Automatic Evaluation of MathBERT Embeddings of Students' Algebra Questions

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Introduction:

Grading algebraic responses in traditional educational settings is a labor-intensive task, particularly in large classrooms. These conventional methods can result in inconsistent assessments and delayed feedback for students. This project explores an automated solution using MathBERT embeddings, a specialized model for mathematical language processing, combined with machine learning (ML) classifiers to categorize student responses as either correct or incorrect. The proposed system aims to enhance grading efficiency, ensure uniformity, and provide timely feedback, addressing a significant gap in the evaluation of descriptive mathematical answers.

Problem Statement:

The goal is to automate the evaluation of open-ended student responses to high school algebra questions. By leveraging machine learning techniques and MathBERT embeddings, the project seeks to classify responses into correct or incorrect categories, thus reducing manual grading efforts and providing standardized assessments.

Objective:

- 1. **Efficiency**: Minimize manual grading time and effort for educators.
- 2. **Consistency**: Deliver unbiased and standardized evaluations.
- 3. **Scalability**: Handle large datasets of student responses effectively.

- 4. **Advanced NLP Usage**: Use MathBERT embeddings to understand mathematical language accurately.
- 5. **Data Insights**: Highlight common errors and provide actionable insights to improve teaching strategies.

Dataset Description:

The dataset includes responses from approximately 50 students to 21 algebraic questions. Each response was transformed into 385-dimensional MathBERT embeddings, yielding 1024 rows in total.

Methodology:

1. Preprocessing:

- a. **Duplicate Removal**: Eliminated redundant entries.
- b. **Handling Missing Values**: Ensured data completeness by addressing null values.

2. Feature Extraction:

a. **Using MathBERT**: Each response was encoded into a 385-dimensional vector, capturing mathematical semantics and syntax.

3. Feature Selection:

- a. Applied correlation techniques to identify and remove irrelevant or redundant features.
- b. Reduced dimensionality from 385 to 384 features postselection, improving model generalization.

TABLE I.	Models and Hyperparameters					
Model	Hyperparameters					
SVM	{'C':1,'gamma':0.1,'kernel':'rbf'}					
KNN	{'K=8 best'}					
Decision Tree	{'criterion':'entropy', 'max depth':'max features':'sqrt', 'min samples leaf':					
RF	{'bootstrap': False,'max _depth': 30, 'min samples leaf': 2,'min samples split': 10, 'n estimators': 100'}					

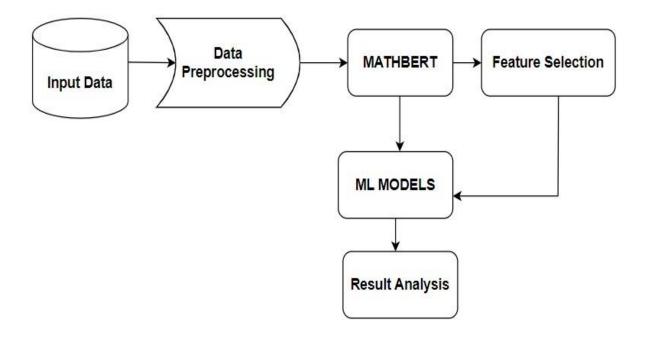
ML Models Employed:

- c. Models tested include Support Vector Machines (SVM), Random Forest (RF), k-Nearest Neighbors (KNN), Decision Trees, and others.
- d. Performed **4-fold cross-validation** to ensure robust evaluation and avoid overfitting.

Performance Metrics:

Metrics such as accuracy, precision, recall, and F1-score were used to evaluate model effectiveness before and after feature selection.

Here are the step wise screenshots of the methodology:



INITIAL DATASET:training_mathbert.xlsx:

```
[1]: import pandas as pd
   # Read the Excel file
   data = pd.read_excel('training_mathbert.xlsx')
   data['Classification'] = (data['output'] >= 4).astype(int)
   # Display the updated DataFrame
  print(data)
  1125 -0.2/918/ 0.0995/1 0.229438 0.19///5 -0.326235 -0.254882 -0.000000
                 embed 8 embed 9 ... embed 376 embed 377 embed 378
         embed 7
        0.094621 0.330203 -0.258730 ... -0.230662 0.173143 -0.259786
  1
       -0.081476 0.213762 -0.105293 ... -0.090271 0.129022 -0.008138
        0.014463 0.104336 -0.014190 ... -0.117493 -0.118993 -0.046860
  3
       0.074028 0.149310 -0.147779 ... -0.100965 0.236099 -0.286450
  4
        0.075697 0.055439 -0.200804 ... -0.230057 0.296528 -0.526185
                           ... ...
                                                    . . . .
                      . . .
                                           . . . .
  1121 0.012244 0.254925 -0.056957 ... -0.316320 0.013955 -0.030025
  1122 0.027731 0.275638 -0.068072 ... -0.419794 0.061882 -0.190783
  1123 0.019028 0.268377 -0.188386 ... -0.354851 0.093440 -0.093673
  1124 0.074879 0.154743 -0.030652 ... -0.428964 0.052585 -0.172558
  1125 0.034733 0.283212 -0.207798 ... -0.275116 -0.012660 0.011353
        0
        -0.316996 -0.389919
                            0.105596 0.196438
                                                 0.117199
                                                              0.0
  1
        -0.220774 -0.021343 -0.029695 0.335977 -0.197539
                                                              0.0
        0.010008 -0.118400 -0.085768 0.512956 0.023334
  2
        -0.130198 -0.051258 -0.047492 0.241473 -0.095162
  3
                                                             0.0
        -0.251471 0.196795 -0.101786 0.570922 0.007743
  4
                                                              0.0
                               ...
  . . .
             . . .
                       . . .
                                           . . . .
                                                      . . . .
  1121 -0.306975 0.139429 -0.256867 0.331288 -0.045333
                                                             5.0
  1122 -0.323777 0.185546 -0.144995 0.347215 -0.024521
                                                             5.0
  1123 -0.271739 0.042851 -0.143179 0.410811 -0.105163
                                                             5.0
  1124 -0.218717 0.201938 -0.085569 0.345646 -0.032904
                                                              5.0
  1125 -0.323538 0.055882 0.001314 0.474825 -0.055474
                                                              5.0
        Classification
  0
  1
                    0
  2
                    0
  3
                    0
                    0
  1121
                    1
  1122
                    1
  1123
                    1
  1124
                    1
  1125
  [1126 rows x 386 columns]
```

AFTER REMOVING OUTPUT:SAVED IN data1_no_output.xlsx file:

```
?]: data.drop(['output'], axis=1)
        embed_0 embed_1 embed_2 embed_3 embed_4 embed_5 embed_6 embed_7 embed_8 embed_9 ... embed_375 embed_376 embed_377 embed_377
     -0.272278
                                                                                                      -0.230662
                                                                                                                0.173143
                                                                                                                         -0.259786
                                                                                            -0.310262
                                                                                                      -0.090271
     1 0.303261 0.084930 0.047369 -0.017244 -0.524733 -0.104934 0.335107 -0.081476 0.213762 -0.105293
                                                                                                                0.129022
                                                                                                                          -0.008138
                       -0.118993
     3 0.118676 0.095572 0.157358 0.225097 -0.632885 -0.125629 0.204013 0.074028 0.149310 -0.147779 ...
                                                                                            -0.030543
                                                                                                      -0.100965
                                                                                                               0.236099
                                                                                                                         -0.286450
      4 0.298772 0.300674 0.366119 -0.022142 -0.748852 -0.035268 0.277504 0.075697 0.055439 -0.200804 ... -0.149575
   -0.316320
                                                                                                               0.013955
                                                                                                                       -0.030025
   1122 -0.342471 0.060391 -0.009947 0.156623 -0.511338 -0.070624 0.140290 0.027731 0.275638 -0.068072 ...
   1123 -0.379174 0.197136 0.149639 0.060261 -0.347212 -0.064022 0.119379 0.019028 0.268377 -0.188386 ... -0.517010
                                                                                                      -0.354851
                                                                                                               0.093440
                                                                                                                        -0.093673
   1124 -0.379726 0.075891 0.100093 0.118006 -0.429774 -0.140415 0.120826 0.074879 0.154743 -0.030652 ... -0.683223
                                                                                                      -0.428964
   1125 -0.279187 0.099571 0.229438 0.197775 -0.326235 -0.254882 -0.000509 0.034733 0.283212 -0.207798 ... -0.574962 -0.275116
  1126 rows × 385 columns
        ......
   [4]: import pandas as pd
       # Assuming 'data' is your DataFrame and 'Average' is the column with values
       # Replace 'data' and 'Average' with your actual DataFrame and column na
       # Create a new column 'Classification' based on the conditions you mentioned
       data = pd.read_excel('training_mathbert.xlsx')
             pd.DataFrame(data)
       data1['Classification'] = (data1['output'] >= 4).astype(int)
       data1 no output = data1.drop(['output'], axis=1)
       # Specify the file path where you want to save the Excel file
       excel_file_path = 'data1_no_output.xlsx'
        # Write the DataFrame without the 'output' column to an Excel file
       data1_no_output.to_excel(excel_file_path, index=False)
        # Print a message indicating the successful write
       print(f"DataFrame without 'output' column written to {excel_file_path}")
       DataFrame without 'output' column written to data1_no_output.xlsx
```

