



Introduction to Graph Representation Learning

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Notes



- Before the hands-on: **set up your conda environment!!!**

```
conda create --name torch_pyg python=3.10
conda activate torch_pyg
pip install torch
pip install torchkge
pip install pandas matplotlib numpy pyyaml tqdm
pip install pytorch-ignite
pip install ipykernel
```

- **Make sure you can run a Jupyter Notebook with your new conda environment!**
- **The reports from the hands-on will be evaluated + final exam**



Introduction and Key Concepts

Key Concept: **Systems Biology**



➤ Computational and mathematical analysis and modeling of **complex biological systems**.

- **Complex Systems**

Systems composed of **many components**

These components may **interact with each others**

Properties emerge from these interactions

The whole is greater than the sum of its parts

Key Concept: **Systems Biology**

- Computational and mathematical analysis and modeling of **complex biological systems**.

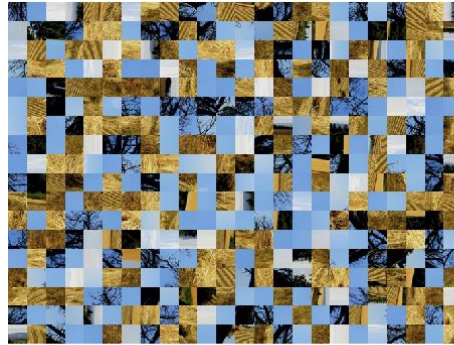
- **Complex Systems**

Systems composed of **many components**

These components may **interact with each others**

Properties emerge from these interactions

The whole is greater than the sum of its parts



(a)



(b)

Source: CatalyzeX. "DNN-Buddies: A Deep Neural Network-Based Estimation Metric for the Jigsaw Puzzle Problem: Paper and Code." CatalyzeX. Accessed September 1, 2023. <https://www.catalyzex.com/>.

Key Concept: **Systems Biology**

➤ Computational and mathematical analysis and modeling of **complex biological systems**.

- **Complex Systems**

Systems composed of **many components**
These components may **interact with each others**
Properties emerge from these interactions

The whole is greater than the sum of its parts

- **Ecological Systems**

Systems components: organisms, ...
Interactions: prey, symbiosis, competition, ...
Emerging properties: resilience, stability, ...

- **Systems Biology**

Systems components: **genes/proteins**, ...
Interactions: **PPI**, **co-expression**, ...
Emerging properties: **Phenotypes**

Phenotype does not emerge from isolated biological molecules but from their interactions

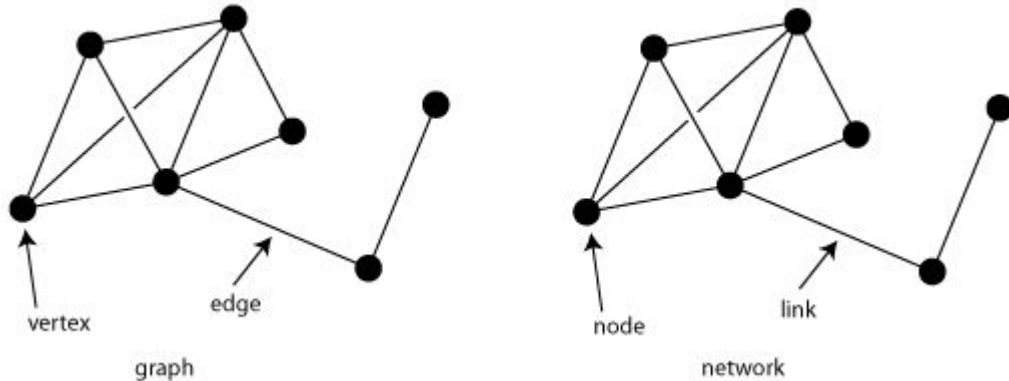
- **Nervous System**

Systems components: neurons, axons, dendrites, ...
Interactions: synaptic transmission, ...
Emerging properties: memory, cognition, ...

Key Concept: **Networks, Graphs and Knowledge Graphs**

- **Networks** are real-world systems modeled using **graphs**.

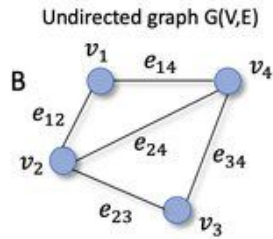
$G = (V, E)$, where V is the set of vertices and $E \subseteq (V \times V)$
is the set of edges



- In practice, the terms **network** and **graph** are often used interchangeably.

Key Concept: **Networks, Graphs and Knowledge Graphs**

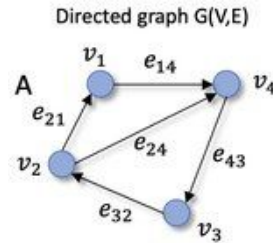
- **Graphs** are defined by an **Adjacency Matrix**
- They can be **undirected**, **directed** and/or **weighted**



F

	v_1	v_2	v_3	v_4
v_1	0	1	0	1
v_2	1	0	1	1
v_3	0	1	0	1
v_4	1	1	1	0

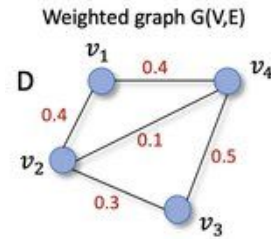
Undirected -> **Symmetric adjacency**



E

	v_1	v_2	v_3	v_4
v_1	0	0	0	1
v_2	1	0	0	1
v_3	0	1	0	0
v_4	0	0	1	0

Directed -> **Asymmetric adjacency**

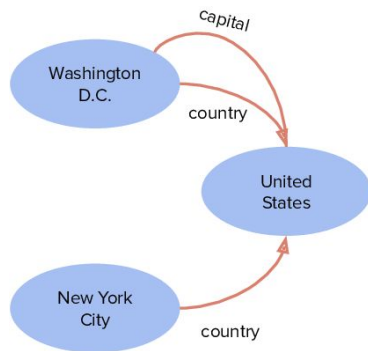


H

	v_1	v_2	v_3	v_4
v_1	0	0.4	0	0.4
v_2	0.4	0	0.3	0.1
v_3	0	0.3	0	0.5
v_4	0.4	0.1	0.5	0

Key Concept: Networks, Graphs and Knowledge Graphs

- **Knowledge Graphs** are structured representations of knowledge in the form of graphs with semantically enriched edges (i.e. relations are typed)



A KG is usually defined as a **set of triplets**:

(head, relation, tail)
or *(h, r, t)*

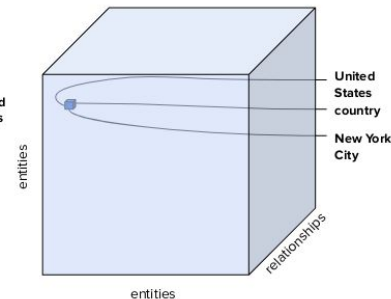
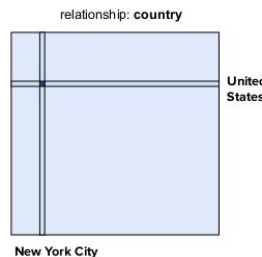
or a **Tensor of adjacency matrices**:

Bianchi, Federico, Gaetano Rossiello, Luca Costabello, Matteo Palmonari, and Pasquale Minervini. "Knowledge Graph Embeddings and Explainable AI," April 30, 2020.
<https://doi.org/10.3233/SSW200011>.

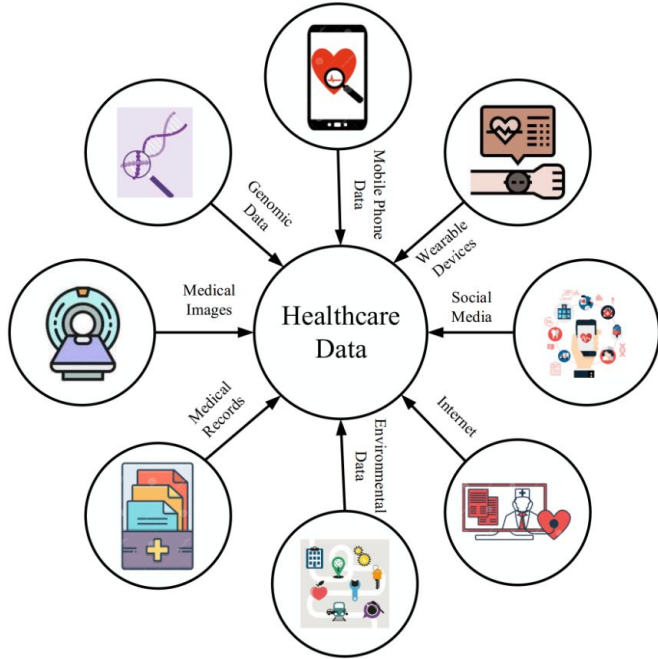
relationship: **country**

0	0	0
0	1	0
0	0	0
0	0	0
0	0	0	0	0

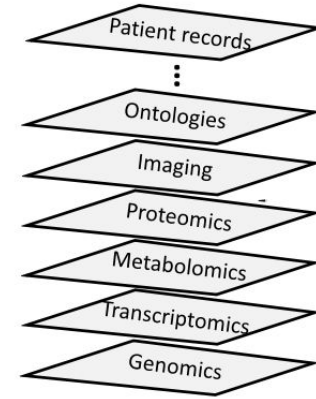
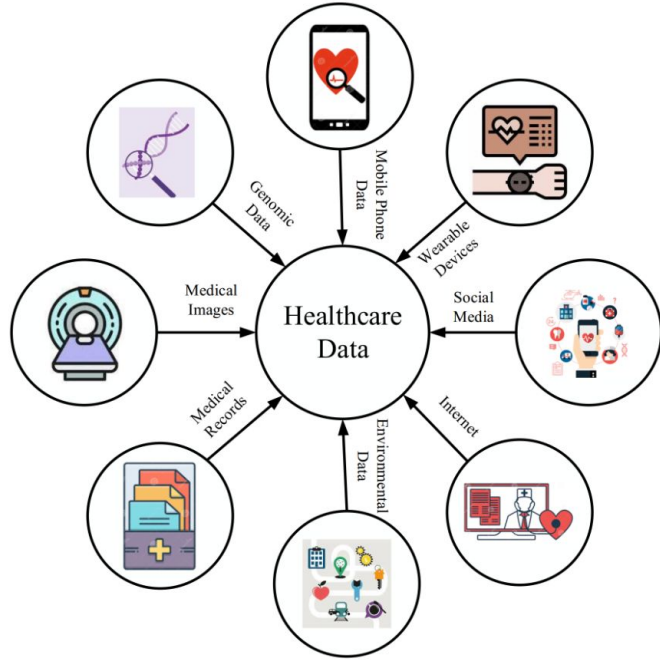
New York City Index



