### Lecture 2 - Basic plotting and tidy data

Make your paper figures professionally: Scientific data analysis and visualization with R

Julien Gagneur

- Motivation
- Grammar of graphics and ggplot2
- Types of plots for discrete and continuous variables
- Further plots for low dimensional datasets
- Summary
- Tidy Data
- Tidying up single data tables
- Concatenating tables
- Merging tables

- There is no single tidy representation of a dataset
- Summary

### Lecture overview

12 April Basic Plots
Tidy data

### **Motivation**

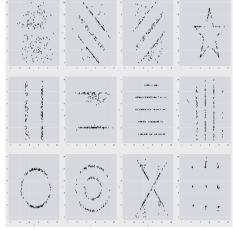
### Why plotting?

- To observe: Discover associations or patterns in the data (Scientific method)
- To communicate findings effectively



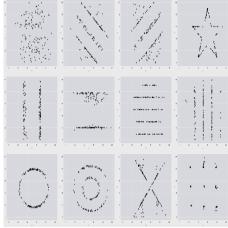
# **Summary statistics lose information**

What have those 12 datasets in common?



## **Summary statistics lose information**

What have those 12 datasets in common?

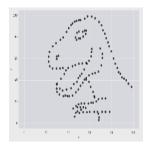


#### These statistics:

- X mean: 52.26
- Y mean: 47.83
- X standard deviation: 16.76
- Y standard deviation: 29.93
- Pearson correlation:-0.06

## **Summary statistics lose information**

This dataset too..



See https://github.com/lockedata/datasauRus

#### These statistics:

- X mean: 52.26
- Y mean: 47.83
- X standard deviation: 16.76
- Y standard deviation: 29.93
- Pearson correlation:-0.06

### Why plotting?

- To observe: Discover associations or patterns in the data (Scientific method)
- To communicate findings effectively
- Summary statistics lose information



# **Another motivating example**

A vector containing 100 (hypothetical) height measurements for adults in Germany: head(height\_dt, n=5)

```
## height
## 1: 1.79
## 2: 1.72
## 3: 1.79
## 4: 1.79
## 5: 1.75

We want to know their average height:
height_dt[, mean(height)]
## [1] 3.3635

Wait... what?
```

### Quiz

Calculating the mean height returns the following output:

height\_dt[, mean(height)]

## [1] 3.3635

#### What happened?

- 4. mean() is not the right function to assess what we want to know.
- 2 B. Adults in Germany are exceptionally tall
- 3 C. A decimal point error in one data point.
- D. It's a multiple testing problem because we are looking at so many data points (n=100).

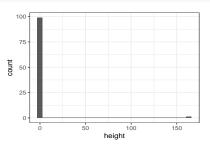
### Solution

#### What happened?

- A. mean() is not the right function to assess what we want to know.
  - No, the mean is exactly what we want.
- B. Adults in Germany are exceptionally tall.
  - OK, no...
- C. A decimal point error in one data point.
- Yes, see next slide.
- D. It's a multiple testing problem because we are looking at so many data points (n=100).
  - This question was intentionally misleading, this does not have anything to do with multiple testing.

# Plotting helps to find outliers in the data

ggplot(height\_dt , aes(height)) + geom\_histogram() + mytheme



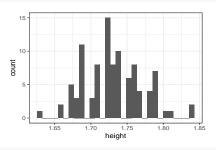
# Removing outliers in the data

A quick way to fix our dataset is to remove our outlier.

height\_dt <- height\_dt[height < 3]

# Removing outliers in the data

ggplot(height\_dt , aes(height)) + geom\_histogram() + mytheme



height\_dt[, mean(height)]

## [1] 1.730808

## Why plotting?

- To observe: Discover associations or patterns in the data (Scientific method)
- To communicate findings effectively
- Summary statistics lose information
- To find "bugs in the data" or bugs in your code



### Our 3 visualization lectures

- Low dimensional visualizations
  - Grammar of graphics
  - 1-d and 2-d plots (e.g. boxplots, histograms, scatterplots)
- High-dimensional visualizations
  - Heatmaps
    - Clustering
    - Dimensionality reduction
- Graphically supported hypotheses
  - Descriptive vs. demonstrative plots
  - Confounding
  - · Guidelines for data visualization and presentation

Grammar of graphics and ggplot2

Grammar of graphics and ggplot2

### **Grammar of Graphics**

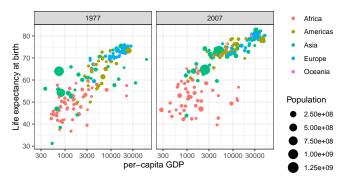
The Grammar of Graphics is a visualization theory developed by Leland Wilkinson in 1999.

- influenced the development of graphics and visualization libraries alike
- 3 key principles
  - Separation of data from aesthetics (e.g. x and y axis, color-coding)
  - Definition of common plot/chart elements (e.g. dot plots, boxplots, etc.)
  - Composition of these common elements (one can combine elements as layers)

# Plotting with ggplot2

The library ggplot2 is a powerful implementation of the grammar of graphics and has become widely used by R programmers.

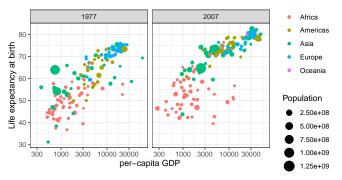
Here is a sophisticated example to compare the relationship between per-capita gross domestic product (GDP) and life expectancy at birth for the years 1997 and 2007:



## Example of a first plot with ggplot2

The code for generating the plot...

```
library(gapminder)
gm_dt <- as.data.table(gapminder)[year %in% c(1977, 2007)]
ggplot(data = gm_dt, aes(x = gdpPercap, y = lifeExp)) + mytheme +
    geom_point(aes(color=continent, size=pop)) + facet_grid(~year) + scale_x_log10() +
    labs(y="Life expectancy at birth", x="per-capita GDP", size="Population")</pre>
```



But how do we create such a plot step by step?

We will have a look at its components and recreate it step by step. . .

# Components of the layered grammar

#### Always:

Data: data.table (or data.frame) object where columns correspond to variables

**Aesthetics:** mapping of data to visual characteristics - what we will see on the plot (aes) - position (x,y), color, size, shape, transparency

**Geometric objects:** geometric representation defining the type of the plot data  $(geom_{-})$  - points, lines, boxplots, . . .

#### Often:

**Scales:** for each aesthetic, describes how visual characteristic is converted to display values (scale\_) - log scales, color scales, size scales, shape scales, . . .

Facets: describes how data is split into subsets and displayed as multiple sub graphs (facet\_)

#### Useful, but with care:

**Stats:** statistical transformations that typically summarize data (stat) - counts, means, medians, regression lines, . . .

#### Domain-specific:

**Coordinate system:** describes 2D space that data is projected onto (coord\_) - Cartesian coordinates, polar coordinates, map projections, . . .

