Homework Assignment 1

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Problem 3.7. Suppose p(x, y, z), the joint probability mass function of the random variables X, Y, and Z, is given by

$$p(1,1,1) = \frac{1}{8}, \quad p(2,1,1) = \frac{1}{4},$$

$$p(1,1,2) = \frac{1}{8}, \quad p(2,1,2) = \frac{3}{16},$$

$$p(1,2,1) = \frac{1}{16}, \quad p(2,2,1) = 0,$$

$$p(1,2,2) = 0, \quad p(2,2,2) = \frac{1}{4}.$$

What is E[X|Y=2]? What is E[X|Y=2,Z=1]?

Solution. \Box

Problem 3.8. An unbiased die is successively rolled. Let X and Y denote, respectively, the number of rolls necessary to obtain a six and a five. Find:

- a. E[X],
- b. E[X|Y = 1],
- c. E[X]Y = 5].

Solution.

Problem 3.9. Show in the discrete case that if X and Y are independent, then

$$E[X|Y=y]=E[X]$$
 for all y.

 \Box

Problem 3.10. Suppose X and Y are independent continuous random variables. Show that

$$E[X|Y=y]=E[X]$$
 for all y.

 \Box

Problem 3.13. Let X be exponential with mean $1/\lambda$; that is,

$$f_X(x) = \lambda e^{-\lambda x}, \quad 0 < x < \infty.$$

Find E[X|X>1].

 \square

Problem 3.14. Let X be uniform over (0,1). Find E[X|X<1/2]. Solution. \Box