AFTER REMOVING DUPLICATES:saved in no_duplicated.xlsx file:

```
[11]: import pandas as pd
      # Assuming 'data' is your DataFrame and 'Average' is the column with values
      # Replace 'data' and 'Average' with your actual DataFrame
      # Create a new column 'Classification' based on the conditions you mentioned
      data = pd.read_excel('no_duplicates.xlsx')
      df1 = pd.DataFrame(data)
[12]: df1
           embed 0 embed 1 embed 2 embed 3 embed 4 embed 5 embed 6 embed 7 embed 8 embed 9 ... embed 375 embed 376 embed 377 embed 378
        0 -0.089926 0.343874 0.176382 0.169358 -0.413337 -0.276315 0.188070 0.094621 0.330203 -0.258730 ... -0.272278 -0.230662
        1 0.303261 0.084930 0.047369 -0.017244 -0.524733 -0.104934 0.335107 -0.081476 0.213762 -0.105293 ... -0.310262 -0.090271 0.129022
        2 -0.274291 0.216801 0.029110 0.259279 -0.655594 -0.289643 0.073369 0.014463 0.104336 -0.014190 ... -0.464926
                                                                                                              -0.117493
                                                                                                                        -0.118993
                                                                                                                                   -0.046860
        3 0.118676 0.095572 0.157358 0.225097 -0.632885 -0.125629 0.204013 0.074028 0.149310 -0.147779 ...
        4 0.298772 0.300674 0.366119 -0.022142 -0.748852 -0.035268 0.277504 0.075697 0.055439 -0.200804 ... -0.149575
                                                                                                              -0.230057
                                                                                                                         0.296528
                                                                                                                                   -0.526185
      -0.030025
      1030 -0.342471 0.060391 -0.009947 0.156623 -0.511338 -0.070624 0.140290 0.027731 0.275638 -0.068072 ... -0.595396 -0.419794
                                                                                                                         0.061882
      1031 -0.379174  0.197136  0.149639  0.060261 -0.347212 -0.064022  0.119379  0.019028  0.268377 -0.188386 ...
                                                                                                    -0.517010 -0.354851
                                                                                                                         0.093440
                                                                                                                                   -0.093673
```

TRAINING AND TESTING SET SHAPE:

```
from sklearn.model_selection import train_test_split
import pandas as pd

data = pd.read_excel('no_duplicates.xlsx')
df1 = pd.DataFrame(data)
# Separate features (X) and target variable (y)
X = df1.drop('classification', axis=1)
y = df1['classification']

# Split the dataset into training and testing sets (80% training, 20% testing)+
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)

# Display the shapes of the training and testing sets
print("Training set shape:", X_train.shape, y_train.shape)
print("Testing set shape:", X_test.shape, y_test.shape)

Training set shape: (827, 384) (827,)
Testing set shape: (227, 384) (227,)
```

KNN CLASSIFIER:(calculating accuracy, precison, f1 score, recall):

```
from sklearn.model_selection import GridSearchCV, train_test_split
from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import accuracy_score
data = pd.read_excel('no_duplicates.xlsx')
# Separate features (X) and target variable (y)
X = df1.drop('Classification', axis=1)
y = df1['Classification']
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
param_grid = {'n_neighbors': np.arange(1, 11)}
# Create the KNN classifier
knn = KNeighborsClassifier()
# Create GridSearchCV object
grid search = GridSearchCV(knn, param grid, cv=5, scoring='accuracy')
# Fit the model
grid_search.fit(X_train, y_train)
# Get the best hyperparameters
best_k = grid_search.best_params_['n_neighbors']
# Train the final model with the best hyperparameters
final_model = KNeighborsClassifier(n_neighbors=best_k)
final_model.fit(X_train, y_train)
y_pred = final_model.predict(X_test)
# Evaluate the model
accuracy = accuracy_score(y_test, y_pred)
print(f"Best k: {best_k}")
print(f"Test Accuracy: {accuracy}")
```

Best k: 8

Test Accuracy: 0.7246376811594203

```
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import pandas as od
from sklearn.model_selection import train_test_split
from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
data = pd.read_excel('no_duplicates.xlsx')
df1 = pd.DataFrame(data)
# Separate features (X) and target variable (y)
X = df1.drop('Classification', axis=1)
y = df1['Classification']
# Split the dataset into training and testing sets (80% training, 20% testing)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
# Convert the continuous target values to discrete classes
y_train_classes = np.round(y_train)
y_test_classes = np.round(y_test)
# Initialize the KNN classifier
knn_model = KNeighborsClassifier(n_neighbors=8) # You can set the desired hyperparameters here
# Train the KNN model on the training set
knn_model.fit(X_train, y_train_classes)
# Predict the output (classes) on the training set
y_train_pred = knn_model.predict(X_train)
# Predict the output (classes) on the testing set
y_test_pred = knn_model.predict(X_test)
# Calculate accuracy on the training set
train_accuracy = accuracy_score(y_train_classes, y_train_pred)
# Calculate accuracy on the testing set
test_accuracy = accuracy_score(y_test_classes, y_test_pred)
# Calculate F1 score, precision, and recall on the testing set
f1 = f1_score(y_test_classes, y_test_pred, average='weighted') # 'weighted' takes class imbalance into account
precision = precision_score(y_test_classes, y_test_pred, average='weighted')
 # Calculate F1 score, precision, and recall on the testing set
  f1 = f1_score(y_test_classes, y_test_pred, average='weighted') # 'weighted' takes class imbalance into account
  precision = precision_score(y_test_classes, y_test_pred, average='weighted')
 recall = recall_score(y_test_classes, y_test_pred, average='weighted')
  # Display the results
 print("Training Accuracy:", train_accuracy)
 print("Testing Accuracy:", test_accuracy)
  print("F1 Score:", f1)
 print("Precision:", precision)
 print("Recall:", recall)
```

Training Accuracy: 0.7859733978234583
Testing Accuracy: 0.7246376811594203
F1 Score: 0.7238517036192456
Precision: 0.7230999930656682
Recall: 0.7246376811594203

```
[16]: import numpy as np
       import pandas as pd
       from sklearn.model_selection import train_test_split
from sklearn.neighbors import KNeighborsClassifier
       from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
       data = pd.read_excel('no_duplicates.xlsx')
       df1 = pd.DataFrame(data)
       # Separate features (X) and target variable (y)
       X = df1.drop('Classification', axis=1)
       y = df1['Classification']
       # Initialize lists to store evaluation metrics
       accuracy_list = []
       f1_list = []
precision_list = []
       recall_list = []
       # Set the number of iterations for random train-test splits
       num iterations = 10
       # Run the model on multiple random train-test splits
       for _ in range(num_iterations):
            # Split the dataset into training and testing sets
            X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=np.random.randint(1, 100))
            # Convert the continuous target values to discrete classes
           y_train_classes = np.round(y_train)
y_test_classes = np.round(y_test)
            # Initialize the KNN classifier
           knn_model = KNeighborsClassifier(n_neighbors=8)
           # Train the KNN model on the training set
           knn_model.fit(X_train, y_train_classes)
            # Predict the output (classes) on the testing set
           y_test_pred = knn_model.predict(X_test)
```

```
f1 = f1_score(y_test_classes, y_test_pred, average='weighted')
precision = precision_score(y_test_classes, y_test_pred, average='weighted')
     recall = recall_score(y_test_classes, y_test_pred, average='weighted')
     # Append metrics to the lists
     accuracy list.append(accuracy)
     f1_list.append(f1)
     precision_list.append(precision)
     recall_list.append(recall)
# Calculate mean and standard deviation for each metric
mean_accuracy = np.mean(accuracy_list)
mean_f1 = np.mean(f1_list)
mean_precision = np.mean(precision_list)
mean_recall = np.mean(recall_list)
std_accuracy = np.std(accuracy_list)
std_f1 = np.std(f1_list)
std_precision = np.std(precision_list)
std_recall = np.std(recall_list)
# Display the results
print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
print("Mean Recall:", mean_recall)
print("Standard Deviation Accuracy:", std_accuracy)
print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
```

Mean Accuracy: 0.7318840579710144
Mean F1 Score: 0.7149047366793011
Mean Precision: 0.714629858188255
Mean Recall: 0.7318840579710144
Standard Deviation Accuracy: 0.02319343745730975
Standard Deviation F1 Score: 0.024610261248219932
Standard Deviation Precision: 0.0253862962701297

