



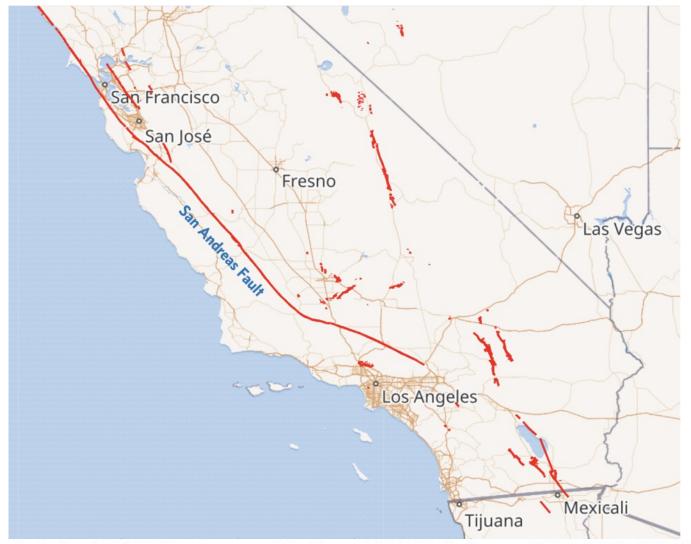
CASE STUDIES IN STATISTICAL THINKING

Introduction to statistical seismology

Justin Bois Lecturer, Caltech

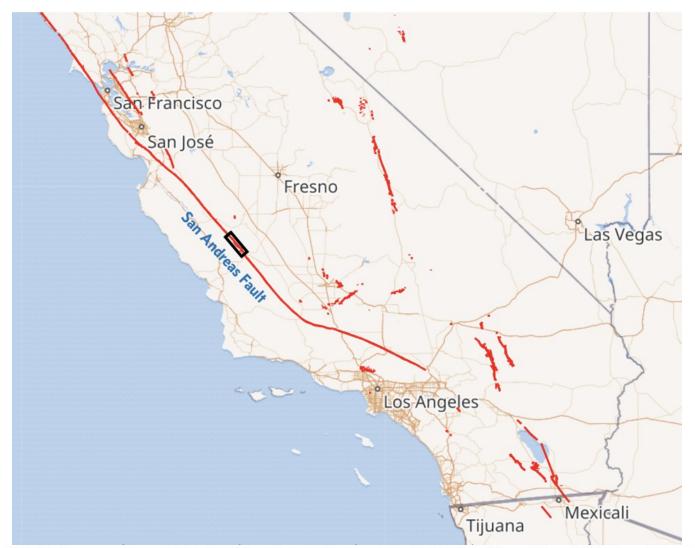


California moves and shakes



Fault data: USGS Quaternary Fault and Fold Database of the United States

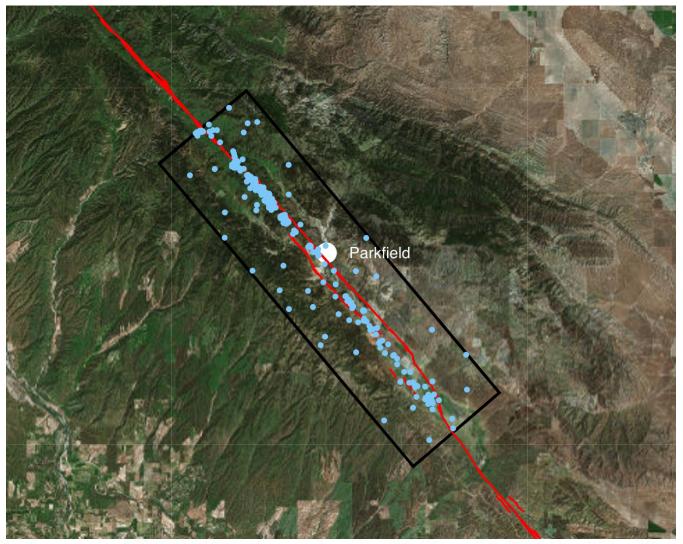
The Parkfield region



Parkfield box proposed by Michael, and Jones, Bull. Seism. Soc. Am. 88, 117-130, 1998



