Practical 7 8-Queen Problem using Back Tracking

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I. Introduction

Aim of this practical is to perform chain matrix multiplication using Dynamic Programming.

- A 8 x 8 chess board and 8 queens where Queens can move horizontally, vertically and diagonally.
- A chessboard with N queens arranged on the board in such a way that no two queens can attack each other.
- use backtracking each time we got bounded by constraints i.e, when we have no more place valid to place the new queens in the board.
- Also, before placing a new queen to the board, at first the position in the board should be throughly checked and if the place is valid then we could place a new queen on the board.

II. IMPLEMENTATION

I. Main Program - **8queen.c**

```
// Author: Gahan Saraiya
  // GiT: http://github.com/gahan9/
  // StackOverflow: https://stackoverflow.com/users/story/7664524
  // Website: http://gahan9.github.io/
        ______
   // Implementing 8-queen Problem
   #include <stdio.h>
  #include <stdlib.h>
  #include <stdbool.h>
  #include <math.h>
13
  int counter = 1;
14
  int placeQueen(int *board, int row_no) {
16
      for (register int i = 0; i < row_no; i++) {</pre>
17
          if (board[i] == board[row_no])
18
             return false; // same column
```

```
if ((board[i] - board[row_no]) == (row_no - i))
               return false; // same major diagonal
21
           if ((board[row_no] - board[i]) == (row_no - i))
               return false; // same minor diagonal
24
       return true;
25
   }
27
   void pretty_print(int q[], int board_size) {
28
       printf("\n");
29
       for (int i = 0; i < board_size; i++) {</pre>
           for (int j = 0; j < board_size; j++) {
               if (q[i] == j)
32
                  printf("Q ");
33
               else
                  printf("* ");
           }
           printf("\n");
37
       }
   }
39
40
   void queenLogic(int *queens, int row_no, int board_size) {
41
       if (row_no == board_size) {
           pretty_print(queens, board_size);
43
           if (counter \% 10 == 1)
44
               printf("%dst solution found...\n", counter);
           else if (counter \% 10 == 2)
               printf("%dnd solution found...\n", counter);
           else if (counter \% 10 == 3)
               printf("%drd solution found...\n", counter);
           else
              printf("%dth solution found...\n", counter);
           counter++;
       } else {
53
           for (int i = 0; i < board_size; i++) {</pre>
               queens[row_no] = i;
               if (placeQueen(queens, row_no))
                   queenLogic(queens, row_no + 1, board_size);
57
           }
       }
   }
60
61
62
   int main() {
       int board_size = 8;
       int *queens = malloc(board_size * sizeof(int));
64
       printf("########"\n"
65
              "#-----#\n"
              "#-----#\n", board_size);
```

```
queenLogic(queens, 0, board_size);
return 1;
}
```

I.1 Output

```
#----#
   #----#
   Q * * * * * * *
   * * * * Q * * *
   * * * * * * * Q
   * * * * * Q * *
   * * Q * * * * *
   * * * * * * Q *
   * () * * * * *
11
   * * * Q * * * *
   1st solution found...
13
   Q * * * * * * *
15
   * * * * * Q * *
16
   * * * * * * * Q
17
   * * Q * * * * *
18
   * * * * * * Q *
   * * * Q * * * *
20
   * Q * * * * *
21
   * * * * Q * * *
22
   2nd solution found...
23
24
   Q * * * * * * *
25
   * * * * * * Q *
   * * * () * * * *
27
   * * * * * () * *
   * * * * * * * Q
29
   * Q * * * * *
   * * * * Q * * *
31
   * * Q * * * * *
   3rd solution found...
34
   Q * * * * * * *
   * * * * * * Q *
```

```
* * * * Q * * *
38
    * * * * * Q * *
41
    * * Q * * * * *
42
    4th solution found...
43
44
    * Q * * * * *
45
    * * * Q * * * *
47
    Q * * * * * * *
50
51
    * * * * Q * * *
52
    5th solution found...
54
    * Q * * * * * *
    * * * * () * * *
    * * * * * * Q *
57
58
    * * * * * * * Q
    * * * * * Q * *
61
    * * * Q * * * *
    6th solution found...
63
64
    * * * * Q * * *
    * * * * * * Q *
    * * * Q * * * *
70
    * * * * * Q * *
71
    * * Q * * * * *
72
    7th solution found...