SUPER VECTOR MACHINE(SVM): (calculating accuracy, precison, f1 score, recall):

```
[17]: import numpy as np
       from sklearn.model_selection import GridSearchCV, train_test_split
       from sklearn.svm import SVC
       from sklearn.metrics import accuracy_score
       data = pd.read_excel('no_duplicates.xlsx')
       df1 = pd.DataFrame(data)
       # Separate features (X) and target variable (y)
      X = df1.drop('Classification', axis=1)
       y = df1['Classification']
       # Split the data
       X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
       # Define the parameter grid
       param_grid =
           'C': [0.1, 1, 10, 100],
          'kernel': ['linear', 'rbf'],
'gamma': ['scale', 'auto', 0.1, 0.01, 0.001]
       # Create the SVM classifier
       svm = SVC()
       # Create GridSearchCV object
      grid_search = GridSearchCV(svm, param_grid, cv=5, scoring='accuracy')
       grid_search.fit(X_train, y_train)
       best_params = grid_search.best_params_
       # Train the final model with the best hyperparameters
       final_model = SVC(**best_params)
       final_model.fit(X_train, y_train)
       # Predict on the test set
      y_pred = final_model.predict(X_test)
      accuracy = accuracy_score(y_test, y_pred)
print(f"Best hyperparameters: {best_params}")
      print(f"Test Accuracy: {accuracy}")
      Best hyperparameters: {'C': 1, 'gamma': 0.1, 'kernel': 'rbf'}
      Test Accuracy: 0.7729468599033816
[8]: import numpy as np
     import pandas as pd
     from sklearn.model_selection import train_test_split
     from sklearn.metrics import accuracy_score, f1_score, precision_score, recall score
     # Read the data from the Excel file
     data = pd.read_excel('no_duplicates.xlsx')
    df1 = pd.DataFrame(data)
     \# Separate features (X) and target variable (y)
    X = df1.drop('Classification', axis=1)
     # Split the dataset into training and testing sets (80% training, 20% testing)
    X\_train,\ X\_test,\ y\_train,\ y\_test\ =\ train\_test\_split(X,\ y,\ test\_size=0.2,\ random\_state=42)
    svm_model = SVC(kernel='rbf', C=1.0) # You can set the desired hyperparameters here
    svm_model.fit(X_train, y_train)
    # Predict the output on the training set
    y_train_pred = svm_model.predict(X_train)
    y_test_pred = svm_model.predict(X_test)
     # Calculate accuracy on the training set
    train_accuracy = accuracy_score(y_train, y_train_pred)
     # Calculate accuracy on the testing set
    test_accuracy = accuracy_score(y_test, y_test_pred)
     # Calculate F1 score, precision, and recall on the testing set
```

f1 = f1 score(y test, y test pred, average='weighted') # 'weighted' takes class imbalance into account

```
# Calculate F1 score, precision, and recall on the testing set
f1 = f1_score(y_test, y_test_pred, average='weighted') # 'weighted' takes class imbalance into account
precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
        # Display the results
       print("Training Accuracy:", train_accuracy)
print("Testing Accuracy:", test_accuracy)
print("F1 Score:", f1)
print("Precision:", precision)
print("Recall:", recall)
       Training Accuracy: 0.7654171704957679
Testing Accuracy: 0.782608695652174
F1 Score: 0.747911515619481
Precision: 0.7748109640831757
        Recall: 0.782608695652174
[19]: import numpy as np
         import pandas as pd
from sklearn.model_selection import train_test_split
          from sklearn.svm import SVC
          from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
         # Read the data from the Excel file
data = pd.read_excel('no_duplicates.xlsx')
         df1 = pd.DataFrame(data)
         # Separate features (X) and target variable (y)
X = df1.drop('Classification', axis=1)
y = df1['Classification']
          # Initialize lists to store evaluation metrics
         accuracy_list = []
f1_list = []
          precision_list = []
         recall_list = []
          # Set the number of iterations for random train-test splits
         num_iterations = 10
          # Run the SVM model on multiple random train-test splits
         for _ in range(num_iterations):
    # Split the dataset into training and testing sets
               X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=np.random.randint(1, 100))
              # Initialize the SVM classifier
svm_model = SVC(kernel='rbf', C=1.0)
               # Train the SVM model on the training set
               svm_model.fit(X_train, y_train)
               # Predict the output on the testing set
               y_test_pred = svm_model.predict(X_test)
              # Calculate evaluation metrics
              accuracy = accuracy score(y test, y test pred)
```

```
accuracy = accuracy_score(y_test, y_test_pred)
f1 = f1_score(y_test, y_test_pred, average='weighted')
precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
       # Append metrics to the lists
       accuracy_list.append(accuracy)
      f1_list.append(f1)
precision_list.append(precision)
       recall_list.append(recall)
# Calculate mean and standard deviation for each metric
mean_accuracy = np.mean(accuracy_list)
mean_f1 = np.mean(f1_list)
mean_precision = np.mean(precision_list)
mean_recall = np.mean(recall_list)
std_accuracy = np.std(accuracy_list)
std_f1 = np.std(f1_list)
std_precision = np.std(precision_list)
std_recall = np.std(recall_list)
# Display the results
print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
print("Mean Recall:", mean_recall)
print("Standard Deviation Accuracy:", std_accuracy)
print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
Mean Accuracy: 0.7521739130434782
Mean F1 Score: 0.6994897563938427
Mean Precision: 0.7526735341015847
Mean Recall: 0.7521739130434782
Standard Deviation F1 Score: 0.03595564471430314
Standard Deviation F1 Score: 0.03595564471430314
Standard Deviation Precision: 0.03030597081159757
```