# ggplot Cheatsheet

https://raw.githubusercontent.com/rstudio/cheatsheets/master/datatable.pdf

#### Data

## 6:

```
Let's have a quick look at our data
head(gm_dt[, .(country, continent, gdpPercap, lifeExp, year)])
##
         country continent gdpPercap lifeExp year
                      Asia 786.1134 38.438 1977
## 1: Afghanistan
## 2: Afghanistan
                      Asia 974.5803 43.828 2007
## 3:
         Albania
                    Europe 3533.0039 68.930 1977
## 4:
         Albania
                    Europe 5937.0295 76.423 2007
        Algeria Africa 4910.4168 58.014 1977
## 5:
```

Africa 6223.3675 72.301 2007

Algeria

### **Data layer**

To start with the visualization we initiate a ggplot object loaded with the data. It generates an empty plot:

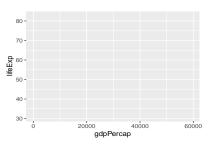
ggplot(gm\_dt)

## **Aesthetics layer**

#### Selecting variables to visualize and their rendering

We next add to the plot an "aesthetic mapping" layer with the function aes(), which defines which variables of the table will be visualized and how they map to so-called aesthetics: axis, colors, point shapes, etc.

For a scatter plot, we need at least to define the mapping to x and y. Now the axes are rendered:  $ggplot(\frac{data=gm_dt}{aes(x=gdpPercap, y=lifeExp)})$ 

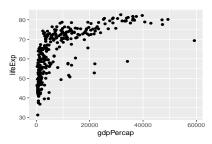


## Geometric object layer

#### Defining the type of the plot

We next add to the plot a "geometric object" layer which defines the type of the plot.

A scatter plot can be plotted using the geometric object function geom\_point():



## Advantage of a layered grammar

### Storing ggplot2 objects

One of the advantages of plotting with ggplot2 is that it returns an object which can be stored (e.g. in a variable called p). The stored object can be further edited and inspected using the names() function:

```
p <- ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp)) + geom_point()
p <- p + labs(x='per-capita GDP')
names(p)</pre>
```

```
## [1] "data" "layers" "scales" "mapping" "theme" ## [6] "coordinates" "facet" "plot_env" "labels"
```

## Advantage of a layered grammar

#### Saving ggplot2 objects

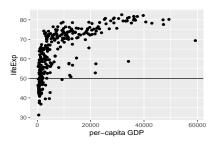
We can also save the ggplot2 object into a file with the help of the function saveRDS():

```
saveRDS(p, "../../extdata/my_first_plot.rds")
p <- readRDS("../../extdata/my_first_plot.rds")</pre>
```

## Advantage of a layered grammar

**Loading** ggplot2 **objects** Later, we can read the saved object with the help of the function readRDS(). We illustrate this by reading the previously saved plot into a variable p and adding a horizontal line at y=50:

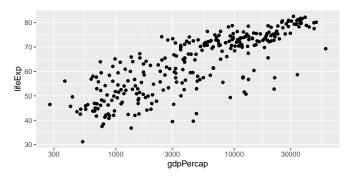
```
p <- readRDS("../../extdata/my_first_plot.rds")
p + geom_hline(yintercept=50)</pre>
```



### Scale layer

For a better visualization of the data points, we apply log scaling (more details later).

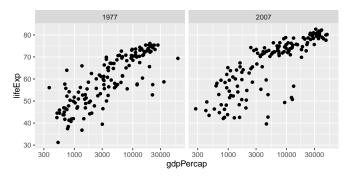
```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp)) +
  geom_point() + scale_x_log10()
```



### **Facets layer**

To compare the data from the year 1977 with the data from 2007, we create a multi-panel plot with facet\_grid(), which takes a formula as argument specifying by which variable(s) the plot should be split by.

```
ggplot(data = gm_dt, aes(x=gdpPercap, y=lifeExp)) +
  geom_point() + scale_x_log10() + facet_grid(~year) # "~year" means "by year"
```

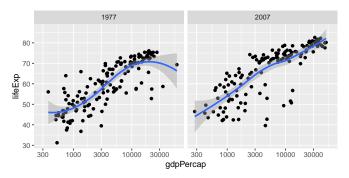


### Stats layer

Stats layer are statistical transformations that typically summarize data. Examples are counts, means, medians, regression lines, smooth trends.

Here is an example of smooth trends:

```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp))+
  geom_point() + scale_x_log10() + facet_grid(-year) +
  stat_smooth()
```

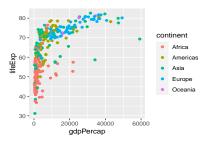


Stats layers can be helpful. However, we recommend to use regression lines an smooth trends if they are well understood as they can mislead the interpretation of a plot.

### More aesthetics: color

We can easily map variables to different colors, sizes or shapes depending on the value of the specified variable using the aes() function:

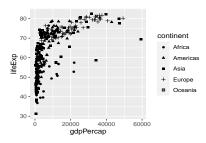
```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp, color=continent)) +
  geom_point()
```



## More aesthetics: shape

To change the shape of our points we can override the shape argument of the aes() function:

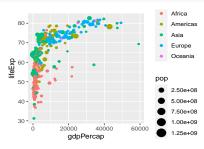
```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp, shape=continent)) +
  geom_point()
```



#### More aesthetics size

Additionally, we distinguish the population of each country by giving a size to the points in the scatter plot:

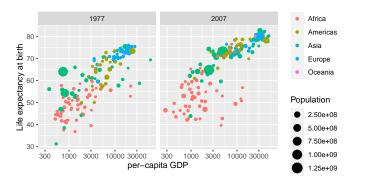
```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp, color=continent, size=pop)) +
geom_point()
```



#### Polishing: Axes labels

We can give better labels of the plot with labs():

```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp, color=continent, size=pop))+
geom_point() + scale_x_log10() + facet_grid(~year) +
labs(x="per-capita GDP", y="Life expectancy at birth", size = 'Population')
```



#### **Polishing: Themes**

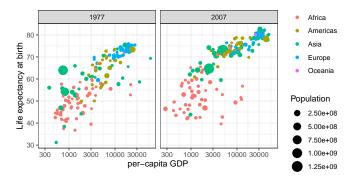
Some default settings can be stored in a so-called theme. Themes can be reused, giving your plots a uniform style across a document. Here we create a theme based on the black and white theme of ggplot2. See ?theme() for details.

```
mysize <- 15 #font size
mytheme <- theme(
    axis.title = element_text(size=mysize),
    axis.text = element_text(size=mysize),
    legend.title = element_text(size=mysize),
    legend.text = element_text(size=mysize)
    ) + theme_bw() # ggplot2's black-and-white theme</pre>
```

## Adding the theme

#### Et voilà:

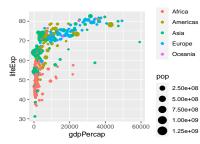
```
ggplot(data=gm_dt, aes(x=gdpPercap, y=lifeExp, color=continent, size=pop)) +
  geom_point(aes(color=continent, size=pop)) + scale_x_log10() + facet_grid(~year) +
  labs(x="per-capita GDP", y="Life expectancy at birth", size = 'Population') +
  mytheme
```



## Global vs. individual mapping

Global mapping mapping is inherited by default to all layers, while mapping at individual layers is only recognized at that layer

```
ggplot(data = gm_dt, aes(x = gdpPercap, y = lifeExp)) +
  geom_point(aes(color = continent, size = pop))
```