73
74
75
```

```
* * * * * * Q *
79
     * * * * * * * Q
     * * Q * * * *
81
     * * * * Q * * *
82
    8th solution found...
83
84
     * () * * * * * *
     * * * * * * * Q
     Q * * * * * * *
     * * * () * * * *
     * * * * * * Q *
     * * * * Q * * *
    9th solution found...
93
95
97
     * * * * * Q * *
99
     * * * * Q * * *
100
     Q * * * * * * *
101
     * * * Q * * * *
102
    10th solution found...
104
     * Q * * * * *
105
     * * * * * * Q *
106
     * * * * Q * * *
107
     * * * * * * * Q
108
109
     * * * Q * * * *
     * * * * * Q * *
111
     * * Q * * * * *
     11st solution found...
113
114
115
116
118
```

```
* * Q * * * * *
119
120
     * * * * * * Q *
     * * * Q * * * *
122
     12nd solution found...
123
124
     * * Q * * * * *
125
     () * * * * * *
126
     * * * * * * Q *
127
     * * * * Q * * *
     * * * * * * * Q
129
     * Q * * * * *
     * * * () * * * *
131
     * * * * * Q * *
132
     13rd solution found...
133
134
136
     * Q * * * * *
138
139
140
     * * * Q * * * *
141
     * * * * * Q * *
142
     14th solution found...
143
144
145
     * * * * () * * *
147
148
     * * * * * Q * *
149
     * * * Q * * * *
150
     * * * * * * Q *
     Q * * * * * * *
152
     15th solution found...
154
     * * Q * * * * *
155
     * * * * Q * * *
156
157
159
```

```
* Q * * * * *
160
161
     * * * * * Q * *
     16th solution found...
163
164
     * * Q * * * * *
165
     * * * * Q * * *
166
     * * * * * * * Q
167
     * * * Q * * * *
168
     Q * * * * * * *
     * * * * * * Q *
170
     * Q * * * * *
171
     * * * * * () * *
172
     17th solution found...
173
174
     * * Q * * * * *
175
     * * * * * Q * *
177
     * * * * Q * * *
179
180
     * * * * * * Q *
181
     * * * Q * * * *
182
     18th solution found...
183
184
186
     * () * * * * *
187
     * * * * * * Q *
188
     () * * * * * *
189
     * * * Q * * * *
190
     * * * * * * * Q
191
     * * * * Q * * *
     19th solution found...
193
195
196
     * Q * * * * *
197
198
200
```

```
* * * * * * * Q
201
202
     20th solution found...
204
     * * Q * * * * *
205
206
     * * * Q * * * *
207
     () * * * * * *
208
209
     * * * * Q * * *
     * * * * * * Q *
211
     * Q * * * * *
212
     21st solution found...
213
214
     * * Q * * * * *
215
     * * * * * Q * *
216
     * * * Q * * * *
218
     * * * * Q * * *
220
     * * * * * * Q *
221
     Q * * * * * * *
222
     22nd solution found...
223
224
     * * Q * * * * *
225
     * * * * * () * *
227
     Q * * * * * * *
228
     * * * Q * * * *
229
     * * * * * * Q *
230
     * * * * Q * * *
231
     * Q * * * * * *
232
     23rd solution found...
234
     * * Q * * * * *
235
     * * * * * Q * *
236
237
238
     * * * * Q * * *
239
241
```

```
* * * Q * * * *
     24th solution found...
243
245
     * * * * * Q * *
246
247
     * Q * * * * *
248
     * * * Q * * * *
249
250
     * * * * * * Q *
     * * * * Q * * *
252
     25th solution found...
254
255
256
     * Q * * * * *
257
     * * * * * * * Q
     * * * * () * * *
259
     Q * * * * * *
     * * * Q * * * *
261
     * * * * * Q * *
262
     26th solution found...
263
264
     * * Q * * * * *
265
266
     * () * * * * *
268
     * * * * * () * *
269
     * * * Q * * * *
270
     Q * * * * * * *
271
     * * * * Q * * *
272
     27th solution found...
273
     * * Q * * * * *
275
     * * * () * * * *
277
278
279
     * * * * * Q * *
280
282
```

```
28th solution found...
283
284
     * * * Q * * * *
286
     * * * * Q * * *
     * * * * * * * Q
288
     * () * * * * * *
289
     * * * * * * Q *
290
     * * Q * * * * *
291
     * * * * * Q * *
     29th solution found...