The Parkfield region



Data source: USGS ANSS Comprehensive Earthquake Catalog (ComCat)



The Parkfield region

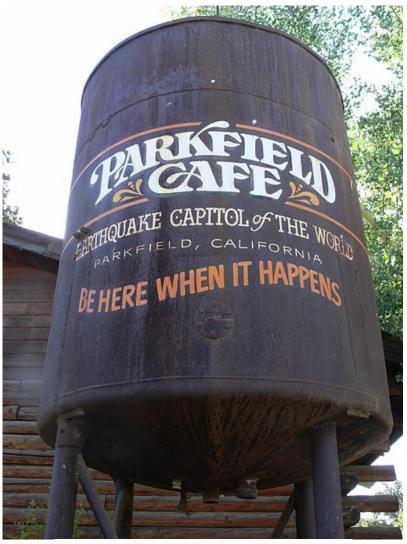
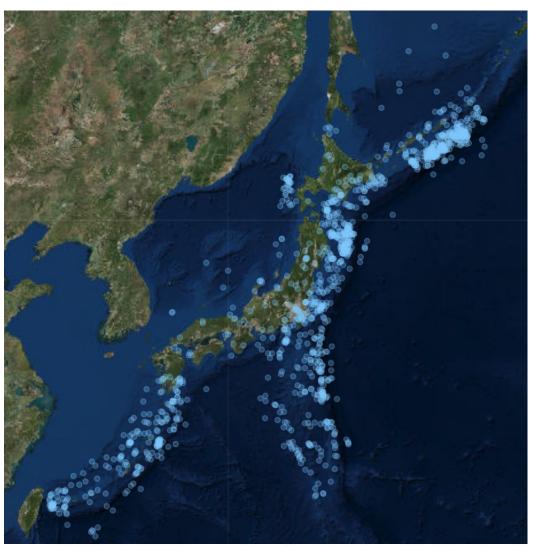


Image: Linda Tanner, CC-BY-2.0



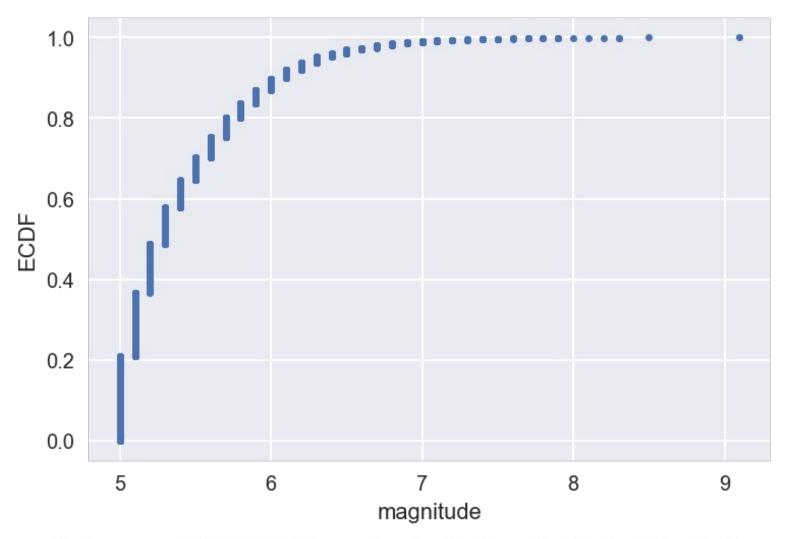
Seismic Japan



Data source: USGS ANSS Comprehensive Earthquake Catalog (ComCat)

