Practical 2 Implementation of B+ Tree

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I. Introduction

Aim of this practical is to implement algorithm of B+ tree

II. IMPLEMENTATION

I. Utility utility.h

```
//
   // Created by jarvis on 17/8/18.
   #ifndef DSA_LAB_UTILITY_H
   #define DSA_LAB_UTILITY_H
   #include <string.h>
   #include <stdarg.h>
10
   int write_log(const char *format, ...) {
11
       if(DEBUG) {
12
            va_list args;
13
            va_start (args, format);
14
            vprintf(format, args);
15
            va_end (args);
       }
17
   }
18
19
   int *get_min_max(int *array, int no_of_elements, int min_max[]){
       // get minimum and maximum of array
21
         printf("elements of array: ");
22
       for(int i=0; i<no_of_elements; i++){</pre>
23
              printf("%d ", *(array + i));
            if (*(array + i) < min_max[0])</pre>
                min_max[0] = *(array + i);
26
            if (*(array + i) > min_max[1])
                min_max[1] = *(array + i);
       }
29
       return min_max;
```

```
}
31
   int display_array(int *array, int no_of_elements){
       // display given array of given size(no. of elements require because sizeof()
34
        → returns max bound value)
       write_log(": ");
35
       for(int i=0; i<no_of_elements; i++){</pre>
            write_log( "%d ", *(array + i));
37
38
       return 0;
39
   }
40
41
42
43
   void swap(int *one, int *two){
       // swap function to swap elements by location/address
       int temp = *one;
45
       *one = *two;
46
       *two = temp;
47
   }
   char** split_string(char* str) {
50
       // split string by separator space
51
       char** splits = NULL;
       char* token = strtok(str, " ");
53
       int spaces = 0;
54
55
       while (token) {
            splits = realloc(splits, sizeof(char*) * ++spaces);
            if (!splits) {
58
                return splits;
            }
            splits[spaces - 1] = token;
61
            token = strtok(NULL, " ");
62
63
       return splits;
64
   }
   void read_file_input() {
67
       // under development function to read inputs from file
       int ptr[100], count = 0, i, ar_count;
       char c[100];
70
       FILE *fp = fopen("file.in", "r");
71
       char in = fgetc(fp);
       // ar_count = (int) (in - '0');
74
       printf("\narr\n");
75
       while (in != EOF){
            if ((int) (in -'0') == -16){
```

II. Constants constant.h

```
// Created by jarvis on 17/8/18.

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#ifndef DSA_LAB_CONSTANT_H

#define DSA_LAB_CONSTANT_H

#define TEST_NUM 5000

#define DEBUG 0

#endif //DSA_LAB_CONSTANT_H
```