293
     * * * () * * * *
295
     Q * * * * * * *
     * * * * Q * * *
297
     * * * * * * * Q
298
     * * * * * Q * *
     * * () * * * * *
300
     * * * * * * Q *
     * () * * * * *
302
     30th solution found...
303
304
     * * * Q * * * *
305
     * Q * * * * *
306
     * * * * Q * * *
307
     * * * * * * * Q
309
     Q * * * * * * *
310
     * * Q * * * * *
311
     * * * * * * Q *
312
     31st solution found...
313
314
     * * * Q * * * *
315
316
     * * * * * * Q *
     * * () * * * * *
318
     * * * * * Q * *
319
     * * * * * * * Q
320
     Q * * * * * * *
321
     * * * * Q * * *
     32nd solution found...
323
```

```
324
     * * * Q * * * *
325
327
329
330
     * * * * Q * * *
331
     Q * * * * * * *
332
     33rd solution found...
333
334
     * * * Q * * * *
336
     * * * * * * Q *
337
     * * * * Q * * *
338
339
     * * * * * * * Q
     * * * * * Q * *
341
     * * Q * * * * *
     34th solution found...
343
344
     * * * Q * * * *
345
     * () * * * * * *
346
     * * * * * * * Q
347
     * * * * Q * * *
348
350
     * * Q * * * * *
351
     * * * * * Q * *
352
     35th solution found...
353
354
355
     * () * * * * * *
357
     * * * * * Q * *
359
     * * Q * * * * *
360
     * * * * Q * * *
361
     * * * * * * Q *
362
     36th solution found...
364
```

```
* * * Q * * * *
366
     Q * * * * * * *
       * * * Q * * *
368
     * Q * * * * *
369
370
     * * Q * * * * *
371
     * * * * * * Q *
372
     37th solution found...
373
     * * * Q * * * *
375
377
     * Q * * * * *
378
     * * * * * * Q *
379
380
     * * Q * * * * *
     * * * * () * * *
382
     38th solution found...
384
     * * * Q * * * *
385
     * * * * * Q * *
386
     * * * * * * * ()
387
     * * Q * * * * *
389
     * * * * * * Q *
     * * * * Q * * *
391
     * () * * * * *
392
     39th solution found...
393
     * * * Q * * * *
395
396
398
     * * * * Q * * *
     * () * * * * *
400
     * * * * * Q * *
401
     * * Q * * * * *
402
     40th solution found...
403
     * * * Q * * * *
405
```

```
406
407
409
     * * * * Q * * *
410
     Q * * * * * * *
411
     * * * * * Q * *
412
     41st solution found...
413
414
     * * * Q * * * *
415
     * * * * * * Q *
416
     * * * * Q * * *
418
     * * * * * Q * *
419
420
     * * Q * * * * *
421
     * * * * * * * Q
     42nd solution found...
423
425
426
     * * * * Q * * *
427
     * * Q * * * * *
428
     Q * * * * * * *
429
430
     * * * * * * * Q
     * () * * * * *
432
     43rd solution found...
433
434
     * * * Q * * * *
435
436
437
439
     * * * * * * Q *
441
     * * * * Q * * *
442
     44th solution found...
443
444
     * * * Q * * * *
446
```

```
448
     * * * * * * Q *
450
     * * * * * Q * *
451
     * * Q * * * * *
452
     45th solution found...
453
454
     * * * Q * * * *
455
     * * * * * * * Q
     * * * * Q * * *
457
     * * Q * * * * *
459
     * * * * * * Q *
     * Q * * * * *
461
     * * * * * Q * *
462
     46th solution found...
464
     * * * * Q * * *
     Q * * * * * * *
466
     * * * Q * * * *
467
     * * * * * Q * *
468
469
     * Q * * * * *
470
     * * * * * * Q *
471
     * * Q * * * * *
     47th solution found...
473
474
     * * * * Q * * *
475
     Q * * * * * * *
476
477
     * * * * * * * Q
     * * * Q * * * *
478
480
     * * Q * * * * *
     * * * * * Q * *
482
     48th solution found...
483
484
     * * * * Q * * *
485
487
```

```
* * * * * Q * *
489
     * * * * * * Q *
     * () * * * * *
491
     * * * Q * * * *
492
     49th solution found...