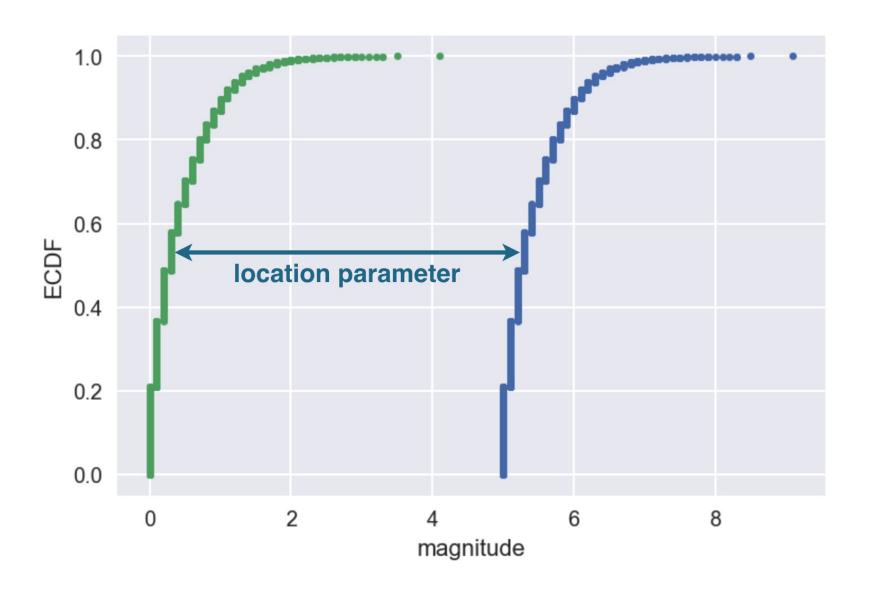


ECDF of magnitudes, Japan, 1990-1999



Data source: USGS ANSS Comprehensive Earthquake Catalog (ComCat)

Location parameters



 $m' \equiv m - 5 \sim {
m Exponential}$

 $m' \equiv m - m_t \sim \text{Exponential}$



The Gutenberg-Richter Law

The magnitudes of earthquakes in a given region over a given time period are Exponentially distributed

One parameter, given by $\overline{m}-m_t$, describes earthquake magnitudes for a region



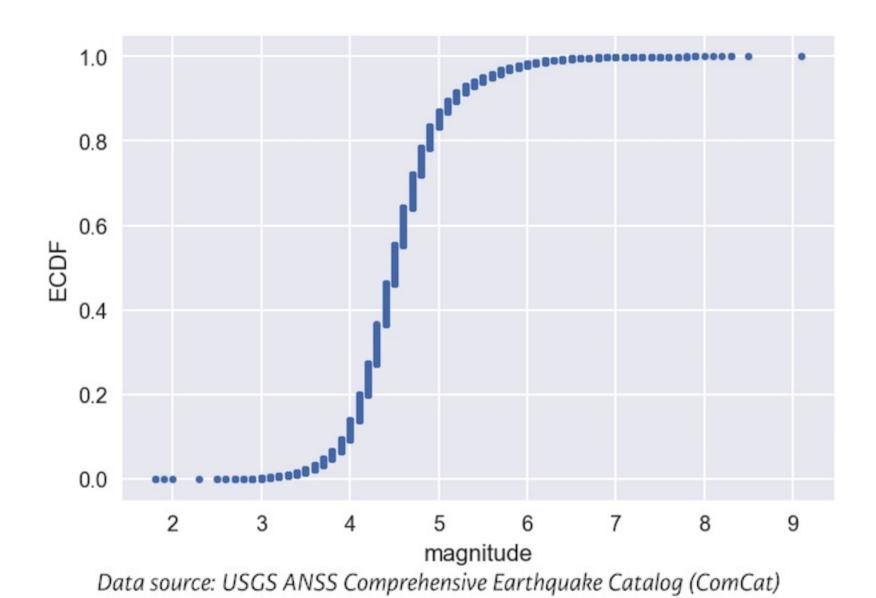
The *b*-value

$$b = (\overline{m} - m_t) \cdot \ln 10$$

```
In [1]: mt = 5
In [2]: b = (np.mean(magnitudes) - mt) * np.log(10)
In [3]: b
Out[3]: 0.97292147426325659
```

