1

# Matrix Applications

## G V V Sharma\*

1

5

## **CONTENTS**

## 1 Balancing Chemical Equations

### 2 Miscellaneous

Abstract—This manual shows how to balance chemical equations using matrices, based on exercises from the NCERT textbooks from Class 6-12.

Download python codes using

svn co https://github.com/gadepall/school/trunk/ ncert/computation/codes

## 1 BALANCING CHEMICAL EQUATIONS

## 1.1. Balance the following chemical equation.

$$HNO_3 + Ca(OH)_2 \to Ca(NO_3)_2 + H_2O$$
(1.1.1)

**Solution:** Let the balanced version of (1.1.1) be

$$x_1HNO_3 + x_2Ca(OH)_2$$
  
 $\to x_3Ca(NO_3)_2 + x_4H_2O$  (1.1.2)

which results in the following equations:

$$(x_1 + 2x_2 - 2x_4)H = 0 (1.1.3)$$

$$(x_1 - 2x_3)N = 0 (1.1.4)$$

$$(3x_1 + 2x_2 - 6x_3 - x_4)O = 0 (1.1.5)$$

$$(x_2 - x_3)Ca = 0 (1.1.6)$$

which can be expressed as

$$x_1 + 2x_2 + 0x_3 - 2x_4 = 0 ag{1.1.7}$$

$$x_1 + 0x_2 - 2x_3 + 0.x_4 = 0$$
 (1.1.8)

$$3x_1 + 2x_2 - 6x_3 - x_4 = 0 (1.1.9)$$

$$0x_1 + x_2 - x_3 + 0.x_4 = 0 (1.1.10)$$

\*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All content in this manual is released under GNU GPL. Free and open source.

resulting in the matrix equation

$$\begin{pmatrix} 1 & 2 & 0 & -2 \\ 1 & 0 & -2 & 0 \\ 3 & 2 & -6 & -1 \\ 0 & 1 & -1 & 0 \end{pmatrix} \mathbf{x} = \mathbf{0}$$
 (1.1.11)

where.

$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \tag{1.1.12}$$

(1.1.11) can be reduced as follows

$$\begin{pmatrix}
1 & 2 & 0 & -2 \\
1 & 0 & -2 & 0 \\
3 & 2 & -6 & -1 \\
0 & 1 & -1 & 0
\end{pmatrix}$$
(1.1.13)

$$\stackrel{R_2 \leftarrow R_2 - R_1}{\underset{R_3 \leftarrow \frac{R_3}{3} - R_1}{\longleftrightarrow}} \begin{pmatrix}
1 & 2 & 0 & -2 \\
0 & -2 & -2 & 2 \\
0 & -\frac{4}{3} & -2 & \frac{5}{3} \\
0 & 1 & -1 & 0
\end{pmatrix} (1.1.14)$$

$$\stackrel{R_2 \leftarrow -\frac{R_2}{2}}{\longleftrightarrow} \begin{pmatrix}
1 & 2 & 0 & -2 \\
0 & 1 & 1 & -1 \\
0 & -\frac{4}{3} & -2 & \frac{5}{3} \\
0 & 1 & -1 & 0
\end{pmatrix} (1.1.15)$$

$$\frac{R_3 \leftarrow R_3 + \frac{4}{3}R_2}{R_4 \leftarrow R_4 - R_2} \begin{pmatrix}
1 & 2 & 0 & -2 \\
0 & 1 & 1 & -1 \\
0 & 0 & -\frac{2}{3} & \frac{1}{3} \\
0 & 0 & -2 & 1
\end{pmatrix} (1.1.16)$$

$$\xrightarrow{R_1 \leftarrow R_1 - 2R_2} \begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & 1 & -1 \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & -2 & 1
\end{pmatrix}$$
(1.1.17)

$$\xrightarrow{R_4 \leftarrow R_4 + 2R_3} \begin{pmatrix} 1 & 0 & -2 & 0 \\ 0 & 1 & 1 & -1 \\ 0 & 0 & 1 & -\frac{1}{2} \\ 0 & 0 & 0 & 0 \end{pmatrix}$$
 (1.1.18)

$$\frac{R_1 \leftarrow R_1 + 2R_3}{R_2 \leftarrow R_2 - R_3} \begin{pmatrix}
1 & 0 & 0 & -1 \\
0 & 1 & 0 & -\frac{1}{2} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & 0 & 0
\end{pmatrix} (1.1.19)$$

