

311 – Numerical Computations

Lab 6: Newton-Raphson Method

Python Libraries (of interest in this course):

- **SciPy**: provides a lot of Numerical Algorithms (Examples: `optimize.bisect` (See Lab 5) and `optimize.newton` (See Current Lab)).
- **NumPy**: Fast array and Matrix manipulation
- **SymPy**: Symbolic Computations (Which is the converse of Numerical Computations).
- In Our course, we will study/use **the first two libraries**, the third will be covered only in the current lab (just as general knowledge).
- Finally there is also the library **Matplotlib**: Creates interactive charts/figures/visualizations.

A) Global variables in Python

```
x=5
def f(w):
    return w+x

print(f(10))           #prints 15
```

```
x=5
def f(w):
    x=x+3
    return w+x

print(f(10))
```

➔ Error: local variable 'x' referenced before assignment

Solution:

```
x=5
def f(w):
    global x
    x=x+3
    return w+x

print(f(10))           #prints 18
```

The rule: You can only access global variables but you must use the keyword: global [variable Name] If you need to modify it.

B) Newton Method in SciPy:

```
from scipy import optimize
def f(x):
    return x**2-4

print(optimize.newton(f,1))
#prints 2.000000000000000004
```

Exercise: Use SciPy's Newton method to solve:

$$(x^2 - 7x + 9)e^{-0.2x} = 0 \quad (\text{with } x_0=6)$$

C) Newton Method Implementation

Based on Newton-Raphson Method, write the function:

```
def nth_root (x, n, e=0.05, maxit=50, init=1)
```

where:

- x: the number that its root is to be computed.
- n: the degree of the root ($n \geq 2$), $n=2$: square root, $n=3$: cubic root and so on.
- e: epsilon.
- maxit: maximum number of iterations.
- init: initial guess, taken by default to be 1.

The good point is that newton's method for roots finding converges for any initial guess.

But we can find a better guess:

Better Initial guess: $1 + (x-1)/n$

D) What about if derivative is not easy to compute?

install “sympy”!!

```
C:\Users\Galal>pip install sympy
Collecting sympy
  Downloading sympy-1.8-py3-none-any.whl (6.1 MB)
    |████████████████████████████████████████| 6.1 MB 1.6 MB/s
Collecting mpmath>=0.19
  Downloading mpmath-1.2.1-py3-none-any.whl (532 kB)
    |████████████████████████████████████████| 532 kB 363 kB/s
Installing collected packages: mpmath, sympy
Successfully installed mpmath-1.2.1 sympy-1.8

C:\Users\Galal>
```

Example (as General Knowledge):

```
from sympy import *  
  
x = Symbol('x')      # create a "symbol" called x  
  
f = sin(x)**2-4*x  
  
fprime = f.diff(x)    #Calculate Derivative  
  
print(fprime)  
  
ff = lambdify(x, f, 'mpmath')  
  
ffprime= lambdify(x, fprime, 'mpmath')  
  
print(ff(0))  
  
print(ffprime(0))
```