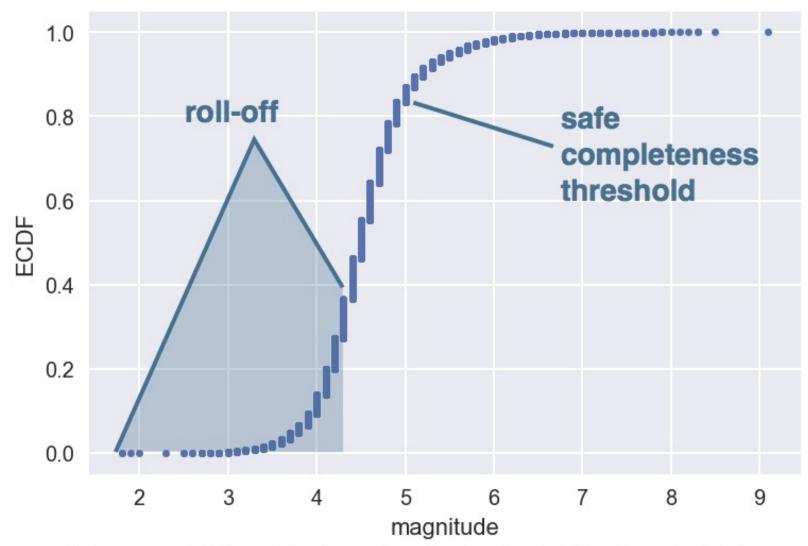


ECDF of all magnitudes





ECDF of all magnitudes



Data source: USGS ANSS Comprehensive Earthquake Catalog (ComCat)



Completeness threshold

The magnitude, m_t , above which all earthquakes in a region can be detected





CASE STUDIES IN STATISTICAL THINKING

Let's practice!