# Global versus individual mapping

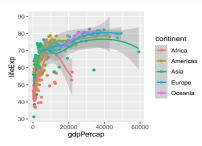
**Local mapping** cannot be recognized by other layers. For instance, adding another layer for smoothing with stat\_smooth() like this does not work:

```
# this doesn't work as stat_smooth didn't know aes(x , y)
ggplot(data = gm_dt) + geom_point(aes(x = gdpPercap, y = lifeExp)) +
    stat_smooth()
```

# Global versus individual mapping

#### Local mapping works like this but is too redundant:

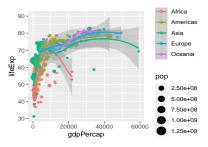
```
# this would work but too redundant
ggplot(data = gm_dt) + geom_point(aes(x = gdpPercap, y = lifeExp, color=continent))
stat_smooth(aes(x = gdpPercap, y = lifeExp, color=continent))
```



# Global versus individual mapping

#### **Local mapping** without redundancy:

```
# the common aes(x, y) shared by all the layers can be put in the ggplot()
ggplot(data = gm_dt, aes(x = gdpPercap, y = lifeExp, color = continent)) +
geom_point(aes(size = pop)) + stat_smooth()
```



#### Quiz

What's the result of the following command?

ggplot(data = mpg)

- Nothing happens
- 2 A blank figure will be produced
- 3 A blank figure with axes will be produced
- All data in mpg will be visualized

### **Solution**

ggplot(data = mpg): a blank figure will be produced

#### Quiz

What's the result of the following command?

- Nothing happens
- 2 A blank figure will be produced
- 3 A blank figure with axes will be produced
- 4 A scatter plot will be produced

#### **Solution**

ggplot(data = mpg, aes(x = hwy, y = cty)): A blank figure with axes will be produced

#### Quiz

What's the result of the following command?

```
ggplot(data = mpg, aes(x = hwy, y = cty)) + geom_point()
```

- Nothing happens
- 2 A blank figure will be produced
- 3 A blank figure with axes will be produced
- A scatter plot will be produced

#### Solution

```
ggplot(data = mpg, aes(x = hwy, y = cty)) + geom_point(): A scatter plot will be produced
```



Types of plots for discrete and continuous variables

#### Types of plots for low dimensional datasets

- In the previous examples, we had a look at scatter plots which are suitable for plotting the relationship between two continuous variables.
- However, there are many more types of plots (e.g. histograms, boxplots) which can be used for plotting in different scenarios.
- Mainly, we distinguish between plotting one or two variables and whether the variables are continuous or discrete.

# Simple plot exercise

#### Plots for one continuous variable

For plotting **one continuous variable** we mainly use histograms, density plots, boxplots, violinplots and beanplots.

Let us prepare some data for plotting continuous variables using the Human Development Index (HDI) dataset:

```
head(ind, n=3)
```

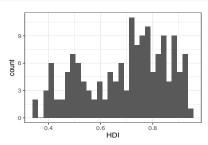
```
##
     V1
            country wbcode CPI
                               HDI
                                              region
        Afghanistan
                      AFG 12 0.465
                                        Asia Pacific
## 1:
## 2:
            Albania
                      ALB 33 0.733 East EU Cemt Asia
      2
## 3: 3
                      DZA 36 0.736
                                                MENA
            Algeria
```

with columns V1: row index, country, wbcode: World Bank Code, CPI: Corruption Perception Index, HDI: Human Development Index, and world region.

## Histograms

A histogram represents the frequencies of values of a continuous variable bucketed into ranges. For this, we can use the function geom\_histogram():

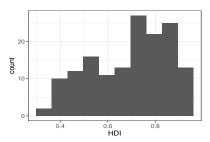
ggplot(ind, aes(HDI)) + geom\_histogram() + mytheme



## Histograms: setting the number of bins

By default, the number of bins in ggplot2 is 30. We can change this by defining the number of desired bins in the bins argument of the geom\_histogram() function:

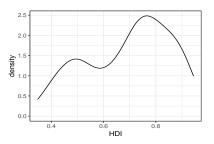
ggplot(ind, aes(HDI)) + geom\_histogram(bins=10) + mytheme



### **Density plots**

Sometimes densities are shown instead of histograms. In ggplot2 we use the function geom\_density():

ggplot(ind, aes(HDI)) + geom\_density() + mytheme



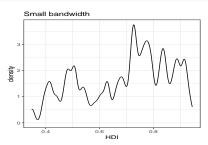
These smoothed distribution plot are typically obtained by kernel density estimation:  $\label{eq:hydro} $$ https://en.wikipedia.org/wiki/Kernel\_density\_estimation $$$ 

## Density plots: setting the bandwidth

The bw argument of the geom\_density() function allows to tweak the bandwidth of a density plot manually.

#### Smaller bandwidth:

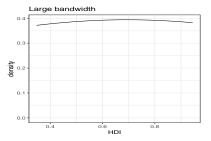
```
ggplot(ind, aes(HDI)) + geom_density(bw=0.01) + ggtitle('Small bandwidth') +
  mytheme
```



# Density plots: setting the bandwidth

#### Larger bandwidth:

```
ggplot(ind, aes(HDI)) + geom_density(bw=1) + ggtitle('Large bandwidth') +
   mytheme
```



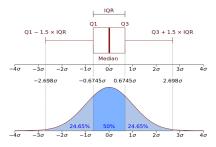
Be careful with density plots as the bandwidth can have strong visual effects. Histograms are not that bad and show the data 'raw'.

General principle: Show the data as raw as possible.

# Histogram exercise

## **Boxplots**

Box plots can give a good graphical insight into the distribution of the data.

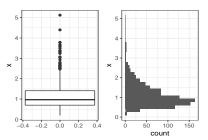


- Median: the center of the data, middle value of a sorted list, 50% quantile of the data
- First quantile (Q1) and the third quantile (Q3): 25% and 75% quantiles of the data
- Interquantile range (IQR): the distance between Q1 and Q3

#### **Boxplots: example**

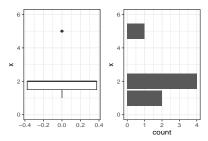
Here is an example of a boxplot with log-normal distribution, which is an asymmetric distribution. The corresponding histogram is shown for comparison.

```
dt <- data.table(x=rlnorm(1000,meanlog=0,sdlog=0.5)) # 1,000 random draws of log-nor
ggplot(dt, aes(x)) + geom_boxplot()</pre>
```



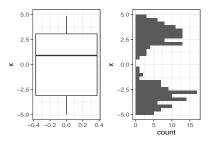
# Boxplots are not appropriate for discrete data

For discrete data (e.g. number of gears of a car, rolls of a dice), a boxplot is not appropriate. Choose a barplot or histogram.



## Boxplots are not appropriate for multi-modal distribution

Boxplot are misleading for multi-modal distributions, i.e. distribution with multiple peaks of densities, for instance made of two separate clusters of data. Choose a histogram.



