

# Falsifiable Experimental Signatures of Density Field Dynamics: Phase Velocity Equals One-Way Light Speed in a Nondispersive Vacuum

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We convert *Density Field Dynamics* (DFD) into a laboratory-focused, falsifiable test program. DFD posits a single scalar field  $\psi(\mathbf{x})$  that governs matter dynamics and photon propagation through a universal, *nondispersive* vacuum refractive structure. The core operational result is that, when dispersion is bounded in-band, the electromagnetic phase velocity is the one-way speed of light; hence precision phase metrology becomes a direct, synchronization-free probe of  $c_1(\mathbf{x})$ . We derive this identity along two independent routes (Fermat/eikonal and Gordon’s optical metric), demonstrate compatibility with classic tests of relativity, and design three GR-null vs DFD-signal protocols—most decisively a co-located cavity–atom frequency ratio measured at two altitudes—with quantified, near-term sensitivities. We audit existing constraints, state explicit refutation criteria, and provide a comprehensive responses-to-criticisms section (simultaneity, equivalence principle, Lorentz invariance, “already ruled out”, dispersion). The question is experimentally decidable with current optical metrology.

## I. FROM PRINCIPLE TO PROTOCOL

Two-way light speed and Lorentz symmetry are constrained to extraordinary precision [1–4]. The *one-way* speed remains entangled with simultaneity conventions [5–7]. DFD proposes a dynamical scalar  $\psi(\mathbf{x})$  that (i) fixes a universal vacuum refractive index  $n = e^\psi$  for photons, and (ii) normalizes the Newtonian limit for matter via  $\mathbf{a} = (c^2/2)\nabla\psi$ . In a verified nondispersive band, geometric optics yields  $v_{\text{phase}} = c/n$ , which, with  $n = e^\psi$ , provides the operational bridge  $c_1 = ce^{-\psi} = v_{\text{phase}}$ . The novelty is experimental: *route-dependent*, synchronization-free observables that are GR-null but DFD-nonnull.

## II. DFD DYNAMICS IN ONE PAGE

Adopt a scalar action with a single crossover scale,

$$\nabla \cdot \left[ \mu \left( \frac{|\nabla\psi|}{a_\star} \right) \nabla\psi \right] = -\frac{8\pi G}{c^2} (\rho_m - \bar{\rho}_m), \quad \mathbf{a} = \frac{c^2}{2} \nabla\psi, \quad (1)$$

so that  $\psi$  is fixed by matter density and yields  $\psi \simeq -2\Phi/c^2$  in weak fields. Photons propagate by Fermat/optical metric (Sec. III). The weak-field normalization is chosen to reproduce GR’s classic optical tests with PPN  $\gamma = 1$  [1, 8]. A Sakharov-style perspective motivates induced kinetic terms from quantum fluctuations [9], but the empirical program below does not rely on specific UV details.

## III. CORE IDENTITY: $v_{\text{phase}} = c_1$

### A. Route I: Fermat/eikonal

Geometric optics extremizes  $T[\gamma] = (1/c) \int_\gamma n(\mathbf{x}) d\ell$ , giving  $v_{\text{phase}} = c/n$  [8, 10, 11]. With  $n = e^\psi$  fixed by

dynamics,  $c_1 = ce^{-\psi} = v_{\text{phase}}$  follows. No distant clocks enter: the observable is local phase kinematics, verified nondispersive.

### B. Route II: Gordon’s optical metric

Light in a linear, isotropic, nondispersive medium follows null geodesics of

$$d\tilde{s}^2 = \frac{c^2}{n^2(\mathbf{x})} dt^2 - d\mathbf{x}^2 \quad (2)$$

[12]. Nullness implies  $d\ell/dt = c/n$ ; with  $n = e^\psi$  the same identity follows. The equality is therefore structural (two logically independent routes), not a definitional tautology.

## IV. EQUIVALENCE PRINCIPLE & LORENTZ INVARIANCE

**Local Lorentz invariance.**  $\psi$  is a scalar; the light cone at a point remains isotropic. Two-way orientation/boost tests remain null at the  $10^{-17}$ – $10^{-18}$  level, consistent with cavity experiments [2–4].

**Universality for matter.** Test bodies obey  $\mathbf{a} = (c^2/2)\nabla\psi$  in the weak field, reproducing free-fall universality and PPN  $\gamma = 1$  optics [1]. Equivalence principle tests remain satisfied in this limit.

**Where differences appear.** DFD predicts *route-dependent*, synchronization-free effects where GR enforces strict nulls: e.g., a co-located cavity–atom *ratio* compared at two altitudes (Sec. VI). This is an LPI probe in a nondispersive vacuum sector not covered by atom–atom redshift verifications.

## V. WHAT EXISTING TESTS DO—AND DO NOT—CONSTRAIN

*Two-way isotropy*  $\mathcal{E}$  *boost* (Michelson–Morley/Kennedy–Thorndike; modern rotating cavities) are exquisitely null [2–4]; DFD predicts the same nulls for two-way observables along fixed paths.

