Homework 1

TK2ICM: Logic Programming (CSH4Y3)

Chinese Lunisolar New Year

Second Term 2018-2019

Day, date : Tuesday, February 5, 2019

Duration : 9 hours (including submission: 12:00 a.m. – 9:00 p.m.)

Type : open all, individual, cooperation is allowed

Instruction:

 You are allowed to discuss these problems with other class participants, but make sure that you write the script individually. Copying answers from elsewhere without understanding them will not enhance your understanding.

- 2. You may use any reference (books, slides, internet) as well as ask other students who are not enrolled to this class.
- 3. Use the predicate name as described in each of the problem. **The name of the predicate must be precisely identical**. Typographical error may lead to the cancellation of your points.
- 4. Submit your work to the provided slot at google classroom under the file name Hwl-<your_name>.pl. For example: Hwl-Albert.pl. Please see an information regarding your nickname at google classroom.

Benjamin's family tree is depicted in Figure 1. The family tree is identical to that appeared in Problem Set 1.

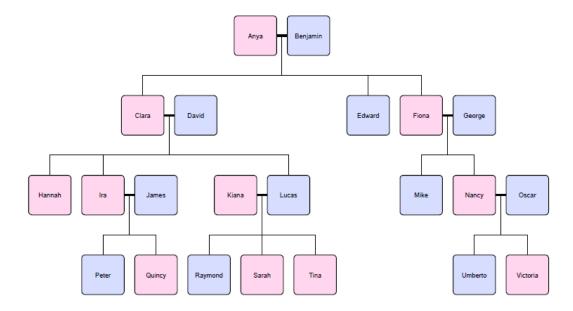


Figure 1: Benjamin's family tree.

We can derive a knowledge base from this tree as follows:

```
% male(X) denotes that X is a male.
male(benjamin).
male(david). male(edward). male(george).
male(james). male(lucas). male(mike). male(oscar).
male(peter). male(raymond). male(umberto).
% female(X) denotes that X is female.
female(anya).
female(clara). female(fiona).
female(hannah). female(ira). female(kiana). female(nancy).
female(quincy). female(sarah). female(tina). female(victoria).
% parent(X,Y) denotes that X is one of Y's parent.
parent(anya,clara). parent(anya,edward). parent(anya,fiona).
parent(benjamin,clara). parent(benjamin,edward). parent(benjamin,fiona).
parent(clara, hannah). parent(clara, ira). parent(clara, lucas).
parent(david, hannah). parent(david, ira). parent(david, lucas).
parent(fiona, mike). parent(fiona, nancy).
parent(george,mike). parent(george,nancy).
parent(ira,peter). parent(ira,quincy).
parent(james,peter). parent(james,quincy).
parent(kiana,raymond). parent(kiana,sarah). parent(kiana,tina).
parent(lucas,raymond). parent(lucas,sarah). parent(lucas,tina).
parent(nancy,umberto). parent(nancy,victoria).
parent(oscar,umberto). parent(oscar,victoria).
% birth(X,Y) explains the birth year of person X.
birth(anya,1938). birth(benjamin,1929).
birth(clara, 1959). birth(david, 1950).
birth(edward, 1963).
birth(fiona, 1965). birth(george, 1962).
birth(hannah, 1980).
birth(ira,1982). birth(james,1979).
birth(kiana, 1990). birth(lucas, 1986).
birth(mike, 1991).
birth(nancy, 1994). birth(oscar, 1992).
birth(peter,2005). birth(quincy,2008).
birth(raymond, 2013). birth(sarah, 2015). birth(tina, 2018).
birth(umberto, 2016). birth(victoria, 2019).
```

Remark 1 You are prohibited to add any additional fact.

Problem 1 (20 points) Construct the rules for the following predicates:

- (a). brother_in_law(X,Y) which means X is a brother in law of Y.
- (b). sister_in_law(X,Y) which means X is a sister in law of Y.

Hint: X is a brother in law of Y if:

- (definition 1): X is the husband of Y's sister; or
- (definition 2): X is the brother of Y's husband or wife; or
- (definition 3): X is a man who is married to the sister or brother of Y's wife or husband.