# **Boxplot** exercise

#### Plots for two variables: one continuous and one discrete variable

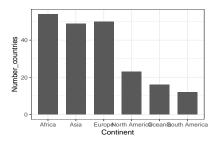
For plotting one continuous variable and one discrete variable we mainly use

- barplots,
- boxplots by category and
- violinplots by category.

## **Barplots**

Barplots are used to highlight individual quantitative values per category. For creating a barplot with ggplot2 we can use the function  $geom\_bar()$ :

```
ggplot(countries_dt, aes(Continent, Number_countries)) +
geom_bar(stat = 'identity', width = .7) + mytheme
```



#### **Barplots with errorbars**

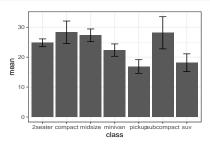
Visualizing uncertainty is important, otherwise, barplots with bars as a result of an aggregation can be misleading. One way to visualize uncertainty is with error bars.

As error bars, we can consider the standard deviation (SD) which can be computed in R with the function sd().

#### **Barplots with errorbars**

In the following example, we plot the average highway miles per gallon hwy per vehicle class class including error bars computed as the average plus/minus standard devation of hwy:

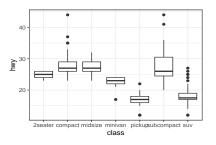
```
as.data.table(mpg) %>% .[, .(mean = mean(hwy), sd = sd(hwy)), by = class] %>%
   ggplot(aes(class, mean, ymax=mean+sd, ymin=mean-sd)) +
   geom_bar(stat='identity') + geom_errorbar(width = 0.3) + mytheme
```



### **Boxplots by category**

Boxplots are well suited to compare distributions, i.e. plotting distributions of a continuous variable with respect to some categories:

ggplot(mpg, aes(class, hwy)) + geom\_boxplot() + mytheme



One favor boxplots over barplots for showing median as they show more data (IQR, outliers)  $\it General\ principle\ Increase\ the\ data/ink\ ratio$ 

### **Boxplots with dots**

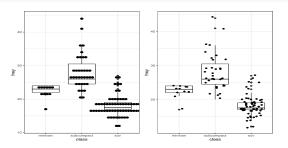
We can add dots (or points) to a box plot using the functions geom\_dotplot() or geom\_jitter():

p <- ggplot(mpg\_, aes(class, hwy)) + geom\_boxplot() + mytheme

p1 <- p + geom\_dotplot(binaxis='y', stackdir='center', dotsize=0.5)

p2 <- p + geom\_jitter(width=0.3)

cowplot::plot\_grid(p1, p2)

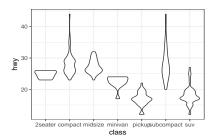


General principle Show the data as raw as possible General principle Increase the data/ink ratio

### **Violin plots**

A violin plot is an alternative to the boxplot. An advantage of the violin plot over the boxplot is that it also shows the distribution of the data. This can be particularly interesting when dealing with multimodal data. For this, we use the <code>geom\_violin()</code> function:

ggplot(mpg, aes(class, hwy)) + geom\_violin() + mytheme



#### Quiz

For which type of data will boxplots produce meaningful visualizations? (2 possible answers)

- For discrete data.
- For bi-modal distributions.
- For non-Gaussian, symmetric data.
- For exponentially distributed data.

#### Solution

For which type of data will boxplots produce meaningful visualizations?

- 3. For non-Gaussian, symmetric data.
- 4. For exponentially distributed data.

Boxplots are bad for bimodal data since they only show one mode (the median), but are ok for both symmetric and non-symmetric data, since the quartiles are not symmetric.

#### Plots for two continuous variables

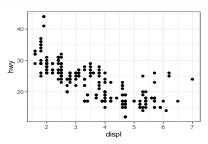
For plotting two continuous variables we mainly use

- scatterplots and
- line plots

### **Scatter plots**

Scatter plots are a useful plot type for easily visualizing the relationship between two continuous variables. To make a scatter plot we use the <code>geom\_point()</code> function:

ggplot(mpg, aes(displ, hwy)) + geom\_point() + mytheme

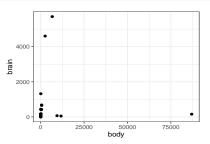


### Scatter plots with logarithmic scaling

Consider this scatter plot showing the weights of the brain and body of different animals:

```
library(MASS) # to access Animals data sets
animals_dt <- as.data.table(Animals)

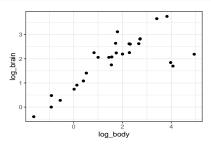
ggplot(animals_dt, aes(x = body, y = brain)) + geom_point() + mytheme</pre>
```



We can clearly see that there are a few points which are notably larger than most of the points. This makes it harder to interpret the relationships between most of these points. In such cases, we can consider **logarithmic** transformations and/or scaling.

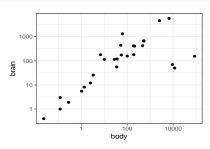
A first idea would be to manually transform the values into a logarithmic space and plot the transformed values instead of the original values:

```
animals_dt[, c('log_body', 'log_brain') := list(log10(body), log10(brain)) ]
ggplot(animals_dt, aes(x = log_body, y = log_brain)) + geom_point() + mytheme
```



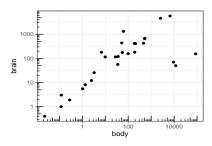
A better option is to logarithmic scales of the plot. The functions  $scale_x_log10()$  and  $scale_y_log10()$  allow appropriate scaling and labeling of the axes:

```
ggplot(animals_dt, aes(x = body, y = brain)) + geom_point() +
    scale_x_log10() + scale_y_log10() + mytheme
```



Log-scale ticks on the axis using annotation\_logticks() make very obvious we look at a logarithmic scale:

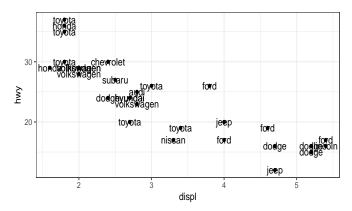
```
ggplot(animals_dt, aes(x = body, y = brain)) + geom_point() +
    scale_x_log10() + scale_y_log10() +
annotation_logticks() + mytheme
```



### Scatter plots with text labeling

Labeling the individual points in a scatter plot may be useful in some applications. For this, ggplot2 offers the function geom\_text(). However, these labels tend to overlap:

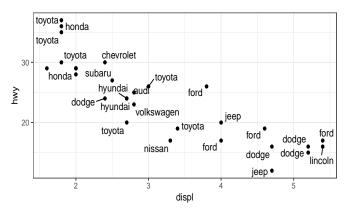
```
ggplot(mpg_subset, aes(displ, hwy, label=manufacturer)) + geom_point() +
  geom_text() + mytheme
```



#### Scatter plots with text labeling

For a better understanding of the labels we exchange the function geom\_text() by geom\_text\_repel() from the library ggrepel:

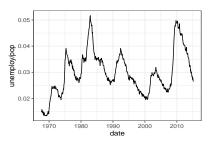
```
library(ggrepel)
ggplot(mpg_subset, aes(displ, hwy, label=manufacturer)) +
  geom_point() + geom_text_repel() + mytheme
```



### Line plots

Line plots can be also used to plot two continuous variables. For this we use the function geom\_line():

ggplot(economics, aes(date, unemploy/pop)) + geom\_line() + mytheme



#### Quiz

When to use a line plot?