III. Main Program - bPlusTree.c

```
//
  // Created by Gahan Saraiya on 20/8/18.
   // Implement B tree then B+ tree
  // Implement B+ tree of degree 4
  // Insertion, Search
  #include <stdio.h>
  #include <stdlib.h>
  #include <stdbool.h>
  #define DEBUG 0
  #include "../utils/utility.h"
11
12
  #define TREE_ORDER 4
13
14
  typedef struct record {
15
       int value;
16
   } record;
17
```

```
typedef struct Node {
19
       int total_keys;
20
       bool is_leaf;
21
       void **ptrs;
22
       int *keys;
23
       struct Node *parent;
24
       struct Node *next;
   } BPlusNode;
26
27
   BPlusNode *insert_into_parent(BPlusNode *, BPlusNode *, int, BPlusNode *);
   int exact_search(BPlusNode *root, int key);
   record *NewRecord(int value) {
31
       record *new_record = (record *) malloc(sizeof(record));
32
       if (new_record == NULL) {
            perror("Record creation.");
34
            exit(EXIT_FAILURE);
35
       } else {
36
            new_record->value = value;
       return new_record;
39
   }
40
   BPlusNode *find_leaf(BPlusNode *root, int key) {
42
         Search Leaf Node for value - key
43
       int i = 0;
44
       BPlusNode *n = root;
       if (n == NULL) {
            return n;
47
48
       while (!n->is_leaf) {
            i = 0;
50
            while (i < n->total_keys) {
51
                if (key >= n->keys[i]) i++;
52
                else break;
            }
            n = (BPlusNode *) n->ptrs[i];
55
       }
56
       return n;
   }
58
   record *find(BPlusNode *root, int key) {
60
       int i = 0;
61
       BPlusNode *c = find_leaf(root, key);
       if (c == NULL) return NULL;
63
       for (i = 0; i < c->total_keys; i++)
64
            if (c->keys[i] == key) break;
       if (i == c->total_keys)
```

```
return NULL;
67
        else
68
            return (record *) c->ptrs[i];
   }
70
71
72
    BPlusNode *newnode(void) {
        BPlusNode *new_node;
74
        new_node = (BPlusNode *) malloc(sizeof(BPlusNode));
75
76
        new_node->keys = (int *) malloc((TREE_ORDER - 1) * sizeof(int));
        new_node->ptrs = (void **) malloc(TREE_ORDER * sizeof(void *));
        new_node->is_leaf = false;
        new_node->total_keys = 0;
82
        new_node->parent = NULL;
83
        new_node->next = NULL;
84
        return new_node;
   }
87
    BPlusNode *insert_at_leaf(BPlusNode *leaf, int key, record *pointer) {
88
        int i, index;
90
91
        index = 0;
92
        while (index < leaf->total_keys && leaf->keys[index] < key)</pre>
            index++;
95
        for (i = leaf->total_keys; i > index; i--) {
            leaf->keys[i] = leaf->keys[i - 1];
            leaf->ptrs[i] = leaf->ptrs[i - 1];
        }
        leaf->keys[index] = key;
100
        leaf->ptrs[index] = pointer;
101
        leaf->total_keys++;
        return leaf;
103
   }
104
   BPlusNode *insert_into_node(BPlusNode *root, BPlusNode *n, int left_index, int
106
        key, BPlusNode *right) {
        int i;
107
108
        for (i = n->total_keys; i > left_index; i--) {
            n->ptrs[i + 1] = n->ptrs[i];
110
            n->keys[i] = n->keys[i - 1];
111
        }
112
        n->ptrs[left_index + 1] = right;
```

```
n->keys[left_index] = key;
114
        n->total_keys++;
115
        return root;
   }
117
118
    BPlusNode *insert_into_node_after_splitting(BPlusNode *root, BPlusNode *old_node,
119

→ int left_index,
                                               int key, BPlusNode *right) {
120
121
        int i, j, s, k_prime;
122
        BPlusNode *new_node, *child;
123
        int *temp_keys;
        BPlusNode **temp_ptrs;
125
126
        temp_ptrs = (BPlusNode **) malloc((TREE_ORDER + 1) * sizeof(BPlusNode *));
127
128
        temp_keys = (int *) malloc(TREE_ORDER * sizeof(int));
129
130
        for (i = 0, j = 0; i < old_node->total_keys + 1; i++, j++) {
131
            if (j == left_index + 1) j++;
132
            temp_ptrs[j] = (BPlusNode *) old_node->ptrs[i];
133
        }
134