Thus,

$$x_1 = x_4, x_2 = \frac{1}{2}x_4, x_3 = \frac{1}{2}x_4$$
 (1.1.20)

$$\implies \mathbf{x} = x_4 \begin{pmatrix} 1\\\frac{1}{2}\\\frac{1}{2}\\1 \end{pmatrix} = \begin{pmatrix} 2\\1\\1\\2 \end{pmatrix} \qquad (1.1.21)$$

by substituting  $x_4 = 2$ 

Hence, (1.1.2) finally becomes

$$2HNO_3 + Ca(OH)_2 \rightarrow Ca(NO_3)_2 + 2H_2O$$
(1.1.22)

1.2. Balance the following chemical equation.

Zinc + Silver nitrate  $\rightarrow$  Zinc nitrate + Silver (1.2.1)

#### **Solution:**

1.2.1 can be written as

$$Zn + AgNO_3 \rightarrow Ag + Zn(NO_3)_2$$
 (1.2.2)

Suppose the balanced form of the equation is

$$x_1Zn + x_2AgNO_3 \rightarrow x_3Ag + x_4Zn(NO_3)_2$$
(1.2.3)

which results in the following equations:

$$(x_1 - 2x_4)Zn = 0 (1.2.4)$$

$$(x_2 - x_3)Ag = 0 ag{1.2.5}$$

$$(x_3 - 2x_4)N = 0 ag{1.2.6}$$

$$(3x_3 - 6x_4)O = 0 (1.2.7)$$

which can be expressed as

$$x_1 + 0x_2 + 0x_3 - x_4 = 0 ag{1.2.8}$$

$$0x_1 + x_2 - x_3 + 0x_4 = 0 ag{1.2.9}$$

$$0x_1 + 0x_2 + x_3 - 2x_4 = 0 (1.2.10)$$

$$0x_1 + 0x_2 + 3x_3 - 6x_4 = 0 (1.2.11)$$

resulting in the matrix equation

$$\begin{pmatrix} 1 & 0 & 0 & -1 \\ 0 & 1 & -1 & 0 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 3 & -6 \end{pmatrix} \mathbf{x} = \mathbf{0}$$
 (1.2.12)

where,

$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \tag{1.2.13}$$

(1.2.12) can be reduced as

$$\begin{pmatrix}
1 & 0 & 0 & -1 \\
0 & 1 & -1 & 0 \\
0 & 0 & 1 & -2 \\
0 & 0 & 3 & -6
\end{pmatrix}$$

$$\xrightarrow{R_4 \leftarrow R_4 - 3R_3}
\begin{pmatrix}
1 & 0 & 0 & -1 \\
0 & 1 & -1 & 0 \\
0 & 0 & 1 & -2 \\
0 & 0 & 0 & 0
\end{pmatrix} (1.2.14)$$

Thus,

$$x_1 = x_4, x_2 = 2x_4, x_3 = 2x_4$$
 (1.2.15)

$$\implies \mathbf{x} = \begin{pmatrix} x_4 \\ 2x_4 \\ 2x_4 \\ x_4 \end{pmatrix} = x_4 \begin{pmatrix} 1 \\ 2 \\ 2 \\ 1 \end{pmatrix} \quad (1.2.16)$$

by substituting  $x_4 = 1$ , we get

$$\implies \mathbf{x} = \begin{pmatrix} 1\\2\\2\\1 \end{pmatrix} \tag{1.2.17}$$

Hence, (1.2.3) finally becomes

$$Zn + 2AgNO_3 \rightarrow 2Ag + Zn(NO_3)_2$$
 (1.2.18)

1.3. Write the balanced chemical equations for the following reaction :

$$BaCl_2 + K_2SO_4 \rightarrow BaSO_4 + KCl$$
 (1.3.1)

**Solution:** We know that the number of atoms of each element remains the same, before and after a chemical reaction.

Equation (1.3.1) can be written as

$$x_1BaCl_2 + x_2K_2SO_4 \rightarrow x_3BaSO_4 + x_4KCl$$
(1.3.2)