A. To show a connection between a series of individual data points B. To show a correlation between two quantitative variables C. To highlight individual quantitative values per category D. To compare distributions of quantitative values across categories

#### Solution

When to use a line plot?

#### A. To show a connection between a series of individual data points

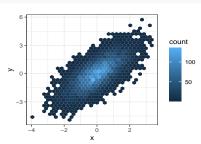
A line plot can be considered for connecting a series of individual data points or to display the trend of a series of data points. This can be particularly useful to show the shape of data as it flows and changes from point to point.

#### 2D-Density plots

In scatter plots, we can not clearly see how many points are at a certain position. This is especially problematic with large datasets. A 2D density plot counts the number of observations within a particular area of the 2D space.

The function geom\_hex() is particularly useful for creating 2D density plots in R:

```
x <- rnorm(10000); y=x+rnorm(10000)
data.table(x, y) %>% ggplot(aes(x, y)) +
  geom_hex() + mytheme
```



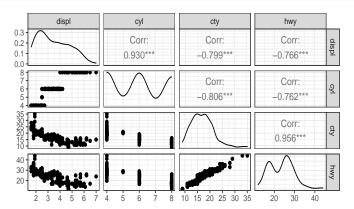
Further plots for low dimensional datasets

Further plots for low dimensional datasets

#### Scatterplot matrix

A scatter plot matrix is useful for exploring the distributions and correlations of a few variables in a matrix-like representation. We can use the function ggpairs() from the library GGally for constructing plot matrices:

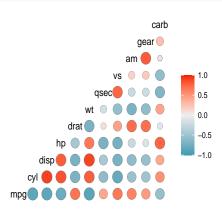
```
library(GGally)
ggpairs(mpg, columns = c("displ","cyl","cty","hwy")) + mytheme
```



Pearson correlations are shown in the upper triangle and their statistical significance marked with

### **Correlation plot**

A correlation plot is a graphical representation of a correlation matrix. It is useful to highlight the most correlated variables in a dataset. As an example, we visualize the correlation between the variables of the dataset mtcars with the help of the function ggcorr() from the library GGally: ggcorr(mtcars, geom = 'circle')



# Scatter plot exercise

Summary

# **Summary**

#### Conclusion - You should remember...

- Visualization helps to
  - explore data
  - communicate observations
  - find "bugs" in the data
- The layers of grammar of graphics
- Which plots to use for univariate and bivariate situations
- Interpret elements of a boxplot
- Plotting guiding principles
  - Show the data as raw as possible
  - Increase data/ink ratio

#### References

- H. Wickham, A Layered Grammar of Graphics, Journal of Computational and Graphical Statistics, 2010 https://vita.had.co.nz/papers/layered-grammar.pdf
- See also Udacity's Data Visualization and D3.js

### Tidy data

Now you will learn...

- The notion of tidy data
- Operations for tidying up messy data tables
- How to concatenate tables with the same format
- How to merge tables by common variables
- There is no single tidy representation of a dataset

This will set us ready for data visualization and analytics.

Tidy Data

**Tidy Data** 

#### **Motivation**

- Without good practices, much of the time of a data analyst can be wasted in data wrangling rather than visualization or analysis.
- The concept of tidy data (Wickham, 2014) offers a standard representation of data, that is easy to manipulate, model and visualize.

Advanced data.table cheatsheet

https://raw.githubusercontent.com/rstudio/cheatsheets/master/datatable.pdf

# **Definition of tidy data**



We say that a data table is in tidy format if:

- Each variable has its own column.
- 2 Each observation has its own row.
- Each value has its own cell.

### **Example dataset**

Data from 2016 US presidential vote<sup>1</sup> is an example of a tidy dataset:

```
##
           candidate state
                           votes total votes
## 1: Hillary Clinton
                       CA 5931283
                                     9631972
## 2:
        Donald Trump CA 3184721
                                     9631972
     Gary Johnson CA 308392
                                     9631972
## 3:
          Jill Stein
                      CA 166311
                                     9631972
## 4:
## 5:
      Gloria La Riva CA
                           41265
                                     9631972
## 6:
                       FL 4605515
                                     9386750
        Donald Trump
```

Each row represents a state and a candidate with each of the four values related to these states stored in the four variables: candidate, state, votes, and total\_votes.

 $<sup>^{1}</sup> https://www.kaggle.com/stevepalley/2016 uspresidential vote by county? select = pres16 results.csv$ 

# Advantages of tidy data

Organizing data in a tidy fashion reduces the burden to frequently reorganize the data.

In particular, the advantages are:

- Easier manipulation using data.table commands such as
  - sub-setting by rows and columns
  - by operations
- Vectorized operations become easier to use
- Many other tools work better with tidy data, including:
  - plotting functions
  - · hypothesis testing functions
  - · modeling functions such as linear regression

### Common signs of untidy datasets

Often, untidy datasets can be identified by one or more of the following issues:

- Column headers are values, not variable names
- Multiple variables are stored in one column
- Variables are stored in both rows and columns
- A single observational unit is stored in multiple tables
- (Multiple types of observational units are stored in the same table)
- H. Wickham, Journ. Stat. Software, 2014

#### Column headers are values, not variable names

A common sign of untidy data is that columns are not descriptive enough to tell what they contain.

In this example (Religion dataset, Wickham 2014), we see that the columns refer to some amount of money, but what exactly: income, donations, etc.? The column headers are themselves values of a variable not explicitly mentioned.

#### Untidy:

religion	<\$10k	\$10-20k	\$20-30k	\$30-40k	\$40-50k	\$50-75k
Agnostic	27	34	60	81	76	137
Atheist	12	27	37	52	35	70
Buddhist	27	21	30	34	33	58
Catholic	418	617	732	670	638	1116
Don't know/refused	15	14	15	11	10	35
Evangelical Prot	575	869	1064	982	881	1486
Hindu	1	9	7	9	11	34
Historically Black Prot	228	244	236	238	197	223
Jehovah's Witness	20	27	$^{24}$	24	21	30
Jewish	19	19	25	25	30	95

Also, avoid when possible special characters in column names!

### Column headers are values, not variable names

In this tidy version it is easy to understand what each column and value contain.

Tidy:

religion	income	$_{\mathrm{freq}}$
Agnostic	<\$10k	27
Agnostic	\$10-20k	34
Agnostic	\$20-30k	60
Agnostic	\$30-40k	81
Agnostic	\$40-50k	76
Agnostic	\$50-75k	137
Agnostic	\$75-100k	122
Agnostic	\$100-150k	109
Agnostic	> 150 k	84
Agnostic	Don't know/refused	96

### Multiple variables are stored in one column

This table is an example of multiple variables are stored in one column. Untidy:

The column 'proportion' is stored as a character containing two values. Further data manipulation (splitting the column, converting to numeric) is needed to compute or do some plotting with it.