DECISION TREE: (calculating accuracy, precison, f1 score, recall):

```
: import pandas as pd
   from sklearn.model_selection import GridSearchCV, train_test_split
   from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy_score
   # Read the data from the Excel file
data = pd.read_excel('no_duplicates.xlsx')
    df1 = pd.DataFrame(data)
    \# Separate features (X) and target variable (y)
   X = df1.drop('Classification', axis=1)
    y = df1['Classification']
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
    # Define the parameter grid for Decision Tree
    param_grid = {
        ram_grid = {
  'criterion': ['gini', 'entropy'],
  'max_depth': [None, 10, 20, 30, 40, 50],
  'min_samples_split': [2, 5, 10],
  'min_samples_leaf': [1, 2, 4],
  'max_features': [None, 'sqrt', 'log2']
   # Create the Decision Tree classifier
   dt_classifier = DecisionTreeClassifier()
    # Create GridSearchCV object
    grid_search = GridSearchCV(dt_classifier, param_grid, cv=5, scoring='accuracy')
    {\tt grid\_search.fit}({\tt X\_train,\ y\_train})
    # Get the best hyperparameters
    best_params = grid_search.best_params_
    # Train the final model with the best hyperparameters
    final_model = DecisionTreeClassifier(**best_params)
   final_model.fit(X_train, y_train)
```

```
grid search.fit(X train, y train)
    # Get the best hyperparameters
    best params = grid search.best params
    # Train the final model with the best hyperparameters
final_model = DecisionTreeClassifier(**best_params)
    final\_model.fit(X\_train, y\_train)
    y_pred = final_model.predict(X_test)
    # Evaluate the model
    accuracy = accuracy_score(y_test, y_pred)
print(f"Best hyperparameters: {best_params}")
    print(f"Test Accuracy: {accuracy}")
    Best hyperparameters: {'criterion': 'gini', 'max depth': 10, 'max features': 'sqrt', 'min samples leaf': 2, 'min samples split': 5}
    Test Accuracy: 0.6763285024154589
                                                                                                                                                                     ★ 10 个 ↓ 占 〒 1
[21]: import numpy as np
        import pandas as pd
        from sklearn.model selection import train test split
        from sklearn.tree import DecisionTreeClassifier
         \begin{tabular}{ll} {\bf from mathins metrics import accuracy\_score, f1\_score, precision\_score, recall\_score \\ {\bf from math import sqrt} & \#Add & this import statement \\ \end{tabular} 
        # Read the data from the Excel file
        data = pd.read_excel('no_duplicates.xlsx')
df1 = pd.DataFrame(data)
        # Separate features (X) and target variable (y)
        X = df1.drop('Classification', axis=1)
y = df1['Classification']
        # Split the dataset into training and testing sets (80% training, 20% testing)
        X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
        # Initialize the Decision Tree classifier
        dt_model = DecisionTreeClassifier(criterion='entropy', max_depth=50, min_samples_split=10, min_samples_leaf=4, max_features='sqrt')
         # Train the Decision Tree model on the training set
        dt_model.fit(X_train, y_train)
        # Predict the output on the training set
y_train_pred = dt_model.predict(X_train)
        # Predict the output on the testing set
        y_test_pred = dt_model.predict(X_test)
        # Calculate accuracy on the training set
        train_accuracy = accuracy_score(y_train, y_train_pred)
        # Calculate accuracy on the testing set
        test_accuracy = accuracy_score(y_test, y_test_pred)
        # Calculate F1 score, precision, and recall on the testing set
f1 = f1_score(y_test, y_test_pred, average='weighted') # 'weighted' takes class imbalance into account
precision = precision_score(y_test, y_test_pred, average='weighted')
        recall = recall score(v test, v test pred, average='weighted')
# Calculate F1 score, precision, and recall on the testing set
f1 = f1_score(y_test, y_test_pred, average='weighted') # 'weighted' takes class imbalance into account
precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
# Display the results
print("Training Accuracy:", train_accuracy)
print("Testing Accuracy:", test_accuracy)
print("F1 Score:", f1)
print("Precision:", precision)
print("Recall:", recall)
Training Accuracy: 0.939540507859734
Testing Accuracy: 0.6811594202898551
F1 Score: 0.6860340443612366
Precision: 0.6919927133207591
Recall: 0.6811594202898551
```

```
[22]: import numpy as np
        import pandas as pd
        from sklearn.model_selection import train_test_split
from sklearn.tree import DecisionTreeClassifier
         from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
        # Read the data from the Excel file
        data = pd.read_excel('no_duplicates.xlsx')
df1 = pd.DataFrame(data)
        \# Separate features (X) and target variable (y)
        X = df1.drop('Classification', axis=1)
y = df1['Classification']
        # Initialize lists to store evaluation metrics
         accuracy_list = []
        f1 list = [
        precision_list = []
        recall list = []
        # Set the number of iterations for random train-test splits
        num_iterations = 10
         # Run the Decision Tree model on multiple random train-test splits
        for _ in range(num_iterations):
    # Split the dataset into training and testing sets
             X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=np.random.randint(1, 100))
             # Initialize the Decision Tree classifier
             dt model = DecisionTreeClassifier(criterion='entropy', max depth=50, min samples split=10, min samples leaf=4, max features='sgrt')
             # Train the Decision Tree model on the training set
             dt_model.fit(X_train, y_train)
             # Predict the output on the testing set
             y_test_pred = dt_model.predict(X_test)
            # Calculate evaluation metric
             accuracy = accuracy score(v test, v test pred)
         f1 = f1_score(y_test, y_test_pred, average='weighted')
          f1 = f1_score(y_test, y_test_pred, average='weighted')
          precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
          # Append metrics to the lists
          accuracy_list.append(accuracy)
          f1_list.append(f1)
precision_list.append(precision)
          recall_list.append(recall)
     # Calculate mean and standard deviation for each metric
     mean_accuracy = np.mean(accuracy_list)
mean_f1 = np.mean(f1_list)
     mean_precision = np.mean(precision_list)
mean_recall = np.mean(recall_list)
     std_accuracy = np.std(accuracy_list)
std_f1 = np.std(f1_list)
     std_precision = np.std(precision_list)
     std_recall = np.std(recall_list)
     # Display the results+
     print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
     print("Mean Recall:", mean_recall)
     print("Standard Deviation Accuracy:", std accuracy)
     print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
     Mean Accuracy: 0.6690821256038648
Mean F1 Score: 0.6664828862927621
     Mean Precision: 0.6659753793759758
     Mean Recall: 0.6690821256038648
     Standard Deviation Accuracy: 0.049419605116123734
Standard Deviation F1 Score: 0.04995152623662305
     Standard Deviation Precision: 0.05172054676452486
Standard Deviation Recall: 0.049419605116123734
```

RANDOM FOREST: (calculating accuracy, precison, f1 score, recall):

```
import pandas as pd
from sklearn.model_selection import train_test_split, GridSearchCV
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import accuracy_score
# Read the data from the Excel file
df1 = pd.DataFrame(data)
# Separate features (X) and target variable (v)
X = df1.drop('Classification', axis=1)
y = df1['Classification']
# Split the dataset into training and testing sets (80% training, 20% testing)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
# Define the parameter grid for Random Forest
     'n_estimators': [50, 100, 200],
    'max_depth': [None, 10, 20, 30],
'min_samples_split': [2, 5, 10],
'min_samples_leaf': [1, 2, 4],
    'bootstrap': [True, False]
# Additional parameters for Random Forest can be added here
# Create the Random Forest classifier
rf = RandomForestClassifier()
# Create GridSearchCV object
grid_search = GridSearchCV(rf, param_grid, cv=5, scoring='accuracy')
{\tt grid\_search.fit}({\tt X\_train,\ y\_train})
best_params = grid_search.best_params_
# Train the final model with the best hyperparameters
# Train the final model with the best hyperparameters
final_model = RandomForestClassifier(**best_params)
```

```
# Train the final model with the best hyperparameters
final_model = RandomForestClassifier(**best_params)
final_model.fit(X_train, y_train)

# Predict on the test set
y_pred = final_model.predict(X_test)

# Evaluate the model
accuracy = accuracy_score(y_test, y_pred)
print(f"Best hyperparameters: {best_params}")
print(f"Test Accuracy: {accuracy}")
```

Best hyperparameters: {'bootstrap': False, 'max_depth': None, 'min_samples_leaf': 4, 'min_samples_split': 5, 'n_estimators': 50}
Test Accuracy: 0.7536231884057971

```
[*]: import numpy as np
      import pandas as pd
      \textbf{from} \  \, \text{sklearn.model\_selection} \  \, \textbf{import} \  \, \text{train\_test\_split}
       from sklearn.ensemble import RandomForestClassifier
       from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
      # Read the data from the Excel file
      data = pd.read_excel('no_duplicates.xlsx')
      df1 = pd.DataFrame(data)
      # Separate features (X) and target variable (y)
      X = df1.drop('Classification', axis=1)
      v = df1['Classification']
      # Initialize lists to store evaluation metrics
      accuracy_list = []
      f1_list = []
precision_list = []
      recall_list = []
      \# Set the number of iterations for random train-test splits
      num iterations = 10
      # Run the Random Forest model on multiple random train-test splits
      for _ in range(num_iterations):
           # Split the dataset into training and testing sets
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=np.random.randint(1, 100))
          rf = RandomForestClassifier()
          # Train the Random Forest model on the training set
          rf.fit(X_train, y_train)
          # Predict the output on the testing set
          y_test_pred = rf.predict(X_test)
      # Calculate evaluation metrics
        accuracy = accuracy_score(y_test, y_test_pred)
        f1 = f1_score(y_test, y_test_pred, average='weighted')
        precision = precision_score(y_test, y_test_pred, average='weighted')
       recall = recall_score(y_test, y_test_pred, average='weighted')
       # Append metrics to the lists
       accuracy_list.append(accuracy)
        f1_list.append(f1)
       precision_list.append(precision)
       recall list.append(recall)
   # Calculate mean and standard deviation for each metric
   mean_accuracy = np.mean(accuracy_list)
   mean_f1 = np.mean(f1_list)
   mean_precision = np.mean(precision_list)
   mean_recall = np.mean(recall_list)
   std_accuracy = np.std(accuracy_list)
   std_f1 = np.std(f1_list)
  std_precision = np.std(precision_list)
std_recall = np.std(recall_list)
   # Display the results
  # Display the results
print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
   print("Mean Recall:", mean_recall)
   print("Standard Deviation Accuracy:", std_accuracy)
   print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
   print("Standard Deviation Recall:", std_recall)
   Mean Accuracy: 0.7493212669683258
   Mean F1 Score: 0.7179199306111091
   Mean Precision: 0.7267727187692207
Mean Recall: 0.7493212669683258
   Standard Deviation Accuracy: 0.017664453661487025
   Standard Deviation F1 Score: 0.01999324826848087
Standard Deviation Procession: 0.01999324826848087
```

AFTER FEATURE SELECTION CODES:

