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## Names of people you worked with:

lacktriangle

## Websites you used:

- https://www.geeksforgeeks.org/python-math-library-isclose-method/
- <a href="https://docs.scipy.org/doc/numpy/reference/generated/numpy.argmin.html">https://docs.scipy.org/doc/numpy/reference/generated/numpy.argmin.html</a>
- https://realpython.com/numpy-array-programming/
- <a href="https://www.geeksforgeeks.org/numpy-sum-in-python/">https://www.geeksforgeeks.org/numpy-sum-in-python/</a>
- <a href="https://stackoverflow.com/questions/13682628/use-savefig-in-python-with-string-and-iterative-index-in-the-name">https://stackoverflow.com/questions/13682628/use-savefig-in-python-with-string-and-iterative-index-in-the-name</a>
- https://matplotlib.org/3.1.1/gallery/statistics/hist.html
- <a href="https://www.w3schools.com/python/numpy">https://www.w3schools.com/python/numpy</a> array shape.asp
- <a href="https://numpy.org/doc/stable/reference/generated/numpy.in1d.html">https://numpy.org/doc/stable/reference/generated/numpy.in1d.html</a>

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Approximately how many hours did it take you to
complete this assignment (to nearest whole number)?

9

The Rules: Everything you do for this lab should be your own work. Don't look up the answers on the web, or copy them from any other source. You can look up general information about Python on the web, but no copying code you find there. Read the code, close the browser, then write your own code.

By writing or typing your name below you affirm that all of the work contained herein is your own, and was not copied or copied and altered.

### Garrett DuBow

Note: Failure to sign this page will result in a 50 percent penalty. Failure to list people you worked with may result in no grade for this lab. Failure to fill out hours approximation will result in a 10-percent penalty.

#### **BEFORE YOU BEGIN**

- 1) Make a new project for this lab
- 2) Make np\_exercises.py
- 3) Browse through the <u>Numpy quickstart</u> page and familiarize yourself with some of the stuff you can do with Numpy. Pay particular attention to how it avoids using for loops in places you might have used them before.

#### **Learning Objectives:**

You should be able to do the following:

- Use vectorized numpy features to avoid using loops
- Compare numeric arrays
- Determine minimum/maximum values and the positions using numpy
- Draw large samples of random numbers in one line of code
- Filter and sort arrays using numpy

#### Thoughts (come back and read these after you've read the problems):

- 1. Numpy is full of features which make your life convenient. This assignment asks you to take full advantage of them, which means that you will need to figure out how to actually do that. For instance, previously when you sampled random numbers, you would import a function from random, make an empty list, and keep appending to that list after calling your random number generator. You should think about what "the Numpy way" is to do that.
- 2. Note that with Numpy arrays, if you try to do array\_a == array\_b, this does not return a value of True or False, but rather an array of True and False values. This means that the following lines of code will get you into trouble:

```
array_a = np.array([1,2])
if array_a == array_a:
    print('Hooray')

ValueError: The truth value of an array with more than one
element is ambiguous. Use a.any() or a.all().
```

If you see this error, it's because Numpy arrays cannot be treated as Booleans like regular Python lists. As the error says, you should use the <code>any()</code> or <code>all()</code> methods, which return a single Boolean value corresponding to whether any/all of the values in the array are True.

## **Grading Checkpoints**

For this assignment, you should not use loops\*\*! You should be using vectorized operations\*. Functional iterators are also not allowed.

\*\*Student assumed conditional blocks are not loops

\*Use numpy

The following operations will be deducted: for, while, comprehensions (like [x for x in range(10)], map(), and filter().

## **Assignment Grading Checkpoints (12 points total)**

- 1. numpy\_close() works for base case (1 point) and mismatched dimensions case (1 point). [2 points total]\*
- 2. simple minimizer() produces the correct values. [3 points total]\*
- 3. simulate\_dice\_rolls() exhibits the expected behavior (1 point)\* and produces a reasonable histogram for simulate\_dice\_rolls(5, 2000) (1 point). [2 points total]
- 4. is transformation matrix returns the correct values. [2 points total]\*
- 5. nearest\_neighbors() returns the correct set of neighbors (2 points)\* and sorts them by distance in ascending order of distance (1 point) [3 points total]\*
- 6. Your code does not use any loops or functional iterators. [1 point off for each loop detected, no lower bound]\*

### **Standard Grading Checkpoints (3.5 points total)**

- [0.5 points] Turn in a properly filled-in PDF to Gradescope.
- [1 point]\* Code passes PEP8 checks with 10 errors max.
- [2 point] Code passes TA-reviewed style checks for cleanliness, layout, readability, etc.

<sup>\*</sup> The autograder will give you immediate feedback if it's right. Hand in all files to Gradescope.

# **Problem 1 Numpy Equals**

For this assignment, create a new file called **np** exercises.py. Put all functions in there.

Write a function called numpy\_close which takes in two Numpy arrays a and b, as well as a third optional argument tol which defaults to 1e-8. It should return True if the arrays have the same shape and the absolute difference of each corresponding pair of elements less than tol.

