

Exercise 05: Operating point of a spiking neuron

Theoretical Neuroscience I

Maria del Cerro

Johannes Gätjen

Lorena Morton

November 23, 2015

In this exercise we simulate a leaky integrate-and-fire neuron with synaptic inputs. Additionally we simulate an identical neuron without a firing mechanism to determine what the average membrane potential of our neuron would be. Figure 1 shows the membrane voltage over time for the spiking and the non-spiking neuron with one excitatory and one inhibitory presynaptic neuron. Because the membrane potential never reaches the threshold potential our neuron does not spike and the membrane potential is identical between the spiking and the non-spiking neuron. Only when we increase the excitatory synaptic activation as in Figure 2 do we see a difference between the two neurons.

Next we vary the number of excitatory and inhibitory inputs and observe the resulting output firing rate ν_{spk} , as well as the coefficient of variation c_v of the inter-spike interval lengths and the corresponding average membrane potential of the non-spiking neuron $\langle V_{\text{ns}} \rangle$. The results are summed up in Table 1. When we fix the number of inhibitory inputs to zero and only change the number of excitatory inputs, $\langle V_{\text{ns}} \rangle$ as well as ν_{spk} rise with increasing N_{ex} , while c_v falls. With N_{ex} fixed c_v also falls with rising $\langle V_{\text{ns}} \rangle$ and ν_{spk} , but the differences are smaller than in the first case (less than 0.01 difference in c_v between 10.3Hz and 28.7Hz). Now a higher N_{in} produces a lower ν_{spk} .

The coefficient of variation is a measure of how regularly a neuron fires. As a rough rule of thumb, one can say, that the higher $\langle V_{\text{ns}} \rangle$ is, the lower c_v is. This is most clear, when comparing the firing behavior of the neuron for values of $\langle V_{\text{ns}} \rangle$ a few mV above the threshold potential of the neuron with the firing behavior when $\langle V_{\text{ns}} \rangle$ is a few mV below the threshold potential. In the former case, the “standard” behavior for the membrane potential is to rise quickly and reach the threshold potential, where it gets reset. Only when by chance a few more inhibitory than excitatory spikes occur, does the membrane potential not reach the threshold. In the latter case the “standard” behavior for the neuron is maintain a membrane potential below the firing threshold, and only fires, when by chance the number of excitatory spikes outnumbers the inhibitory spikes by enough.

Operating point

To determine the operating point of the neuron, we fix $N_{\text{ex}} = 100$ and vary N_{in} to find the maximum value of c_v . Figure 3 shows a plot of c_v as a function of $\langle V_{\text{ns}} \rangle$. c_v decreases linearly for values of $\langle V_{\text{ns}} \rangle > -58\text{mV}$ but for smaller values of $\langle V_{\text{ns}} \rangle$ the data does not show a clear relation, as the values for c_v fluctuate strongly. Nevertheless, there appears to be a downward trend for smaller values of $\langle V_{\text{ns}} \rangle$. As such, the operating point of the neuron can be estimated to be around -62mV , or 8mV below the threshold potential (-54mV).

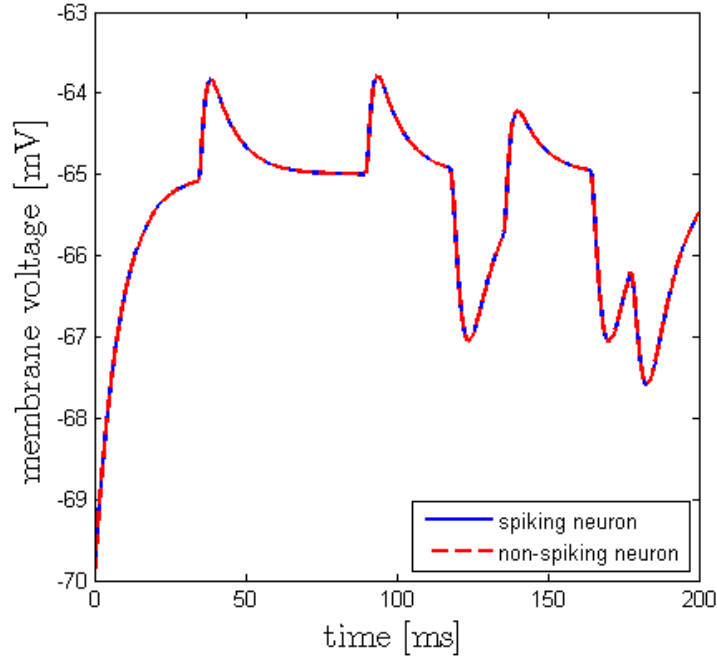


Figure 1: The membrane potential of a LIF neuron with synaptic inputs in blue compared with a non-spiking neuron shown with dashed red. The number of excitatory and inhibitory presynaptic neurons N_{ex} and N_{in} are both set to one, with the spiking rates $\nu_{\text{ex}} = \nu_{\text{in}} = 20\text{Hz}$. Whenever a presynaptic spike occurs the membrane potential increases or decreases a bit, depending on if the presynaptic spike was in the excitatory or the inhibitory neuron, before it relaxes back to the resting potential. Because the threshold potential is never reached the neuron never fires and there is no difference between the spiking and the non-spiking neuron.