*Atomic clock redshift* confirms GR at  $\sim 10^{-16}$  per meter and below [13, 14]; spaceborne tests reach  $2.5 \times 10^{-5}$  relative precision [15]. These are atom–atom or remote-transfer comparisons.

**Critical gap:** To our knowledge, no published measurement reports a *co-located cavity–atom frequency ratio* recorded at two different gravitational potentials with  $< 10^{-16}$  fractional uncertainty. That is the target of Protocol C.

## VI. LABORATORY PROTOCOLS (GR-NULLED VS DFD-SIGNAL)

All protocols enforce nondispersion via multi-wavelength checks which bound  $|\partial n / \partial \omega|$  in the measurement band (so phase=group=front) [10, 16].

### Protocol A: Crossed ultra-stable cavities (orientation/height sweep)

Two orthogonal high- $Q$  cavities (length  $L$ ) support modes  $f_m \simeq \frac{m}{2L} \frac{c}{n}$ . A change  $\delta\psi$  imparts  $\delta f/f = -\delta n/n = -\delta\psi$ . Orientation reversals and vertical translations by  $\Delta h$  probe geometry-locked shifts. *Target sensitivity:*  $10^{-17}$ – $10^{-16}$  fractional, routinely achieved [2, 4].

### Protocol B: Reciprocity-broken fiber loop (two heights)

A monochromatic tone circulates both ways around an asymmetric loop with vertical separation  $\Delta h$  and a nonreciprocal element. The accumulated phase  $\phi = \frac{\omega}{c} \int n(\mathbf{x}) d\ell$  yields a forward–backward difference  $\propto \oint \psi d\ell$  that vanishes in GR (static loop, Sagnac subtracted) but not in DFD if  $\nabla\psi \cdot \hat{z} \neq 0$ . Operate near a zero-dispersion wavelength; multi- $\lambda$  tracking bounds dispersion [17].

### Protocol C (decisive): Co-located cavity–atom ratio across altitude

Lock a laser to a vacuum cavity (frequency  $f_{\text{cav}} \propto c/n$ ) and compare to a co-located optical atomic transition  $f_{\text{at}}$  via a frequency comb; form  $R \equiv f_{\text{cav}}/f_{\text{at}}$  at altitude  $h_1$ , repeat at  $h_2 = h_1 + \Delta h$ .

*GR:* Moving the *co-located* package changes neither the local ratio nor local physics; gravitational redshift appears

Protocol	Observable	DFD signal (order)
A: Crossed cavities	$\delta f/f$ on rotate/ $\Delta h$	$10^{-16}$ per m (vertical)
B: Fiber loop	$\Delta\phi_{\odot} - \Delta\phi_{\ominus}$	geometry-locked, $< 10^{-16}$ eqv.
C: Cavity/atom ratio	$\Delta R/R$ across $\Delta h$	$2g\Delta h/c^2 \approx 2.2 \times 10^{-14}$ per 100 m

TABLE I. Order-of-magnitude DFD signals in verified nondispersive band. GR predicts strict nulls for A/B and near-null for C.

upon comparison between distinct potentials, so  $R$  is (to excellent approximation) constant.

*DFD (nondispersive):* With  $\psi \simeq -2\Phi/c^2$ ,  $f_{\text{cav}} \propto e^{-\psi} \simeq 1 + 2\Phi/c^2$ , while the atomic transition is leading-order  $\psi$ -insensitive (matter-sector universality). Thus

$$\frac{\Delta R}{R} \simeq 2 \frac{\Delta\Phi}{c^2} \approx 2 \frac{g\Delta h}{c^2} \sim 2.2 \times 10^{-14} \text{ per 100 m.} \quad (3)$$

A variant with small matter-sector coupling yields  $\frac{\Delta R}{R} = \xi \Delta\Phi/c^2$  with  $0 < \xi \leq 2$ , still at the  $10^{-16} \text{ m}^{-1}$  scale. *Feasibility:* present clocks and cavities reach  $10^{-17}$ – $10^{-16}$  [2, 4, 13, 14].

*Systematics & controls (all protocols).* (i) Multi- $\lambda$  dispersion bound; (ii) temperature/strain control, Allan budgeting; (iii) polarization scrambles and hardware swaps; (iv) blind orientation/height reversals; (v) environmental monitors (pressure, tilt, vibration).

## VII. PREDICTED SIGNAL SIZES AND SENSITIVITY TABLE

## VIII. REFUTATION CRITERIA (CLEAN KILL CONDITIONS)

Any of the following falsifies this DFD formulation:

1. Protocol C yields  $\Delta R/R$  consistent with zero at or below  $|\Delta\Phi|/c^2$  while dispersion and thermal budgets pass all checks.
2. Protocols A or B yield nulls where DFD predicts nonzero geometry-locked signals after reversals/path swaps.
3. A verified nonzero dispersion ( $\partial n / \partial \omega$ ) fully accounts for any residuals across the band.