135
        for (i = 0, j = 0; i < old_node->total_keys; i++, j++) {
136
            if (j == left_index) j++;
137
            temp_keys[j] = old_node->keys[i];
138
        }
139
        temp_ptrs[left_index + 1] = right;
141
        temp_keys[left_index] = key;
142
143
        if (TREE_ORDER % 2 == 0)
144
            s = TREE_ORDER / 2;
145
        else
146
            s = TREE_ORDER / 2 + 1;
147
        new_node = newnode();
149
150
        old_node->total_keys = 0;
151
        for (i = 0; i < s - 1; i++) {
152
            old_node->ptrs[i] = temp_ptrs[i];
153
            old_node->keys[i] = temp_keys[i];
154
155
            old_node->total_keys++;
        }
        old_node->ptrs[i] = temp_ptrs[i];
157
        k_prime = temp_keys[s - 1];
158
        for (++i, j = 0; i < TREE_ORDER; i++, j++) {
159
            new_node->ptrs[j] = temp_ptrs[i];
```

```
new_node->keys[j] = temp_keys[i];
161
             new_node->total_keys++;
162
163
        new_node->ptrs[j] = temp_ptrs[i];
165
        new_node->parent = old_node->parent;
166
        for (i = 0; i <= new_node->total_keys; i++) {
             child = (BPlusNode *) new_node->ptrs[i];
168
             child->parent = new_node;
169
170
        return insert_into_parent(root, old_node, k_prime, new_node);
171
    }
172
173
    BPlusNode *insert_into_parent(BPlusNode *root, BPlusNode *left, int key,
174
        BPlusNode *right) {
175
        int left_index;
176
        BPlusNode *parent;
177
        parent = left->parent;
179
180
        if (parent == NULL) {
181
             BPlusNode *r = newnode();
182
             r->keys[0] = key;
183
             r->ptrs[0] = left;
184
             r->ptrs[1] = right;
185
             r->total_keys++;
186
             r->parent = NULL;
             left->parent = r;
188
             right->parent = r;
189
             return r;
190
        }
191
192
        left_index = 0;
193
194
        while (left_index <= parent->total_keys && parent->ptrs[left_index] != left) {

→ left_index++; }
196
        if (parent->total_keys < (TREE_ORDER - 1))</pre>
             return insert_into_node(root, parent, left_index, key, right);
199
        return insert_into_node_after_splitting(root, parent, left_index, key,
200
         → right);
    }
201
202
    BPlusNode *split(BPlusNode *root, BPlusNode *leaf, int key, record *pointer) {
203
        BPlusNode *leaf_s;
204
        int *newkeys;
```

```
void **newptrs;
206
        int insertindex, s, new_key, i, j;
207
        leaf_s = newnode();
        leaf_s->is_leaf = true;
210
211
        newkeys = (int *) malloc(TREE_ORDER * sizeof(int));
213
        newptrs = (void **) malloc(TREE_ORDER * sizeof(void *));
214
215
        insertindex = 0;
216
        while (insertindex < TREE_ORDER - 1 && leaf->keys[insertindex] < key)
            insertindex++;
218
219
        for (i = 0, j = 0; i < leaf->total_keys; i++, j++) {
220
            if (j == insertindex) j++;
221
            newkeys[j] = leaf->keys[i];
222
            newptrs[j] = leaf->ptrs[i];
223
        }
224
225
        newkeys[insertindex] = key;
226
        newptrs[insertindex] = pointer;
227
        leaf->total_keys = 0;
229
230
        if ((TREE_ORDER - 1) % 2 == 0)
231
            s = (TREE_ORDER - 1) / 2;
232
        else
233
            s = ((TREE_ORDER - 1) / 2) + 1;
234
235
        for (i = 0; i < s; i++) {
236
            leaf->ptrs[i] = newptrs[i];
237
            leaf->keys[i] = newkeys[i];
238
            leaf->total_keys++;
239
        }
240
241
        for (i = s, j = 0; i < TREE_ORDER; i++, j++) {
242
            leaf_s->ptrs[j] = newptrs[i];
243
            leaf_s->keys[j] = newkeys[i];
            leaf_s->total_keys++;
245
        }
246
247
248
        leaf_s->ptrs[TREE_ORDER - 1] = leaf->ptrs[TREE_ORDER - 1];//BPlusNode pointed
         → by last pointer now should be pointed by new BPlusNode
        leaf->ptrs[TREE_ORDER - 1] = leaf_s; //new BPlusNode should be now pointed by
250

→ previous BPlusNode
```