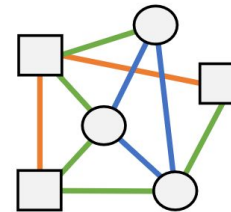
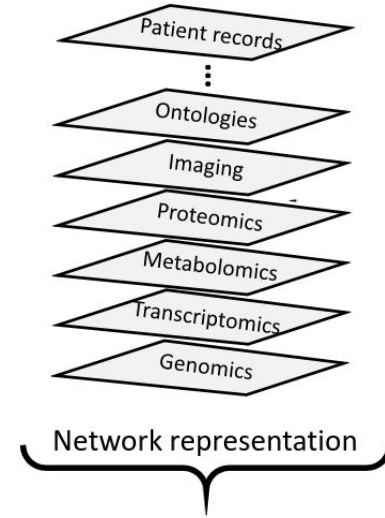
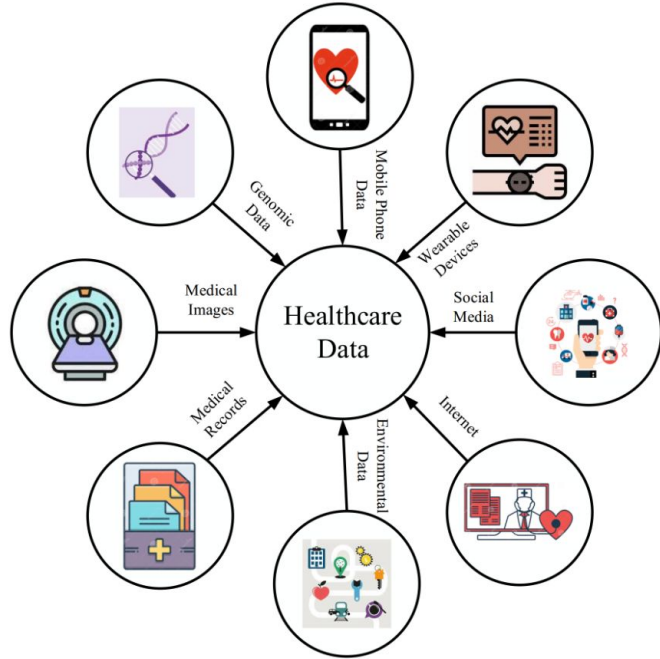
Knowledge Graphs in Biomedicine



Knowledge Graphs in Biomedicine

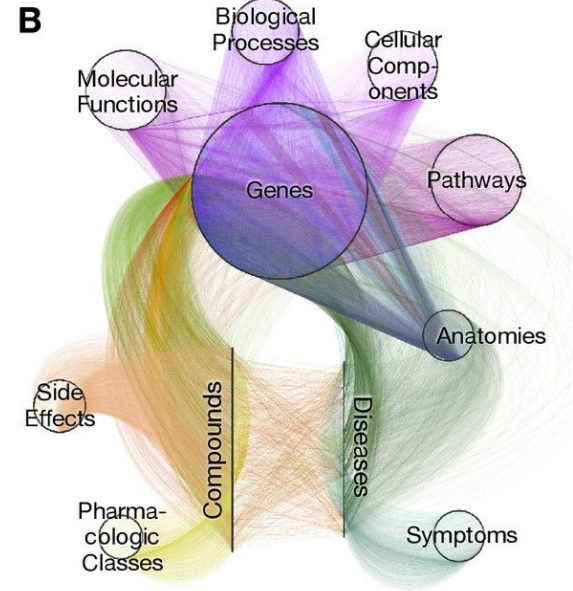
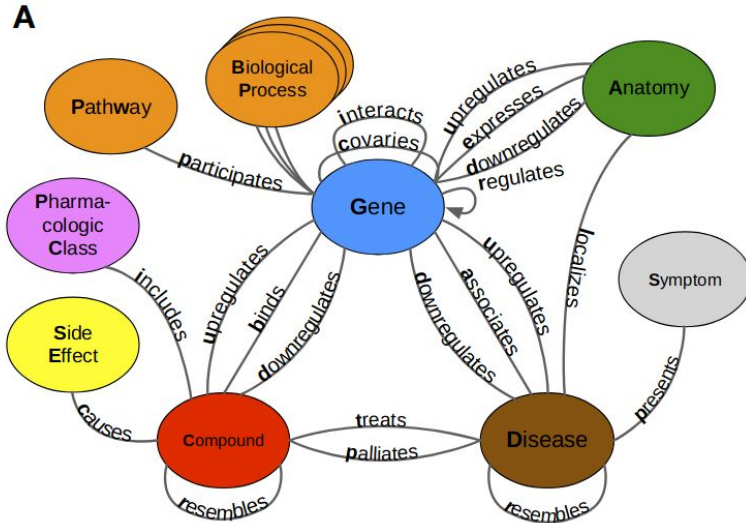


Knowledge Graphs in Biomedicine



Multiple node types (e.g. protein, disease, pathway, etc.)
Multiple edge types (e.g. PPI, regulates, part of, etc.)

Knowledge Graphs in Biomedicine



Himmelstein, Daniel Scott, Antoine Lizee, Christine Hessler, Leo Brueggeman, Sabrina L Chen, Dexter Hadley, Ari Green, Pouya Khankhanian, and Sergio E Baranzini. "Systematic Integration of Biomedical Knowledge Prioritizes Drugs for Repurposing." eLife 6 (September 22, 2017): e26726. <https://doi.org/10.7554/eLife.26726>.

Biomedical KGs: statistics

Node Type	Count	Percent (%)	Data Sources
Biological process	28,642	22.1	CTD, Entrez Gene, Gene Ontology
Protein	27,671	21.4	Bgee, CTD, DisGeNET, DrugBank, Entrez Gene, Human Phenotype Ontology, Human PPI Network, Reactome, UMLS
Disease	17,080	13.2	CTD, DisGeNET, Disease Ontology, Drug Central, Human Phenotype Ontology, Mayo Clinic, MONDO Disease Ontology, Orphanet
Phenotype	15,311	11.8	DisGeNET, Human Phenotype Ontology, SIDER
Anatomy	14,035	10.8	Bgee, UBERON
Molecular function	11,169	8.6	CTD, Entrez Gene, Gene Ontology
Drug	7,957	6.2	DrugBank, Drug Central, SIDER
Cellular component	4,176	3.2	CTD, Entrez Gene, Gene Ontology
Pathway	2,516	1.9	Reactome
Exposure	818	0.6	CTD
Total	129,375	100.0	20 primary data sources

Chandak, P., Huang, K. & Zitnik, M. Building a knowledge graph to enable precision medicine. Sci Data 10, 67 (2023). <https://doi.org/10.1038/s41597-023-01960-3>

Thousands of entities

Millions of relations

KG can be very **complex**, **large** and **dense**, making their exploration difficult

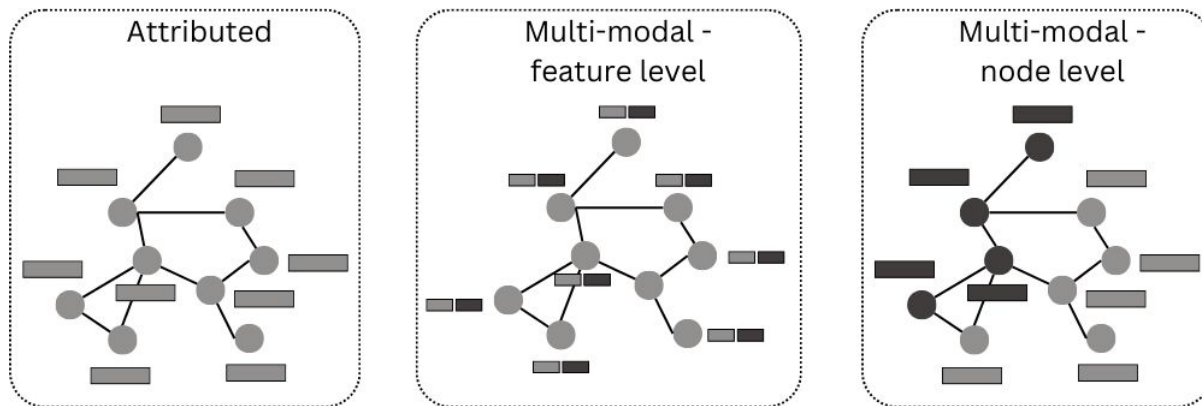
Relation type	Count	Percent (%)
Anatomy - Protein (present)	3,036,406	37.5
Drug - Drug	2,672,628	33.0
Protein - Protein	642,150	7.9
Disease - Phenotype (positive)	300,634	3.7
Biological process - Protein	289,610	3.6
Cellular component - Protein	166,804	2.1
Disease - Protein	160,822	2.0
Molecular function - Protein	139,060	1.7
Drug - Phenotype	129,568	1.6
Biological process - Biological process	105,772	1.3
Pathway - Protein	85,292	1.1
Disease - Disease	64,388	0.8
Drug - Disease (contraindication)	61,350	0.8
Drug - Protein	51,306	0.6
Anatomy - Protein (absent)	39,774	0.5
Phenotype - Phenotype	37,472	0.5
Anatomy - Anatomy	28,064	0.3
Molecular function - Molecular function	27,148	0.3
Drug - Disease (indication)	18,776	0.2
Cellular component - Cellular component	9,690	0.1
Phenotype - Protein	6,660	0.1
Drug - Disease (off-label use)	5,136	0.1
Pathway - Pathway	5,070	0.1
Exposure - Disease	4,608	0.1
Exposure - Exposure	4,140	0.1
Exposure - Biological process	3,250	<0.1
Exposure - Protein	2,424	<0.1
Disease - Phenotype (negative)	2,386	<0.1
Exposure - Molecular function	90	<0.1
Exposure - Cellular component	20	<0.1
Total	8,100,498	100.0

Key concept: Multimodal Knowledge Graphs

Nodes can be **described with multimodal attributes**:

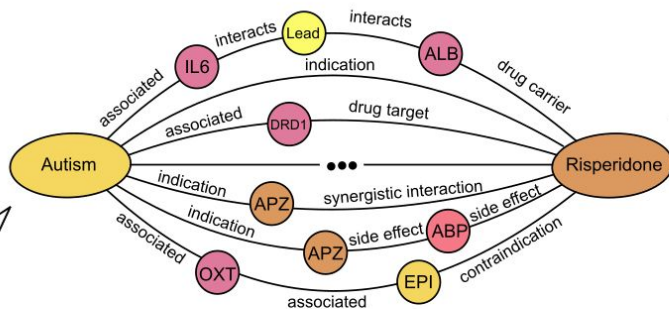
- Descriptive text
- Omics data
- Images
- Sequences
- ...

This multi-modal data can be included in the graph structure:



Key concept: Multimodal Knowledge Graphs

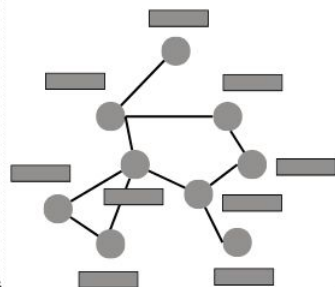
A spectrum of developmental disorders that includes autism, and Asperger syndrome. Signs and symptoms include poor communication skills, defective social interactions, and repetitive behaviors. Each child with autism spectrum disorder is likely to have a unique pattern of behavior [...] Autism spectrum disorder has no single known cause. [...] Autism spectrum disorder affects children of all races and nationalities, but certain factors increase a child's risk [...] There's no way to prevent autism spectrum disorder, but there are treatment options.



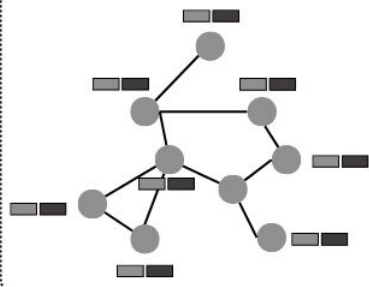
Risperidone is a second-generation antipsychotic (SGA) medication used in the treatment of a number of mood and mental health conditions including schizophrenia and bipolar disorder. The half-life is 3 hours in extensive metabolizers. Though its precise mechanism of action is not fully understood, current focus is on the ability of risperidone to inhibit the D2 dopaminergic receptors and 5-HT_{2A} serotonergic receptors in the brain. [...] Risperidone and its active metabolite, 9-hydroxyrisperidone, are ~88% and ~77% protein-bound in human plasma, respectively. [...] The primary action of risperidone is to decrease dopaminergic and serotonergic pathway activity in the brain, therefore decreasing symptoms of schizophrenia and mood disorders.

