S}) = \|\mathbf{P} - \mathbf{S}\| \|\mathbf{Q} - \mathbf{S}\| \cos \angle PSQ$$

$$\angle PSQ = 82.82^\circ$$

$$(\mathbf{P} - \mathbf{S})^T(\mathbf{R} - \mathbf{S}) = \|\mathbf{P} - \mathbf{S}\| \|\mathbf{R} - \mathbf{S}\| \cos \angle PSR$$

$$\angle PSR = 97.17^\circ$$

The above calculations are found by executing the following python file

```
codes/finding_angles.py
```

Therefore,  $\angle PSR > \angle PSQ$