251

```
for (i = leaf->total_keys; i < TREE_ORDER - 1; i++)//key holes in a BPlusNode
252
             leaf->ptrs[i] = NULL;
253
        for (i = leaf_s->total_keys; i < TREE_ORDER - 1; i++)</pre>
254
             leaf_s->ptrs[i] = NULL;//pointer holes in a BPlusNode
255
256
        leaf_s->parent = leaf->parent;
257
        new_key = leaf_s->keys[0];
259
        return insert_into_parent(root, leaf, new_key, leaf_s);
260
    }
261
262
    BPlusNode *insert(BPlusNode *root, int key, int value) {
263
        record *pointer;
264
        BPlusNode *leaf;
265
266
        if (root == NULL) {
267
               Initializing Tree
    //
268
             BPlusNode *1 = newnode();
269
270
             l->is_leaf = true;
271
             root = 1:
272
             root->keys[0] = key;
273
             root->ptrs[0] = pointer;
274
             root->ptrs[TREE_ORDER - 1] = NULL;
275
             root->parent = NULL;
276
             root->total_keys++;
277
             // write_log("\nRoot--> keys[0] = %d", root->keys[0]);
278
             return root;
279
        }
280
281
        if (find(root, key) != NULL)
282
             return root;
283
284
        pointer = NewRecord(value);
285
        leaf = find_leaf(root, key);
286
        if (leaf->total_keys < TREE_ORDER - 1) {</pre>
288
    //
               No splitting require as datum can be accommodate in free space
289
             leaf = insert_at_leaf(leaf, key, pointer);
             return root;
291
        }
292
        return split(root, leaf, key, pointer);
293
294
    }
    int path_to_root(BPlusNode *root, BPlusNode *child) {
296
        int length = 0;
297
        BPlusNode *c = child;
298
        while (c != root) {
```

```
c = c->parent;
300
             length++;
301
302
         return length;
303
    }
304
305
    BPlusNode *queue = NULL;
306
307
    void Queue(BPlusNode *new_node) {
308
         BPlusNode *c;
309
         if (queue == NULL) {
310
             queue = new_node;
             queue->next = NULL;
312
313
         }
         else {
314
             c = queue;
315
             while (c->next != NULL) {
316
                  c = c->next;
317
318
             c->next = new_node;
319
             new_node->next = NULL;
320
         }
321
    }
322
323
    BPlusNode *deQueue(void) {
324
         BPlusNode *n = queue;
325
         queue = queue->next;
326
         n->next = NULL;
327
         return n;
328
    }
329
330
    void pretty_print(BPlusNode *root) {
331
         write_log("Printing Tree\n");
332
         BPlusNode *n = NULL;
333
         int i = 0;
334
         int rank = 0;
335
         int new_rank = 0;
336
337
         if (root == NULL) {
             printf("\nOpsss... It seems no value exist, Kindly consider adding
339

    element(s)\n");

             return;
340
341
         }
         queue = NULL;
343
         Queue(root);
344
         while (queue != NULL) {
345
             n = deQueue();
```

```
if (n->parent != NULL && n == n->parent->ptrs[0]) {
347
                 new_rank = path_to_root(root, n);
348
                 if (new_rank != rank) {
                     rank = new_rank;
                     printf("\n");
351
                 }
352
            }
354
            for (i = 0; i < n->total_keys; i++) {
355
                 printf("%d ", n->keys[i]);
356
            }
            if (!n->is_leaf) {
                 for (i = 0; i \le n->total_keys; i++)
359
                     Queue((BPlusNode *) n->ptrs[i]);
360
            }
361
            printf(" | ");
362
363
        printf("\n");
364
    }
365
366
    int cut(int length) {
367
        if (length \% 2 == 0)
368
            return length / 2;
        else
370
            return length / 2 + 1;
371
    }
372
373
374
    int get_neighbor_index(BPlusNode *n) {
375
376
        int i;
377
        for (i = 0; i <= n->parent->total_keys; i++)
378
            if (n->parent->ptrs[i] == n)
379
                 // return neighbouring node.
380
                 return i - 1;
381
        printf("Search for non-existent pointer to BPlusNode in parent.\n");
383
        printf("Node: %#lx\n", (unsigned long) n);
384
        exit(EXIT_FAILURE);
    }
386
387
    int search(BPlusNode *root, int key) {
388
        write_log("In batch search");
        int i = 0, match = 0;
        //----first find in leaf BPlusNode is the key is
391
         → found.-----
        BPlusNode *c = find_leaf(root, key);
        if (c == NULL) {
```

```
// data/key not exist
394
             match = 0;
395
        for (i = 0; i < c->total_keys; i++) {
397
             if (c->keys[i] == key) {
398
                 // data found
399
                 match = 1;
                 break;
401
             }
402
        }
403
        return match;
    }
405
406
    int batch_search(BPlusNode *root) {
407
        write_log("In batch search");
408
409
        int start, end, flag = 1;
410
        BPlusNode *n = NULL;
411
