

1 Binary Addition (2.5pts): There are multiple possible solutions, here is one.

$$\begin{aligned}
W_{xh} &= \begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix} \\
W_{hh} &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \\
W_{hy} &= \begin{bmatrix} 1 & -1 & 1 \end{bmatrix} \\
b_h &= \begin{bmatrix} -0.5 \\ -1.5 \\ -2.5 \end{bmatrix} \\
b_y &= 0
\end{aligned} \tag{1}$$

2 LSTM Gradient (3.5pts):

$$\begin{aligned}
\overline{h^{(t)}} &= \frac{\partial L^{(t)}}{\partial h^{(t)}} + \overline{g^{(t+1)}}(1 - g^{(t+1)})w_{hg} + \overline{o^{(t+1)}}o^{(t+1)}(1 - o^{(t+1)})w_{ho} + \overline{f^{(t+1)}}f^{(t+1)}(1 - f^{(t+1)})w_{hf} \\
&\quad + \overline{i^{(t+1)}}i^{(t+1)}(1 - i^{(t+1)})w_{hi} \\
\overline{c^{(t)}} &= \overline{h^{(t)}}o^{(t)}(1 - \tanh^2(c^{(t)})) + \overline{c^{(t+1)}}f^{(t+1)} \\
\overline{g^{(t)}} &= \overline{c^{(t)}}i^{(t)} \\
\overline{o^{(t)}} &= \overline{h^{(t)}}\tanh(c^{(t)}) \\
\overline{f^{(t)}} &= \overline{c^{(t)}}c^{(t-1)} \\
\overline{i^{(t)}} &= \overline{c^{(t)}}g^{(t)}
\end{aligned}$$

$$\overline{w_{xi}} = \sum_{t=1}^T \overline{i^{(t)}}i^{(t)}(1 - i^{(t)})x^{(t)}$$

3 Convolutional Neural Networks (2pts):

1. **(1pt)** Number of parameters = 207,507,816.
2. **(1pt)** The one on the left.

4 Autoregressive Generative Models (2pt):

1. (a) $\mathcal{O}(dHWk^2)$
(b) $\mathcal{O}(d)$
2. (a) $\mathcal{O}(dHWk^2)$
(b) $\mathcal{O}(d\sqrt{HW})$