KNN CLASSIFIER:

```
[5]: import numpy as no
     \textbf{from} \  \, \text{sklearn.model\_selection} \  \, \textbf{import} \  \, \text{train\_test\_split}
      from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
      from sklearn.neighbors import KNeighborsClassifier
     # Load the data from the Excel file
     data = pd.read_excel('no_duplicates.xlsx')
     df1 = pd.DataFrame(data)
     X = df1.drop('Classification', axis=1)
y = df1['Classification']
     # Calculate the correlation matrix
     mask = np.triu(np.ones_like(correlation_matrix, dtype=bool))
     # Set the threshold for high correlation
threshold = 0.8  # Example threshold (change as needed)
      # Find index of feature columns with correlation greater than the threshold
     high_correlation = correlation_matrix.mask(mask).stack() > threshold
     high_correlation_features = high_correlation[high_correlation].index.tolist()
      # Get unique features involved in high correlation
      features_to_drop = set()
      for feat1, feat2 in high_correlation_features:
        features_to_drop.add(feat1 if correlation_matrix.loc[feat1, 'Classification'] < correlation_matrix.loc[feat2, 'Classification'] else feat2)
      # Drop highly correlated features from the dataset
     X_filtered = X.drop(columns=features_to_drop)
      # Initialize lists to store evaluation metrics
     accuracy_list = []
f1_list = []
precision_list = []
    precision_list = []
     recall_list = []
    # Set the number of iterations for random train-test splits
    num iterations = 10
     # Run the KNN model on multiple random train-test splits
    for _ in range(num_iterations):
         # Split the dataset into training and testing sets
         X\_train, \ X\_test, \ y\_train, \ y\_test = train\_test\_split(X\_filtered, \ y, \ test\_size=0.2, \ random\_state=np.random.randint(1, \ 100)) 
         # Initialize the KNN classifier
         knn = KNeighborsClassifier(n_neighbors=8) # Adjust parameters as needed
         # Train the KNN model on the training set
         knn.fit(X_train, y_train)
         # Predict the output on the testing set
        y_test_pred = knn.predict(X_test)
        # Calculate evaluation metrics
         accuracy = accuracy_score(y_test, y_test_pred)
         f1 = f1_score(y_test, y_test_pred, average='weighted')
         precision = precision_score(y_test, y_test_pred, average='weighted')
         recall = recall_score(y_test, y_test_pred, average='weighted')
         # Append metrics to the lists
         accuracy_list.append(accuracy)
         f1 list.append(f1)
         precision list.append(precision)
         recall_list.append(recall)
     # Calculate mean and standard deviation for each metric
    mean accuracy = np.mean(accuracy list)
    mean_f1 = np.mean(f1_list)
    mean_precision = np.mean(precision_list)
    mean_recall = np.mean(recall_list)
    std_accuracy = np.std(accuracy_list)
    std_f1 = np.std(f1_list)
```

```
std_precision = np.std(precision_list)

std_recall = np.std(recall_list)

# Display the results

print("Mean Accuracy:", mean_accuracy)

print("Mean F1 Score:", mean_f1)

print("Mean Precision:", mean_precision)

print("Mean Precision:", mean_recall)

print("Standard Deviation Accuracy:", std_accuracy)

print("Standard Deviation F1 Score:", std_f1)

print("Standard Deviation Precision:", std_precision)

print("Standard Deviation Recall:", std_precision)

print("Standard Deviation Recall:", std_precision)

Mean Accuracy: 0.7294685990338163

Mean F1 Score: 0.7085109487242736

Mean Precision: 0.7130388948897278

Mean Recall: 0.7294685990338163

Standard Deviation Accuracy: 0.021926194623981113

Standard Deviation Precision: 0.02748986023943192

Standard Deviation Precision: 0.02748986023943192

Standard Deviation Recall: 0.021926194623981113
```

SVM(SUPPORT VECTOR MACHINE):

```
import pandas as pd
\textbf{from} \  \, \text{sklearn.model\_selection} \  \, \textbf{import} \  \, \text{train\_test\_split}
from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
from sklearn.svm import SVC
from sklearn.preprocessing import StandardScaler
# Load the data from the Excel file
data = pd.read_excel('no_duplicates.xlsx')
df1 = pd.DataFrame(data)
# Separate features (X) and target variable (y)
X = df1.drop('Classification', axis=1)
y = df1['Classification']
# Calculate the correlation matrix
correlation_matrix = X.corr().abs()
# Create a mask to ignore the upper triangle of the correlation matrix
mask = np.triu(np.ones_like(correlation_matrix, dtype=bool))
# Set the threshold for high correlation
threshold = 0.8 # Example threshold (change as needed)
# Find index of feature columns with correlation greater than the threshold
high_correlation = correlation_matrix.mask(mask).stack() > threshold
high_correlation_features = high_correlation[high_correlation].index.tolist()
# Get unique features involved in high correlation
features_to_drop = set()
for feat1, feat2 in high_correlation_features:
    features_to_drop.add(feat1 if correlation_matrix.loc[feat1, 'Classification'] < correlation_matrix.loc[feat2, 'Classification'] else feat2)
# Drop highly correlated features from the dataset
X_filtered = X.drop(columns=features_to_drop)
scaler = StandardScaler()
X_filtered_standardized = scaler.fit_transform(X_filtered)
```

```
# Standardize the features using StandardScaler
  scaler = StandardScaler()
  X_filtered_standardized = scaler.fit_transform(X_filtered)
  # Initialize lists to store evaluation metrics
  accuracy_list = []
  f1_list = []
precision_list = []
  recall list = []
  # Set the number of iterations for random train-test splits
  num iterations = 10
  # Run the SVM model on multiple random train-test splits
  for _ in range(num_iterations):
       # Split the dataset into training and testing sets

X_train, X_test, y_train, y_test = train_test_split(X_filtered_standardized, y, test_size=0.2, random_state=np.random.randint(1, 100))
       # Initialize the SVM classifier
       svm_model = SVC(kernel='rbf', C=1.0)
# Train the SVM model on the training set
       svm_model.fit(X_train, y_train)
       # Predict the output on the testing set
       y_test_pred = svm_model.predict(X_test)
       # Calculate evaluation metrics
       accuracy = accuracy_score(y_test, y_test_pred)
       action of actionary store yets, y_test_pred, average='weighted')
precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
       # Append metrics to the lists
       accuracy_list.append(accuracy)
f1_list.append(f1)
       precision_list.append(precision)
       recall_list.append(recall)
  # Calculate mean and standard deviation for each metric
  mean_accuracy = np.mean(accuracy_list)
# Calculate mean and standard deviation for each metric
mean_accuracy = np.mean(accuracy_list)
mean_f1 = np.mean(f1_list)
mean_precision = np.mean(precision_list)
mean_recall = np.mean(recall_list)
std accuracy = np.std(accuracy list)
std_f1 = np.std(f1_list)
std_precision = np.std(precision_list)
std_recall = np.std(recall_list)
# Display the results
print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
print("Mean Recall:", mean_recall)
print("Standard Deviation Accuracy:", std_accuracy)
print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
Mean Accuracy: 0.7468599033816424
Mean F1 Score: 0.7118455765929317
Mean Precision: 0.732581213416721
Mean Recall: 0.7468599033816424
```

Standard Deviation F1 Score: 0.024840502670883943 Standard Deviation F1 Score: 0.027977276752283075 Standard Deviation Precision: 0.030488572383062372 Standard Deviation Recall: 0.024840502670883943



```
[20]: import numpy as np
       import pandas as pd
       from sklearn.model_selection import train_test_split
       from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
from sklearn.tree import DecisionTreeClassifier
       # Load the data from the Excel file
       data = pd.read_excel('no_duplicates.xlsx')
       df1 = pd.DataFrame(data)
       # Separate features (X) and target variable (y)
       X = df1.drop('Classification', axis=1)
       y = df1['Classification']
       # Calculate the correlation matrix
       correlation_matrix = X.corr().abs()
       # Create a mask to ignore the upper triangle of the correlation matrix
       mask = np.triu(np.ones_like(correlation_matrix, dtype=bool))
       # Set the threshold for high correlation
       threshold = 0.8 # Example threshold (change as needed)
       # Find index of feature columns with correlation greater than the threshold
high_correlation = correlation_matrix.mask(mask).stack() > threshold
       high_correlation_features = high_correlation[high_correlation].index.tolist()
        # Get unique features involved in high correlation
       features to drop = set()
       for feat1, feat2 in high_correlation_features:
           features_to_drop.add(feat1 if correlation_matrix.loc[feat1, 'Classification'] < correlation_matrix.loc[feat2, 'Classification'] else feat2)
        # Drop highly correlated features from the dataset
       X filtered = X.drop(columns=features to drop)
       # Initialize lists to store evaluation metrics
       accuracy_list = []
       f1_list = []
precision_list = []
precision_ist = []
       recall_list = []
       # Set the number of iterations for random train-test splits
       num iterations = 10
       # Run the Decision Tree model on multiple random train-test splits
       for _ in range(num_iterations):
            # Split the dataset into training and testing sets
           X_train, X_test, y_train, y_test = train_test_split(X_filtered, y, test_size=0.2, random_state=np.random.randint(1, 100))
           decision_tree = DecisionTreeClassifier(criterion='entropy', max_depth=50, min_samples_split=10, min_samples_leaf=4, max_features='sqrt') # Adjust pai
           # Train the Decision Tree model on the training set
           decision_tree.fit(X_train, y_train)
           # Predict the output on the testing set
           y_test_pred = decision_tree.predict(X_test)
           accuracy = accuracy_score(y_test, y_test_pred)
f1 = f1_score(y_test, y_test_pred, average='weighted')
           precision = precision_score(y_test, y_test_pred, average='weighted')
recall = recall_score(y_test, y_test_pred, average='weighted')
           # Append metrics to the lists
            accuracy_list.append(accuracy)
           f1 list.append(f1)
           precision_list.append(precision)
           recall_list.append(recall)
       # Calculate mean and standard deviation for each metric
       mean_accuracy = np.mean(accuracy_list)
      mean_f1 = np.mean(f1_list)
mean_precision = np.mean(precision_list)
       mean_recall = np.mean(recall_list)
       std_accuracy = np.std(accuracy_list)
       std_f1 = np.std(f1_list)
std precision = np.std(precision list)
```

```
# Calculate mean and standard deviation for each metric
mean_accuracy = np.mean(accuracy_list)
mean_rf1 = np.mean(f1_list)
mean_recision = np.mean(precision_list)
mean_recall = np.mean(recall_list)

std_accuracy = np.std(accuracy_list)
std_f1 = np.std(f1_list)
std_precision = np.std(precision_list)
std_precision = np.std(precision_list)
std_recall = np.std(precision_list)

# Display the results
print("Mean Accuracy:", mean_accuracy)
print("Mean Precision:", mean_precision)
print("Mean Precision:", mean_precision)
print("Standard Deviation Accuracy:", std_accuracy)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
```