#### Variables are stored in both rows and columns

In the following table (Weather dataset, Wickham, 2014):

- the variable date is stored across multiple columns (year, month, d1-d31)
- the element column is not a variable; it stores the names of variables

#### Untidy:

id	year	month	element	d1	d2	d3	d4	d5	d6	d7	d8
MX17004	2010	1	tmax	_	_	_		_		_	_
MX17004	2010	1	$_{ m tmin}$	_	_	_		_			_
MX17004	2010	2	tmax	_	27.3	24.1	_	_	_	_	_
MX17004	2010	2	$_{ m tmin}$		14.4	14.4			_	_	_
MX17004	2010	3	$_{\rm tmax}$	_	_	_	_	32.1	_	_	_
MX17004	2010	3	$_{ m tmin}$	_	_	_	_	14.2	_	_	_
MX17004	2010	4	$_{\rm tmax}$	_	_	_		_	_	_	_
MX17004	2010	4	$_{ m tmin}$		_			_	_	_	_
MX17004	2010	5	$_{\rm tmax}$	_	_	_	_	_	_	_	_
MX17004	2010	5	$_{ m tmin}$	—	_	_	—	_	_	_	_

## A single observational unit is stored in multiple tables

A subset of the World Health Organization Global Tuberculosis Report (tidyr package):

#### Untidy

```
## $Afghanistan
##
     year cases population
## 1: 1999
             745
                   19987071
## 2: 2000 2666
                   20595360
##
## $Brazil
##
     year cases population
  1: 1999 37737 172006362
## 2: 2000 80488 174504898
##
## $China
##
     year
            cases population
  1: 1999 212258 1272915272
## 2: 2000 213766 1280428583
```

It is hard to work across multiple tables. One would rather work with a single concatenated table with an extra column "country".

# Quiz: Is the following dataset tidy?

```
Dataset: mtcars (Motor Trend Car Road Tests)

• mpg: Miles/(US) gallon

• cyl: Number of cylinders
```

```
hp: Gross horsepower
wt: Weight (1000 lbs)
```

```
## 1: Mazda RX4 21.0 6 110 2.620
## 2: Mazda RX4 Wag 21.0 6 110 2.875
## 3: Datsun 710 22.8 4 93 2.320
## 4: Hornet 4 Drive 21.4 6 110 3.215
## 5: Hornet Sportabout 18.7 8 175 3.440
## 6: Valiant 18.1 6 105 3.460
```

- Yes
- O No

## Quiz: Is the following dataset tidy?

Dataset: mtcars (Motor Trend Car Road Tests)

mpg: Miles/(US) gallon

## 4:

## 6:

```
cyl: Number of cylinders
 hp: Gross horsepower

    wt: Weight (1000 lbs)

##
                  model mpg cyl hp
              Mazda RX4 21.0
                               6 110 2,620
## 1:
## 2:
          Mazda RX4 Wag 21.0 6 110 2.875
## 3:
             Datsun 710 22.8 4 93 2.320
```

## 5: Hornet Sportabout 18.7 8 175 3.440

Hornet 4 Drive 21.4 6 110 3.215

Valiant 18.1 6 105 3.460

Answer: Yes, each row (observation) is a car model and all columns contain different variables,

therefore, it is tidy.

# Quiz: Is the following dataset tidy?

```
## country 1999 2000
## 1: Afghanistan 745 2666
## 2: Brazil 37737 80488
## 3: China 212258 213766
```

O No

# Quiz: Is the following dataset tidy?

```
## country 1999 2000
## 1: Afghanistan 745 2666
## 2: Brazil 37737 80488
## 3: China 212258 213766
```

Answer: No, the column names are values not variable names.

# Tidy data exercise

Tidying up single data tables

Tidying up single data tables

## Tidying up single data tables

- melt tables (wide to long)
- cast tables (long to wide)
- separate columns
- unite columns

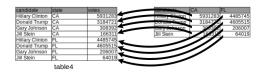
### From wide to long: column headers are values, not variable names

One of the most used operations to obtain tidy data is to transform a wide table into a long table. This operation is called melting, by analogy with melting a piece of metal.

As an example, consider the table below which reports vote counts for two US states, California and Florida. In this untidy table, the column names CA and FA are values of a variable state.

```
## candidate CA FL
## 1: Hillary Clinton 5931283 4485745
## 2: Donald Trump 3184721 4605515
## 3: Gary Johnson 308392 206007
## 4: Jill Stein 166311 64019
```

# From wide to long: column headers are values, not variable names



Melting the previous table can be achieved by using the data.table function melt():

```
melt(table4, id.vars = "candidate", measure.vars = c("CA", "FL"),
    variable.name = "state", value.name = "votes") %>% head(n=6)
```

```
candidate state
##
                            votes
## 1: Hillary Clinton
                       CA 5931283
## 2:
        Donald Trump
                     CA 3184721
## 3:
        Gary Johnson CA
                           308392
          Jill Stein
                       CA
                           166311
## 4:
## 5: Hillary Clinton FL 4485745
## 6:
        Donald Trump
                       FL 4605515
```

# Understanding the melting function

```
melt(table4, id.vars = "candidate", measure.vars = c("CA", "FL"),
    variable.name = "state", value.name = "votes") %>% head(n=6)
```

When melting, all values in the columns specified by the measure.vars argument are **gathered into one column** with name specified in the variable.name argument.

Additionally, a new column with name in the value.name argument is created containing all values which were previously stored in the measure.vars column names.

After melting, we have a table in a tidy format where a row represents the number of votes for a candidate in a state. The new table also makes clear that the quantities are numbers of votes thanks to the column name.

### From long to wide: multiple variables are stored in one column

The other way around also happens frequently.

In the table below, multiple values, namely the number of votes for a candidate and the total number of votes, are reported in one column:

#### table2

```
##
           candidate state
                                         value
                                  type
## 1: Hillary Clinton
                        CA
                                 votes 5931283
## 2: Hillary Clinton
                        CA total votes 9631972
## 3:
        Donald Trump
                        CA
                                 votes 3184721
        Donald Trump CA total votes 9631972
## 4:
## 5: Garv Johnson
                        CA
                                 votes 308392
## 6:
        Gary Johnson
                        CA total votes 9631972
```

It is not easy to compute the percentage of votes given to a candidate in this format. To tidy up this table we have to **separate** those values **into two columns**.

