

170) Given two 2×2 Matrices A and B

$$A = \begin{pmatrix} 1 & 7 \\ 3 & 5 \end{pmatrix} \quad B = \begin{pmatrix} 1 & 3 \\ 7 & 5 \end{pmatrix}$$

Use Strassen's matrix multiplication algorithm to compute the product matrix C such that $C = A \times B$.

Test Cases:

Consider the following matrices for testing your implementation:

Test Case 1:

$$A = \begin{pmatrix} 1 & 7 \\ 3 & 5 \end{pmatrix}, \quad B = \begin{pmatrix} 6 & 8 \\ 4 & 2 \end{pmatrix}$$

Expected Output:

$$C = \begin{pmatrix} 18 & 14 \\ 62 & 66 \end{pmatrix}$$

AIM: TO write a python program for Given two 2×2 Matrices A and B

PROGRAM :

```
import numpy as np
```

```
def strassen_multiply(A, B):
```

```
    # Base case: when the matrices are 1x1
```

```
    if len(A) == 1:
```

```
        return A * B
```

```
    a11, a12, a21, a22 = A[0, 0], A[0, 1], A[1, 0], A[1, 1]
```

```
    b11, b12, b21, b22 = B[0, 0], B[0, 1], B[1, 0], B[1, 1]
```

```
    p1 = (a11 + a22) * (b11 + b22)
```

```
    p2 = (a21 + a22) * b11
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$p3 = a11 * (b12 - b22)$

$p4 = a22 * (b21 - b11)$

$p5 = (a11 + a12) * b22$

$p6 = (a21 - a11) * (b11 + b12)$

$p7 = (a12 - a22) * (b21 + b22)$

Combine the 7 products to get the final 2x2 result matrix

$c11 = p1 + p4 - p5 + p7$

$c12 = p3 + p5$

$c21 = p2 + p4$

$c22 = p1 + p3 - p2 + p6$

Construct the resulting matrix

$C = \text{np.array}([c11, c12], [c21, c22])$

return C

$A = \text{np.array}([1, 7], [3, 5])$

$B = \text{np.array}([6, 8], [4, 2])$

$C = \text{strassen_multiply}(A, B)$

print("Resultant Matrix C:")

print(C)

INPUT: Resultant Matrix C:

OUTPUT:

$\begin{bmatrix} 34 & 22 \\ 38 & 34 \end{bmatrix}$

TIME COMPLEXITY: $O(n^3)$