Mean Accuracy: 0.6492753623188406 Mean F1 Score: 0.6481860006601761 Mean Precision: 0.6483451174923448 Mean Recall: 0.6492753623188406

Standard Deviation Accuracy: 0.02682790990708179 Standard Deviation F1 Score: 0.02815674220787503 Standard Deviation Precision: 0.030436615337206763 Standard Deviation Recall: 0.02682790990708179

RANDOM FOREST:

```
[23]: import numpy as np
       import pandas as pd
       from sklearn.model_selection import train_test_split
       from sklearn.metrics import accuracy_score, f1_score, precision_score, recall_score
       from sklearn.ensemble import RandomForestClassifier
       from sklearn.preprocessing import StandardScaler
       # Load the data from the Excel file
       data = pd.read_excel('no_duplicates.xlsx')
      df1 = pd.DataFrame(data)
      \# Separate features (X) and target variable (y)
      X = df1.drop('Classification', axis=1)
      y = df1['Classification']
      correlation_matrix = X.corr().abs()
      # Create a mask to ignore the upper triangle of the correlation matrix
      mask = np.triu(np.ones_like(correlation_matrix, dtype=bool))
       # Set the threshold for high correlation
      threshold = 0.8 # Example threshold (change as needed)
      high_correlation = correlation_matrix.mask(mask).stack() > threshold
high_correlation_features = high_correlation[high_correlation].index.tolist()
       # Get unique features involved in high correlation
       for feat1, feat2 in high correlation features:
           features to drop.add(feat1 if correlation_matrix.loc[feat1, 'Classification'] < correlation_matrix.loc[feat2, 'Classification'] else feat2)
       # Drop highly correlated features from the dataset
      X_filtered = X.drop(columns=features_to_drop)
       # Standardize the features using StandardScaler
       scaler = StandardScaler()
       X_filtered_standardized = scaler.fit_transform(X_filtered)
```

```
# Initialize lists to store evaluation metrics
 accuracy_list = []
 f1_list = []
precision_list = []
 recall_list = []
 # Set the number of iterations for random train-test splits
 num iterations = 10
 # Run the Random Forest model on multiple random train-test splits
 for _ in range(num_iterations):
      # Split the dataset into training and testing sets
     \textbf{X\_train, X\_test, y\_train, y\_test = train\_test\_split(\textbf{X\_filtered\_standardized, y, test\_size=0.2, random\_state=np.random.randint(1, 100))}
      # Initialize the Random Forest classifier
      param_grid = {
      'n_estimators': [50, 100, 200],
      'max_depth': [None, 10, 20, 30], 'min_samples_split': [2, 5, 10],
      'min_samples_leaf': [1, 2, 4],
      'bootstrap': [True, False]
      # Additional parameters for Random Forest can be added here
      rf = RandomForestClassifier(n_estimators=50, random_state=42)
      # Train the Random Forest model on the training set
      rf.fit(X_train, y_train)
     # Predict the output on the testing set
y_test_pred = rf.predict(X_test)
      # Calculate evaluation metrics
      accuracy = accuracy_score(y_test, y_test_pred)
      f1 = f1_score(y_test, y_test_pred, average='weighted')
precision = precision_score(y_test, y_test_pred, average='weighted')
      recall = recall_score(y_test, y_test_pred, average='weighted')
      # Annend metrics to the Lists
     # Append metrics to the lists
     accuracy_list.append(accuracy)
     f1 list.append(f1)
     precision_list.append(precision)
     recall_list.append(recall)
# Calculate mean and standard deviation for each metric
mean_accuracy = np.mean(accuracy_list)
mean_f1 = np.mean(f1_list)
mean_precision = np.mean(precision_list)
mean_recall = np.mean(recall_list)
std_accuracy = np.std(accuracy_list)
std_f1 = np.std(f1_list)
std_recall = np.std(recall_list)
std_recall = np.std(recall_list)
print("Mean Accuracy:", mean_accuracy)
print("Mean F1 Score:", mean_f1)
print("Mean Precision:", mean_precision)
print("Mean Recall:", mean_recall)
print("Standard Deviation Accuracy:", std_accuracy)
print("Standard Deviation F1 Score:", std_f1)
print("Standard Deviation Precision:", std_precision)
print("Standard Deviation Recall:", std_recall)
Mean Accuracy: 0.7314009661835749
Mean F1 Score: 0.6901696657909827
Mean Precision: 0.7035321660212347
Mean Recall: 0.7314009661835749
```

Standard Deviation Accuracy: 0.027768324373333174
Standard Deviation F1 Score: 0.03552162984686795
Standard Deviation Precision: 0.032355436373300656 Standard Deviation Recall: 0.027768324373333174

CODES AND OUTPUTS OF PLOTTINGS:

```
import matplotlib.pyplot as plt
import numpy as np

# Data for the models, mean accuracy, and standard deviation
models = ['KNN', 'SVM', 'Decision Tree', 'RF']
mean_accuracy = [0.73, 0.75, 0.66, 0.73]
std_accuracy = [0.82, 0.82, 0.84, 0.82]

# Set the bar width
bar_width = 0.35

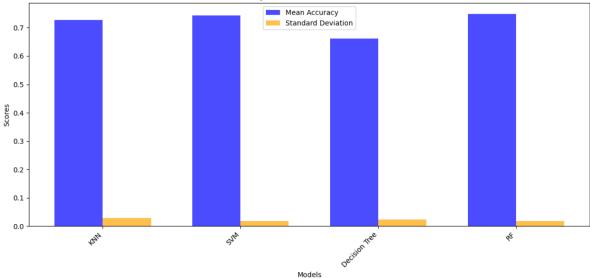
# Create a grouped bar plot for mean accuracy and standard deviation
fig, ax = plt.subplots(figsize=(12, 6))

bar1 = ax.bar(np.arange(len(models)), mean_accuracy, bar_width, color='blue', alpha=0.7, label='Mean Accuracy')
bar2 = ax.bar(np.arange(len(models)) + bar_width, std_accuracy, bar_width, color='orange', alpha=0.7, label='Standard Deviation')

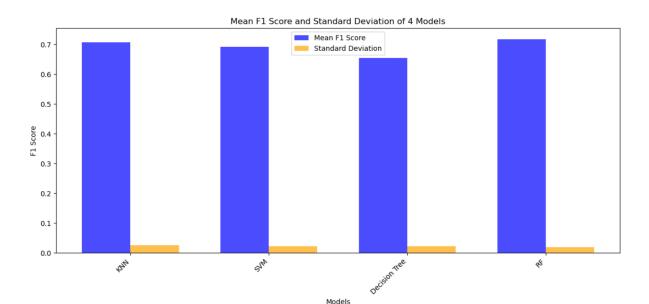
# Labeling and formatting
ax.set_xlabel('Models')
ax.set_xlabel('Models')
ax.set_xlabel('Crosses')
ax.set_xlabel('Crosses')
ax.set_xlabel('Crosses')
ax.set_xtick(ap.arange(len(models)) + bar_width / 2)
ax.set_xtick(ap.arange(len(models)), ha='right')
ax.legend()

# Show the plot
plt.tight_layout()
plt.show()
```