# From long to wide: multiple variables are stored in one column

candidate	state	type	value		state			votes
Hillary Clinton	CA	votes	5931283	Hillary Clinton		→ 5931283	7	9631972
Hillary Clinton	CA	total votes	9631972	Donald Trump	CA	3184721	7	9631972
Donald Trump	CA	votes	3184721	 Gany Johnson	ĈA .	308392	7	9631972
Donald Trump	CA	total votes	9631972	 				
Gary Johnson	CA	votes	308392					
Gary Johnson	CA	total_votes	9631972					

Casting transforms a long table into a wide table and is achieved with the dcast() function whose most frequent usage is:

```
dcast(data, formula, value.var = guess(data))
```

- formula specifies which column contains the categories by which the new columns should be created
- value, var refers to which column the values have to be extracted from

```
dcast(table2, ... ~ type, value.var = "value")
##
            candidate state total_votes
                                          votes
```

Donald Trump CA 9631972 3184721 ## 2: Gary Johnson CA 9631972 308392

Julien Gagneur

# Melt/cast exercise

### **Separating columns**

This untidy data stores multiple variables into one column:

#### table3

We split up the proportion column into two columns, one containing the votes and the other one containing the total votes with the function separate() from the tidyr package. By default, columns are separated by any non-alphanumerical character (such as ",", ";", "/",...):

```
separate(table3, col = proportion,
    into = c("votes", "total_votes"))
```

# **Uniting columns**

Here the first and last names are separated columns without a real need for it (we will not compute any stats over all Hillary's):

#### table5

```
##
       name surname state
                          votes total votes
                                   9631972
## 1: Hillary Clinton
                      CA 5931283
## 2:
     Donald
             Trump CA 3184721
                                   9631972
       Gary Johnson CA 308392 9631972
## 3:
       Jill
              Stein
                      CA 166311 9631972
## 4:
## 5:
     Gloria La Riva
                      CA
                          41265
                                   9631972
```

We unite multiple variables into a single variable with the function unite() from the tidyr:

```
unite(table5, col = candidate, name, surname, sep = " ")
```

```
##
          candidate state
                          votes total votes
## 1: Hillary Clinton
                      CA 5931283
                                    9631972
## 2:
        Donald Trump CA 3184721
                                    9631972
## 3: Gary Johnson CA 308392
                                   9631972
## 4:
         Jill Stein
                      CA 166311
                                   9631972
## 5:
      Gloria La Riva
                      CA
                           41265
                                    9631972
```

The sep argument defines the separating character(s) used to unite the different column values into one

religion	<\$10k	\$10-20k	\$20-30k	\$30-40k	\$40-50k	\$50-75k
Agnostic	27	34	60	81	76	137
Atheist	12	27	37	52	35	70
Buddhist	27	21	30	34	33	58
Catholic	418	617	732	670	638	1116
Don't know/refused	15	14	15	11	10	35

- cast
- melt
- 3 cast and melt
- unite

#### Answer: 2. melt only. Tidy form:

religion	income	${\rm freq}$
Agnostic	<\$10k	27
Agnostic	\$10-20k	34
Agnostic	\$20-30k	60
Agnostic	\$30-40k	81
Agnostic	\$40-50k	76
Agnostic	\$50-75k	137
Agnostic	\$75-100k	122
Agnostic	\$100-150k	109
Agnostic	> 150 k	84
Agnostic	Don't know/refused	96

id	year	month	element	d1	d2	d3	d4	d5	d6	d7	d8
MX17004	2010	1	tmax	_	_	_	_	_	_	_	_
MX17004	2010	1	$\operatorname{tmin}$	_	_	_	_	_	_	_	_
MX17004	2010	2	tmax	_	27.3	24.1	_	_	_	_	_
MX17004	2010	2	$_{ m tmin}$	_	14.4	14.4	_	_	_	_	_
MX17004	2010	3	tmax	_	_	_	_	32.1	_	_	_
MX17004	2010	3	$\operatorname{tmin}$	_	_	_	_	14.2	_	_	_

- separate
- unite
- melt and cast
- melt, unite and cast

#### **Answer:** 4. melt, unite and cast. Tidy form:

id	date	$_{ m tmax}$	tmin
MX17004	2010-01-30	27.8	14.5
MX17004	2010-02-02	27.3	14.4
MX17004	2010-02-03	24.1	14.4
MX17004	2010-02-11	29.7	13.4
MX17004	2010-02-23	29.9	10.7
MX17004	2010-03-05	32.1	14.2
MX17004	2010-03-10	34.5	16.8
MX17004	2010-03-16	31.1	17.6
MX17004	2010-04-27	36.3	16.7
MX17004	2010 - 05 - 27	33.2	18.2

- Goal: Concatenate (i.e. append) tables of same format
- Example: Daily COVID-19 data
- Of Get all file names of the directory into a list called files:

```
files <- list.files('path_to_your_directory')
head(files)
## [1] "../../extdata/cov concatenate//covid cases 01 03 2020.csv"</pre>
```

```
## [2] ".././extdata/cov_concatenate//covid_cases_02_03_2020.csv"
## [3] ".././extdata/cov_concatenate//covid_cases_03_03_2020.csv"
## [4] ".././extdata/cov_concatenate//covid_cases_04_03_2020.csv"
## [5] ".././extdata/cov_concatenate//covid_cases_05_03_2020.csv"
## [6] ".././extdata/cov_concatenate//covid_cases_06_03_2020.csv"
```

```
Oliver 1 load all file contents with fread using lapply
# name the list elements by the filenames
names(files) <- basename(files)
# read all files at once into a list of data.tables
tables <- lapply(files, fread)
 View first table:
head(tables[[1]])
##
      cases deaths countriesAndTerritories geoId countryterritoryCode popData2019
         54
                                                                              83019213
## 1:
                  0
                                     Germany
                                                 DF.
                                                                      DEU
## 2:
                                                                              60359546
        240
                                       Italy
                                                 IT
                                                                      ITA
      continentExp Cumulative number for 14 days of COVID-19 cases per 100000
##
## 1:
            Europe
                                                                        0.1156359
            Europe
                                                                        1.8638311
## 2:
```

To combine the different tables into one, we can use the data.table function rbindlist() which gives us the option to introduce a new column idcol containing the list names (filenames):

```
# bind all tables into one using rbindlist,
# keeping the list names (the filenames) as an id column.
dt <- rbindlist(tables, idcol = 'filename')</pre>
head(dt, n=3)
##
                         filename cases deaths countriesAndTerritories geoId
## 1: covid_cases_01_03_2020.csv
                                     54
                                              0
                                                                 Germany
                                                                            DE
## 2: covid cases 01 03 2020.csv
                                    240
                                              8
                                                                            IT
                                                                   Italy
## 3: covid cases 02 03 2020.csv
                                     18
                                              0
                                                                 Germany
                                                                            DE
      countryterritoryCode popData2019 continentExp
##
## 1:
                        DEU
                               83019213
                                               Europe
                        TTA
## 2:
                               60359546
                                               Europe
## 3:
                        DEU
                               83019213
                                               Europe
##
      Cumulative number for 14 days of COVID-19 cases per 100000
## 1:
                                                         0.1156359
                                                         1.8638311
## 2:
```

## 3:

0.1373176

Merging tables

### Merging tables

Merging two data tables into one by common column(s) is frequently needed. This can be achieved using the merge function whose core signature is:

### Types of merges

The four types of merges (also commonly called joins) are:

- Inner (default): consider only rows with matching values in the by columns.
- Outer or full (all): return all rows and columns from x and y. If there are no matching values, return NAs
- Left (all.x): consider all rows from x, even if they have no matching row in y.
- Right (all.y): consider all rows from y, even if they have no matching row in x.