CASE STUDIES IN STATISTICAL THINKING

Timing of major earthquakes

Justin Bois Lecturer, Caltech



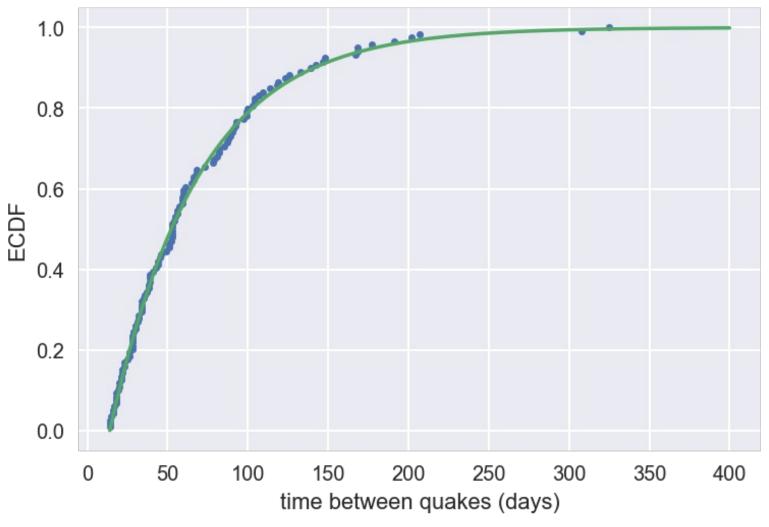
Models for earthquake timing

• Exponential: Earthquakes happen like a Poisson process

• Gaussian: Earthquakes happen with a well-defined period



Stable continental region earthquakes



Data source: USGS Earthquake Catalog for Stable Continental Regions



The Nankai Trough



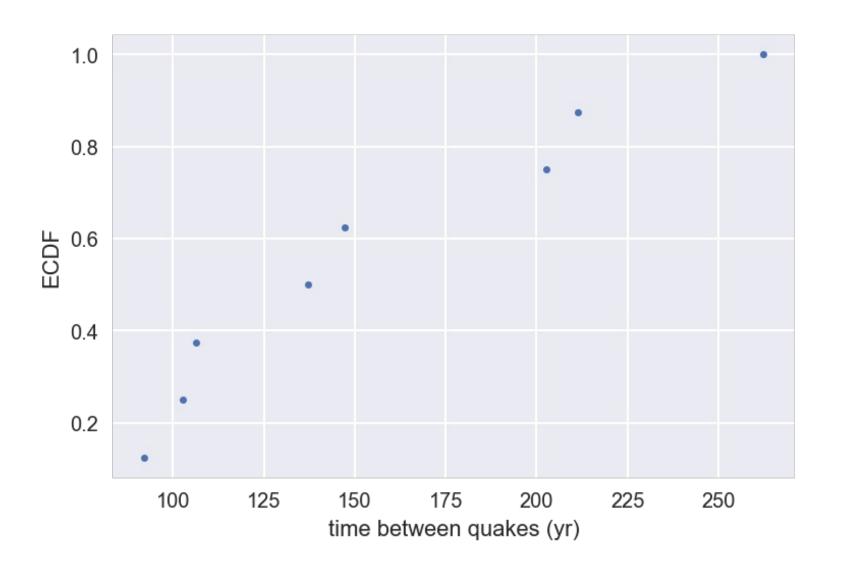


Earthquakes in the Nankai Trough

Date	Magnitude
684-11-24	8.4
887-08-22	8.6
1099-02-16	8.0
1361-07-26	8.4
1498-09-11	8.6
1605-02-03	7.9
1707-10-18	8.6
1854-12-23	8.4
1946-12-24	8.1



