

frame.m ← main code

coding.m  
- G-def.m

$$\left. \begin{aligned} g_i(l) &= x_s(l) x_s(l-i), \quad l=0, \dots, \text{SOF}-1 \\ h_i(l) &= x_p(l) x_p(l-i), \quad l=0, \dots, \text{PLSC}-1 \end{aligned} \right\} i=1, 2, 4, 8, 16, 32$$

!  $x_s \rightarrow$  mapped SOF symbols,  $x_p \rightarrow$  subsampled PLSC symbols

without PL headers

channel.m  $\Rightarrow y_k = x_k e^{j(2\pi \Delta f k M + \phi_k)} + v_k, \quad k=1, \dots, N$

$\downarrow$   
noise

$$y = \frac{y_k}{|y_k|}$$

detec\_sof\_plsc\_pls\_gld.m  $\rightarrow$  Global summation of SOF/PLS detect SOF

$$dn_1(k) = m_i(k) = \sum_{l=0}^{\text{PLSC}-1} e^{j(\theta(k-l) - \theta(k-l-i))} \cdot h_i(l)$$

$$dn_2(k) = n_i(k) = \sum_{l=0}^{\text{SOF}-1} e^{j(\theta(k-l) - \theta(k-l-i))} \cdot g_i(l)$$

$k=1, \dots, N$

$$P_i(k) = \max \left( |n_i(k - \text{PLSC}) + m_i(k)|, |n_i(k - \text{PLSC}) - m_i(k)| \right), \quad \text{for } k > \text{PLSC}$$

without PL header =  $d = \sum_{i=1} P_i(k), \quad i=1, 2, 4, 8, 16, 32$

with PL header

with PL header  $\Rightarrow$  same as previous case by adding PLS

$$T = \text{threshold} = \frac{\max_i}{99} * (i-1), \quad \max_i = \max \left( \begin{array}{l} \text{with PL header,} \\ \text{without PL header} \end{array} \right)$$

$$P_{FA} = \frac{\sum \text{sign}(|\text{without PL header}| - T)}{N}$$

$$P_{MD} = \frac{\sum \text{sign}(T - |\text{with PL header}|)}{(N + \text{PLSC} + \text{SOF})}$$