

Date: 14/3/2022

CS211 (Theory of Computation I)

**DUE: March 22nd****HOMEWORK I (CO1)****NAME:****ID:**

**Notes: 1- Type your solution in this file using MS Word and save it using your ID followed by the letters H1 as a filename (For example, 12345678H1.docx)**

**2- Submit your solution as a single PDF file using Moodle.**

**3- Organization and Presentation worth 20% of the mark.**

**Q1.** Problem 40 – page 16 in Textbook . (Proof by contradiction)

**Q2.** Prove by *induction* that  $\sum_{k=0}^n x^k = \frac{x^{n+1} - 1}{(x-1)}$

**Q3.** Language  $L$  on  $\Sigma = \{0, 1\}$  is defined as  $L = \{ 0^{2k+1} 1^{2m} \mid k, m \geq 0 \}$ .

a) Write all words in  $L$  of size  $\leq 4$  .

b) Find a grammar for  $L$ .

**Q4.** Design a grammar for  $L = \{ a^{2k} b^{2m+1} c^n \mid k \geq 1, m \geq 0, n \geq 0 \}$ .

Show the derivation of the string **aabbbbbbcc**.

**Q5.** Design a grammar for  $L = \{ v w v : v, w \in \{a, b\}^*, |v| = 2 \}$ .

Show the derivation of the string **ababbaab**.

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