493
494
     * * * * Q * * *
495
496
     * * * () * * * *
     * * * * * Q * *
498
     * * Q * * * * *
500
     Q * * * * * * *
501
     * * * * * * Q *
502
     50th solution found...
503
     * * * * () * * *
505
     * () * * * * *
     * * * Q * * * *
507
     * * * * * * Q *
508
     * * Q * * * * *
509
     * * * * * * * ()
510
     * * * * * Q * *
511
     Q * * * * * * *
512
     51st solution found...
514
     * * * * Q * * *
515
     * Q * * * * * *
516
     * * * * * Q * *
517
     () * * * * * *
518
519
     * * * Q * * * *
     * * * * * * * Q
521
     * * Q * * * * *
     52nd solution found...
523
524
     * * * * Q * * *
525
526
528
```

```
* * * Q * * * *
530
     * * Q * * * * *
     * * * * * Q * *
532
     53rd solution found...
533
534
     * * * * () * * *
535
     * * Q * * * * *
536
     Q * * * * * * *
537
     * * * * * Q * *
     * * * * * * * Q
539
     * Q * * * * * *
     * * * () * * * *
541
     * * * * * * Q *
     54th solution found...
543
544
     * * * * Q * * *
546
     Q * * * * * * *
     * * * * * * Q *
548
     * Q * * * * * *
549
550
     * * * * * Q * *
551
     * * * Q * * * *
552
     55th solution found...
553
     * * * * () * * *
555
     * * Q * * * * *
     * * * * * * * Q
557
     * * * Q * * * *
558
     * * * * * * Q *
559
560
     * * * * * Q * *
     * Q * * * * * *
562
     56th solution found...
564
     * * * * Q * * *
565
     * * * * * * Q *
566
     Q * * * * * * *
567
569
```

```
* * * * * Q * *
     * * * () * * * *
571
     * () * * * * *
     57th solution found...
573
574
     * * * * Q * * *
575
     * * * * * * Q *
576
     Q * * * * * * *
577
     * * * Q * * * *
578
     * Q * * * * * *
     * * * * * * * Q
580
     * * * * * Q * *
     * * Q * * * * *
582
     58th solution found...
583
584
     * * * * Q * * *
585
     * * * * * * Q *
587
     * * * Q * * * *
589
     Q * * * * * * *
590
     * * Q * * * * *
591
     * * * * * Q * *
592
     59th solution found...
593
594
     * * * * () * * *
596
     * Q * * * * * *
597
     * * * * * Q * *
598
     * * () * * * * *
599
     Q * * * * * * *
600
     * * * Q * * * *
601
     * * * * * * * Q
     60th solution found...
603
     * * * * () * * *
605
606
     * Q * * * * *
607
     * * * * * Q * *
608
610
```

```
* * * * * * * Q
612
     61st solution found...
614
     * * * * () * * *
615
616
     * * * Q * * * *
617
     Q * * * * * * *
618
     * * Q * * * * *
619
     * * * * * * * Q
     * * * * * Q * *
621
     * Q * * * * *
     62nd solution found...
623
     * * * * Q * * *
625
626
     * * * Q * * * *
628
     * * * * * Q * *
630
     * Q * * * * *
631
     * * * * * * Q *
632
     63rd solution found...
633
634
     * * * * Q * * *
635
637
     Q * * * * * * *
638
639
     * () * * * * * *
640
     * * * * * Q * *
641
     * * Q * * * * *
642
     64th solution found...
644
     * * * * * Q * *
     Q * * * * * * *
646
     * * * * Q * * *
647
     * Q * * * * *
648
     * * * * * * * Q
649
651
```

```
* * * Q * * * *
652
     65th solution found...
653
655
656
657
     () * * * * * *
658
     * * Q * * * * *
659
     * * * * Q * * *
660
     * * * * * * * Q
     * * * Q * * * *
662
     66th solution found...
664
     * * * * * () * *
665
666
667
     Q * * * * * * *
669
     * * * * Q * * *
671
     * * Q * * * * *
672
     67th solution found...
673
674
     * * * * * Q * *
675
676
678
     * * * * () * * *
679
680
     * Q * * * * *
681
     * * * Q * * * *
682
     68th solution found...
683
685
     * * Q * * * * *
687
688
     * * * () * * * *
689
690
692
```

```
69th solution found...
693
694
     * * * * * Q * *
696
698
     * * * * Q * * *
     * Q * * * * *
700
     * * * Q * * * *
701
     * * * * * * Q *
     70th solution found...