Chandak, P., Huang, K. & Zitnik, M. Building a knowledge graph to enable precision medicine. Sci Data 10, 67 (2023). <https://doi.org/10.1038/s41597-023-01960-3>

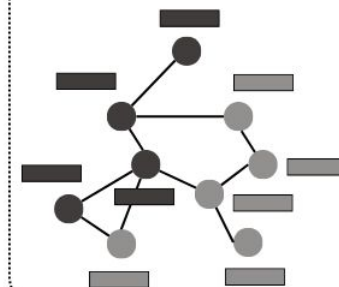
Attributed



Multi-modal - feature level



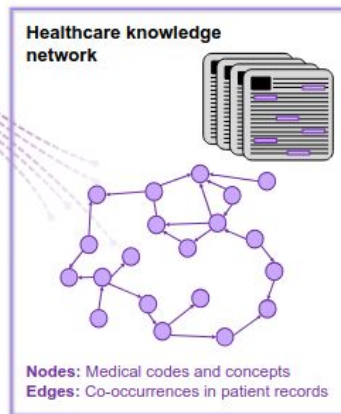
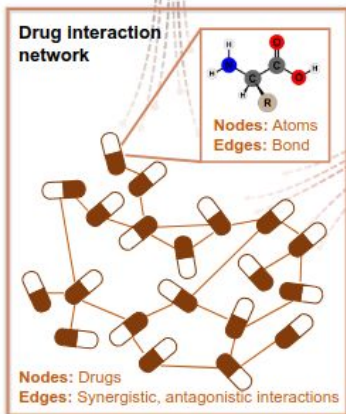
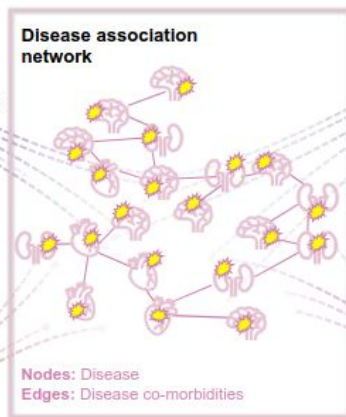
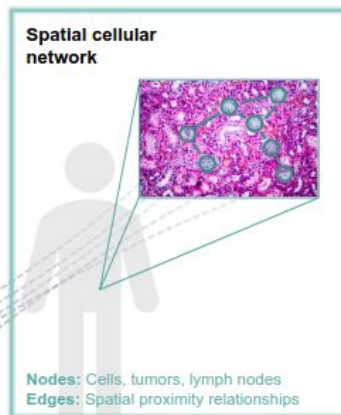
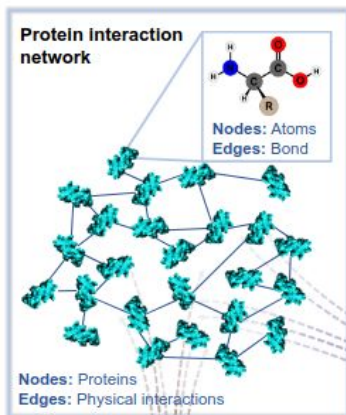
Multi-modal - node level



Key

Nodes

This m



Is associated with

Has phenotype

Is indicated for

Has phenotype

Li, Michelle M., Kexin Huang, and Marinka Zitnik. "Graph representation learning in biomedicine and healthcare." Nature Biomedical Engineering 6.12 (2022): 1353-1369.

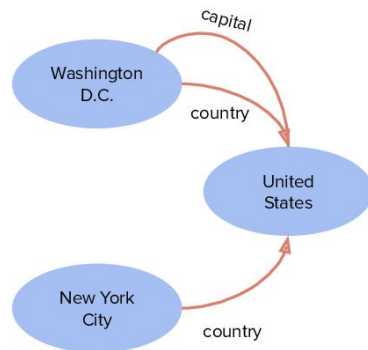


Biological scale

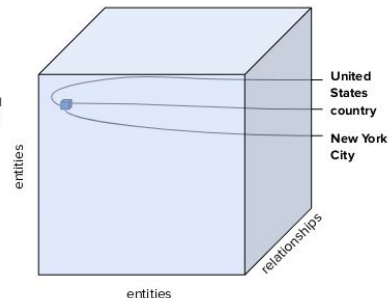
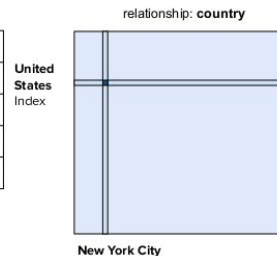


Key Concept 3: Knowledge Graph Embedding

Bianchi, Federico, Gaetano Rossiello, Luca Costabello, Matteo Palmonari, and Pasquale Minervini. "Knowledge Graph Embeddings and Explainable AI," April 30, 2020. <https://doi.org/10.3233/SSW200011>.



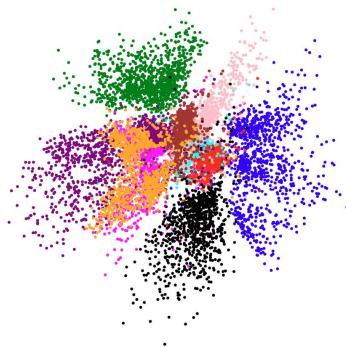
relationship: country					
0	0	0	0
0	1	0	0
0	0	0	0
0	0	0
0	0	0	0	0	0
New York City Index					



High-dimensional node vector representation

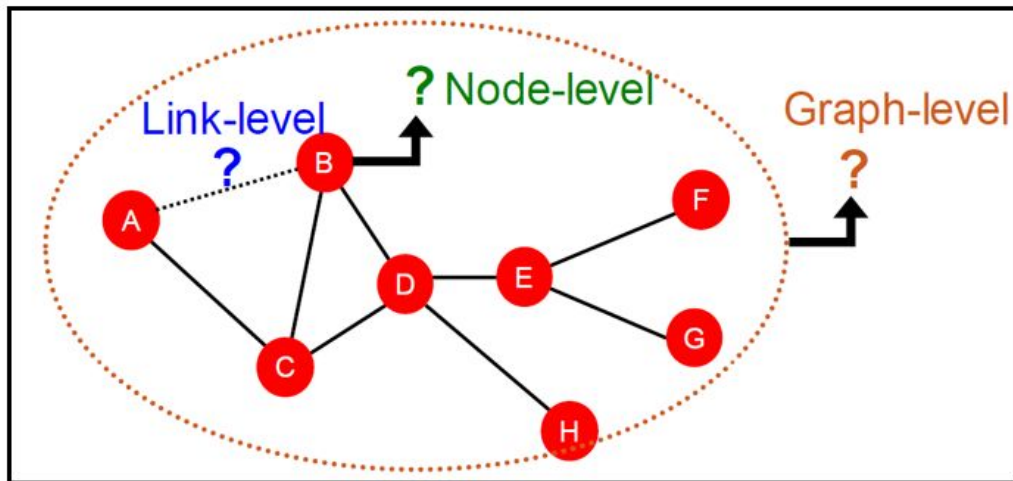
Embedding

Washington D.C.	New York City	United States	country	capital
1	1	5	1	2
2	2	6	2	2
4	5	4	4	5
5	4	4	1	1
6	7	8	4	5
7	7	7	5	5



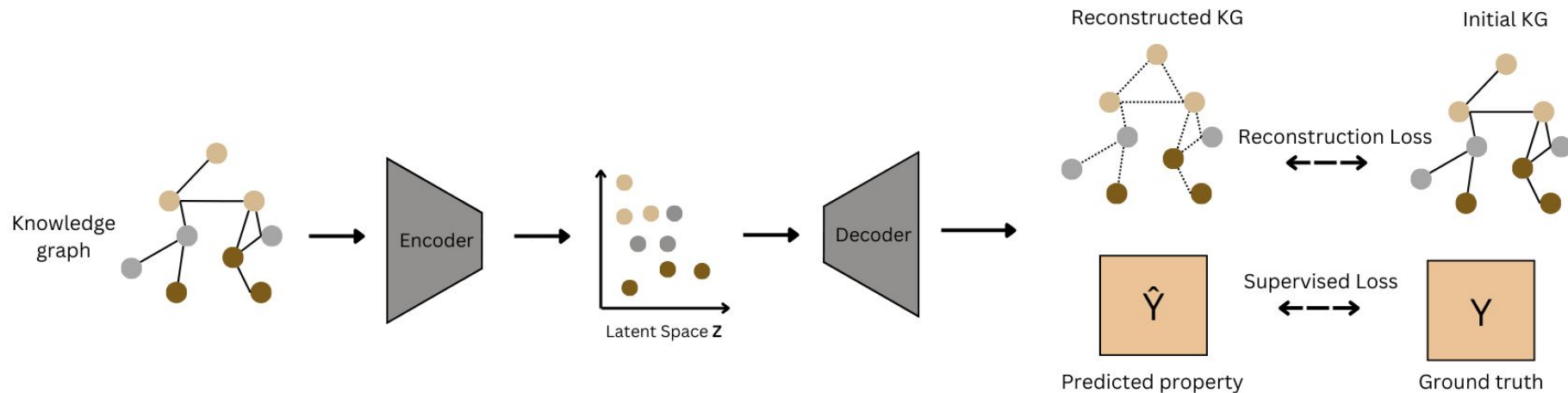
Encoding nodes and relations in a lower-dimensional space

Tasks in Knowledge Graph Embedding

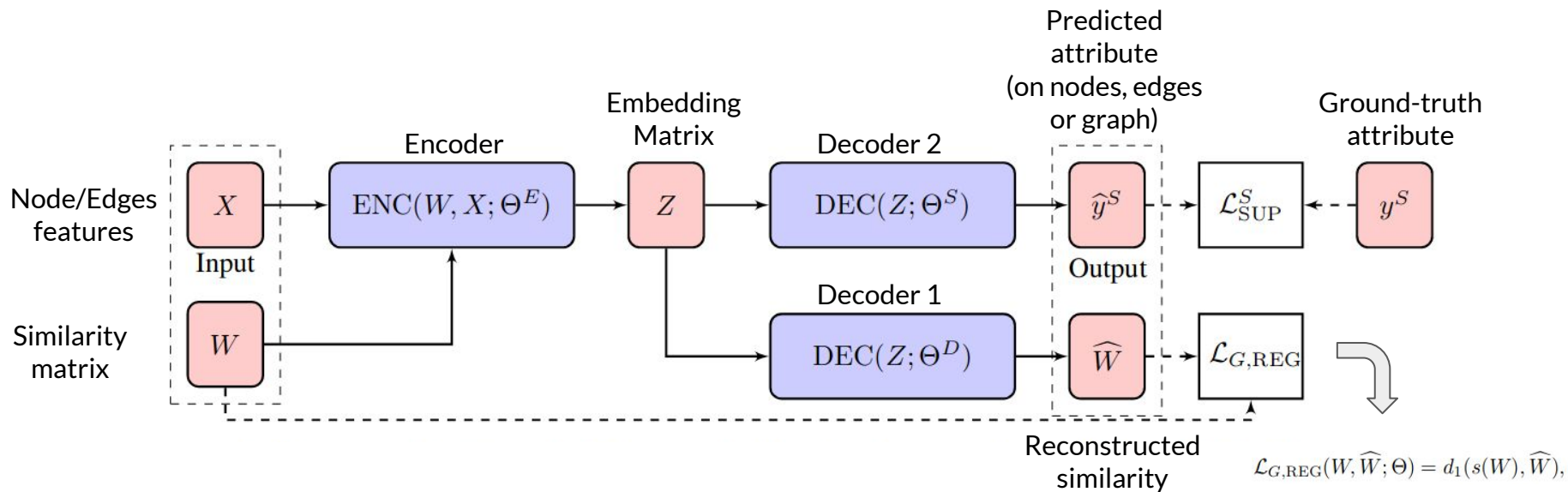


- **Classification**
 - Positive/negative triplet
 - Node properties
 - Graph properties
- **Clustering**
 - Node clustering
 - Graph clustering
 - (Edge clustering)
- **Regression**
 - Node properties
 - Edge weights
 - Graph properties

