John Romero Programming Proverbs

John Romero, "The Early Days of Id Software - John Romero @ WeAreDevelopers Conference 2017"

- de-tour
 - recall we can predict the time a point travels a distance by:

s = distance

u = initial velocity

a = acceleration

t = time

De-tour

- if we were to drop a small ball bearing from 1 metre, how long would it take to hit the ground?
- initial velocity (u = 0)
- acceleration approx (a = 10) ms^2

De-tour

thus

De-tour

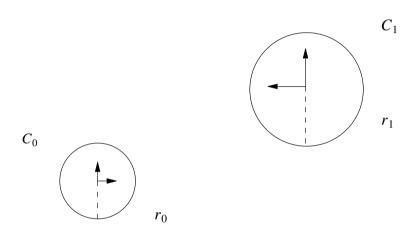
$$t = 0.45$$

$$t = -0.45$$

we also note that for more complicated quadratic equations we can use the formula:

$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

for any equation matching: $at^2 + bt + c = 0$



- each circle has a radius, position, velocity and acceleration
 - radius is a scalar, all others are vectors

- remember that when these circles collide the distance between the two circle mid points will be $r_0 + r_1$
- we know generally that the distance between the circles can be calculated as: $\sqrt{(c_{0x} c_{1x})^2 + (c_{0y} c_{1y})^2}$
- so we need to find the time when: $r_0 + r_1 = \sqrt{(c_{0x} c_{1x})^2 + (c_{0y} c_{1y})^2}$

using the formula for initial position, velocity and acceleration:

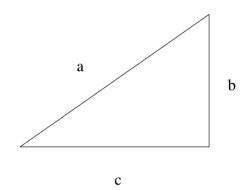
$$s = s_0 + ut + \frac{at^2}{2}$$
 it is also known that the position circle c_0 at time, t ,

is:
$$\left[c_{0x} + v_{0x}t + \frac{a_{0x}t^2}{2}, c_{0y} + v_{0y}t + \frac{a_{0y}t^2}{2}\right]$$

 \blacksquare correspondingly the position circle c_1 at time, t, is:

$$\left[c_{1x} + v_{1x}t + \frac{a_{1x}t^2}{2}, c_{1y} + v_{1y}t + \frac{a_{1y}t^2}{2}\right]$$

recall Pythagorean theorem can be used to find the length of the hypotenuse from the length of the base and height of a right angled triangle



$$a^2 = b^2 + c^2$$

- \blacksquare a is the radius of circle 0 and circle 1
- **b** is the difference of the y-axis position of the circles
- lacktriangleright c is the difference of the x-axis position of the circles

therefore we need to find the time at which the distance between both circles is $r_0 + r_1$ which is:

which can be easily rearranged as:

$$0 = \left[\left(c_{0x} + v_{0x}t + \frac{a_{0x}t^2}{2} \right) - \left(c_{1x} + v_{1x}t + \frac{a_{1x}t^2}{2} \right) \right]^2 + \left[\left(c_{0y} + v_{0y}t + \frac{a_{0y}t^2}{2} \right) - \left(c_{1y} + v_{1y}t + \frac{a_{1y}t^2}{2} \right) \right]^2 - (r_0 + r_1)^2$$

we need to multiply the equation and separate out the values: A, B, C, D, E where:

$$At^4 + Bt^3 + Ct^2 + Dt + E = 0$$

- then we solve for, t and the smallest value of t which is greater than zero is the next collision time
- see pge/twoDsim.mod in the function findCollisionCircles

fortunately, we have a tool called wxmaxima (similar to Mathematica) which will manipulate the algebra without mistake :-)

```
ri + rj == sqrt(abs(xin-xjn)^2 + abs(yin-yjn)^2) for values of t
ri + rj == sqrt(((xi + vxi * t + aix * t^2 / 2.0) - (xj + vxj * t + ajx * t^2 / 2.0))^2 +
                ((yi + vyi * t + aiy * t^2 / 2.0) - (yj + vyj * t + ajy * t^2 / 2.0))^2)
let:
a = xi
b = xj
c = vxi
d = vxj
e = aix
f = ajx
g = yi
h = yj
k = vyi
1 = vyj
m = aiy
n = ajy
o = ri
p = rj
t = t
```

```
solve polynomial:

A := sqr(n)-2.0*m*n+sqr(m)+sqr(f)-2.0*e*f+sqr(e);

B := (4.0*1-4.0*k)*n+(4.0*k-4.0*1)*m+(4.0*d-4.0*c)*f+(4.0*c-4.0*d)*e;

C := (4.0*h-4.0*g)*n+(4.0*g-4.0*h)*m+4.0*sqr(1)-8.0*k*1+4.0*sqr(k)+
(4.0*b-4.0*a)*f+(4.0*a-4.0*b)*e+4.0*sqr(d)-8.0*c*d+4.0*sqr(c);

D := (8.0*h-8.0*g)*1+(8.0*g-8.0*h)*k+(8.0*b-8.0*a)*d+(8.0*a-8.0*b)*c;

E := 4.0*sqr(h)-8.0*g*h+4.0*sqr(g)+4.0*sqr(b)-8.0*a*b+4.0*sqr(a)-sqr(2.0*(p+o));
```

fortunately, we can cut and paste the output from wxmaxima into our code and carefully convert it into program code and it works!

Conclusion

- we have seen that we can predict when two circles will collide in the future
 - using x and y components based on $s = ut + a \frac{t^2}{2}$
- in the next lecture we will extend this to look at calculating the time a circle hits a polygon