Conversely, reproducible nonzero signals that (i) scale with  $\Delta h$  or orientation as predicted, (ii) survive multi- $\lambda$  tests, and (iii) pass swap/blind controls, would be decisive.

## IX. COSMOLOGICAL CONTEXT (BRIEF)

With  $\psi \simeq -2\Phi/c^2$ , Gordon’s metric reproduces classic weak-field optics [1, 8]. DFD suggests that nearby structure can bias line-of-sight cosmography at low  $z$ , providing a plausible context for directional  $H_0$  inferences; early-universe constraints (CMB/BAO) remain intact [18, 19].

These motivate but do not underwrite the laboratory program.

## X. COMPREHENSIVE RESPONSES TO STANDARD CRITICISMS

(1) **“You haven’t solved simultaneity; one-way  $c$  is conventional.”** We agree that simultaneity is conventional in SR. DFD makes a different claim: in a *verified nondispersive* band, local phase velocity equals the one-way propagation speed. Our observables are local and synchronization-free; they exploit *route dependence* where GR says strict null. This turns a philosophical impasse into a falsifiable statement [5–7].

(2) **“ $n = e^\psi$  makes  $c_1 = c/n$  definitional (circular).”** The identity  $v_{\text{phase}} = c/n$  follows from standard optics (Fermat/eikonal and Gordon’s metric) *independently* [8, 10, 12]. DFD then supplies *dynamics* for  $\psi$  (Eq. 1), fixed by classic-test normalization [1]. The bridge is therefore derived, not stipulated.

(3) **“Equivalence principle is violated: photons vs matter.”** Matter test bodies obey  $\mathbf{a} = (c^2/2)\nabla\psi$  (universality preserved in weak field). Photons see the optical metric which reproduces GR’s lensing/redshift (PPN  $\gamma = 1$ ). Our key test (Protocol C) is an *LPI* probe in the nondispersive vacuum sector; either a residual appears (then LPI is violated in this sector) or it does not (DFD is falsified).

(4) **“Lorentz symmetry constraints already exclude this.”** Two-way isotropy/boost tests [2–4] remain null in DFD. Differences appear only between *paths* sampling different  $\psi$  (height/orientation). This is not what SME-style cavity rotations constrain [20].

(5) **“Existing optical clocks at different elevations would have seen it.”** Published redshift verifications are atom–atom or remote-transfer comparisons [13–15]. They confirm GR and are orthogonal to our decisive *co-located cavity–atom ratio* across altitudes. To our knowledge, such a ratio-vs-altitude measurement at  $< 10^{-16}$  is not yet published; Protocol C is designed to fill this gap.

(6) **“This is just superluminal phase velocity; information rides on front velocity.”** Correct in dispersive media [16]. Our tests operate in a verified nondispersive band where phase=group=front [10]; the identity is invoked only under those conditions.

(7) **“ $\psi$  is ad hoc and parameters are tuned.”** The weak-field normalization is fixed by classic tests; induced-

gravity arguments [9] motivate scalar kinetic terms. However, our claims do not hinge on UV priors: the laboratory identity and protocols stand on their own as empirical tests.

## XI. CONCLUSIONS

We have turned DFD into a concrete, near-term experimental program: (i) a structural identity that makes phase metrology a one-way- $c$  probe in a verified nondispersive vacuum; (ii) three synchronization-free protocols with GR-null vs DFD-signal contrasts and quantified targets; (iii) an explicit constraints audit and clean refutation logic. The decisive experiment (Protocol C) is implementable now with optical cavities, clocks, and frequency combs. Either the geometry-locked phase-velocity effects appear (opening a new sector of physics) or the present DFD is falsified.

### Appendix A: Geometrical optics and nondispersion

Let  $S$  be the eikonal:  $\mathbf{k} = \nabla S$ ,  $\omega = -\partial_t S$ . For  $\omega = (c/n)|\mathbf{k}|$ ,  $v_{\text{phase}} = \omega/|\mathbf{k}| = c/n$  and  $v_g = \partial\omega/\partial|\mathbf{k}| = c/n$ ; the Sommerfeld–Brillouin front velocity coincides in the nondispersive limit [10, 16].

### Appendix B: Round-trip nulls, clocks, and GPS

For a fixed path  $\gamma$ ,  $T_{2w} = \frac{2}{c} \int_\gamma n \, dl$ ; at fixed geometry, orientation rotations preserve two-way times (Michelson–Morley nulls). Clock redshift verifications rely on atom–atom or remote transfers consistent with GR [13–15]; our decisive observable is a *local* cavity–atom ratio across altitude.

### Appendix C: Minimal implementation checklist

**Cavities:** ULE/silicon spacers; PDH locking; cryogenic option;  $10^{-17}$  stability [2, 4].

**Fibers:** zero-dispersion operation; Faraday isolators; dual- $\lambda$  phase-tracking [17].

**Clocks:** Sr/Yb lattice or  $\text{Al}^+$  logic; comb-based ratio readout [13, 14].

**Analysis:** publish  $\sigma_y(\tau)$ ; blinded reversals; multi- $\lambda$  linearity fits; environmental logs.

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