

1 Backpropagation (2pts)

1. $\frac{\partial \mathcal{L}}{\partial \mathbf{x}} = (\mathbf{I}_N + \mathbf{W}^{(1)T} \text{diag}(\sigma'(\mathbf{x})) \mathbf{W}^{(2)T})(\mathbf{y} - \mathbf{s}) + \mathbf{W}^{(1)T} \text{diag}(\sigma'(\mathbf{x})) \mathbf{r}$

3 Linear Regression (3pts)

1. **Deriving the Gradient (0.5pt)** $\frac{\partial L}{\partial \mathbf{W}} =$.

2. **Underparameterized Model (0.5pt)**

(a) $\mathbf{w} = (\mathbf{X}^T \mathbf{X}) \mathbf{X}^T \mathbf{t}$. Yes, the solution is unique.

3. **Overparameterized Model: 2D Example (1pt)**

(a) $2w_1 + w_2 = 2$

4. **Overparameterized Model: General Case (1pt)**

(a) $\mathbf{w} = \mathbf{X}^T (\mathbf{X} \mathbf{X}^T \mathbf{t})$

3 Linear Regression and Optimization (3pts)

1. **Stochastic Gradient Descent (1pt):** Yes

2. **Mini-Batch SGD (1pt):** Yes

3. **Adaptive Methods (1pt):** No