2

<sup>&</sup>lt;sup>2</sup>https://documentation.mindsphere.io/resources/html/predictive-learning/en-US/Types\_of\_Joins.htm

# Merging examples

We provide examples of each type using the following made up tables:

```
## 1: G008 Germany
## 2: F027 France
## 3: U093 USA
```

#### Inner merge

An inner merge returns only rows with matching values in the by columns and discards all other rows:

```
# Inner merge, default one, all = FALSE
m <- merge(dt1, dt2, by = "p_id", all = FALSE)
m</pre>
```

```
## p_id value country
## 1: F027 0.4841822 France
## 2: G008 0.5260630 Germany
```

#### Inner merge

Note that the column order got changed after the merging in the previous example.

To prevent this and, therefore, to keep the original ordering we can use the argument sort and set it to FALSE:

```
m <- merge(dt1, dt2, by = "p_id", all = FALSE, sort = FALSE)
m</pre>
```

```
## p_id value country
## 1: G008 0.5260630 Germany
## 2: F027 0.4841822 France
```

Note that the column order got changed after the merging.

# Outer (full) merge

An outer merge returns all rows and columns from x and y. If there are no matching values, it yields missing values (NA):

```
merge(dt1, dt2, by = "p_id", all = TRUE)

## p_id value country

## 1: F027 0.4841822 France

## 2: G008 0.5260630 Germany

## 3: L051 1.6767429 <NA>

## 4: U093 NA USA
```

# Outer (full) merge, all = TRUE

### Left merge

Returns all rows from x, even if they have no matching row in y. Rows from x with no matching in y lead to missing values (NA).

```
# Left merge, all.x = TRUE
merge(dt1, dt2, by = "p_id", all.x = TRUE)

## p_id value country
## 1: F027 0.4841822 France
## 2: G008 0.5260630 Germany
```

<NA>

## 3: L051 1.6767429

### Right merge

# Right, all.y = TRUE

Returns all rows from y, even if they have no matching row in x. Rows from y with no matching in x lead to missing values (NA).

```
merge(dt1, dt2, by = "p_id", all.y = TRUE)

## p_id value country

## 1: F027 0.4841822 France

## 2: G008 0.5260630 Germany

## 3: U093 NA USA
```

### Merging by more than one column

Merging can also be done using more than two columns. Here are two made up tables to illustrate this use case:

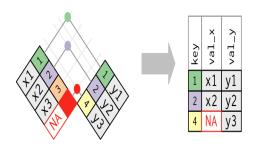
# Merging by more than one column

We merge now dt1 and dt2 by first name and last name:

```
merge(dt1, dt2, by=c("firstname", "lastname"))
## firstname lastname x y
## 1: Alice    Coop 1 A
## 2:    Bob    Smith 3 C
Note that merging by first name only gives a different result (as expected):
merge(dt1, dt2, by="firstname")
```

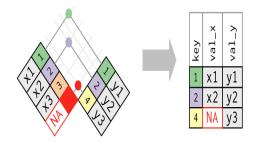
```
##
     firstname lastname.x x lastname.y y
## 1:
         Alice
                     Coop 1
                                  Coop A
         Alice
                    Smith 2
## 2:
                                  Coop A
## 3:
           Bob
                    Smith 3
                                Marley B
## 4:
           Bob
                    Smith 3
                                 Smith C
```

# Quiz: How do you perform the data table merge pictured here?



- 1 Inner, all = FALSE
- **②** Full, all = TRUE
- **3** Left, all.x = TRUE
- Right, all.y = TRUE

## Quiz: How do you perform the data table merge pictured here?



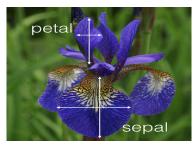
Answer: 4. Right, all.y = TRUE

There is no single tidy representation of a dataset

There is no single tidy representation of a dataset

#### Fisher's Iris dataset

- 150 iris flowers from 3 different iris species with measurements of 4 different attributes.
- R. Fisher (1936). See https://en.wikipedia.org/wiki/Iris\_flower\_data\_set



#### The tidy representation depends on what the observation is

We can have different tidy representations depending on what we consider to be an observation, and what the goal of our analysis is.

Here each row represents one flower. Tidy:

```
# Iris dataset, usual representation
iris_dt[1:3,]
```

```
##
     Flower Sepal.Length Sepal.Width Petal.Length Petal.Width Species
                  5.1
                            3.5
                                        1.4
## 1:
       F_1
                                                  0.2 setosa
                                     1.4
## 2: F 2
                  4.9
                         3.0
                                                  0.2 setosa
## 3: F 3
                  4.7
                          3.2
                                        1.3
                                                  0.2 setosa
```

Here each row represents one measurement. Also tidy:

```
# Another tidy representation
iris_melt[1:3,]
```

```
## Flower Species Attribute value
## 1: F_1 setosa Sepal.Length 5.1
## 2: F_2 setosa Sepal.Length 4.9
## 3: F 3 setosa Sepal.Length 4.7
```

### On multiple types of observational units in the same table

Remember the typical hallmarks of messy datasets (Wickham, 2014):

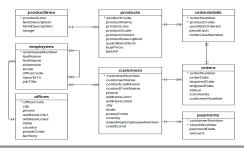
- Column headers are values, not variable names
- Multiple variables are stored in one column
- Variables are stored in both rows and columns
- A single observational unit is stored in multiple tables
- (Multiple types of observational units are stored in the same table)

Wickham (2014) mentions the latter may be not so bad...

## Data tables are typically normalized in databases

Normalized databases ensure that no multiple types of observational units are stored in the same table.

#### Database example (back-end)



#### Data analyst tables do not have to be normalized

As data analysts, we are not interested in maintaining a database (back-end), rather in having the desired data in a ready-to-use format which depends on our needs (front-end).

#### R script example (front-end)

A table combining product and customer data, even if product or customer data are replicated, can be useful:

```
productCode quantOrdered priceEach customerNumber customerName state
##
## 1:
             p018
                                       450
                                                      c001
                                                                             CA
                                                                   Smith
             080g
## 2:
                                       600
                                                      c001
                                                                   Smith
                                                                             CA
## 3:
             p018
                                       450
                                                      c002
                                                                   Lewis
                                                                             AZ
```

Then we can perform easily operations like:

```
prod_dt[, totalPrice := quantOrdered * priceEach]
prod_dt[, N_prod := .N, by = state]
```

# Front-end vs. back-end: An analogy





Summary

# **Summary**

#### **Summary**

By now, you should be able to:

- define what a tidy dataset is
- recognize untidy data
- perform the operations of melting and casting
- perform the operations of uniting and splitting
- append tables with the same format by rows
- understand and perform the 4 merging operations

#### Resources

H. Wickham, Journal of Statistical Software, 2014, Volume 59, Issue 10  $\label{eq:https://www.jstatsoft.org/v59/i10/paper} https://www.jstatsoft.org/v59/i10/paper$ 

https://r4ds.had.co.nz/tidy-data.html

https://cran.r-project.org/web/packages/data.table/vignettes/datatable-reshape.html

#### Cheatsheets

 $ggplot\ cheatsheet\ https://raw.githubusercontent.com/rstudio/cheatsheets/master/datatable.pdf$ 

Advanced data.table cheatsheet

https://raw.githubusercontent.com/rstudio/cheatsheets/master/datatable.pdf