        int i = 0, rank = 0, new_rank = 0;
412
        int exact_match_flag = 0;
413
        printf("\nstart value: ");
414
        scanf("%d", &start);
415
        printf("\nend value: ");
416
        scanf("%d", &end);
417
418
        queue = NULL;
419
        Queue(root);
420
        while (queue != NULL) {
421
             n = deQueue();
422
             if (n->parent != NULL && n == n->parent->ptrs[0]) {
423
                 new_rank = path_to_root(root, n);
424
                 if (new_rank != rank) {
425
                      rank = new_rank;
426
                      printf("Depth level: %d", rank);
427
                      printf("\n");
428
                 }
             }
430
431
             for (i = 0; i < n->total_keys; i++) {
                 if (n-)is_leaf \&\& n-)keys[i] >= start \&\& n-)keys[i] <= end) {
433
                      if (flag) {
434
                           write_log("Traversed neighbour\n");
435
                          flag = 0;
                      printf("%d ", n->keys[i]);
438
                 }
439
             }
440
             if (!n->is_leaf) {
441
```

```
for (i = 0; i \le n->total_keys; i++)
442
                                                          Queue((BPlusNode *) n->ptrs[i]);
443
                                  }
444
                      }
445
                      return 0;
446
          }
447
449
          int main(int argc, char *argv[]) {
450
                             int degree;
451
           //
                             if (atoi(argv[1]))
           //
                                        degree = atoi(argv[1]);
453
           //
                             else
454
455
                                        degree = TREE_ORDER;
                      int find_key, batch_search_value[100], n, i = 0, max, min;
                      BPlusNode *root;
457
                      root = NULL;
458
459
                      printf("\nB+ Tree Degree (must be at least 3): %d", TREE_ORDER);
460
                      461
                                           "\n1. Insert"
462
                                           "\n2. Search"
463
                                           "\n3. Batch Search"
                                           "\n4. Print Tree"
465
                                           "\n5. Exit"
466
                                           "\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pr
467
                      int choice;
468
                      while (choice != 5){
                                  printf("choice: ");
470
                                  scanf("%d", &choice);
471
                                  int value, result;
472
                                  int start, end;
473
                                  switch (choice) {
474
                                              case 1:
475
                                                         printf("\nValue: ");
476
                                                         scanf("%d", &value);
                                                         root = insert(root, value, value);
478
                                                          printf("\nB+ Tree : \n");
479
                                                         pretty_print(root);
                                                         break;
481
                                              case 2:
482
                                                          printf("\nSearch Value: ");
483
                                                          scanf("%d", &value);
                                                          result = search(root, value);
                                                          if (result)
486
                                                                     printf("Value %d matched\n", value);
487
                                                          else
488
                                                                     printf("Value %d does not exist\n", value);
```

```
break;
490
              case 3:
491
                  printf("\nBatch Search: ");
                  result = batch_search(root);
493
                  printf("\n");
494
                  break;
495
              case 4:
                  pretty_print(root);
497
                  break;
498
              case 5:
499
                  printf("\nGreetings!!! see you later...\n");
                  return 0;
              default:
502
                  printf("\nKindly select correct value...\n");
503
                  504
                         "\n1. Insert"
505
                         "\n2. Search"
506
                         "\n3. Batch Search"
507
                         "\n4. Print Tree"
                         "\n5. Exit"
509
510
                            "\n###########################;");
          }
511
       }
512
513
       return 0;
514
   }
515
```

