

311 – Numerical Computations

Lab 8: Numerical Methods for Solving System of Linear Equations: Gauss-Seidel Method

The basic formula for a single approximation step of Gauss-Seidel Method to solve the $n \times n$ system: $\mathbf{Ax} = \mathbf{b}$:

$$\begin{bmatrix} A_{0,0} & \cdots & \vdots \\ \vdots & \ddots & \vdots \\ \cdots & \cdots & A_{n-1,n-1} \end{bmatrix} \begin{bmatrix} x_0 \\ \vdots \\ x_{n-1} \end{bmatrix} = \begin{bmatrix} b_0 \\ \vdots \\ b_{n-1} \end{bmatrix} \quad is$$

for i in range (n): # 0 to $n-1$

$$x_i = \frac{1}{A_{i,i}} \left(b_i - \sum_{j=0, j \neq i}^{j=n-1} A_{i,j} x_j \right)$$

Spring 2020-2021 Final Exam question:

Write a (Numpy-based) program (i.e. uses Numpy Arrays) that implements the Gauss-Seidel Method. It prints the first K approximations (K is input) of \mathbf{x} using Gauss-Seidel Method to solve an $N \times N$ system (inputs are taken from user).

Always Use the initial guess ($K=0$): $\mathbf{x}^0 = [0, 0, \dots, 0]$

Assume the input matrix \mathbf{a} is diagonally dominant.

Quiz 3:

Topic: Numpy Library and Solving Linear Systems

Sunday 24-April-2022

Additional Exercise (to prepare for the quiz):

Assume that the user already has a Numpy (one dimensional) array W.

Example: `W = np.array([1,2,3,4,5,6])`

Using the Numpy library, write a Python code that prints the elements of W in every possible matrix size.

Example: if W is of length 12 then matrices of size: 1x12, 2x6, 3x4, 4x3, 6x2 and 12x1 should be printed.

If W is of length 5 then matrices of size: 1x5 and 5x1 should be printed.

Remark: The needed functions from Numpy Library are:

- `W.reshape(x,y)`, which will return a matrix of size x by y (if possible), and
- `T.print()`, which will print the matrix T in rectangular matrix format.

Sample Run:

Assuming `W=np.array([1,2,3,4])`

Output:

```
[[1 2 3 4]]
```

```
[[1 2]
```

```
[3 4]]
```

```
[[1]
```

```
[2]
```

```
[3]
```

```
[4]]
```