A Framework for Benchmarking Clustering Algorithms

Marek Gagolewski^{a,b}

ARTICLE INFO

Keywords: clustering machine learning benchmark data noise points external cluster validity partition similarity score

Abstract

The evaluation of clustering algorithms can involve running them on a variety of benchmark problems, and comparing their outputs to the reference, ground-truth groupings provided by experts. Unfortunately, many research papers and graduate theses consider only a small number of datasets. Also, the fact that there can be many equally valid ways to cluster a given problem set is rarely taken into account. In order to overcome these limitations, we have developed a framework whose aim is to introduce a consistent methodology for testing clustering algorithms. Furthermore, we have aggregated, polished, and standardised many clustering benchmark dataset collections referred to across the machine learning and data mining literature, and included new datasets of different dimensionalities, sizes, and cluster types. An interactive datasets explorer, the documentation of the Python API, a description of the ways to interact with the framework from other programming languages such as R or MATLAB, and other details are all provided at https://clustering-benchmarks.gagolewski.com.

Please cite this paper as: Gagolewski M., A framework for benchmarking clustering algorithms, SoftwareX 20, 101270, 2022, DOI:10.1016/j.softx.2022.101270. This preprint includes some minor corrections.

Metadata	
Current code version	1.1.2
Permanent link to code repository	https://github.com/gagolews/clustering-benchmarks
Legal code license	GNU AGPL v3
Code versioning system used	git
Software code language used	Python
Compilation requirements, operating	Python 3.7+ with numpy, scipy, pandas, matplotlib, scikit-learn, and genieclust
environments and dependencies	
Link to developer documentation/manual	https://clustering-benchmarks.gagolewski.com
Feature requests and bug tracker	https://github.com/gagolews/clustering-benchmarks/issues

1. Introduction

Cluster analysis [1–3] is a data mining task where we discover *semantically useful* dataset partitions in a purely unsupervised manner. We know that there is no single "best" all-purpose algorithm [4], but some methods are better than others for certain problem types. However, a lot is still yet to be done [3, 5, 6] with regard to separating promising approaches from the systematically disappointing ones.

One approach to clustering validation relies on using the so-called internal measures, which are supposed to summarise the quality of partitions into a single number [7–9]. In practice, they can only focus on a single property of a given split (e.g., set separability or compactness) and the partitions they promote might be far from sound [10].

Another approach is to use the external validity measures [11–14] that quantify the similarity between the generated clusterings and the reference (ground-truth) partitions provided by experts.

Unfortunately, it is not rare for research papers and graduate theses to consider only a small number of benchmark datasets. We regularly come across the same 5–10 test problems from the UCI [15] database. This is obviously too few to make any evaluation rigorous enough and thus may lead to overfitting [16, 17]. Some authors propose their own datasets, but do not test their methods against other benchmark batteries. This might give rise to biased conclusions, as there is a risk that only the problems "easy" for a method of interest were included. On the other hand, the researchers

Email address: m.gagolewski@deakin.edu.au (M. Gagolewski) URL: https://www.gagolewski.com (M. Gagolewski)

ORCID(s): 0000-0003-0637-6028 (M. Gagolewski)

^aWarsaw University of Technology, Faculty of Mathematics and Information Science, ul. Koszykowa 75, 00-662 Warsaw, Poland

^bDeakin University, Data to Intelligence Research Centre, School of IT, Geelong, VIC 3220, Australia

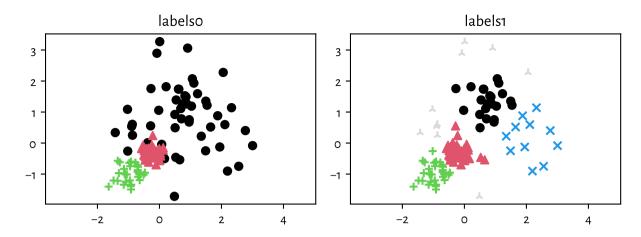


Figure 1: An example benchmark dataset (wut/x2) and the two corresponding reference partitions (k = 3 and k = 4; noise points marked in grey).

who generously share their data (e.g., [15, 18–21]), unfortunately, might not make the interaction with their batteries particularly smooth, as each of them uses different file formats.

Furthermore, the existing repositories do not reflect the idea there might be many equally valid/plausible/useful partitions of the same dataset; see [2, 22] for discussion.

On the other hand, some well-agreed-upon benchmark problems for a long time have existed in other machine learning domains (classification and regression datasets from the aforementioned UCI [15]; but also test functions for testing global optimisation solvers, e.g., [23, 24]).