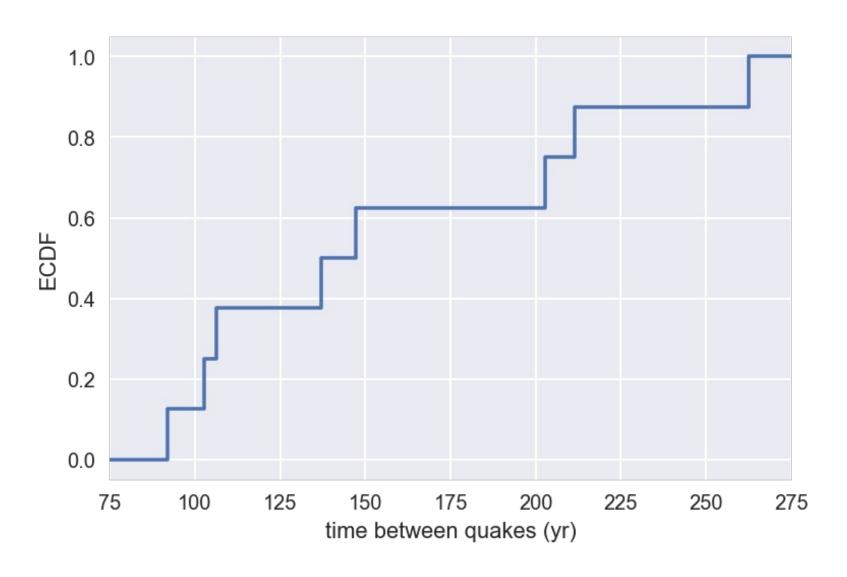
ECDF of time between Nankai quakes



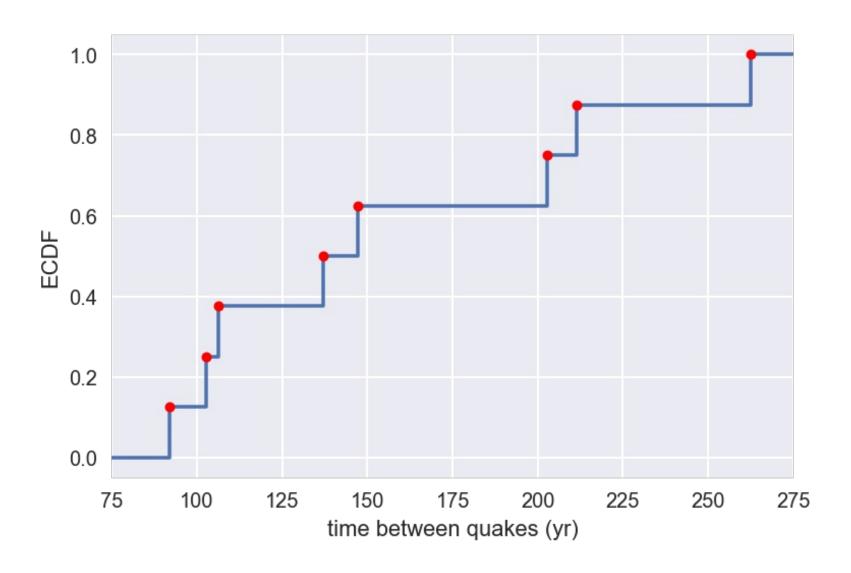


 $ECDF(x) = fraction of data points \le x$



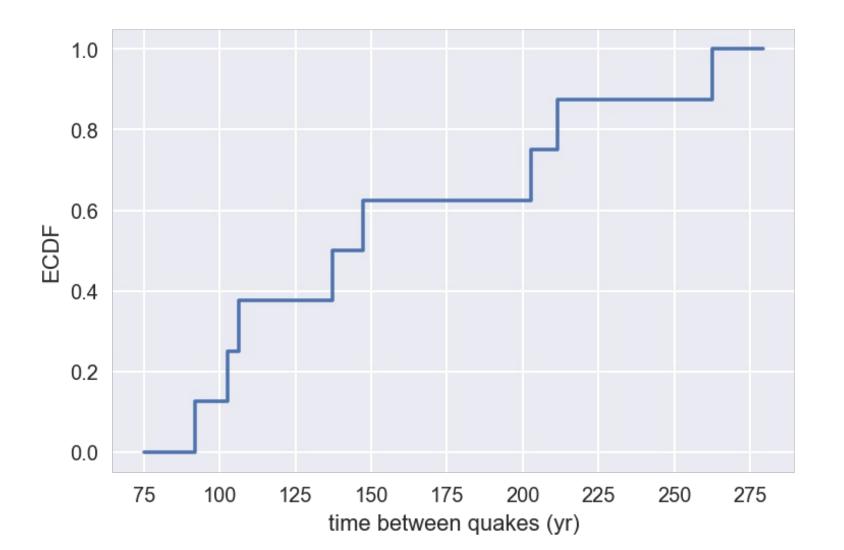








```
# time_gap is an array of interearthquake times
_ = plt.plot(*dcst.ecdf(time_gap, formal=True))
_ = plt.xlabel('time between quakes (yr)')
_ = plt.ylabel('ECDF')
```





Generating theoretical distributions

```
# Compute the mean time gap
mean_time_gap = np.mean(time_gap)

# Standard deviation of the time gap
std_time_gap = np.std(time_gap)
```

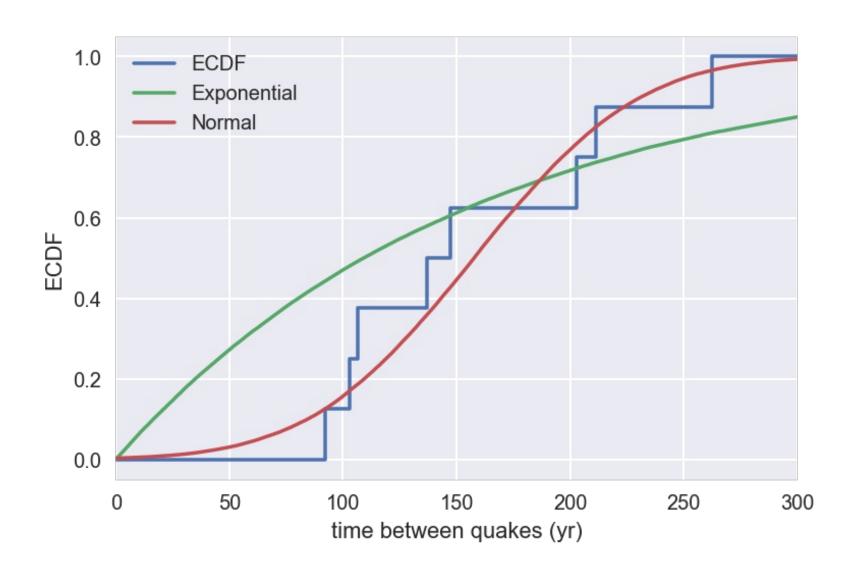
```
# Generate theoretical Exponential distribution of timings
time_gap_exp = np.random.exponential(mean_time_gap, size=100000)

# Generate theoretical Normal distribution of timings
time_gap_norm = np.random.normal(mean_time_gap, std_time_gap, size=100000)
```

```
# Plot theoretical CDFs
_ = plt.plot(*dcst.ecdf(time_gap_exp))
_ = plt.plot(*dcst.ecdf(time_gap_norm))
```



Model for Nankai Trough







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Let's practice!



