

(4) Find the no. of times to perform solving supplying for Selection Sort also estimate the time complexity for the orders of rotation sets $(12, 7, 5, -2, 18, 6, 13, 4)$

The Selection Sort algorithm always makes exactly $n-1$ Swaps in the worst case, where n is the no. of elements in the list.

Given $S = \{12, 7, 5, -2, 18, 6, 13, 4\}$

No. of elements $n = 8$

No. of Swaps: $n-1 = 8-1 = 7$

Time Complexity: $O(n^2)$

the no. of Swaps is 7, and the Complexity is $O(n^2)$

(5) Find the index of the target value 10 using binary Solution Search for the following List of elements

$[2, 4, 6, 8, 10, 12, 14, 16, 18, 20]$ given List $[2, 4, 6, 8, 10, 12, 14, 16, 18, 20]$ and value = 10.

low = 0, and high = 9

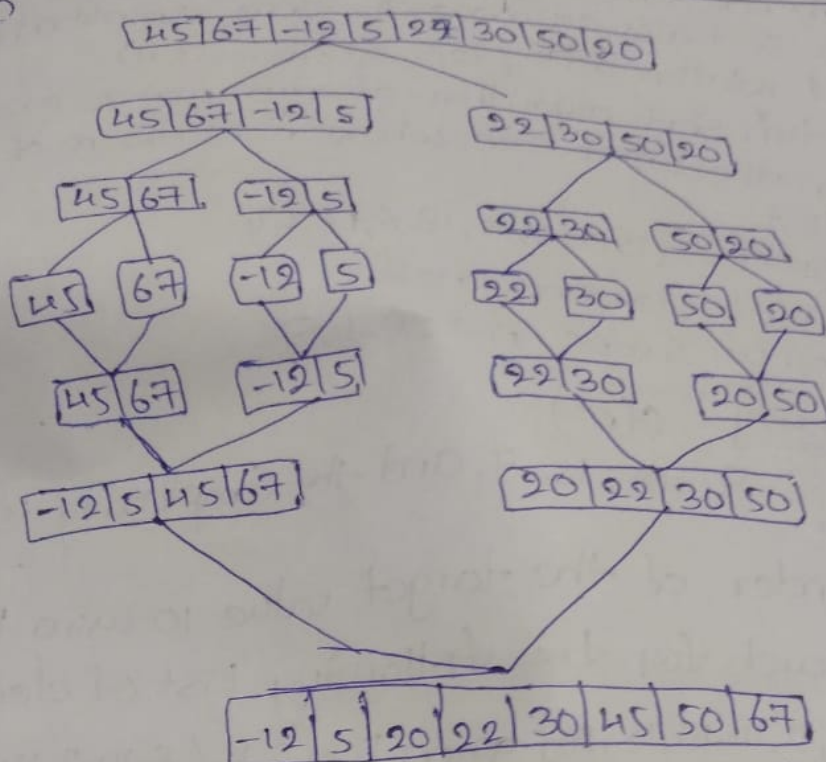
$$\text{mid} = \frac{\text{low} + \text{high}}{2} = \frac{0 + 9}{2} = 4.$$

List[4] = mid = 10 mid = value

Since $10 == 10$ the target is found at index 4

\therefore The Target value = 10 is found at index 4.

Solution



→ the sorted list: $\{-12, 5, 20, 22, 30, 45, 50, 67\}$

(4) → find the no of times to perform Supplying for Selection Sort estimate the time.

Recurrence relation for Comparisons:

$$T(n) = 2T(n/2) + O(n)$$

if $n=1, T(1)=0$.

→ At each level of Recursion most $n-1$ comparisons to merge two of size n so it becomes,

$$T(n) = 2T(n/2) + (n-1)$$

Solving recurrence relation we get

$$T(n) = n \log_2(n) = n+1$$

$$\therefore T(n) = O(n \log n)$$

The recurrence relation is $T(n) = 2T(n/2) + O(n)$

$$T(n) = n \log_2(n) \cdot n+1$$

- ① given an array of $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, -8, 11, -9]$ integers and find the maximum and minimum product that can be obtained by multiplying two integers from the array

Solution:

array is $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, -8, 11, -9]$
we need to consider the largest and smallest product that can be formed by selecting two numbers from the array

1) Sort the array

Sorted array

$[-9, -8, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]$

2) Identify possible candidates for maximum product

3) identify possible candidates for minimum product

Calculating maximum products:

- The two largest positive numbers are 10 and 11

$$10 \times 11 = 110$$

- The two smallest negative numbers are -9 and -8

$$-9 \times -8 = 72$$

The maximum product is 110

Calculating minimum product:

The largest positive and negative number is 11 and -9

$$11 \times -9 = -99$$

The Smallest positive and negative

$$-9 \times -8 = 72$$

-99 is smaller than 72 So

maximum product = 110, and minimum product = -99

2) Demonstrate the binary search algorithm to find the key 23 from the array: $\{2, 5, 8, 12, 16, 23, 38, 56, 72, 91\}$

Solution

given key = 23 and array: $\{2, 5, 8, 12, 16, 23, 38, 56, 72, 91\}$

1) Initialize pointers.

low = 0 and high = 9

calculate mid: $\left\lfloor \frac{\text{low} + \text{high}}{2} \right\rfloor = \left\lfloor \frac{0 + 9}{2} \right\rfloor = 4$

Compare arr[mid] with key:

arr[4] = 16

Since $16 < 23$ update low = mid + 1 = 5

Calculate mid: $\left\lfloor \frac{\text{low} + \text{high}}{2} \right\rfloor = \left\lfloor \frac{5 + 9}{2} \right\rfloor = 7$

Compare arr[mid] with key

arr[7] = 56

Since $56 > 23$ update high = mid - 1 = 6

mid: $\left\lfloor \frac{5 + 6}{2} \right\rfloor = 5$

arr[mid] : arr[5] = 23

$23 == 23$ The key is found at index 5

\therefore The key: 23 is found at index 5.

Apply merge sort and other list of 8 elements, $d = (45, 67, -12, 5, 22, 30, 50, 20)$. Set up recursive solution to find the numbers of key comparison made by merge.