In order to overcome these gaps, the current project proposes a consistent framework for benchmarking clustering algorithms. Its description is given in the next section. Then, in Section 3, we describe a Python API (the *clustering-benchmarks* package available at PyPI; see https://pypi.org/project/clustering-benchmarks/) that makes the interaction therewith relatively easy. Section 4 concludes the paper and proposes a few ideas for the future evolution of this framework.

2. Methodology

We have compiled a quite large suite of example real and simulated benchmark datasets. For reproducibility, the releases of our suite are versioned: e.g., https://github.com/gagolews/clustering-data-v1/releases/tag/v1.1.0 links to a revision that has been published in September 2022 [25]. Currently, there are nine batteries (collections), each of which features several datasets of different origins, dimensionalities, size imbalancedness, and level of overlap; including, but not limited to, [12, 15, 18–21, 26–32]¹; see the project's homepage for the detailed list.

Note that the datasets and the described software are independent of each other. Thanks to this, new datasets can easily be added in the future. Also, the users are free to use their own collections or access data from within other programming environments. The current framework defines the suggested unified file format which is detailed on the project's homepage.

Reference partitions. When referring to a particular benchmark problem, we use the convention "battery/dataset", e.g, "wut/x2". Let X be one of such datasets that consists of n points in \mathbb{R}^d . Each dataset is equipped with a reference partition assigned by experts. Such a grouping of the points into $k \ge 2$ clusters is encoded using a label vector \mathbf{y} , where $y_i \in \{1, \dots, k\}$ gives the cluster ID of the i-th object. For instance, the left subfigure of Figure 1 depicts the ground-truth 3-clustering of wut/x2 (which is based on the information about how this dataset has been generated from a mixture of three Gaussian distributions).

¹The original datasets were not equipped with alternative labellings nor with noise point markers; these were added by the current author.

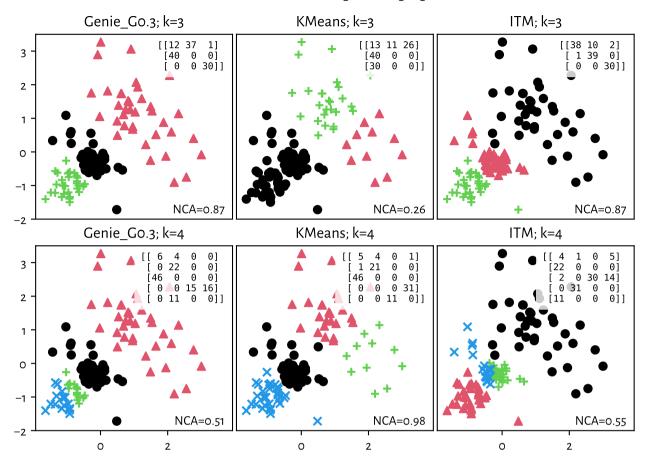


Figure 2: Clusterings of an example dataset (wut/x2) discovered by Genie (g=0.3) [33, 34], k-means, and ITM [35] (k=3 and k=4). Confusion matrices and normalised clustering accuracies (NCA; Eq. (1); comparisons against the reference partitions depicted in Figure 1) are also reported. Note that the second ground-truth partition features some noise points: hence, in the k=4 case, the first row of the confusion matrix is not taken into account.

Running the algorithm in question. Let us consider a clustering algorithm whose quality we would like to assess. When we apply it on X to discover a new k-partition (in an unsupervised manner, i.e., without revealing the true y), we obtain a vector of predicted labels encoding a new grouping, \hat{y} . For example, the first row of scatterplots in Figure 2 depicts the 3-partitions of wut/x2 discovered by three different methods.

Assessing partition similarity. Ideally, we would like to work with algorithms that yield partitions closely matching the reference ones. This should be true on as wide a set of problems as possible. Hence, we need to *relate* the predicted labels to the reference ones.

We can determine the confusion matrix C, where $c_{i,j}$ denotes the number of points in the *i*-th reference cluster that the algorithm assigned to the *j*-th cluster. Even though such a matrix summarises all the information required to judge the similarity between the two partitions, if we wish to compare the quality of different algorithms, we would rather have it aggregated in the form of a single number. As one of the many external cluster validity indices (see, e.g., [12–14]), we can use the normalised clustering accuracy [11] given by:

$$NCA(\mathbf{C}) = \max_{\sigma:\{1,...,k\}} \frac{1}{j} \sum_{j=1}^{k} \frac{c_{\sigma(j),j} - \frac{1}{k} c_{\sigma(j),j}}{c_{\sigma(j),} - \frac{1}{k} c_{\sigma(j),}},$$
(1)

which is the averaged percentage of correctly classified points in each cluster above the perfectly uniform label distri-

bution. As the actual cluster IDs do not matter (a partition is a *set* of clusters and sets are, by definition, unordered), the optimal matching between the cluster labels is performed automatically by finding the best permutation σ of the set $\{1, \ldots, k\}$.