Output

```
B+ Tree :
5 59 |
choice: 1
Value: 66
B+ Tree :
5 59 66 |
choice: 1
Value: 14
B+ Tree :
59 |
5 14 | 59 66 |
choice: 1
Value: 98
B+ Tree :
59 l
5 14 | 59 66 98 |
choice: 1
Value: 105
B+ Tree :
59 98 |
5 14 | 59 66 | 98 105 |
choice: 1
Value: 1500
B+ Tree :
59 98 |
5 14 | 59 66 | 98 105 1500 |
choice: 1
Value: 1109
B+ Tree :
59 98 1109 |
5 14 | 59 66 | 98 105 | 1109 1500 |
choice: 1
Value: 23
```

```
B+ Tree :
59 98 1109 |
5 14 23 | 59 66 | 98 105 | 1109 1500 |
choice: 1
Value: 50
B+ Tree :
59 |
23 | 98 1109 |
5 14 | 23 50 | 59 66 | 98 105 | 1109 1500 |
choice: 1
Value: 109
B+ Tree :
59 |
23 | 98 1109 |
5 14 | 23 50 | 59 66 | 98 105 109 | 1109 1500 |
choice: 1
Value: 90
B+ Tree :
59 I
23 | 98 1109 |
5 14 | 23 50 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 51
B+ Tree :
59 |
23 | 98 1109 |
5 14 | 23 50 51 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 52
B+ Tree :
59 l
23 51 | 98 1109 |
5 14 | 23 50 | 51 52 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 25
B+ Tree :
```

```
59 |
23 51 | 98 1109 |
5 14 | 23 25 50 | 51 52 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 26
B+ Tree :
59 |
23 26 51 | 98 1109 |
5 14 | 23 25 | 26 50 | 51 52 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 27
B+ Tree :
59 |
23 26 51 | 98 1109 |
5 14 | 23 25 | 26 27 50 | 51 52 | 59 66 90 | 98 105 109 | 1109 1500 |
choice: 1
Value: 28
B+ Tree :
26 59 I
23 | 28 51 | 98 1109 |
5 14 | 23 25 | 26 27 | 28 50 | 51 52 | 59 66 90 | 98 105 109 | 1109 1500
choice: 1
Value: 100
B+ Tree :
26 59 |
23 | 28 51 | 98 105 1109 |
5 14 | 23 25 | 26 27 | 28 50 | 51 52 | 59 66 90 | 98 100 | 105 109 | 1109

→ 1500 |

choice: 1
Value: 92
B+ Tree :
26 59 98 |
23 | 28 51 | 90 | 105 1109 |
5 14 | 23 25 | 26 27 | 28 50 | 51 52 | 59 66 | 90 92 | 98 100 | 105 109

→ | 1109 1500 |

choice: 1
```

```
Value: 53
B+ Tree :
26 59 98 |
23 | 28 51 | 90 | 105 1109 |
5 14 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100 | 105
→ 109 | 1109 1500 |
choice: 1
Value: 17
B+ Tree :
26 59 98 |
23 | 28 51 | 90 | 105 1109 |
5 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100 | 105
→ 109 | 1109 1500 |
choice: 1
Value: 1
B+ Tree :
26 59 98 |
14 23 | 28 51 | 90 | 105 1109 |
1 5 | 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100

→ | 105 109 | 1109 1500 |

choice: 1
Value: 0
B+ Tree :
26 59 98 |
14 23 | 28 51 | 90 | 105 1109 |
0 1 5 | 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100

→ | 105 109 | 1109 1500 |

choice: 1
Value: 103
B+ Tree :
26 59 98 |
14 23 | 28 51 | 90 | 105 1109 |
0 1 5 | 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100

→ 103 | 105 109 | 1109 1500 |

choice: 1
Value: 108
B+ Tree :
```

```
26 59 98 |
14 23 | 28 51 | 90 | 105 1109 |
0 1 5 | 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100
→ 103 | 105 108 109 | 1109 1500 |
choice: 2
Search Value: 52
Value 52 matched
choice: 2
Search Value: 555
Value 555 does not exist
choice: 3
Batch Search:
start value: 5
end value: 52
Depth level: 1
Depth level: 2
5 14 17 23 25 26 27 28 50 51 52
choice: 4
26 59 98 |
14 23 | 28 51 | 90 | 105 1109 |
0 1 5 | 14 17 | 23 25 | 26 27 | 28 50 | 51 52 53 | 59 66 | 90 92 | 98 100
→ 103 | 105 108 109 | 1109 1500 |
choice: 5
Greetings!!! see you later...
```

III. Summary

- all leaves at the same lowest level
- all nodes at least half full (except root)

Let f be the degree of tree and n be the total number of data then

Space Complexity

	Max # pointers	Max # keys	Min # pointers	Min # keys
Non-leaf	f	f-1	$\lceil f/2 \rceil$	$\lceil f/2 \rceil - 1$
Root	f	f-1	2	1
Leaf	f	f-1	$\lfloor f/2 \rfloor$	$\lfloor f/2 \rfloor$

- Number of disk accesses proportional to the height of the B-tree. - The ***worst-case height*** of a B+ tree is:

Let f be the degree of tree and n be the total number of data then

Space Complexity

	Time Complexity	Remarks
height	$O(\log_f n)$	
Root	$O(f\log_f n)$	linear search inside each nodes
search	$O(\log_2 f \log_f n)$	binary search inside each node
insert	$O(\log_f n)$	if splitting not require
insert	$O(f \log_f n)$	if splitting require
insert	$O(\log_f n)$	if merge not require
insert	$O(f \log_f n)$	if merge require