

**1 Hard-Coding a Multilayer Perceptron (2pts):** There are many possible solutions, here is one.

$$\mathbf{W}^{(1)} = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 1 \end{bmatrix} \mathbf{b}^{(1)} = [0 \ 0 \ 0] \mathbf{W}^{(2)} = [1 \ 1 \ 1] \mathbf{b}^{(2)} = -2.5 \quad (1)$$

**2 Sparsifying Activation Function (3pts):**

- $\frac{\partial L}{\partial w_1} = 0$  - Yes
- $\frac{\partial L}{\partial w_2} = 0$  - Yes
- $\frac{\partial L}{\partial w_3} = 0$  - No

**3 Universal Approximation Theorem (5pts):**

- $W_0 = [-1 \ 1]^T$ ,  $b_0 = [b \ -a]^T$ ,  $W_1 = [h \ h]^T$ ,  $b_1 = -h$