There can be many valid partitions. What is more, it is in the very spirit of unsupervised learning that, in many cases, there might be many equally valid ways to split a given dataset. An algorithm should be rewarded for finding a partition that closely matches *any* of the reference ones. This might require running the method multiple times (unless it is a hierarchical one) to find the clusterings of different cardinalities. Then, the generated outputs are evaluated against all the available reference labellings and the *maximal* similarity score is reported.

Noise points. Also, to make the clustering problem more difficult, some datasets might feature *noise points* (e.g., outliers or irrelevant points in between the actual clusters). They are specially marked in the ground-truth vectors: we assigned them cluster IDs of 0; compare the right subfigure of Figure 1, where they are coloured grey. A clustering algorithm must never be informed about the location of such "problematic" points. Once the partition of the dataset is determined, they are excluded from the computation of the external cluster validity measures. In other words, it does not matter to which clusters the noise points are allocated.

3. The Python API

To facilitate the employment of the aforementioned framework, we have implemented an open-source package for Python named *clustering-benchmarks*. It can be installed from PyPI (https://pypi.org/project/clustering-benchmarks/), e.g., via a call to pip3 install clustering-benchmarks. Then, it can be imported by calling:

```
import clustbench # clustering-benchmarks
import os.path, genieclust, sklearn.cluster # we will need these later
```

Fetching benchmark data. The example datasets repository [25] (or any custom repository provided by the user) can be queried easily. Let us assume that we store it in the following directory:

```
data_path = os.path.join("~", "Projects", "clustering-data-v1") # example
```

A particular dataset (here, for example: wut/x2) can be accessed by calling:

```
battery, dataset = "wut", "x2"
b = clustbench.load_dataset(battery, dataset, path=data_path)
```

The above call returns a named tuple, whose data field gives the data matrix, labels gives the list of all ground-truth partitions (encoded as label vectors), and n_clusters gives the corresponding numbers of subsets. For instance, here is a way in which we have generated Figure 1.

```
for i in range(len(b.labels)):
    plt.subplot(1, len(b.labels), i+1)
    genieclust.plots.plot_scatter(
         b.data, labels=b.labels[i]-1, axis="equal", title=f"labels{i}")
plt.show()
```

Fetching precomputed results. Suppose we would like to study some precomputed clustering results (see https://github.com/gagolews/clustering-results-v1) which we store locally in the following directory:

```
results_path = os.path.join("~", "Projects", "clustering-results-v1", "original")
```

The partitions can be fetched by calling:

```
res = clustbench.load_results(
    "Genie", b.battery, b.dataset, b.n_clusters, path=results_path)
print(list(res.keys()))
## ['Genie_GO.1', 'Genie_GO.3', 'Genie_GO.5', 'Genie_GO.7', 'Genie_G1.0']
```

We thus have got access to data on the *Genie* [33, 34] algorithm with different gini_threshold (g) parameter settings (g = 1.0 gives the single linkage method).

Computing external cluster validity measures. Here is a way to compute the external cluster validity measures:

```
round(clustbench.get_score(b.labels, res["Genie_G0.3"]), 2)
## 0.87
```

By default, the aforementioned normalised clustering accuracy (Eq. (1)) is applied, but this might be changed to any other score by setting the metric argument explicitly. As explained above, we compare the predicted clusterings against all the reference partitions (ignoring the noise points), and report the maximal score.

Applying clustering methods manually. We can use clustbench.fit_predict_many to generate all the partitions required to compare ourselves against the reference labels. Let us test the k-means algorithm as implemented in the scikit-learn package [36]:

```
m = sklearn.cluster.KMeans()
res["KMeans"] = clustbench.fit_predict_many(m, b.data, b.n_clusters)
round(clustbench.get_score(b.labels, res["KMeans"]), 2)
### 0.98
```

We see that k-means (which specialises in detecting symmetric Gaussian-like blobs) performs better than *Genie* on this particular dataset; see Figure 2 for an illustration (also featuring the results generated by the ITM method [35]).

The project's homepage and documentation discuss many more functions.