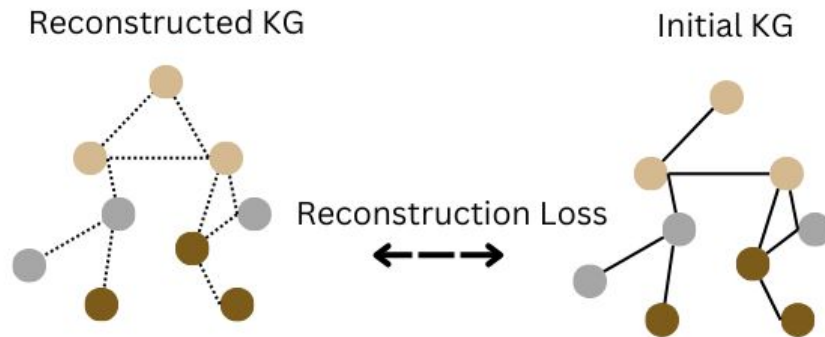
Key Concept: KGE as Auto-Encoder Frameworks



Key Concept: KGE as Auto-Encoder Frameworks



Key concept: **Negative Sampling**

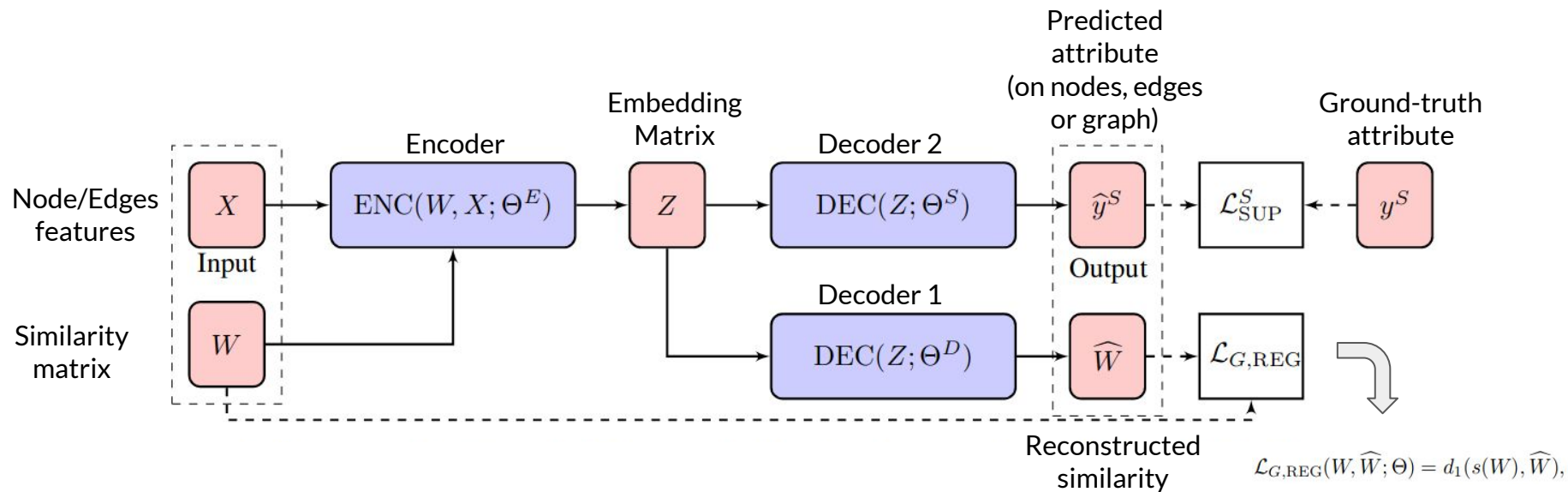


In practice, these models are trained to embed **entities from true triplets closer to each other than those from negative triplets**. These negative triplets are generated by randomly replacing either the head or tail entity for a given triplet: this is called **Negative Sampling**.

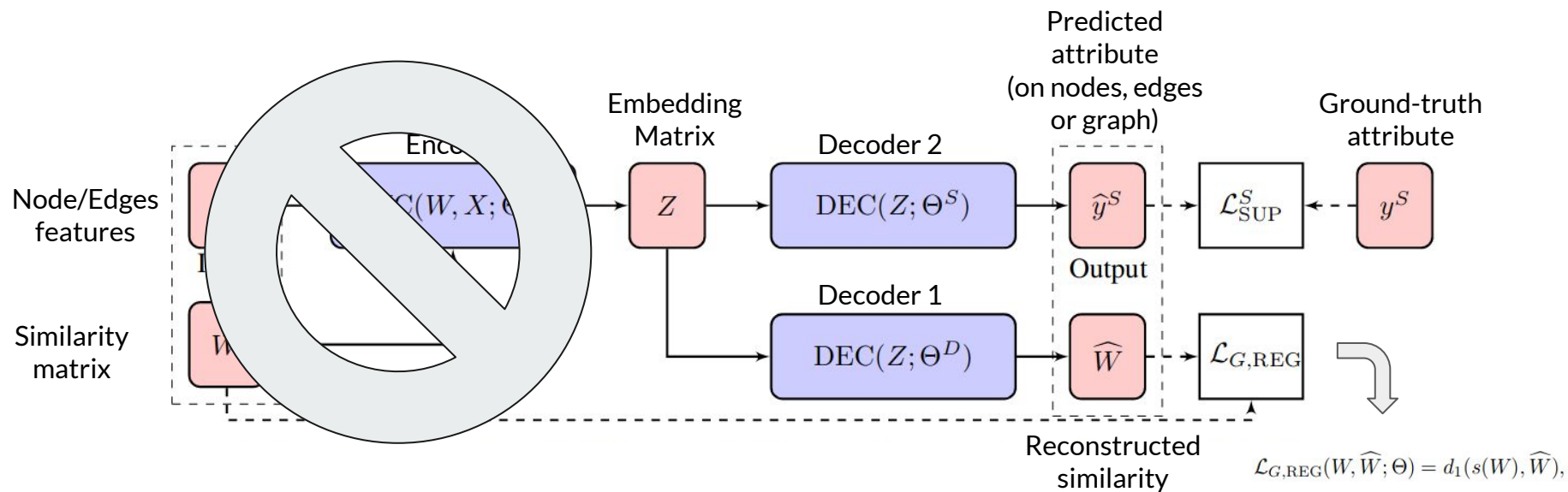


Overview of KG embedding strategies

Shallow VS Deep Embedding

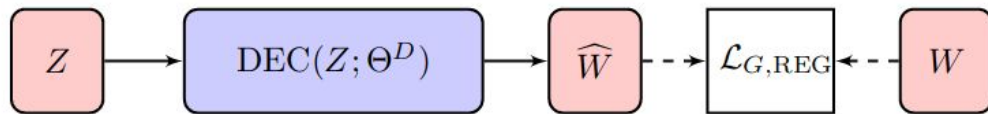


Shallow VS Deep Embedding



Shallow embedding

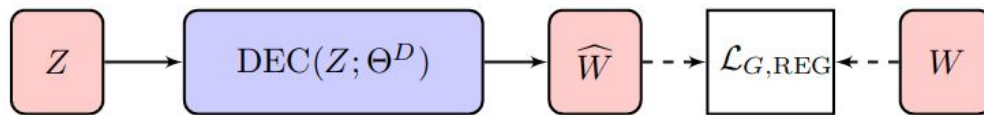
The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

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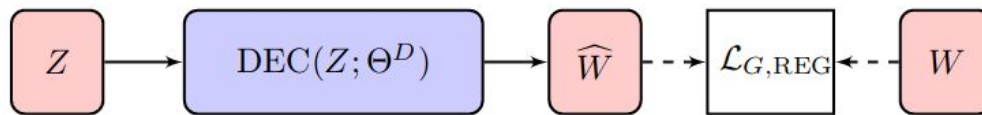
Translational Models

Bilinear Models

Random Walk based Models

Shallow embedding

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Translational Models

Bilinear Models

Random Walk based Models

Shallow Embedding: Translational Models



$$\text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}) = -\|\phi(\mathbf{h}, \mathbf{r}) - \psi(\mathbf{t}, \mathbf{r})\|_p$$

Where:

- $\phi(\mathbf{h}, \mathbf{r})$: Transformation of the head entity embedding \mathbf{h} based on the relation embedding \mathbf{r} .
- $\psi(\mathbf{t}, \mathbf{r})$: Transformation of the tail entity embedding \mathbf{t} based on the relation embedding \mathbf{r} .
- $\|\cdot\|_p$: Norm (e.g., $p = 1$ for L_1 -norm or $p = 2$ for L_2 -norm).

Shallow Embedding: Translational Models

Margin-based loss

$$\text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}) = -\|\phi(\mathbf{h}, \mathbf{r}) - \psi(\mathbf{t}, \mathbf{r})\|_p$$

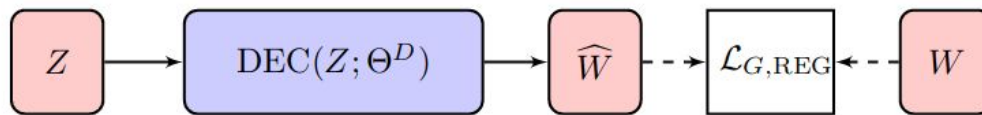
$$\mathcal{L} = \sum_{(h,r,t) \in \mathcal{T}_{\text{train}}} \sum_{(h',r,t') \in \mathcal{T}_{\text{neg}}} \max(0, \gamma + \text{Score}(\mathbf{h}', \mathbf{r}, \mathbf{t}') - \text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}))$$

- $\mathcal{T}_{\text{train}}$: Set of positive triples (ground truth).
- \mathcal{T}_{neg} : Set of negative triples generated via corruption (e.g., replacing h or t).
- γ : Margin hyperparameter.
- **Goal**: Separate scores of positive and negative triples by at least γ :

$$\text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}) > \text{Score}(\mathbf{h}', \mathbf{r}, \mathbf{t}') + \gamma$$

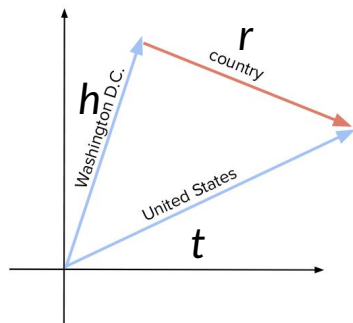
Shallow embedding: **Translational Models**

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TransE



$$\mathbf{h} + \mathbf{r} \approx \mathbf{t} \quad \text{if } (h, r, t) \text{ holds}$$

$$\mathcal{L} = \sum_{h, r, t \in S} \sum_{h', r', t' \in S'_{h, r, t}} [\gamma + d(\mathbf{h} + \mathbf{r}, \mathbf{t}) - d(\mathbf{h}' + \mathbf{r}', \mathbf{t}')]_+,$$

Advantages:

- Inverse relationships
- Antisymmetric relationships
- Compositions

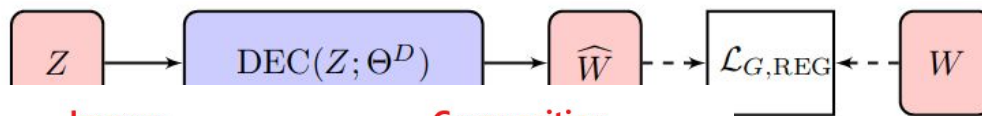
Limitations:

- One-to-many/many-to-many relationships
- Symmetric relationships
- Hierarchical relationships

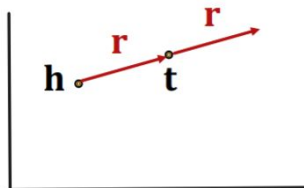
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Shallow embedding: **Translational Models**

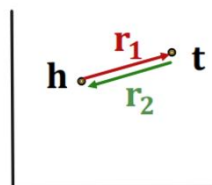
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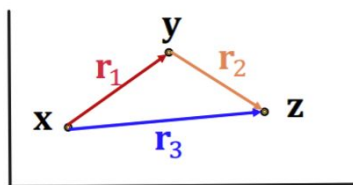
AntiSymmetric



Inverse



Composition



Machine Learning on Graphs: A
2005.03675.

