COMP9444 Neural Networks and Deep Learning
Term 3, 2020

Solutions to Exercise 6: Word Vectors

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1. Consider the sentence

    "two flowers grew tall on two tall towers"

    a. Write the co−occurrence matrix X for this sentence, using a 4−word context window (i.e. two context words on either side of the central word)

	flowers	grew	on	tall	towers	two
flowers	0	1	0	1	0	1
grew	1	0	1	1	0	1
on	0	1	0	2	0	1
tall	1	1	2	0	1	2
towers	0	0	0	1	0	1
two	1	1	1	2	1	0

    b. Use `torch.svd()` to compute the singular value decompositon of this matrix X = USV^T

    ```
    import torch

    M = torch.Tensor(
    [[0,1,0,1,0,1],
    [1,0,1,1,0,1],
    [0,1,0,2,0,1],
    [1,1,2,0,1,2],
    [0,0,0,1,0,1],
    [1,1,1,2,1,0]]);

    U, S, V = torch.svd(M)

    torch.set_printoptions(precision=2)

    print(U)
    print(S)
    print(V)

    tensor([[-0.30,  0.24,  0.38, -0.36,  0.41,  0.64],
            [-0.37, -0.11, -0.03,  0.80,  0.47,  0.04],
            [-0.41,  0.53,  0.29, -0.12,  0.08, -0.67],
            [-0.56, -0.74,  0.16, -0.27, -0.13, -0.14],
            [-0.22,  0.19,  0.37,  0.36, -0.75,  0.29],
            [-0.50,  0.25, -0.78, -0.13, -0.17,  0.17]])
    tensor([4.83, 2.53, 1.70, 1.10, 0.40, 0.11])
    tensor([[-0.30, -0.24, -0.38,  0.36,  0.41,  0.64],
            [-0.37,  0.11,  0.03, -0.80,  0.47,  0.04],
            [-0.41, -0.53, -0.29,  0.12,  0.08, -0.67],
    ```

```
              [-0.56,  0.74, -0.16,  0.27, -0.13, -0.14],
              [-0.22, -0.19, -0.37, -0.36, -0.75,  0.29],
              [-0.50, -0.25,  0.78,  0.13, -0.17,  0.17]])
```

(Note: replacing U and V with –U and –V would preserve $X = USV^T$)

c. Extract a word representation from the first two columns of U and use `matplotlib` to plot the words on a 2–dimensional graph.
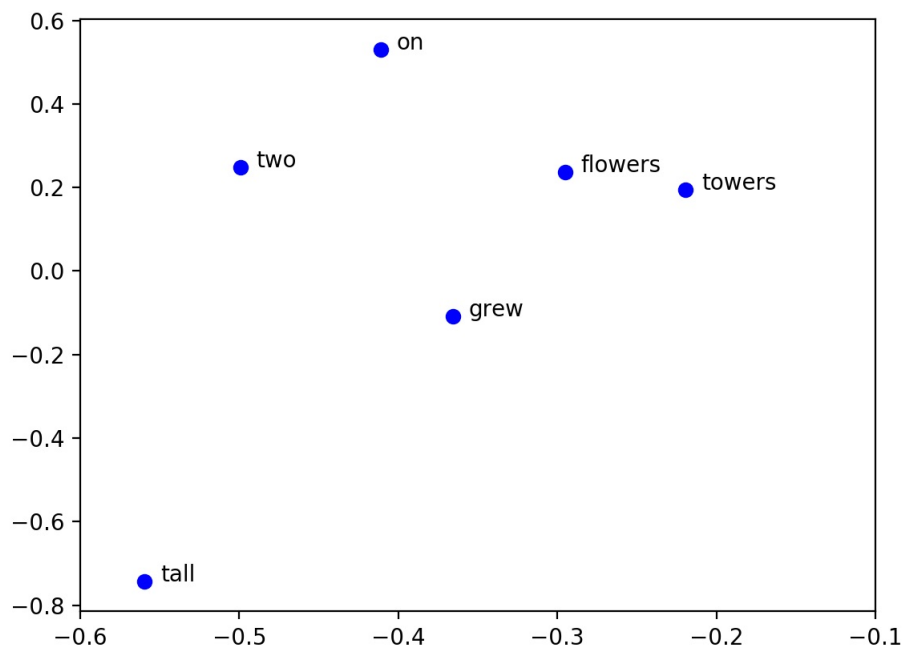
```
import matplotlib.pyplot as plt

Lex = ['flowers','grew','on','tall','towers','two']

plt.scatter(U[:,0],U[:,1],c='B')
plt.xlim([-0.6,-0.1])

for a in range(U.size()[0]):
    plt.text(0.01+U[a,0],U[a,1],Lex[a])

plt.savefig('vectors.png')
plt.show()
```


(Note: the image may be rotated, depending on the sign of U)