4. Conclusion

The current project is designed to be extensible so that it can accommodate new datasets and/or label vectors in the future — so as to make the clustering algorithm evaluation much more rigorous. Any contributions are warmly welcome; see https://github.com/gagolews/clustering-benchmarks/issues for a feature request and bug tracker. In particular, we have implemented an interactive standalone application that can be used for preparing our own two-dimensional datasets (*Colouriser*).

Future versions of the benchmark suite will include methods for generating random samples of arbitrary sizes/cluster size distribution similar to a given dataset (e.g., with more noise points). Thanks to this, in the case of algorithms that feature many tunable parameters, it will be possible to implement some means to separate validation datasets (where we are allowed to learn the "best" settings; see, e.g., [17] and the references therein) from the testing ones (used in the final comparisons), which is a quite standard approach in other machine learning domains.

Moreover, the framework can be extended to cover overlapping clusterings as well as semi-supervised learning tasks, where an algorithm knows about the right assignment of some of the input points in advance.

Acknowledgements and Data Availability

This research was supported by the Australian Research Council Discovery Project ARC DP210100227.

Documentation and data are publicly available at https://clustering-benchmarks.gagolewski.com, https://github.com/gagolews/clustering-data-v1, and https://github.com/gagolews/clustering-results-v1. A big thank-you to all the researchers who share their datasets with the clustering community.

