

Shallow water model

Validation

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Overview

- 1 The model
 - Geometry
 - model
 - Halo
- 2 Validation of the model
 - Validation conditions
 - error eval
 - Advection terms
 - Mass conservation
- 3 Testing the model
 - Initial conditions
 - First results

Geometry

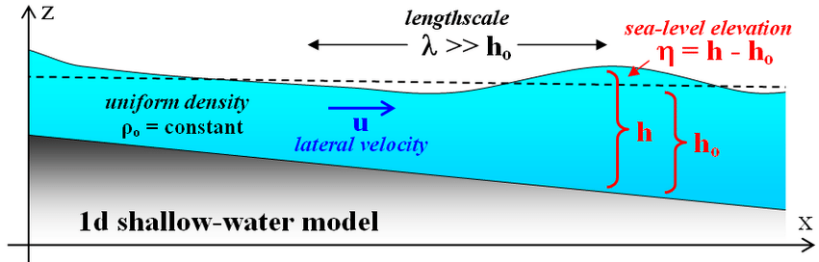


Figure: Shallow water model scheme

SW model

SW equations

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} - fv = -g \frac{\partial \eta}{\partial x} \quad (1)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} - fv = -g \frac{\partial \eta}{\partial y} \quad (2)$$

$$\frac{\partial \eta}{\partial t} + u \frac{\partial (uh)}{\partial x} + v \frac{\partial (vh)}{\partial y} = S(x, y, t) \quad (3)$$

Halo

Some problems about the Halo:

- Visualize the halo and it's function
- Implementation the halo on the code

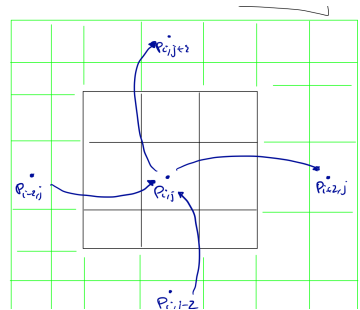


Figure: Halo scheme

Validation conditions

- $L = 1$
- $H = L$
- Mesh = [10 50 100
200 500 700 1000]
- $\Delta x = \frac{H/L}{mesh(1,i)}$
- $t = 1$
- Problems with MATLAB matrix creation method
- Operators to simplify some operations

Validation equations

P1,P2

$$P_u1 = -\frac{\partial(uu)}{\partial x} - \frac{\partial(uv)}{\partial x} \quad (4)$$

$$P_u2 = u\left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y}\right) \quad (5)$$

$$u(x, y, t) = \sin(2 \cdot \pi \cdot x) \cdot \cos(2 \cdot \pi \cdot y) \cdot t \quad (6)$$

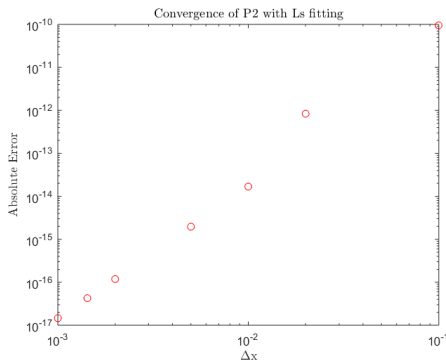
$$v(x, y, t) = \cos(2 \cdot \pi \cdot x) \cdot \sin(2 \cdot \pi \cdot y) \cdot t \quad (7)$$

$$h(x, y, t, D) = \cos(2 \cdot \pi \cdot x) \cdot \cos(2 \cdot \pi \cdot y) \cdot t + D \quad (8)$$

Error evaluation

$$Error(\Delta x(1, i)) = \frac{\sum_{i,j}^{N,M} (num_{i,j} - sym_{i,j})^2}{\Delta x(1, i)} \quad (9)$$

P2



Problems when trying to visualize the errors

- Solution = error mesh.
- Method to visualize the results obtained

Figure: Convergence of the advection term P2

P1

Problems when trying to visualize the errors

- Method to visualize the results obtained
- Error programming the TVD in one index
- sym function MATLAB

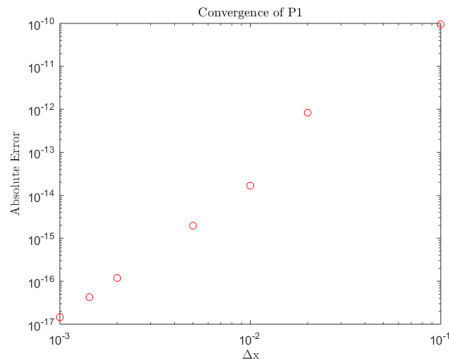
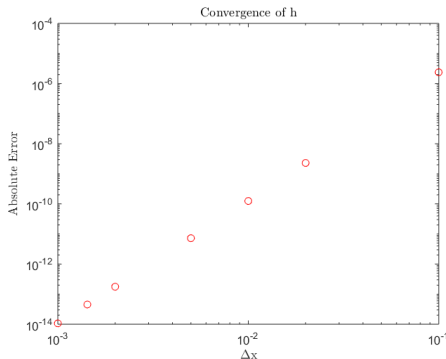


Figure: Convergence of the advection term P1

η



Problems when trying to visualize the errors

- Same to P1 because of the similarity of both methods

Figure: Convergence of the advection term P1

Initial conditions

Once the program is tested a simulation has been done in order to visualize the effect of a single perturbation and its evolution.

- Single perturbation as an integer value at eta in $t = 0$

- $N = M = 20$

- $T = 100 \text{ s}$

- $L=H=1$

- $\eta(5, 5, 1) = 4$

Water drop

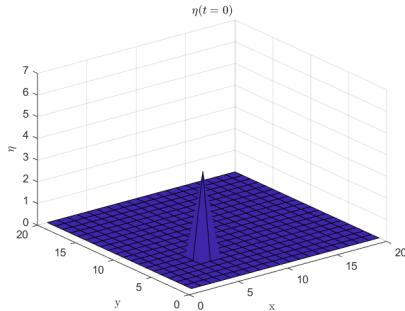


Figure: $\eta_{t=0}$

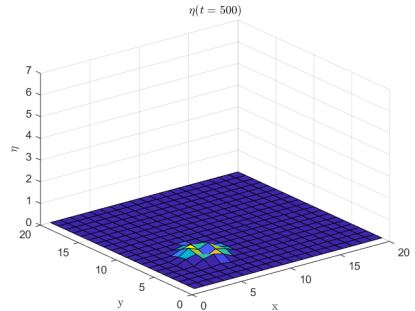


Figure: $\eta_{t=200}$

Water Drop

Thank you for your attention