

$$\begin{pmatrix} 2 & 3 & 4 \\ 1 & -1 & 2 \end{pmatrix}_{2 \times 3} \begin{pmatrix} 1 & 2 \\ -1 & 1 \end{pmatrix}_{3 \times 2} = \begin{pmatrix} 1 & 8 \\ -2 & 4 \end{pmatrix}_{2 \times 2}$$

$$\left(A_{m \times n} \cdot B_{n \times p} \rightarrow m \times p \right)$$

$\text{Span}\{v_1, \dots, v_m\}$ is always a subspace

10b) $A = X D X^{-1}$

$$D = \begin{pmatrix} \lambda_1 & & 0 \\ & \ddots & \\ 0 & & \lambda_n \end{pmatrix} \quad \text{(smiley face)$$

A is nonsingular, $\lambda_1, \dots, \lambda_n \neq 0$

$$A^{-1} = X \underline{D}^{-1} X^{-1}$$

$$D^{-1} = \begin{pmatrix} \frac{1}{\lambda_1} & & 0 \\ & \ddots & \\ 0 & & \frac{1}{\lambda_n} \end{pmatrix}$$

eigenvalues of A^{-1} : $\frac{1}{\lambda_1}, \frac{1}{\lambda_2}, \dots, \frac{1}{\lambda_n}$

$$\sum \text{Nullity}(A - \lambda_i I) = n$$