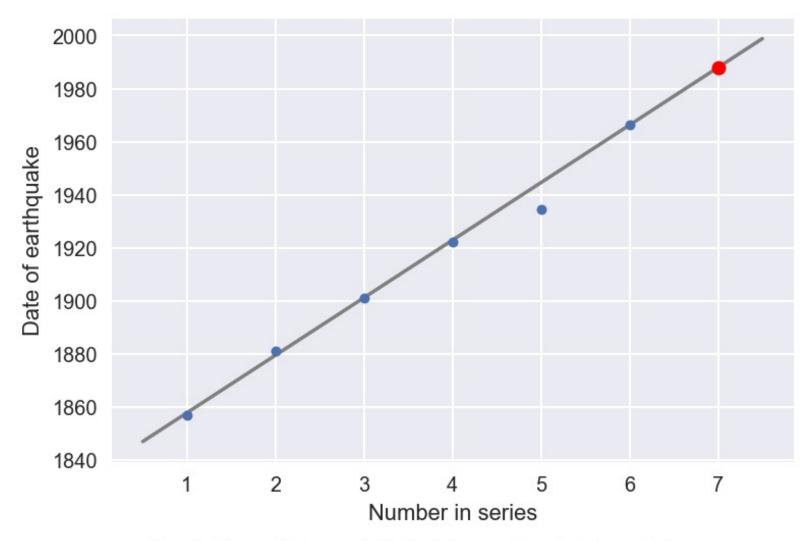


CASE STUDIES IN STATISTICAL THINKING

How are the Parkfield interearthquake times distributed?

Justin Bois Lecturer, Caltech

The Parkfield Prediction



Adapted from Bakun and Lindh, Science, 229, 619-624, 1985



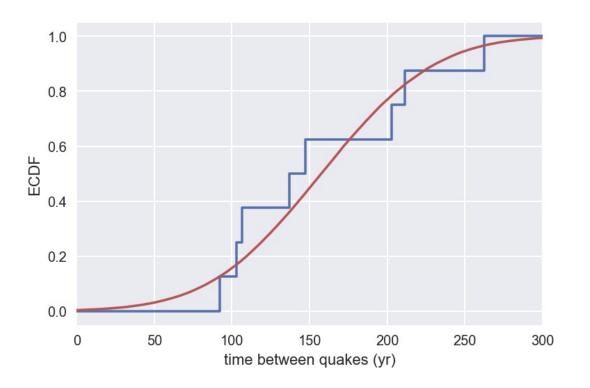
Hypthesis test on the Nankai megathrust earthquakes

 Hypothesis: The time between Nankai Trough earthquakes is Normally distributed with a mean and standard deviation as calculated from the data

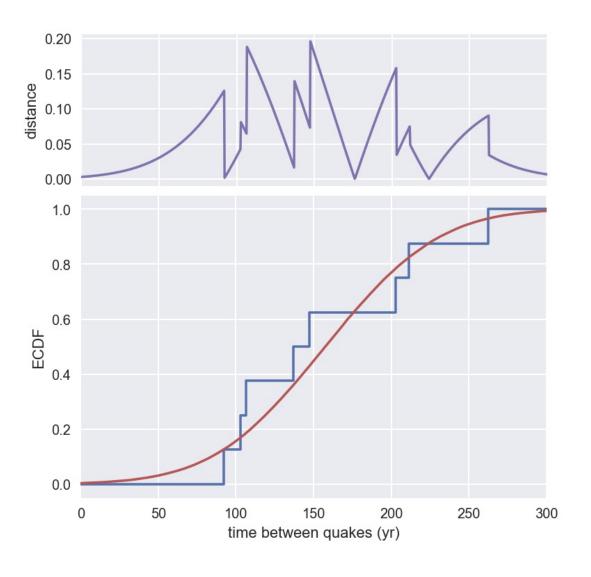
• Test statistic: ??

• At least as extreme as: ??