References

- [1] C. Hennig, What are the true clusters?, Pattern Recognition Letters 64 (2015) 53-62. doi:10.1016/j.patrec.2015.04.009.
- [2] U. von Luxburg, R. Williamson, I. Guyon, Clustering: Science or art?, in: I. Guyon, et al. (Eds.), Proc. ICML Workshop on Unsupervised and Transfer Learning, Vol. 27 of Proc. Machine Learning Research, 2012, pp. 65–79.
- [3] I. Van Mechelen, et al., Benchmarking in cluster analysis: A white paper (2018). URL https://arxiv.org/pdf/1809.10496.pdf
- [4] M. Ackerman, S. Ben-David, S. Brânzei, D. Loker, Weighted clustering: Towards solving the user's dilemma, Pattern Recognition 120 (2021) 108152. doi:10.1016/j.patcog.2021.108152.
- [5] H. Xiong, Z. Li, Clustering validation measures, in: C. Aggarwal, C. Reddy (Eds.), Data Clustering: Algorithms and Applications, CRC Press, 2014, pp. 571–606.
- [6] B. Tavakkol, J. Choi, M. Jeong, S. Albin, Object-based cluster validation with densities, Pattern Recognition 121 (2022) 108223. doi: 10.1016/j.patcog.2021.108223.
- [7] G. Milligan, M. Cooper, An examination of procedures for determining the number of clusters in a data set, Psychometrika 50 (2) (1985) 159–179.
- [8] U. Maulik, S. Bandyopadhyay, Performance evaluation of some clustering algorithms and validity indices, IEEE Transactions on Pattern Analysis and Machine Intelligence 24 (12) (2002) 1650–1654. doi:10.1109/TPAMI.2002.1114856.
- [9] O. Arbelaitz, I. Gurrutxaga, J. Muguerza, J. Pérez, I. Perona, An extensive comparative study of cluster validity indices, Pattern Recognition 46 (1) (2013) 243–256. doi:https://doi.org/10.1016/j.patcog.2012.07.021.
- [10] M. Gagolewski, M. Bartoszuk, A. Cena, Are cluster validity measures (in)valid?, Information Sciences 581 (2021) 620–636. doi:10.1016/j.ins.2021.10.004.
- [11] M. Gagolewski, Normalised clustering accuracy: An asymmetric external cluster validity measure, under review (preprint) (2023). doi: 10.48550/arXiv.2209.02935.URL https://arxiv.org/pdf/2209.02935.pdf
- [12] M. Rezaei, P. Fränti, Set matching measures for external cluster validity, IEEE Transactions on Knowledge and Data Engineering 28 (8) (2016) 2173–2186. doi:10.1109/TKDE.2016.2551240.
- [13] S. Wagner, D. Wagner, Comparing clusterings An overview, Tech. Rep. 2006-04, Faculty of Informatics, Universität Karlsruhe (TH) (2006). URL https://illwww.iti.kit.edu/extra/publications/ww-cco-06.pdf
- [14] D. Horta, R. Campello, Comparing hard and overlapping clusterings, Journal of Machine Learning Research 16 (93) (2015) 2949–2997.
- [15] D. Dua, C. Graff, UCI Machine Learning Repository, http://archive.ics.uci.edu/ml (2022).
- [16] T. Ullmann, A. Beer, M. Hünemörder, T. Seidl, A.-L. Boulesteix, Over-optimistic evaluation and reporting of novel cluster algorithms: An illustrative study, Advances in Data Analysis and Classification (2022). doi:10.1007/s11634-022-00496-5.
- [17] T. Ullmann, C. Hennig, A.-L. Boulesteix, Validation of cluster analysis results on validation data: A systematic framework, Wiley Interdisciplinary Reviews: Data Mining and Knowledge Discovery 12 (3) (2021) e14444. doi:10.1002/widm.1444.
- [18] D. Graves, W. Pedrycz, Kernel-based fuzzy clustering and fuzzy clustering: A comparative experimental study, Fuzzy Sets and Systems 161 (2010) 522–543. doi:10.1016/j.fss.2009.10.021.
- [19] A. Ultsch, Clustering with SOM: U*C, in: Workshop on Self-Organizing Maps, 2005, pp. 75-82.
- [20] M. Thrun, A. Ultsch, Clustering benchmark datasets exploiting the fundamental clustering problems, Data in Brief 30 (2020) 105501. doi: 10.1016/j.dib.2020.105501.
- [21] P. Fränti, S. Sieranoja, K-means properties on six clustering benchmark datasets, Applied Intelligence 48 (12) (2018) 4743–4759. doi: 10.1007/s10489-018-1238-7.
- [22] S. Dasgupta, V. Ng, Single data, multiple clusterings, in: Proc. NIPS Workshop Clustering: Science or Art? Towards Principled Approaches, 2009.
- [23] M. Jamil, X.-S. Yang, H.-J. Zepernick, 8-test functions for global optimization: A comprehensive survey, in: Swarm Intelligence and Bio-Inspired Computation, 2013, pp. 193–222. doi:10.1016/B978-0-12-405163-8.00008-9.
- [24] T. Weise, et al., Benchmarking optimization algorithms: An open source framework for the traveling salesman problem, IEEE Computational Intelligence Magazine 9 (3) (2014) 40–52. doi:10.1109/MCI.2014.2326101.
- [25] M. Gagolewski, et al., A benchmark suite for clustering algorithms: Version 1.1.0 (2022). doi:10.5281/zenodo.7088171. URL https://github.com/gagolews/clustering-data-v1/releases/tag/v1.1.0
- [26] M. Thrun, Q. Stier, Fundamental clustering algorithms suite, SoftwareX 13 (2021) 100642. doi:10.1016/j.softx.2020.100642.
- [27] G. Karypis, E. Han, V. Kumar, CHAMELEON: Hierarchical clustering using dynamic modeling, Computer 32 (8) (1999) 68–75. doi: 10.1109/2.781637.
- [28] J. Bezdek, J. Keller, R. Krishnapuram, L. Kuncheva, N. Pal, Will the real iris data please stand up?, IEEE Transactions on Fuzzy Systems 7 (3) (1999) 368–369. doi:10.1109/91.771092.
- [29] L. McInnes, J. Healy, S. Astels, hdbscan: Hierarchical density based clustering, The Journal of Open Source Software 2 (11) (2017) 205. doi:10.21105/joss.00205.
- [30] P. Fränti, O. Virmajoki, Iterative shrinking method for clustering problems, Pattern Recognition 39 (5) (2006) 761–765.
- [31] S. Sieranoja, P. Fränti, Fast and general density peaks clustering, Pattern Recognition Letters 128 (2019) 551–558. doi:10.1016/j.patrec. 2019.10.019.
- [32] A. Jain, M. Law, Data clustering: A user's dilemma, Lecture Notes in Computer Science 3776 (2005) 1-10.
- [33] M. Gagolewski, M. Bartoszuk, A. Cena, Genie: A new, fast, and outlier-resistant hierarchical clustering algorithm, Information Sciences 363 (2016) 8–23. doi:10.1016/j.ins.2016.05.003.
- [34] M. Gagolewski, genieclust: Fast and robust hierarchical clustering, SoftwareX 15 (2021) 100722. doi:10.1016/j.softx.2021.100722.
- [35] A. Müller, S. Nowozin, C. Lampert, Information theoretic clustering using minimum spanning trees, in: Proc. German Conference on Pattern Recognition, 2012.
- [36] F. Pedregosa, et al., Scikit-learn: Machine learning in Python, Journal of Machine Learning Research 12 (85) (2011) 2825–2830.