TransE

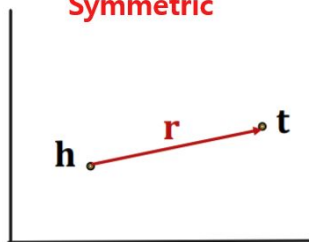
Advantages:

- Inverse relationships
- Antisymmetric relationships
- Compositions

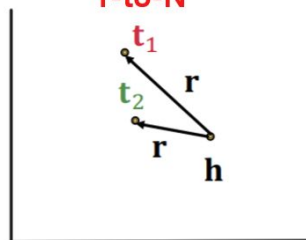
Limitations:

- One-to-many/many-to-many relationships
- Symmetric relationships
- Hierarchical relationships

Symmetric



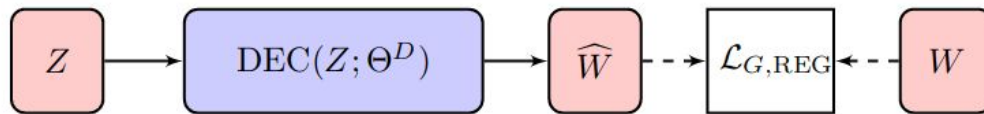
1-to-N



Lee S. AAA (All About AI) 2021. (CS224W)
10. Knowledge Graph Embeddings. Available
from: <https://seunghan96.github.io/gnn/gnn10/>

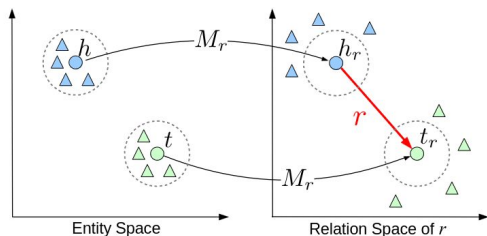
Shallow embedding: **Translational Models**

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

TransR



$$\mathbf{h}_r + \mathbf{r} \approx \mathbf{t}_r \text{ if } (h, r, t) \text{ holds}$$

$$\mathbf{h}_r = \mathbf{h} * \mathbf{M}_r \text{ with } \mathbf{M}_r \text{ the projection matrix for relation } r$$

$$\mathbf{t}_r = \mathbf{t} * \mathbf{M}_r$$

Advantages:

- Inverse relationships
- Antisymmetric relationships
- One-to-many/many-to-many relationships
- Symmetric relationships

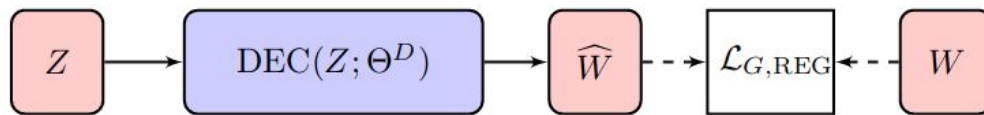
Limitations:

- Compositions

Lin, Yankai, Zhiyuan Liu, Maosong Sun, Yang Liu, and Xuan Zhu. "Learning Entity and Relation Embeddings for Knowledge Graph Completion." Proceedings of the AAAI Conference on Artificial Intelligence 29, no. 1 (February 19, 2015). <https://doi.org/10.1609/aaai.v29i1.9491>.

Shallow embedding

The graph structure (W) is only used in the loss function.




Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

Translational Models

Bilinear Models

Random Walk based Models

Shallow Embedding: Bilinear Models



$$\text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}) = \mathbf{h}^\top \mathbf{M}_r \mathbf{t}$$

Where:

- \mathbf{h} : Embedding of the head entity.
- \mathbf{t} : Embedding of the tail entity.
- \mathbf{M}_r : Relation-specific transformation matrix that captures how the head and tail interact for the relation \mathbf{r} .

Shallow Embedding: Bilinear Models

Binary-cross Entropy Loss

$$\text{Score}(\mathbf{h}, \mathbf{r}, \mathbf{t}) = \mathbf{h}^\top \mathbf{M}_r \mathbf{t}$$

$$\mathcal{L} = - \sum_{(h,r,t)} [y \cdot \log(\text{Score}(h, r, t)) + (1 - y) \cdot \log(1 - \text{Score}(h, r, t))]$$

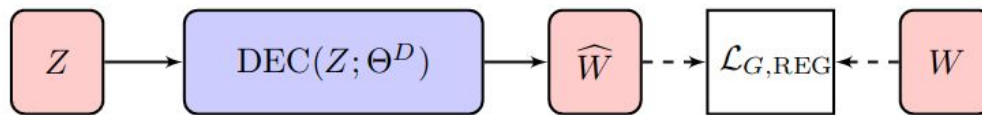
Where:

- $y = 1$ for positive triples, $y = 0$ for negative triples.

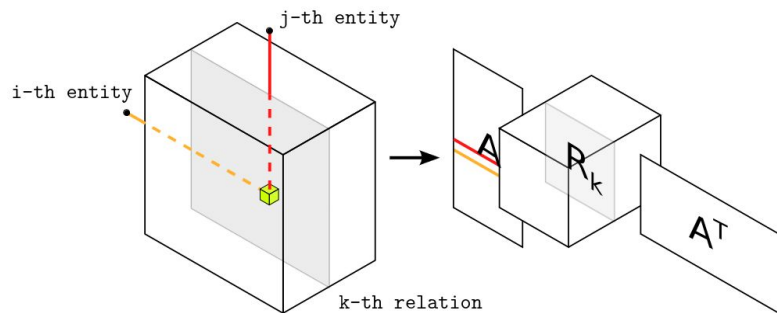
Goal: Maximize the likelihood of assigning higher probabilities to positive triples.

Shallow embedding: **Bilinear Models**

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.



RESCAL

Advantages:

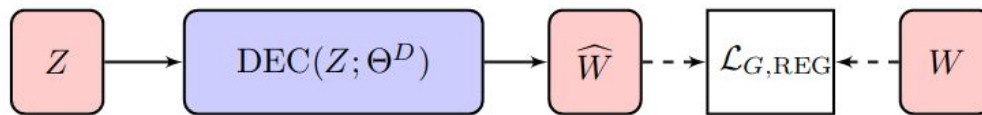
- Fully expressive
- Collective learning

Limitations:

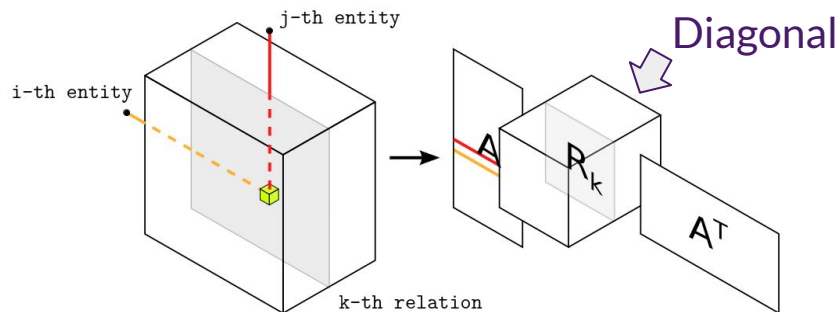
- Computationally intensive
- Prone to overfitting

Shallow embedding: **Bilinear Models**

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.



DistMult

Advantages:

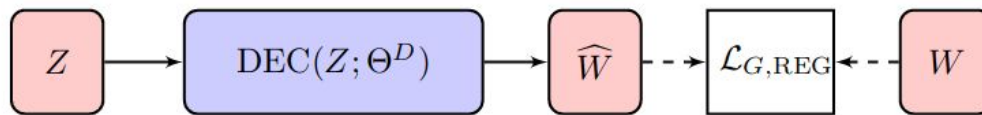
→ Collective learning

Limitations:

→ Cannot differentiate between head and tail (all relations are modeled as symmetric)

Shallow embedding

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

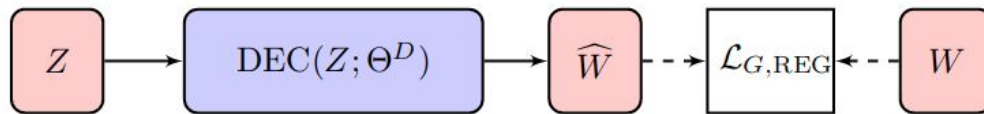
Translational Models

Bilinear Models

Random Walk based Models

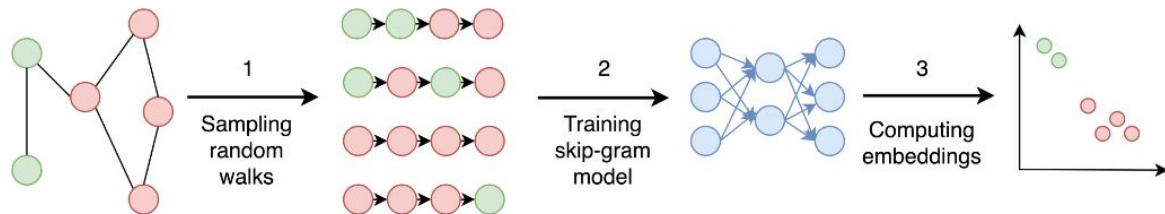
Shallow embedding: Random Walk-based Models

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

NLP model: Skip-gram maximizes the co-occurrence probability among the words that appear within a window in a sentence



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

DeepWalk, node2vec, ...

Advantages:

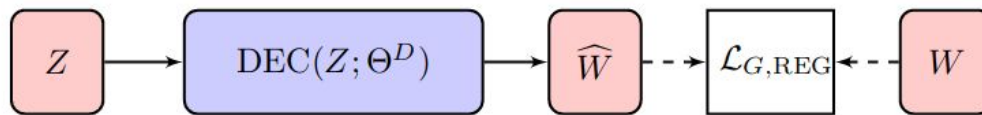
- Higher-order similarities
- Capture neighborhood similarities and community membership
- Many walking strategy

Limitations:

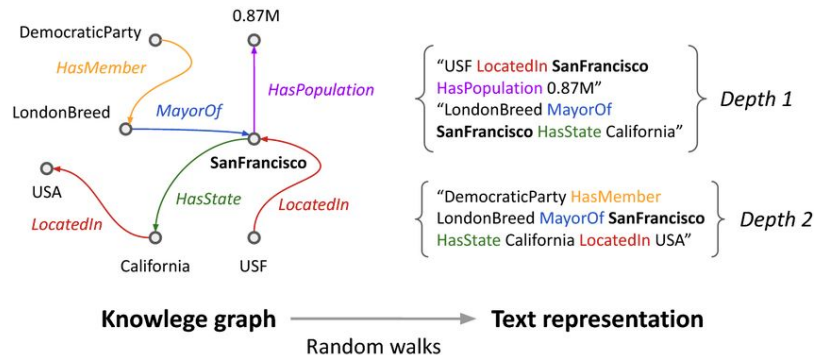
- For networks (do not consider relationship types)

Shallow embedding: **Random Walk-based Models**

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.