Element wise contribution in forming the respective chemical compound can be written in the form of equation as

$$Ba: x_1 + 0x_2 - x_3 - 0x_4 = 0$$
 (1.3.3)

$$Cl: 2x_1 + 0x_2 - 0x_3 - 1x_4 = 0$$
 (1.3.4)

$$K: 0x_1 + 2x_2 - 0x_3 - 1x_4 = 0 (1.3.5)$$

$$S: 0x_1 + 1x_2 - 1x_3 - 0x_4 = 0$$
 (1.3.6)

$$O: 0x_1 + 4x_2 - 4x_3 - 0x_4 = 0 (1.3.7)$$

In matrix form this can be written as

$$A\mathbf{x} = 0 \tag{1.3.8}$$

$$\begin{pmatrix}
1 & 0 & -1 & 0 \\
2 & 0 & 0 & -1 \\
0 & 2 & 0 & -1 \\
0 & 1 & -1 & 0 \\
0 & 4 & -4 & 0
\end{pmatrix}
\begin{pmatrix}
x_1 \\
x_2 \\
x_3 \\
x_4
\end{pmatrix} = \begin{pmatrix}
0 \\
0 \\
0 \\
0 \\
0
\end{pmatrix}$$
(1.3.9)

Using Gaussian Elimination method

$$\stackrel{R_2 \leftrightarrow R_5}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 4 & -4 & 0 & 0 \\
0 & 2 & 0 & -1 & 0 \\
0 & 1 & -1 & 0 & 0 \\
2 & 0 & 0 & -1 & 0
\end{pmatrix} (1.3.10)$$

$$\stackrel{R_5 \leftarrow 2R_1 - R_5}{\rightleftharpoons} \begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 4 & -4 & 0 & 0 \\
0 & 2 & 0 & -1 & 0 \\
0 & 1 & -1 & 0 & 0 \\
0 & 0 & -2 & 1 & 0
\end{pmatrix} (1.3.11)$$

$$(1 & 0 & -1 & 0 & 0$$

$$\stackrel{R_5 \leftrightarrow R_5}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 4 & -4 & 0 & 0 \\
0 & 0 & 4 & -2 & 0 \\
0 & 0 & -2 & 1 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix} (1.3.13)$$

$$\stackrel{R_4 \leftarrow 2R_4 - R_3}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 4 & -4 & 0 & 0 \\
0 & 0 & 4 & -2 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix} (1.3.14)$$

Clearly the system is linearly dependent. Therefore by fixing the value of  $x_4 = 2$ , one of the possible vectors  $\mathbf{x}$  is

$$\mathbf{x} = \begin{pmatrix} 1\\1\\1\\2 \end{pmatrix} \tag{1.3.15}$$

Hence by putting the values of  $x_1, x_2, x_3, x_4$  in equation (1.3.1) we get our balanced chemical equation as

$$BaCl_2 + K_2SO_4 \rightarrow BaSO_4 + 2KCl$$
 (1.3.16)

1.4. Balance the following chemical equation.

$$Fe + H_2O \rightarrow Fe_3O_4 + H_2$$
 (1.4.1)

#### **Solution:**

Let the balanced version of (1.4.1) be

$$x_1Fe + x_2H_2O \rightarrow x_3Fe_3O_4 + x_4H_2$$
 (1.4.2)

which results in the following equations

$$(x_1 - 3x_3) Fe = 0$$
  
 $(2x_2 - 2x_4) H = 0$  (1.4.3)  
 $(x_2 - 4x_3) O = 0$ 

which can be expressed as

$$x_1 + 0.x_2 - 3x_3 + 0.x_4 = 0$$

$$0.x_1 + 2x_2 + 0.x_3 - 2x_4 = 0$$

$$0.x_1 + x_2 - 4x_3 + 0.x_4 = 0$$
(1.4.4)

resulting in the matrix equation

$$\begin{pmatrix} 1 & 0 & -3 & 0 \\ 0 & 2 & 0 & -2 \\ 0 & 1 & -4 & 0 \end{pmatrix} \mathbf{x} = \mathbf{0}$$
 (1.4.5)

where

$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \tag{1.4.6}$$

(1.4.5) can be row reduced as follows

$$\begin{pmatrix}
1 & 0 & -3 & 0 \\
0 & 2 & 0 & -2 \\
0 & 1 & -4 & 0
\end{pmatrix}
\xrightarrow{R_2 \leftarrow \frac{R_2}{2}}
\begin{pmatrix}
1 & 0 & -3 & 0 \\
0 & 1 & 0 & -1 \\
0 & 1 & -4 & 0
\end{pmatrix}$$

$$\xrightarrow{R_3 \leftarrow R_3 - R_2}
\begin{pmatrix}
1 & 0 & -3 & 0 \\
0 & 1 & 0 & -1 \\
0 & 0 & -4 & 1
\end{pmatrix}$$

$$\xrightarrow{R_1 \leftarrow 4R_1 - 3R_3}
\begin{pmatrix}
4 & 0 & 0 & -3 \\
0 & 1 & 0 & -1 \\
0 & 0 & -4 & 1
\end{pmatrix}$$