Mean Accuracy and Standard Deviation of 4 Models

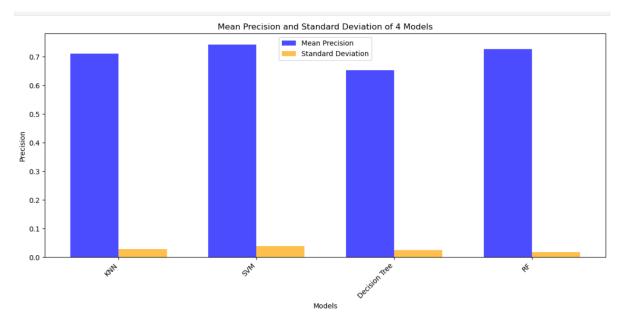


```
•[21]: import matplotlib.pyplot as plt
                                                                                                                                                                                   ≮厄个↓占早ⅰ
          # Data for the models, mean F1 score, and standard deviation models = ['KNN', 'SVM', 'Decision Tree', 'RF'] mean_f1 = [0.71, 0.69, 0.66, 0.71] std_f1 = [0.024, 0.03, 0.04, 0.01]
          # Set the bar width
          bar_width = 0.35
          # Create a grouped bar plot for mean F1 score and standard deviation
          fig, ax = plt.subplots(figsize=(12, 6))
          bar1 = ax.bar(np.arange(len(models)), mean_f1, bar_width, color='blue', alpha=0.7, label='Mean F1 Score')
bar2 = ax.bar(np.arange(len(models)) + bar_width, std_f1, bar_width, color='orange', alpha=0.7, label='Standard Deviation')
          # Labeling and formatting
          ax.set_title('Mean F1 Score and Standard Deviation of 4 Models')
ax.set_xlabel('Models')
          ax.set_ylabel('F1 Score')
          ax.set_xticks(np.arange(len(models)) + bar_width / 2)
          ax.set_xticklabels(models, rotation=45, ha='right')
          ax.legend()
          # Show the plot
          plt.show()
```



Models

```
import matplotlib.pyplot as plt
import numpy as np
# Data for the models, mean precision, and standard deviation
models = ['KNN', 'SVM', 'Decision Tree', 'RF']
mean_precision = [0.71, 0.75, 0.66, 0.72]
std_precision = [0.02, 0.03, 0.05, 0.01]
bar_width = 0.35
# Create a grouped bar plot for mean precision and standard deviation fig, ax = plt.subplots(figsize=(12, 6)) \,
bar1 = ax.bar(np.arange(len(models)), mean_precision, bar_width, color='blue', alpha=0.7, label='Mean Precision')
bar2 = ax.bar(np.arange(len(models)) + bar_width, std_precision, bar_width, color='orange', alpha=0.7, label='Standard Deviation')
# Labeling and formatting
ax.set_title('Mean Precision and Standard Deviation of 4 Models')
ax.set_valabel('Models')
ax.set_vlabel('Precision')
ax.set_vticks(np.arange(len(models)) + bar_width / 2)
ax.set_xticklabels(models, rotation=45, ha='right')
ax.legend()
# Show the plot
plt.tight_layout()
plt.show()
```



```
import matplotlib.pyplot as plt
import numpy as np

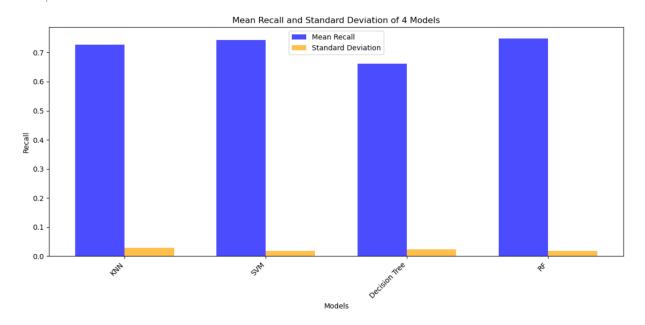
# Data for the models, mean recall, and standard deviation
models = ['KNN', 'SVN', 'Decision Tree', 'RF']
mean_recall = [0.73, 0.75, 0.66, 0.74]
std_recall = [0.02, 0.02, 0.04, 0.01]

# Set the bar width
bar_width = 0.35

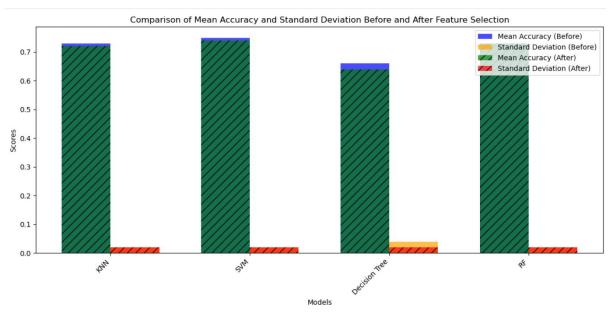
# Create a grouped bar plot for mean recall and standard deviation
fig, ax = plt.subplots(figsize=(12, 6))

bar1 = ax.bar(np.arange(len(models)), mean_recall, bar_width, color='blue', alpha=0.7, label='Mean Recall')
bar2 = ax.bar(np.arange(len(models)) + bar_width, std_recall, bar_width, color='orange', alpha=0.7, label='Standard Deviation')

# Labeling and formatting
ax.set_title('Mean Recall and Standard Deviation of 4 Models')
ax.set_vilabel('Models')
ax.set_vilabel('Models')
ax.set_vilabel('Recall') # Updated y-axis label
ax.set_xticks(np.arange(len(models)) + bar_width / 2)
ax.set_xticks(np.arange(len(models)) + bar_width / 2
```

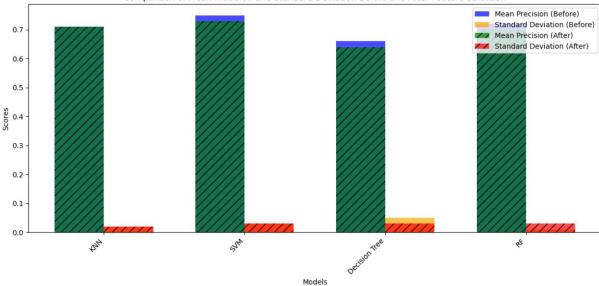


```
]: import matplotlib.pyplot as plt
    import numpy as np
    # Data for the models, mean accuracy, and standard deviation before feature selection models = ['KNN', 'SVM', 'Decision Tree', 'RF']
mean_accuracy_before = [0.73, 0.75, 0.66, 0.73]
std_accuracy_before = [0.02, 0.02, 0.04, 0.02]
    # Data for the models, mean accuracy, and standard deviation after feature selection mean_accuracy_after = [0.72, 0.74, 0.64, 0.73] std_accuracy_after = [0.02, 0.02, 0.02, 0.02]
    bar_width = 0.35
     # Create a grouped bar plot for mean accuracy and standard deviation before and after feature selection
    fig, ax = plt.subplots(figsize=(12, 6))
    bar1_before = ax.bar(np.arange(len(models)), mean_accuracy_before, bar_width, color='blue', alpha=0.7, label='Mean Accuracy (Before)')
    bar2_before = ax.bar(np.arange(len(models)) + bar_width, std_accuracy_before, bar_width, color='orange', alpha=0.7, label='Standard Deviation (Before)')
    bar1_after = ax.bar(np.arange(len(models)), mean_accuracy_after, bar_width, color='green', alpha=0.7, label='Mean Accuracy (After)', hatch='//')
bar2_after = ax.bar(np.arange(len(models)) + bar_width, std_accuracy_after, bar_width, color='red', alpha=0.7, label='Standard Deviation (After)', hatch=
    # Labeling and formatting
    ax.set_title('Comparison of Mean Accuracy and Standard Deviation Before and After Feature Selection')
    ax.set_xlabel('Models')
ax.set_ylabel('Scores')
    ax.set_xticks(np.arange(len(models)) + bar_width / 2)
    ax.set_xticklabels(models, rotation=45, ha='right')
    ax.legend()
     # Show the plot
    plt.tight_layout()
    plt.show()
```