Similar definition applies to sister in law as well.

```
Input: ?- brother_in_law(james, hannah).
Output: true
Explanation: definition 1
Input: ?- brother_in_law(lucas, james).
Output: true
Explanation: definition 2
Input: ?- brother_in_law(david,george).
Output: true
Explanation: definition 3
Input: ?- brother_in_law(kiana, james).
Output: false
Input: ?- brother_in_law(lucas, hannah).
Output: false
Input: ?- sister_in_law(kiana,ira).
Output: true
Explanation: definition 1
Input: ?- sister_in_law(fiona,david).
Output: true
Explanation: definition 2
Input: ?- sister_in_law(kiana, james).
Output: true
Explanation: definition 3
Input: ?- sister_in_law(james,kiana).
Output: false
Input: ?- sister_in_law(clara,fiona).
Output: false
```

Problem 2 (20 points) Construct the rules for the following predicates:

- (a). son_in_law(X,Y) which means X is a son in law of Y,
- (b). $daughter_in_law(X,Y)$ which means X is a daughter in law of Y.

Hint: X is a son in law of Y if X is married to Y's daugther. Similarly, X is a daugther in law of Y if X is married to Y's son.

```
Input: ?- son_in_law(david,anya).
Output: true
Input: ?- son_in_law(george,benjamin).
Output: true
Input: ?- son_in_law(edward,anya).
Output: false
Input: ?- son_in_law(kiana,david).
Output: false
Input: ?- son_in_law(james,clara).
Output: true
Input: ?- daughter_in_law(kiana,david).
Output: true
Input: ?- daughter_in_law(kiana,clara).
Output: true
Input: ?- daughter_in_law(james,david).
Output: false
Input: ?- daughter_in_law(clara,kiana).
Output: false
Input: ?- daughter_in_law(quincy,ira).
Output: false
```

Problem 3 (20 points) Construct the rules for the following predicates:

- (a). father_in_law(X,Y) which means that X is father in law of Y,
- (b). $mother_in_law(X,Y)$ which means that X is mother in law of Y.

Hint: you may use the son_in_law(X,Y) and daughter_in_law(X,Y) in Problem 2.

```
Input: ?- father_in_law(benjamin,david).
Output: true
Input: ?- father_in_law(david,kiana).
Output: true
Input: ?- father_in_law(anya,george).
Output: false
Input: ?- father_in_law(fiona,oscar).
Output: false
Input: ?- father_in_law(george,oscar).
Output: true
Input: ?- mother_in_law(fiona,oscar).
Output: true
Input: ?- mother_in_law(clara,kiana).
Output: true
Input: ?- mother_in_law(kiana,clara).
Output: false
Input: ?- mother_in_law(anya,george).
Output: true
Input: ?- mother_in_law(david, james).
Output: false
```

Problem 4 Construct the rules for the following predicates:

- (a). older(X,Y) which means X is older than Y,
- (b). younger(X,Y) which means X is younger than Y.

Hint: use the predicate birth/2 defined in the knowledge base. X is older than Y if X is born before Y, and X is younger than Y if X is born after Y.

```
Input: ?- older(benjamin,anya).
Output: true
Input: ?- older(anya,benjamin).
Output: false
Input: ?- younger(clara,george).
Output: false
Input: ?- younger(george,clara).
Output: true
Input: ?- older(mike, james).
Output: false
Input: ?- younger(mike, james).
Output: true
Input: ?- younger(mike, mike).
Output: false
Input: ?- older(mike, mike).
Output: false
```

Problem 5 (20 points) Construct the rules for the following predicates:

- (a). xiaodidi(X,Y) which means that X is a younger brother of Y,
- (b). xiaomeimei(X,Y) which means that X is a younger sister of Y,

Hint: use the predicate older/2 and younger/2 in Problem 4. The phrases *xiǎo dì di* and *xiǎo mèi mei* respectively refer to younger brother and younger sister in Mandarin.

```
Input: ?- xiaodidi(edward,clara).
Output: true
Input: ?- xiaodidi(edward,fiona).
Output: false
Input: ?- xiaodidi(lucas, hannah).
Output: true
Input: ?- xiaodidi(lucas,ira).
Output: true
Input: ?- xiaodidi(nancy,mike).
Output: false
Input: ?- xiaomeimei(nancy,mike).
Output: true
Input: ?- xiaomeimei(clara,edward).
Output: false
Input: ?- xiaomeimei(fiona,edward).
Output: true
Input: ?- xiaomeimei(edward,clara).
Output: false
Input: ?- xiaomeimei(fiona,clara).
Output: true
```