703
     * * * * * Q * *
705
     * * Q * * * * *
     * * * * Q * * *
707
     * * * * * * Q *
708
     Q * * * * * * *
     * * * () * * * *
710
     * Q * * * * *
     * * * * * * * Q
712
     71st solution found...
713
714
     * * * * * () * *
715
     * * Q * * * * *
716
     * * * * Q * * *
717
719
     * * * Q * * * *
720
     * Q * * * * * *
721
     * * * * * * Q *
722
     72nd solution found...
723
724
     * * * * * () * *
725
726
     * * * * * * Q *
     * () * * * * *
728
     * * * Q * * * *
729
     * * * * * * * Q
730
     Q * * * * * * *
731
     * * * * Q * * *
     73rd solution found...
733
```

```
734
735
737
738
739
     * * * * Q * * *
740
     Q * * * * * * *
741
     * * * Q * * * *
742
     74th solution found...
743
744
     * * * * * Q * *
745
746
     * * * * * * Q *
747
748
749
     * * * * * * Q
     * () * * * * *
751
     * * * * Q * * *
     75th solution found...
753
754
     * * * * * Q * *
755
     * * * Q * * * *
756
     Q * * * * * * *
757
     * * * * Q * * *
758
760
     * * * * * * Q *
761
     * * Q * * * * *
762
     76th solution found...
763
764
765
     * * * Q * * * *
767
     * * * * () * * *
769
     * * * * * * Q *
770
     Q * * * * * * *
771
     * * Q * * * * *
772
     77th solution found...
773
774
```

```
* * * * * Q * *
776
     * * * * * * Q *
778
     * * Q * * * * *
779
     * * * * Q * * *
780
     * Q * * * * *
781
     * * * * * * * Q
782
     78th solution found...
783
785
     * * * Q * * * *
787
     Q * * * * * * *
789
790
     * * * * Q * * *
     * * Q * * * * *
792
     79th solution found...
794
     * * * * * Q * *
795
796
797
     * * * Q * * * *
799
     * * * * * * Q *
     * * * * Q * * *
801
     * * Q * * * * *
802
     80th solution found...
803
804
     * * * * * * Q *
805
806
808
     * * * * * Q * *
     * * * () * * * *
810
     * Q * * * * * *
811
     * * * * Q * * *
812
     81st solution found...
813
     * * * * * * Q *
815
```

```
817
819
     * * * * Q * * *
820
     * * Q * * * * *
821
     * * * * * Q * *
822
     82nd solution found...
823
824
     * * * * * * Q *
     * Q * * * * * *
826
     * * * * * Q * *
828
     Q * * * * * * *
     * * * Q * * * *
830
     * * * * * * * Q
831
     * * * * Q * * *
     83rd solution found...
833
835
836
     Q * * * * * * *
837
     * * * * * Q * *
838
839
     * * * * Q * * *
840
     * () * * * * *
     * * * Q * * * *
842
     84th solution found...
843
844
845
847
     * * * * Q * * *
849
     * * * * * Q * *
851
     * * * Q * * * *
852
     85th solution found...
853
854
856
```

```
858
860
     * * Q * * * * *
861
     * * * * * Q * *
862
     86th solution found...
863
864
     * * * * * * Q *
865
     * * * Q * * * *
867
869
     Q * * * * * * *
870
     * * Q * * * * *
871
     * * * * Q * * *
872
     87th solution found...
874
     * * * * * * Q *
     * * * * Q * * *
876
     * * Q * * * * *
877
878
     * * * * * Q * *
879
     * * * * * * * Q
     * Q * * * * * *
881
     * * * Q * * * *
     88th solution found...
883
884
885
     * Q * * * * * *
886
     * * * Q * * * *
887
888
     * * * * Q * * *
890
     * * Q * * * * *
     * * * * * Q * *
892
     89th solution found...
893
894
895
897
```

```
899
     * * * * * * Q *
901
     * * * * * Q * *
     90th solution found...
903
905
906
     * * * * * Q * *
908
     * Q * * * * * *
     * * * * () * * *
910
     * * * * * * Q *
911
     * * * Q * * * *
912
     91st solution found...
913
914
915
     * * * Q * * * *
917
918
919
     * Q * * * * *
920
     * * * * * * Q *
921
     * * * * Q * * *
922
     92nd solution found...
```