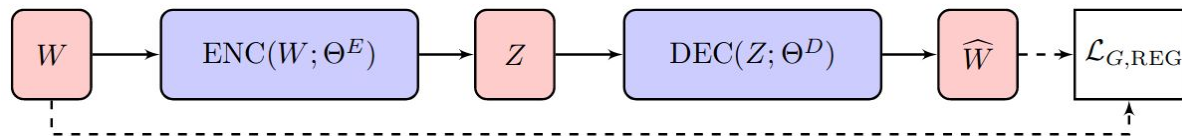
RDF2vec

Advantages:

- Higher-order similarities
- Capture neighborhood similarities and community membership

Deep embedding

The graph structure (W) is only used in the encoder and in the loss function.

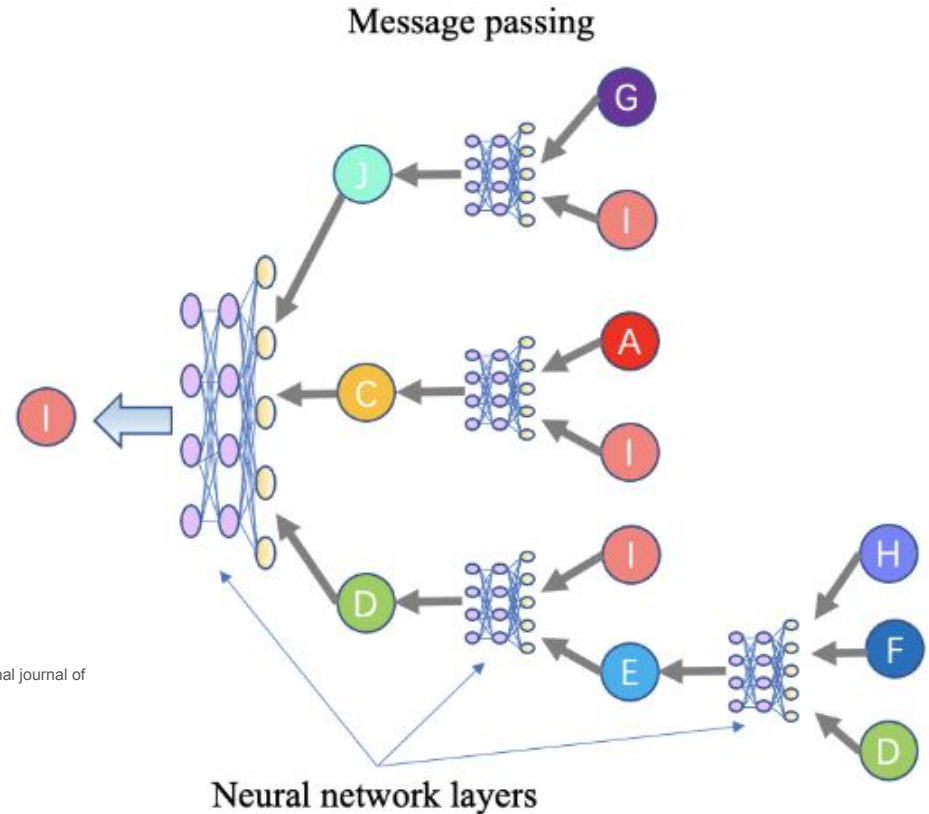
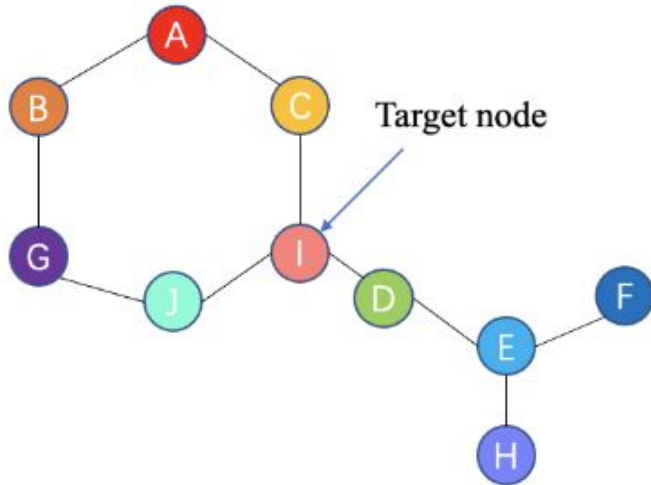


Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

Graph Neural Networks

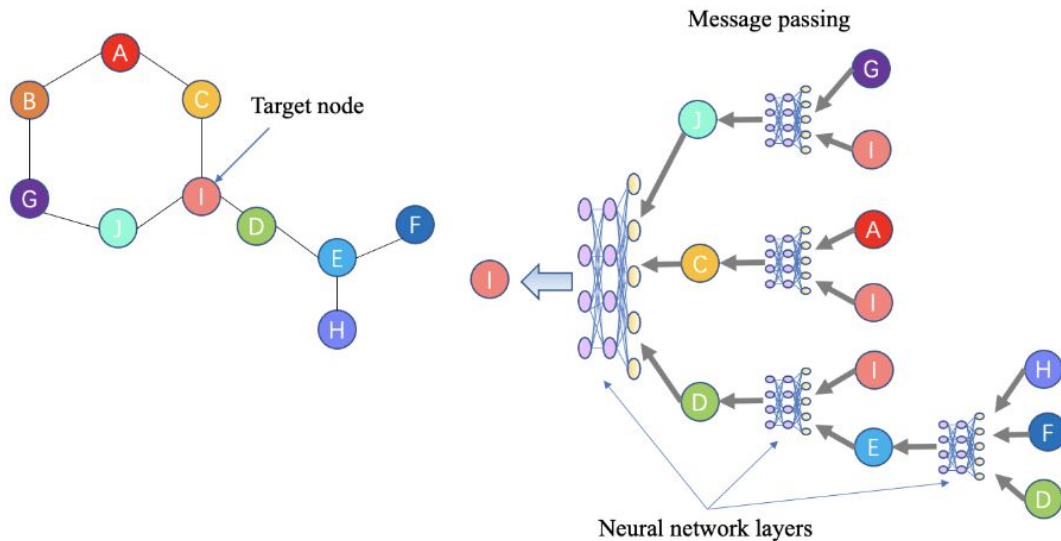
Graph Transformers

Deep embedding: the concept of **Message Passing**



Zhang, Yue, et al. "Application of computational biology and artificial intelligence in drug design." International journal of molecular sciences 23.21 (2022): 13568.

Deep embedding: the concept of **Message Passing**



Initialisation

- Random
- Shallow embeddings
- Node features

Aggregation

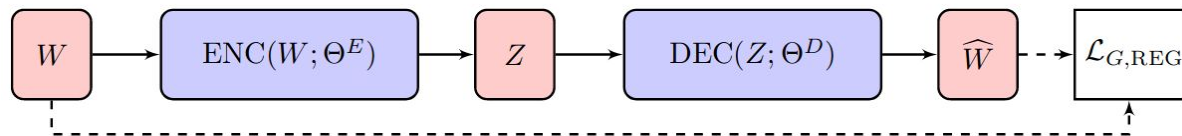
$$m_v^i = A \left(\{s_u^i\}_{u \in \mathcal{N}(v)} \right),$$

Update

$$s_v^{i+1} = U \left(s_v^i, m_v^i \right),$$

Deep embedding

The graph structure (W) is only used in the encoder and in the loss function.



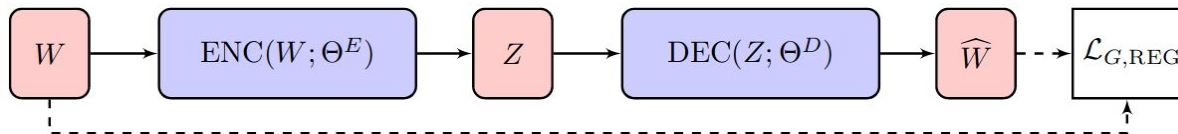
Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

Graph Neural Networks

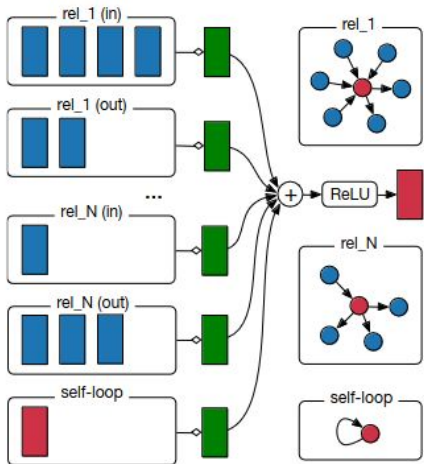
Graph Transformers

Deep embedding: Graph Neural Networks

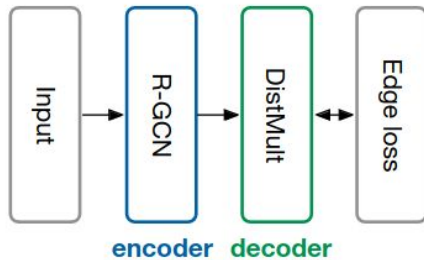
The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.



$$h_i^{(l+1)} = \sigma \left(\sum_{r \in \mathcal{R}} \sum_{j \in \mathcal{N}_i^r} \frac{1}{c_{i,r}} W_r^{(l)} h_j^{(l)} + W_0^{(l)} h_i^{(l)} \right)$$



R-GCN

Advantages:

- Expressive for local and global relationships
- Inductive

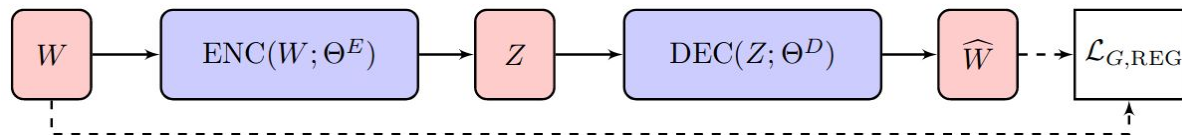
Limitations:

- All neighbors for relation type r have the same importance when updating a node embedding

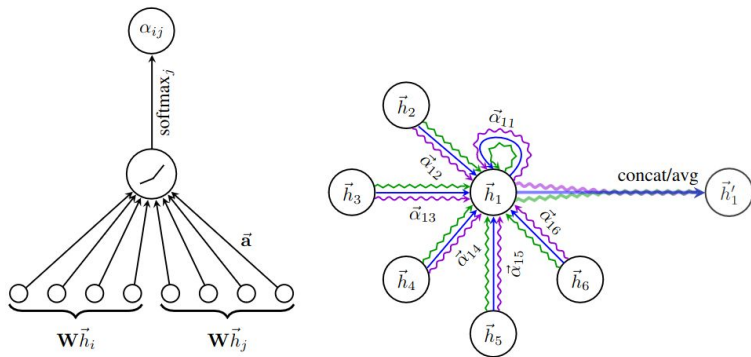
Schlichtkrull, Michael, Thomas N. Kipf, Peter Bloem, Rianne van den Berg, Ivan Titov, and Max Welling. "Modeling Relational Data with Graph Convolutional Networks." arXiv, October 26, 2017. <http://arxiv.org/abs/1703.06103>.

Deep embedding: **Graph Attention Networks**

The graph structure (W) is only used in the loss function.



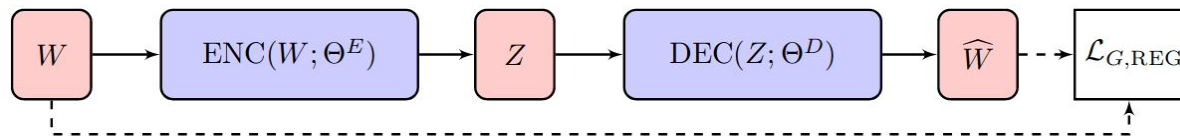
Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.



Veličković, Petar, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Liò, and Yoshua Bengio. "Graph Attention Networks." arXiv, February 4, 2018. <http://arxiv.org/abs/1710.10903>.