$$\xrightarrow{R_1 \leftarrow \frac{1}{4}}$$

$$\xrightarrow{R_3 \leftarrow -\frac{1}{4}R_3}
\begin{pmatrix}
1 & 0 & 0 & -\frac{3}{4} \\
0 & 1 & 0 & -1 \\
0 & 0 & 1 & -\frac{1}{4}
\end{pmatrix}$$

$$\xrightarrow{R_1 \leftarrow \frac{1}{4}}$$

$$\xrightarrow{R_3 \leftarrow -\frac{1}{4}R_3}
\begin{pmatrix}
1 & 0 & 0 & -\frac{3}{4} \\
0 & 1 & 0 & -1 \\
0 & 0 & 1 & -\frac{1}{4}
\end{pmatrix}$$

$$\xrightarrow{R_1 \leftarrow \frac{1}{4}}$$

Thus,

$$x_1 = \frac{3}{4}x_4, x_2 = x_4, x_3 = \frac{1}{4}x_4$$
 (1.4.11) (1.4.12)

$$\implies \mathbf{x} = x_4 \begin{pmatrix} \frac{3}{4} \\ 1 \\ \frac{1}{4} \\ 1 \end{pmatrix} = \begin{pmatrix} 3 \\ 4 \\ 1 \\ 4 \end{pmatrix} \tag{1.4.13}$$

upon substituting  $x_4 = 4$ . (1.4.2) then becomes

$$3Fe + 4H_2O \rightarrow Fe_3O_4 + 4H_2$$
 (1.4.14)

1.5. Balance the following chemical equation.

$$NaOH + H_2SO_4 \rightarrow Na_2SO_4 + H_2O$$
 (1.5.1)

**Solution:** Let the balanced version of (1.5.1) be

$$x_1NaOH + x_2H_2SO_4 \rightarrow x_3Na_2SO_4 + x_4H_2O$$
 (1.5.2)

which results in the following equations:

$$(x_1 - 2x_3)Na = 0 (1.5.3)$$

$$(x_1 + 4x_2 - 4x_3 - x_4)O = 0 (1.5.4)$$

$$(x_1 + 2x_2 - 2x_4)H = 0 (1.5.5)$$

$$(x_2 - x_3)S = 0 (1.5.6)$$

which can be expressed as

$$x_1 + 0x_2 - 2x_3 + 0x_4 = 0 (1.5.7)$$

$$x_1 + 4x_2 - 4x_3 - x_4 = 0 (1.5.8)$$

$$x_1 + 2x_2 + 0x_3 - 2x_4 = 0 ag{1.5.9}$$

$$0x_1 + x_2 - x_3 + 0x_4 = 0 (1.5.10)$$

resulting in the matrix equation

$$\begin{pmatrix} 1 & 0 & -2 & 0 \\ 1 & 4 & -4 & -1 \\ 1 & 2 & 0 & -2 \\ 0 & 1 & -1 & 0 \end{pmatrix} \mathbf{x} = \mathbf{0}$$
 (1.5.11)

where,

$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \tag{1.5.12}$$

(1.5.11) can be reduced as

$$\begin{pmatrix}
1 & 0 & -2 & 0 \\
1 & 4 & -4 & -1 \\
1 & 2 & 0 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}
\xrightarrow{R_2 \leftarrow R_2 - R_1}
\xrightarrow{R_3 \leftarrow R_3 - R_1}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 4 & -2 & -1 \\
0 & 2 & 2 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}$$

$$(1.5.13)$$

$$\xrightarrow{R_2 \leftarrow \frac{R_2}{4}}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 2 & 2 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}$$

$$(1.5.14)$$

$$\xrightarrow{R_3 \leftarrow R_3 - 2R_2}
\xrightarrow{R_4 \leftarrow R_4 - R_2}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 0 & 3 & -\frac{3}{2} \\
0 & 0 & -\frac{1}{2} & \frac{1}{4}
\end{pmatrix}$$

$$(1.5.15)$$

$$\xrightarrow{R_3 \leftarrow \frac{R_3}{3}}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 0 & 3 & -\frac{3}{2} \\
0 & 0 & -\frac{1}{2} & \frac{1}{4}
\end{pmatrix}$$

$$(1.5.15)$$

$$\xrightarrow{R_3 \leftarrow \frac{R_3}{3}} \begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & -\frac{1}{2} & \frac{1}{4}
\end{pmatrix}$$
(1.5.16)

$$\begin{array}{c}
\stackrel{R_2 \leftarrow R_2 + \frac{R_3}{2}}{\longleftrightarrow} \\
\stackrel{R_4 \leftarrow R_4 + \frac{R_3}{2}}{\longleftrightarrow} \\
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & 0 & -\frac{1}{2} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & 0 & 0
\end{pmatrix}$$
(1.5.17)

$$\stackrel{R_1 \leftarrow R_1 + 2R_3}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & 0 & -1 \\
0 & 1 & 0 & -\frac{1}{2} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & 0 & 0
\end{pmatrix}$$
(1.5.18)