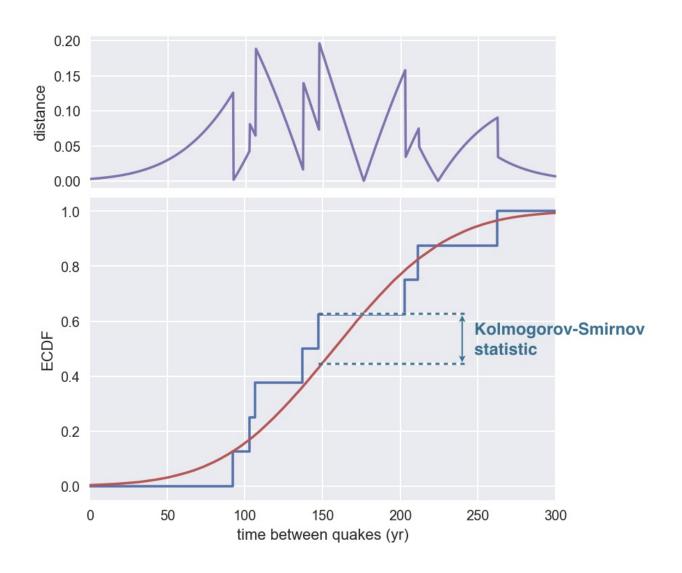




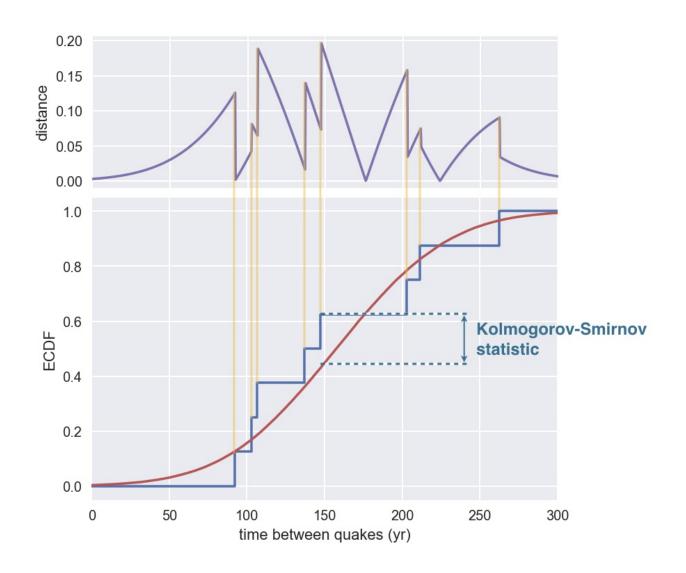




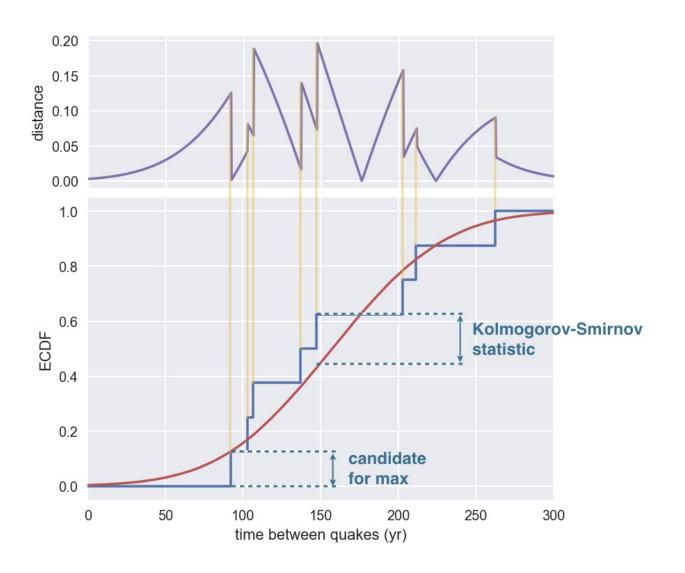














Kolmogorov-Smirnov test

 Hypothesis: The time between Nankai Trough earthquakes is Normally distributed with a mean and standard deviation as calculated from the data

• **Test statistic**: Kolmogorov-Smirnov statistic

• At least as extreme as: ≥ observed K-S statistic



Simulating the null hypothesis

- Draw lots of samples out of the theoretical distribution and store them
 - Draw n samples out of the theoretical distribution
 - Compute the K-S statistic from the samples





CASE STUDIES IN STATISTICAL THINKING

Let's practice!