Deep embedding: Graph Attention Networks

The graph structure (W) is only used in the loss function.



Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

r-GAT

$$\text{att}_{viu}^k = f^k [e_v^k || r_i^k || e_u^k]$$

Contribution of neighbor u to update node v embedding (for rel i and channel k)

$$e_v^{(l)} = \bigg\|_{k=1}^K \sigma_1 \left(\sum_{u \in \mathcal{N}_v} \sum_{i \in \mathcal{R}_{vu}} \alpha_{viu}^k [e_u^k * r_i^k] \right)$$

Update considers all channels K and all neighbors for every relation

Chen, Meiqi, Yuan Zhang, Xiaoyu Kou, Yuntao Li, and Yan Zhang. "R-GAT: Relational Graph Attention Network for Multi-Relational Graphs." arXiv, September 13, 2021. <http://arxiv.org/abs/2109.05922>.

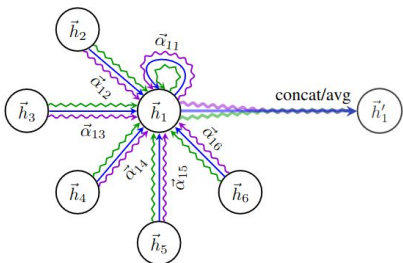
Advantages:

- Expressive for local and global relationships
- Assign a similar embedding to node i and to its more similar or important neighbors
- Inductive

Limitations:

- Computationally intensive

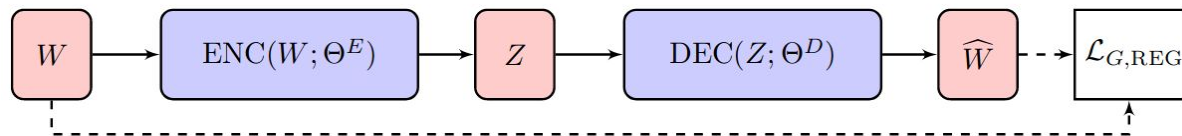
Brody, Shaked, Uri Alon, and Eran Yahav. "How Attentive Are Graph Attention Networks?," 2021. <https://openreview.net/forum?id=F72ximsx7C1>.



Veličković, Petar, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Liò, and Yoshua Bengio. "Graph Attention Networks." arXiv, February 4, 2018. <http://arxiv.org/abs/1710.10903>.

Deep embedding

The graph structure (W) is only used in the encoder and in the loss function.



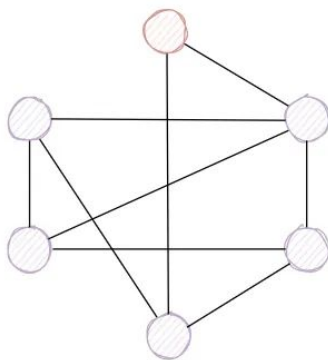
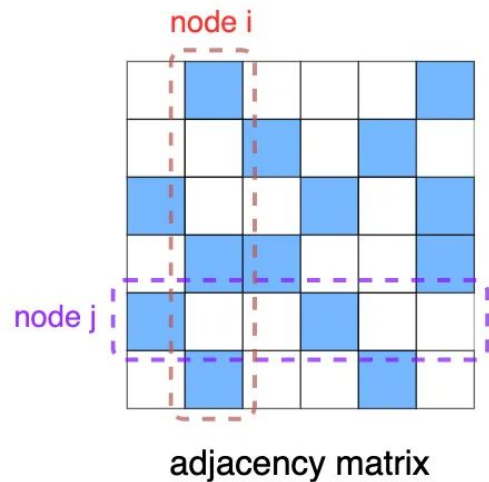
Chami, Ines, Sami Abu-El-Hajja, Bryan Perozzi, Christopher Ré, and Kevin Murphy. "Machine Learning on Graphs: A Model and Comprehensive Taxonomy." arXiv, April 11, 2022. <http://arxiv.org/abs/2005.03675>.

Graph Neural Networks

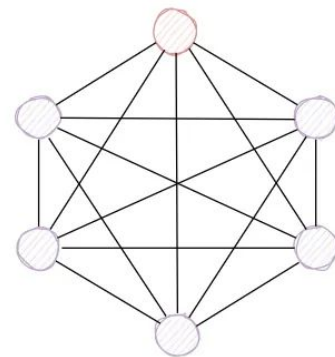
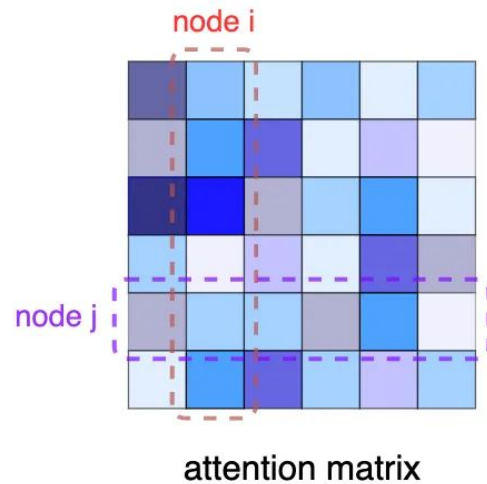
Graph Transformers

Deep embedding: **Graph Transformers**

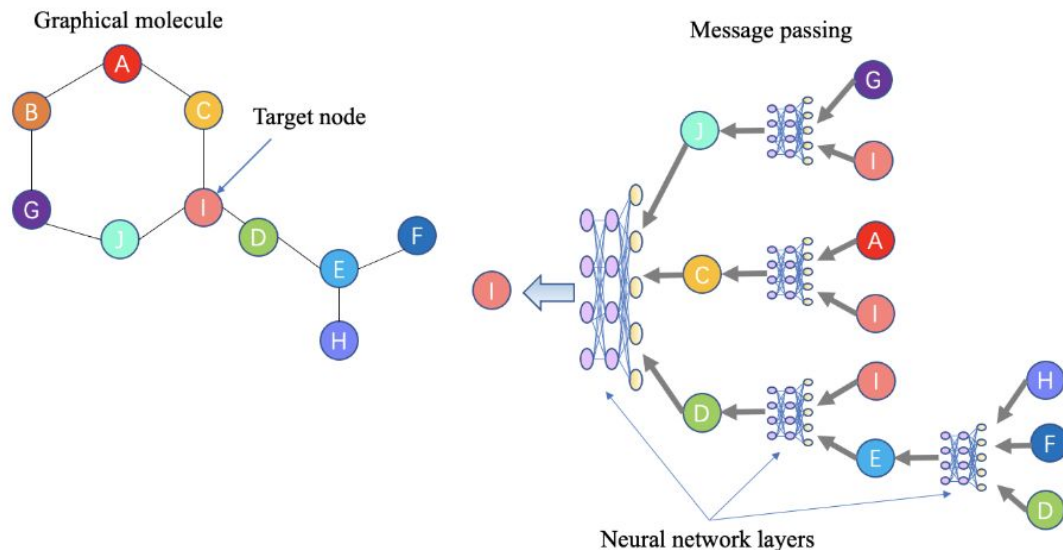
Graph Neural Networks



Transformers



Deep embedding: **Using node features**



Zhang, Yue, et al. "Application of computational biology and artificial intelligence in drug design." International journal of molecular sciences 23.21 (2022): 13568.

Initialisation

- Random
- Shallow embeddings
- **Node features**

Aggregation

$$m_v^i = A \left(\{s_u^i\}_{u \in \mathcal{N}(v)} \right),$$

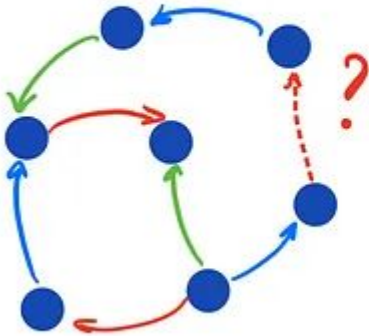
Update

$$s_v^{i+1} = U \left(s_v^i, m_v^i \right),$$

Key concept: Inductive and Transductive learning

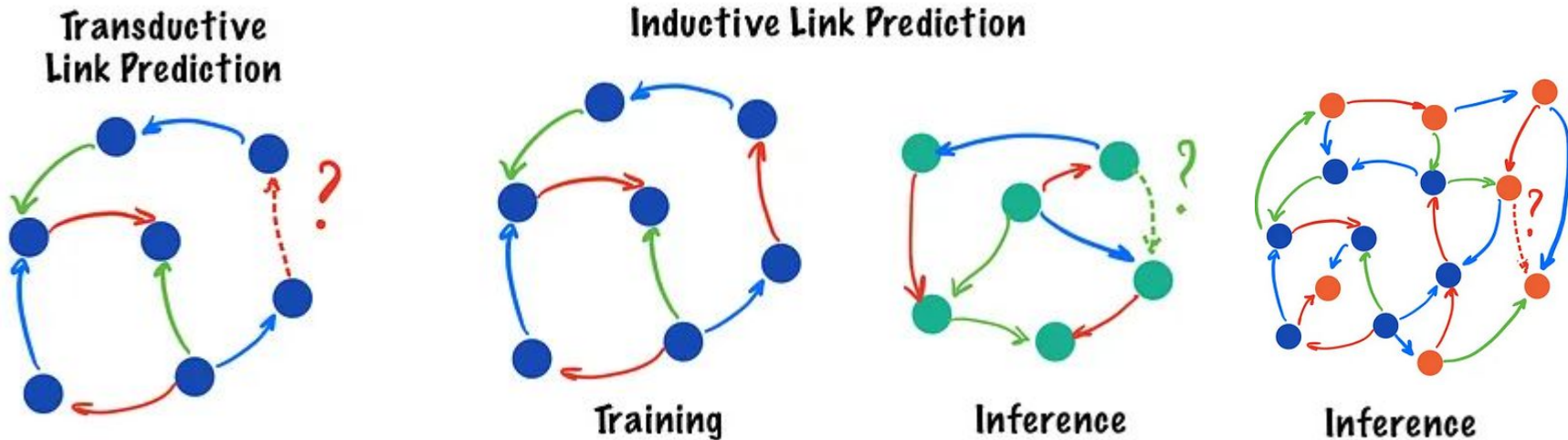
Galkin M. Medium. 2022 [cited 2024 Nov 22]. Inductive Link Prediction in Knowledge Graphs. Available from:
<https://towardsdatascience.com/inductive-link-prediction-in-knowledge-graphs-23f249c31961>

Transductive Link Prediction



Key concept: Inductive and Transductive learning

Galkin M. Medium. 2022 [cited 2024 Nov 22]. Inductive Link Prediction in Knowledge Graphs. Available from:
<https://towardsdatascience.com/inductive-link-prediction-in-knowledge-graphs-23f249c31961>



- Transductive models learn node-specific representations for known nodes.
- Inductive models learn generalizable functions based on node features and their context.



Training a KG embedding model

Available tools for KG embedding



PyTorch:
Training



TorchKGE:
Shallow embedding



PyG

Pytorch Geometric:
Graph Neural Networks

Framework	Model Name	Model Type	Implementation
Decoders	TransE	Translational	TorchKGE
	TransH		
	TransR		
	TransD		
	TorusE		
	RESCAL	Bilinear	
	DistMult		
	HoIE		
	Complex		
	ANALOGY		
ConvKB	Convolutional		
Encoders	RGCNConv	Deep	PyTorch Geometric
	RGATConv		

KGE workflow for link prediction



- **Splitting the graph triplets** into train, validation, and test sets.