Thus,

$$x_1 = x_4, x_2 = \frac{1}{2}x_4, x_3 = \frac{1}{2}x_4$$
 (1.5.19)

$$\implies \mathbf{x} = x_4 \begin{pmatrix} 1 \\ \frac{1}{2} \\ \frac{1}{2} \\ 1 \end{pmatrix} \qquad (1.5.20)$$

by substituting  $x_4 = 2$ 

$$\mathbf{x} = \begin{pmatrix} 2\\1\\1\\2 \end{pmatrix} \tag{1.5.21}$$

Hence, (1.5.2) finally becomes

$$2NaOH + H_2SO_4 \rightarrow Na_2SO_4 + 2H_2O$$
 (1.5.22)

#### 2 MISCELLANEOUS

2.1. A trust fund has ₹30,000 that must be invested in two different types of bonds. The first bond pays 5% interest per year, and the second bond pays 7% interest per year. Using matrix multiplication, determine how to divide ₹ 30,000 among the two types of bonds. If the trust fund must obtain an annual total interest of:

#### (a) ₹1800 (b)₹2000

Solution: Let ₹30000 be divided into two part  $x_1$  and  $x_2$  in part a), and into two part  $y_1$ and  $y_2$  in part b). Then  $x_1, x_2, y_1, y_2$  satisfies following equations

$$x_1 + x_2 = 30000$$
 (2.1.1)

$$0.05x_1 + 0.07x_2 = 1800 (2.1.2)$$

$$y_1 + y_2 = 30000$$
 (2.1.3)

$$0.05y_1 + 0.07y_2 = 2000 (2.1.4)$$

From (2.1.1) and (2.1.2) we get

$$\begin{pmatrix} 1 & 1 \\ 0.05 & 0.07 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 30000 \\ 1800 \end{pmatrix}$$
 (2.1.5)

and from (2.1.3) and (2.1.4) we get

$$\begin{pmatrix} 1 & 1 \\ 0.05 & 0.07 \end{pmatrix} \begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} 30000 \\ 2000 \end{pmatrix}$$
 (2.1.6)

Combining the two we get

$$\begin{pmatrix} 1 & 1 \\ 0.05 & 0.07 \end{pmatrix} \begin{pmatrix} x_1 & y_1 \\ x_2 & y_2 \end{pmatrix} = \begin{pmatrix} 30000 & 30000 \\ 1800 & 2000 \end{pmatrix}$$

$$\stackrel{R_2 = R_2 - 0.05R_1}{\longrightarrow} \begin{pmatrix} 1 & 1 \\ 0 & 0.02 \end{pmatrix} \begin{pmatrix} x_1 & y_1 \\ x_2 & y_2 \end{pmatrix} = \begin{pmatrix} 30000 & 30000 \\ 300 & 500 \end{pmatrix}$$

$$\stackrel{R_2 = 50R_2}{\longrightarrow} \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_1 & y_1 \\ x_2 & y_2 \end{pmatrix} = \begin{pmatrix} 30000 & 30000 \\ 15000 & 25000 \end{pmatrix}$$

$$\stackrel{R_1 = R_1 - R_2}{\longrightarrow} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_1 & y_1 \\ x_2 & y_2 \end{pmatrix} = \begin{pmatrix} 15000 & 5000 \\ 15000 & 25000 \end{pmatrix}$$

$$(2.1.7)$$

From (2.1.7) we get  $x_1 = ₹15000$ ,  $x_2 = ₹15000$ ,  $y_1$ =₹5000 and  $y_2$ =₹25000. Therefore to get an annual total interest of ₹1800 trust must invest ₹15000 in first bond and ₹15000 in second bond and to get an annual interest of ₹2000 trust must invest ₹5000 in first bond and ₹25000 in second bond.

2.2. The bookshop of a particular school has 10 dozen chemistry books, 8 dozen physics books, 10 dozen economics books. Their selling prices are ₹80, ₹60 and ₹40 each respectively. Find the total amount the bookshop will receive from selling all the books using matrix algebra.

**Solution:**