• Your function should be able to work on arrays of arbitrary dimensions (they could be 1-D, 2-D, 8-D, etc.)

Comments for grader/additional information (if any)

### **Problem 2 Minimization**

Write a function simple\_minimizer which takes in four arguments:

- A function reference func which represents a 1-D function, e.g.  $f(x) = x^2$ . You can assume that it also will work on a Numpy array, so that if you do func (x values), you will get a corresponding array of y values.
- A start and end, floats which represent the region to search for a minimum. (Throw a ValueError if start > end.)
- An optional param num which defaults to 100.

It should then evaluate func at num evenly-spaced points between start and end (endpoint *inclusive*) and **return two values**: The x corresponding to the **minimum** value of f(x), followed by the actual minimum value. For example, if out of all the values you tested the minimum was f(0.5) = 2.4, you would return (0.5, 2.4).

#### Example:

```
my_func = lambda x: x**2
simple_minimizer(my_func, -1.75, 2.25, num=5)
# Should return (0.25, 0.0625)
```

Comments for grader/additional information (if any)

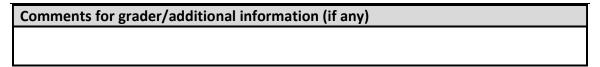
## **Problem 3 Dice roll simulation**

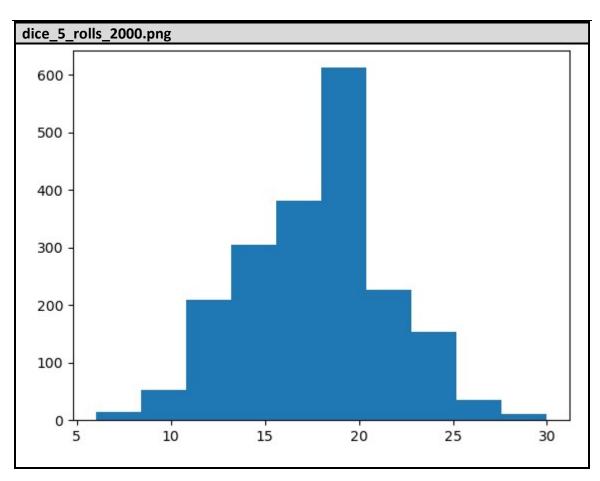
Write a function simulate\_dice\_rolls which takes in two params, num\_rolls and iterations. It should return a 1-D Numpy array of length iterations, where each item is the sum of throwing a fair 6-sided die num rolls times.

### It should also automatically output a histogram of the rolls to the file

 $dice_{0}_{nolls_{1}.png}$ , where  $\{0\}$  is  $num_{nolls}$  and  $\{1\}$  is iterations. (No need for any labels, title, legends, etc.)

Run your function for num rolls = 5 and iterations = 2000 and paste the plot here.





### **Problem 4 Transformation matrix**

Recall that a transformation matrix T is a 4x4 matrix which can be used to represent the position and orientation of a coordinate frame relative to a base frame. A transformation matrix has the following form:

$$T = \begin{bmatrix} R & p \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} & p_1 \\ r_{21} & r_{22} & r_{23} & p_2 \\ r_{31} & r_{32} & r_{33} & p_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

p is a 3x1 matrix in  $\mathbb{R}^3$ , and R is a 3x3 rotation matrix. All rotation matrices have the property that the *transpose* of R is equal to its *inverse*, i.e.  $R^TR = I$ , where I is the 3x3 identity matrix.

Write a function is\_transformation\_matrix that takes in a 4x4 Numpy array and returns True if it's a valid transformation matrix, and False otherwise.

### Example:

```
tf_valid = np.array([
        [0, 0, -1, 4],
        [0, 1, 0, 2.4],
        [1, 0, 0, 3],
        [0, 0, 0, 1]
])

tf_invalid = np.array([
        [1, 2, 3, 1],
        [0, 1, -3, 4],
        [0, 1, 1, 1],
        [-0.5, 4, 0, 2]
])

print(is_transformation_matrix(tf_valid)) # True
print(is_transformation_matrix(tf_invalid)) # False
```

#### Comments for grader/additional information (if any)

## **Problem 5 Nearest neighbors**

Write a function nearest\_neighbors which takes in three arguments: an N x D Numpy array, a 1-dimensional array of length D point, and a distance threshold dist. It should return an M x D Numpy (M <= N) array of all points in the array which are within Euclidean distance dist of point.

The output points should be sorted by the distance from the corresponding point, with closest elements coming first. (You will receive partial credit if the correct points are output but not sorted.)

Example (on Nx3 array):

```
array = np.array([[1, 1, 1], [2, 3, 5], [0, 1, 1], [1.5, 1, 1], [10, 9,
9]])
target_pt = np.array([0, 1, 1])
nearest_neighbors(array, target_pt, 3.0)
# Should return [[0, 1, 1], [1, 1, 1], [1.5, 1, 1]]
```

Hint: You may be interested in the <u>argsort</u> function, which produces a Numpy array of indexes which will sort a given array.