N_{ex}	N_{in}	$\nu_{\text{spk}}[\text{Hz}]$	$\langle V_{\text{ns}} \rangle [\text{mV}]$	c_v
30	0	10.53	-57.35	0.86
40	0	30.27	-55.17	0.70
56	0	69.13	-51.98	0.53
100	30	10.33	-61.33	0.953
100	22	28.7	-58.62	0.946
100	13	70	-54.55	0.833

Table 1: Number of excitatory presynaptic neurons N_{ex} , Number of inhibitory presynaptic neurons N_{in} , output spiking rate ν_{spk} , average non-spiking membrane potential $\langle V_{\text{ns}} \rangle$ and coefficient of variation c_v . In the top part N_{in} was fixed to zero and N_{ex} was varied, in the bottom part N_{ex} was fixed to 100 and N_{in} was varied.

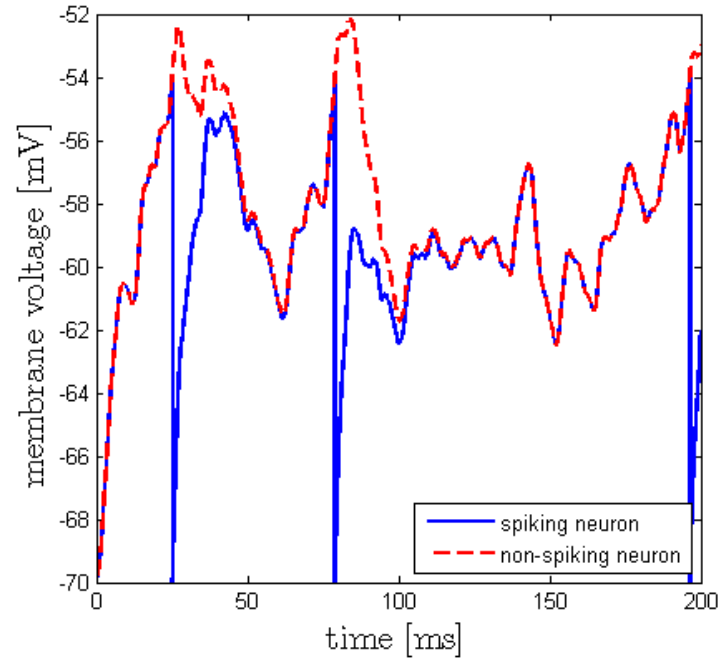


Figure 2: The same setup as in Figure 1, but with $N_{\text{ex}} = 30$. Multiple excitatory spikes in a short amount of time now push the membrane potential above the threshold potential and the spiking neuron fires, whereas the membrane potential of the non-spiking neuron continues to rise. If no spike occurs for some time the two membrane potentials become (almost) equal again.

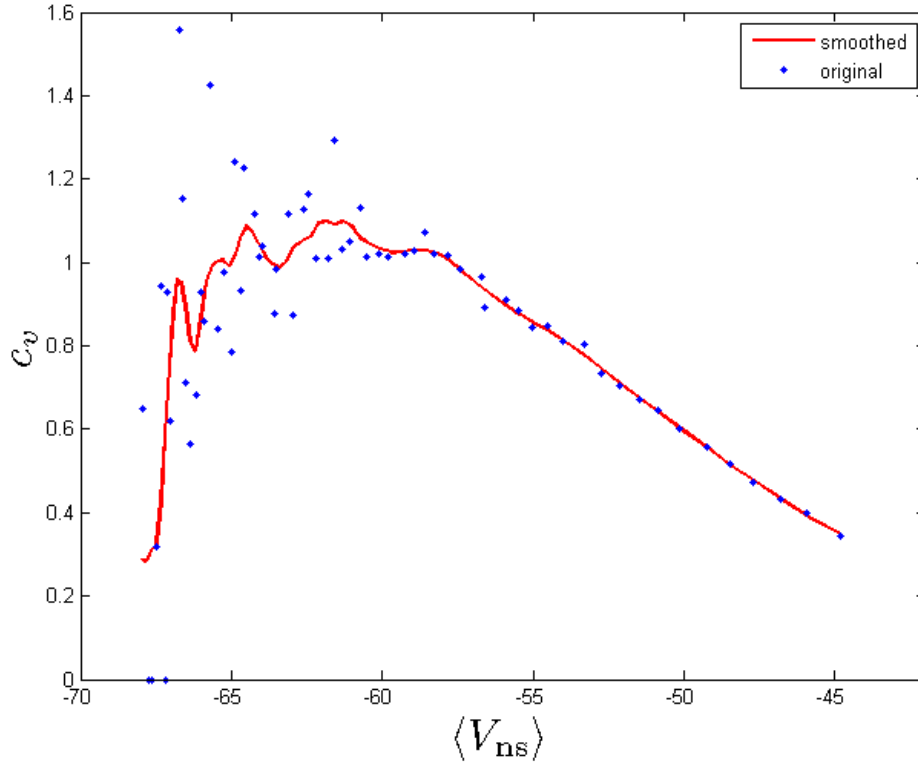


Figure 3: c_v as a function of $\langle V_{\text{ns}} \rangle$. The original data points are shown with blue points, and smoothed data is shown with the red line.