KGE workflow for link prediction

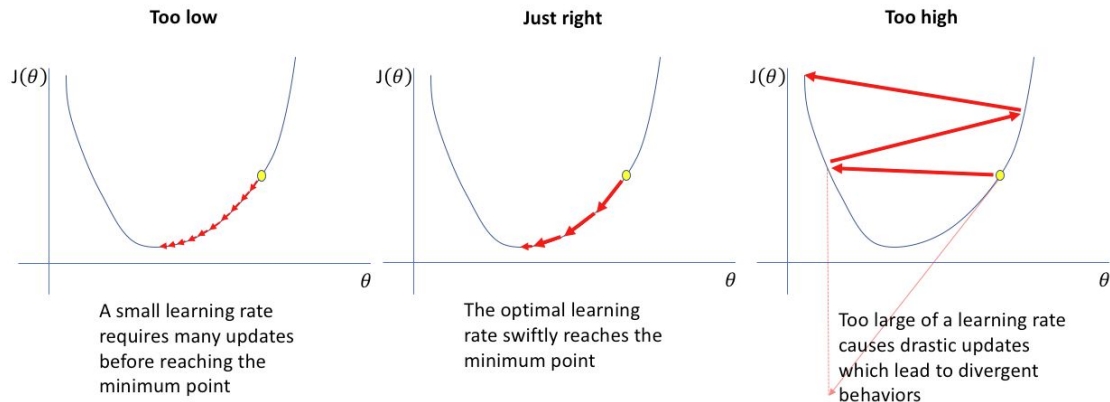


- **Splitting the graph triplets** into train, validation, and test sets.
- **Defining the model:**
 - Choose the model type (TransE, RESCAL, ...)
 - Specify the loss function (e.g., margin ranking loss, binary-cross-entropy loss, ...).
 - Select the optimizer (e.g., Adam, SGD, ..).

KGE workflow for link prediction

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 - Select the optimizer (e.g., Adam, SGD, ..).
- **Defining the hyperparameters:**
 - Set the embedding dimension.
 - Determine the number of epochs.
 - Specify additional hyperparameters (e.g., learning rate, regularization terms).

Jeremy Jordan [Internet]. 2018 [cited 2024 Nov 22].
Setting the learning rate of your neural
network. Available from:
<https://www.jeremyjordan.me/nn-learning-rate/>



KGE workflow for link prediction



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- **Defining the negative sampling strategy:**
 - Choose how to generate negative samples

KGE workflow for link prediction



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- **Defining the negative sampling strategy:**
 - Choose how to generate negative samples
- **Defining a quality metric** for evaluating the model on the validation set (e.g., MRR, Hits@K).

KGE workflow for link prediction

Known Facts in the KG:

Paris, city_of, France
Marseille, city_of, France
New York, city_of, USA
Washington, city_of, USA

Élysée, located_in, Paris
White House, located_in, Washington
Broadway, located_in, New York
Eiffel Tower, located_in, Paris
Bonne Mère, located_in, Marseille

Élysée, is_a, Government Building
White House, is_a, Government Building
Broadway, is_a, Cultural Landmark
Eiffel Tower, is_a, Cultural Landmark
Bonne Mère, is_a, Cultural Landmark

Washington, capital_of, USA

Embeddings

Paris
Marseille
New York
Washington
France
USA
Élysée
White House
Broadway
Eiffel Tower
Bonne Mère
Government Building
Cultural Landmark
city_of
located_in
is_a
capital_of



Link Prediction: finding the capital of France

Computing a score for each possible head
(?, capital_of, France)

$s(\text{Paris, capital_of, France}) = 0.9$
 $s(\text{Marseille, capital_of, France}) = 0.7$
 $s(\text{Washington, capital_of, France}) = 0.6$
 $s(\text{New York, capital_of, France}) = 0.5$
 $s(\text{Élysée, capital_of, France}) = 0.4$
 $s(\text{White House, capital_of, France}) = 0.2$
 $s(\text{USA, capital_of, France}) = 0.2$
etc...

with $s(h, r, t)$, a model-dependant scoring function

KGE workflow for link prediction

Known Facts in the KG:

Paris, city_of, France
Marseille, city_of, France
New York, city_of, USA
Washington, city_of, USA

Élysée, located_in, Paris
White House, located_in, Washington
Broadway, located_in, New York
Eiffel Tower, located_in, Paris
Bonne Mère, located_in, Paris

Élysée, is_a, Government Building
White House, is_a, Government Building
Broadway, is_a, Road
Eiffel Tower, is_a, Tower
Bonne Mère, is_a, Cultural Landmark

Washington, capital_of, USA

Embeddings

Paris
Marseille
New York
Washington



Link Prediction: finding the capital of France

Computing a score for each possible head
(?, capital_of, France)

Link Prediction tasks evaluated with metric

Mean Reciprocal Rank

$$\text{MRR} = \frac{1}{N} \sum_{i=1}^N \frac{1}{\text{rank}_i}$$

= 0.9
(France) = 0.7
(France) = 0.6
(France) = 0.5
) = 0.4
(France) = 0.2
= 0.2

ndant scoring function

KGE workflow for link prediction

- **Splitting the graph triplets** into train, validation, and test sets.
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 - Select the optimizer (e.g., Adam, SGD, ..).
- **Defining the hyperparameters:**
 - Set the embedding dimension.
 - Determine the number of epochs.
 - Specify additional hyperparameters (e.g., learning rate, regularization terms).
- **Defining the negative sampling strategy:**
 - Choose how to generate negative samples
- **Defining a quality metric** for evaluating the model on the validation set (e.g., MRR, Hits@K).

$$\text{MRR} = \frac{1}{N} \sum_{i=1}^N \frac{1}{\text{rank}_i}$$

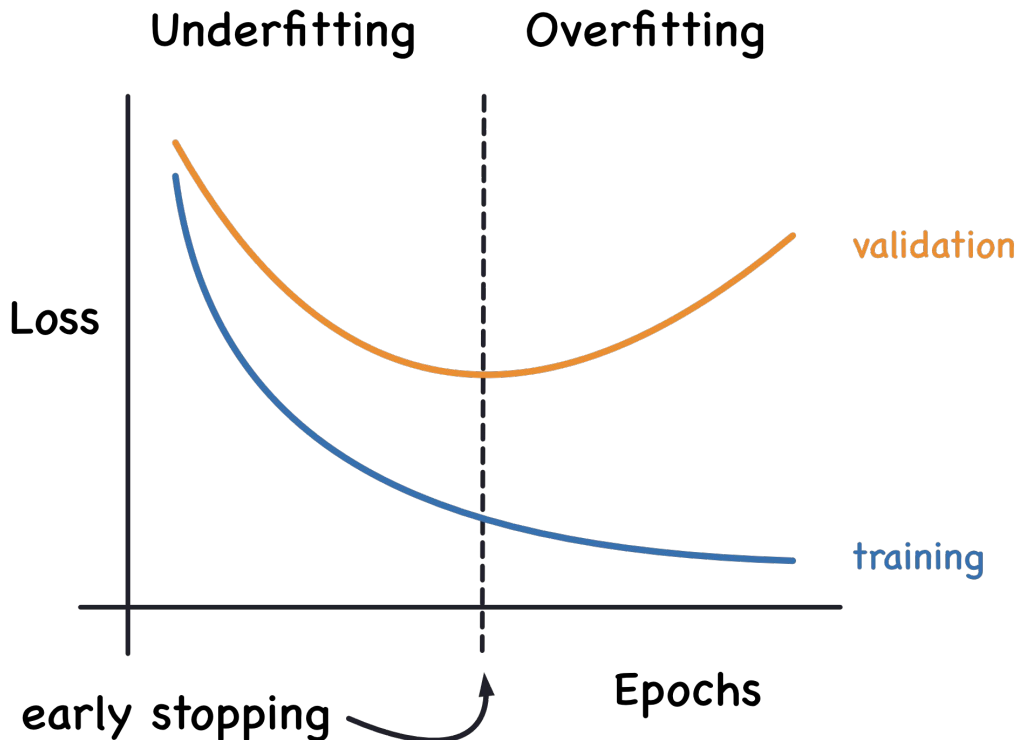
KGE workflow for link prediction



- **Splitting the graph triplets** into train, validation, and test sets.
- **Defining the model:**
 - Choose the model type (TransE, RESCAL, ...)
 - Specify the loss function (e.g., margin ranking loss, binary-cross-entropy loss, ...).
 - Select the optimizer (e.g., Adam, SGD, ..).
- **Defining the hyperparameters:**
 - Set the embedding dimension.
 - Determine the number of epochs.
 - Specify additional hyperparameters (e.g., learning rate, regularization terms).
- **Defining the negative sampling strategy:**
 - Choose how to generate negative samples
- **Defining a quality metric** for evaluating the model on the validation set (e.g., MRR, Hits@K).
- **Training the model**, and monitoring:
 - Monitoring performances on the training and validation sets

KGE workflow for link prediction

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- **Training the model**, and monitoring:
 - Monitoring performances on the training and validation sets
- **Evaluating the model:**
 - Assess the model's performance on the test set using the defined quality metrics.
 - **Good enough? Inference!**
 - **Not good enough? Back to step 2!**

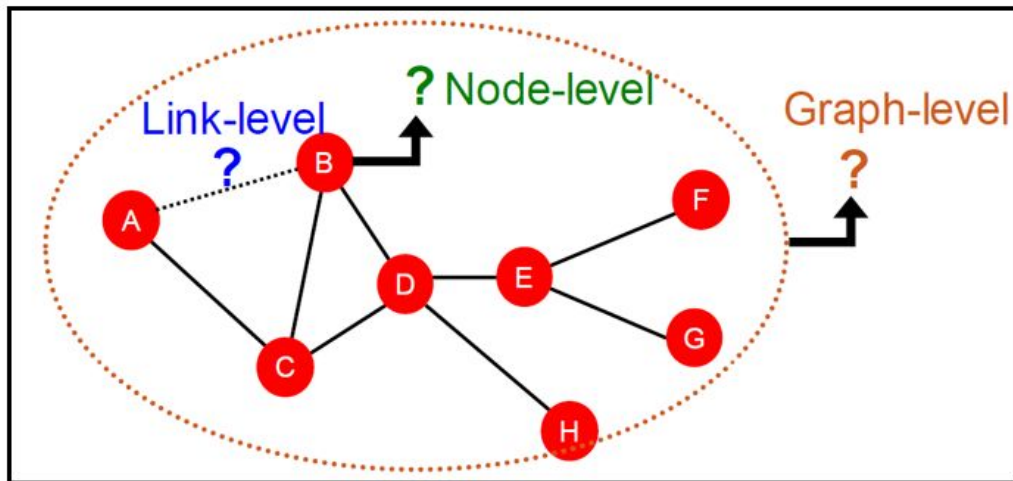
KGE workflow for link prediction

- **Splitting the graph triplets** into train, validation, and test sets.
- **Defining the model:**
 - Choose the model type (TransE, RESCAL, ...)
 - Specify the loss function (e.g., margin ranking loss, binary cross entropy)
 - Select the optimizer (e.g., Adam, SGD, ..).
- **Defining the hyperparameters:**
 - Set the embedding dimension
 - Determine the number of epochs
 - Specify additional hyperparameters
- **Defining the evaluation metrics:**
 - Choose the evaluation metrics (e.g., Mean Reciprocal Rank (MRR), Hits@K).
- **Training the model:**
 - Train the model on the training set using the defined quality metrics.
- **Evaluating the model:**
 - Assess the model's performance on the test set using the defined quality metrics.
 - Good enough? Inference!
 - Not good enough? Back to step 2!



Applications in Biomedicine

Tasks in Knowledge Graph Embedding



- **Classification**
 - Positive/negative triplet
 - Node properties
 - Graph properties
- **Clustering**
 - Node clustering
 - Graph clustering
 - (Edge clustering)
- **Regression**
 - Node properties
 - Edge weights
 - Graph properties

Towards Graph Learning for omics data integration?