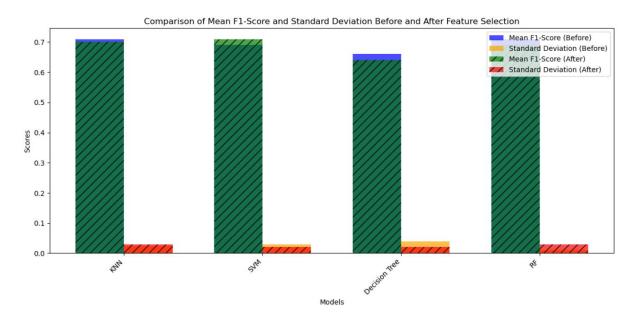


```
7]: import matplotlib.pyplot as plt
       import numpy as np
       # Data for the models, mean Precision, and standard deviation before feature selection
       models = ['KNN', 'SVM', 'Decision Tree', 'RF']
mean_precision_before = [0.71, 0.75, 0.66, 0.72]
std_precision_before = [0.02, 0.03, 0.05, 0.01]
       # Data for the models, mean Precision, and standard deviation after feature selection mean_precision_after = [0.71, 0.73, 0.64,0.70] std_precision_after = [0.02, 0.03, 0.03, 0.03]
       # Set the bar width
       bar_width = 0.35
       # Create a grouped bar plot for mean Precision and standard deviation before and after feature selection
       fig, ax = plt.subplots(figsize=(12, 6))
       bar1_before = ax.bar(np.arange(len(models)), mean_precision_before, bar_width, color='blue', alpha=0.7, label='Mean Precision (Before)')
bar2_before = ax.bar(np.arange(len(models)) + bar_width, std_precision_before, bar_width, color='orange', alpha=0.7, label='Standard Deviation (Before)')
       bar1_after = ax.bar(np.arange(len(models)), mean_precision_after, bar_width, color='green', alpha=0.7, label='Mean Precision (After)', hatch='//')
bar2_after = ax.bar(np.arange(len(models)) + bar_width, std_precision_after, bar_width, color='red', alpha=0.7, label='Standard Deviation (After)', hatch
       # Labeling and formatting
ax.set_title('Comparison of Mean Precision and Standard Deviation Before and After Feature Selection')
       ax.set_xlabel('Models')
ax.set_ylabel('Scores')
       ax.set_xticks(np.arange(len(models)) + bar_width / 2)
       ax.set_xticklabels(models, rotation=45, ha='right')
       ax.legend()
       # Show the plot
       plt.tight_layout()
       plt.show()
```





```
[45]: import matplotlib.pyplot as plt
           import numpy as np
          # Data for the models, mean F1-Score, and standard deviation before feature selection
          models = ['KNN', 'SVM', 'Decision Tree', 'RF']
mean_f1_before = [0.71, 0.69, 0.66, 0.71]
std_f1_before = [0.024, 0.03, 0.04, 0.01]
          # Data for the models, mean F1-Score, and standard deviation after feature selection mean\_f1\_after = [0.70, 0.71, 0.64, 0.69] std\_f1\_after = [0.03, 0.02, 0.02, 0.03]
          # Set the bar width
          bar_width = 0.35
          # Create a grouped bar plot for mean F1-Score and standard deviation before and after feature selection
          fig, ax = plt.subplots(figsize=(12, 6))
          bar1_before = ax.bar(np.arange(len(models)), mean_f1_before, bar_width, color='blue', alpha=0.7, label='Mean F1-Score (Before)')
bar2_before = ax.bar(np.arange(len(models)) + bar_width, std_f1_before, bar_width, color='orange', alpha=0.7, label='Standard Deviation (Before)')
          barl_after = ax.bar(np.arange(len(models)), mean_fl_after, bar_width, color='green', alpha=0.7, label='Mean F1-Score (After)', hatch='//')
bar2_after = ax.bar(np.arange(len(models)) + bar_width, std_fl_after, bar_width, color='red', alpha=0.7, label='Standard Deviation (After)', hatch='//')
          ax.set_title('Comparison of Mean F1-Score and Standard Deviation Before and After Feature Selection')
ax.set_xlabel('Models')
          ax.set_ylabel('Scores')
          ax.set_yiabel( scores )
ax.set_xticks(np.arange(len(models)) + bar_width / 2)
ax.set_xticklabels(models, rotation=45, ha='right')
          ax.legend()
          # Show the plot
          plt.tight_layout()
          plt.show()
```



```
[43]: import matplotlib.pyplot as plt
import numpy as np

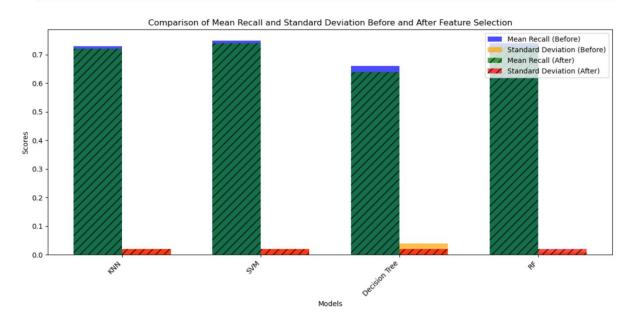
# Data for the models, mean Recall, and standard deviation before feature selection
models = ['KNM', 'SVM', 'Decision Tree', 'BF']
mean_recall_before = [0.32, 0.75, 0.66, 0.74]
std_recall_before = [0.32, 0.92, 0.04, 0.01]
# Data for the models, mean Recall, and standard deviation after feature selection
mean_recall_after = [0.02, 0.02, 0.04, 0.01]
# Set the bar width
bar_width = 0.35

# Create a grouped bar plot for mean Recall and standard deviation before and after feature selection
fig, ax = plt.subplots(figsize(12, 6))

barl_before = ax.bar(np.arange(len(models)), mean_recall_before, bar_width, color='blue', alpha=0.7, label='Mean Recall (Before)')
bar2_before = ax.bar(np.arange(len(models)), bar_width, std_recall_before, bar_width, color='orange', alpha=0.7, label='Standard Deviation (Before)')

bar1_after = ax.bar(np.arange(len(models)), bar_width, std_recall_after, bar_width, color='reen', alpha=0.7, label='Standard Deviation (Before)')

bar2_after = ax.bar(np.arange(len(models)) + bar_width, std_recall_after, bar_width, color='reen', alpha=0.7, label='Standard Deviation (After)', hatch='/
# labeling and formatting
ax.set_xlabel('Models')
ax.set_xlabel('Models')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Scores')
ax.set_xlabel('Models') har_width / 2)
ax.set_xlabel('Models')
ax.set_xlabel('Mo
```



Result and Analysis:

MODEL	TRAINING ACCURACY			PRECISION	RECALL
KNN	78.58%	72.46%	0.72	0.72	0.72
SVM	76.54%	78.26%	0.74	0.77	0.78
DECISION TREE	93.95%	68.11%	0.68	0.69	0.68
RF	99.03%	77.77%	0.76	0.76	0.77

Before Feature Selection:

a. **SVM** emerged as the best-performing model, with superior accuracy and precision compared to other models like RF, KNN, and Decision Trees.

Models	Accuracy		Precision		Recall		F1-Score	
	Mean	STD	Mean	STD	Mean	STD	Mean	STD
KNN	0.73	0.02	0.71	0.02	0.73	0.02	0.71	0.02
SVM	0.75	0.02	0.75	0.03	0.75	0.02	0.69	0.03
DECISION TREE	0.66	0.04	0.66	0.05	0.66	0.04	0.66	0.01
RF	0.73	0.02	0.72	0.01	0.74	0.01	0.71	0.01

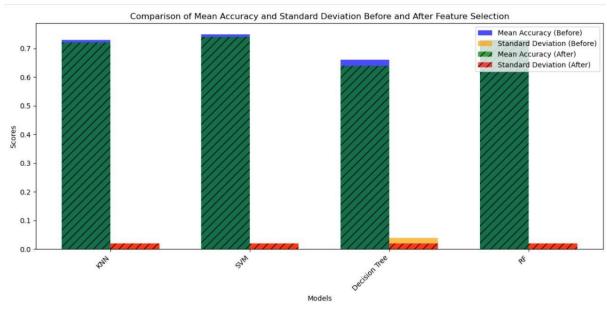
2. After Feature Selection:

- a. SVM maintained its position as the most accurate model, demonstrating resilience to dimensionality reduction.
- b. Mean accuracy slightly decreased post-feature selection, but the reduction in standard deviation indicated greater consistency.

Models	Accuracy		Precision		Recall		F1-Score	
	Mean	STD	Mean	STD	Mean	STD	Mean	STD
KNN	0.72	0.02	0.71	0.02	0.72	0.02	0.70	0.03
SVM	0.74	0.02	0.73	0.03	0.74	0.02	0.71	0.02
DECISION TREE	0.64	0.02	0.64	0.03	0.64	0.02	0.64	0.02
RF	0.73	0.02	0.70	0.03	0.73	0.02	0.69	0.03

3. Performance Metrics Visualization:

a. Bar plots of accuracy, precision, recall, and F1-scores highlighted SVM as the leading model across all metrics, followed by ensemble methods like Random Forest.



Explanation of MathBert:

MathBERT is a fine-tuned variant of BERT tailored for mathematical contexts. It processes mathematical language, equations, and problem statements effectively by leveraging contextual embeddings. These embeddings are dense vectors that encapsulate the meaning and structure of student responses, enabling accurate classification by ML models.

Transformation Process:

- 1. Convert raw text responses into embeddings using MathBERT.
- 2. Encode mathematical relationships and semantics into 385dimensional vectors for downstream ML tasks.

Conclusion:

- This project demonstrates the feasibility of automating the evaluation of descriptive algebra responses using MathBERT embeddings and machine learning classifiers.
- Among the tested models, SVM consistently outperformed others, proving to be the most effective for this task.
- Dimensionality reduction through feature selection further enhanced the consistency of the results.