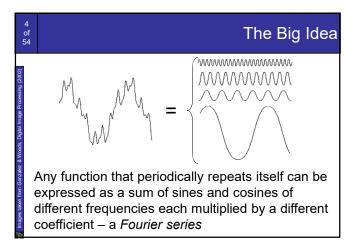
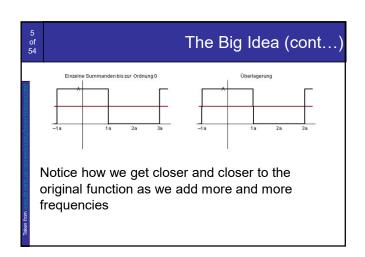
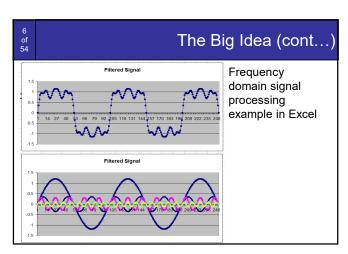


modern engineering





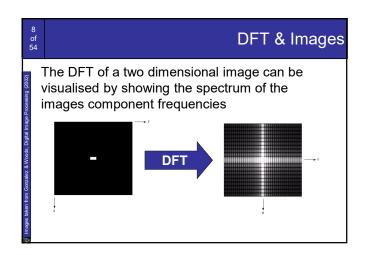


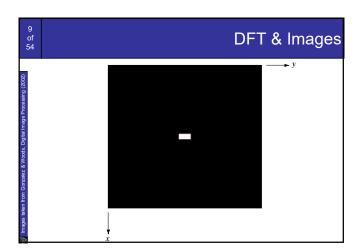
The Discrete Fourier Transform (DFT)

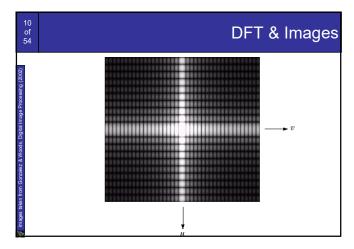
The *Discrete Fourier Transform* of f(x, y), for x = 0, 1, 2...M-1 and y = 0,1,2...N-1, denoted by F(u, v), is given by the equation:

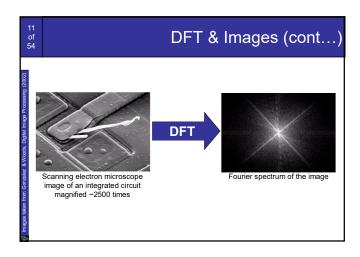
$$F(u,v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) e^{-j2\pi(ux/M + vy/N)}$$

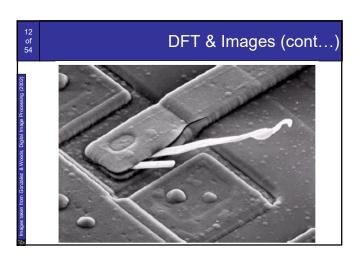
for u = 0, 1, 2...M-1 and v = 0, 1, 2...N-1.

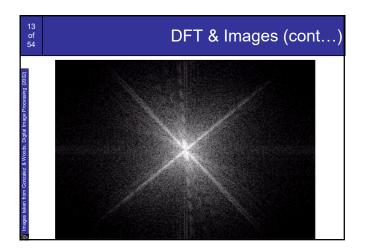


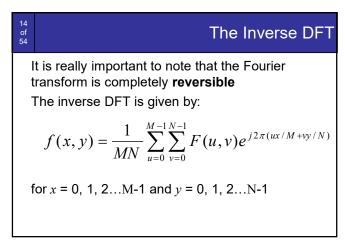


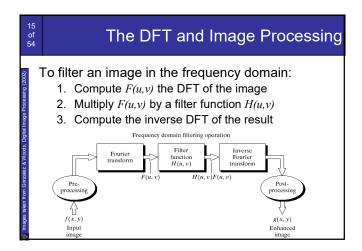


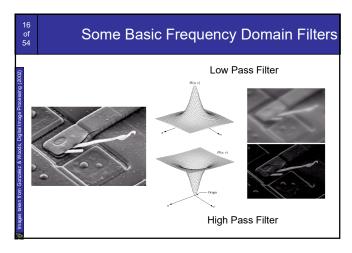




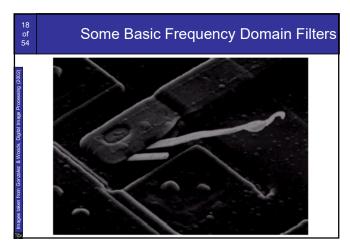












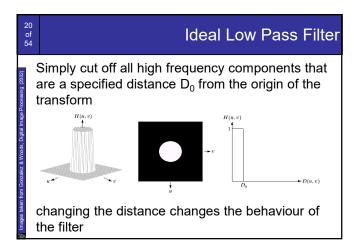
Smoothing Frequency Domain Filters

Smoothing is achieved in the frequency domain by dropping out the high frequency components The basic model for filtering is:

$$G(u,v) = H(u,v)F(u,v)$$

where F(u,v) is the Fourier transform of the image being filtered and H(u,v) is the filter transform function

Low pass filters – only pass the low frequencies, drop the high ones



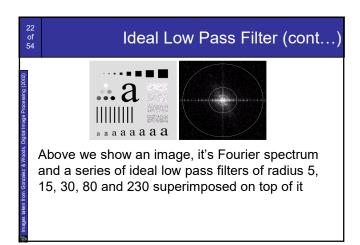
ldeal Low Pass Filter (cont...)

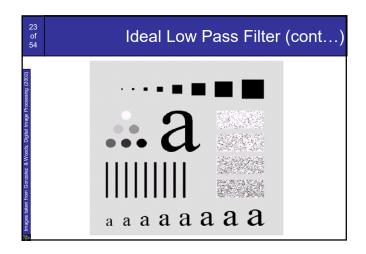
The transfer function for the ideal low pass filter can be given as:

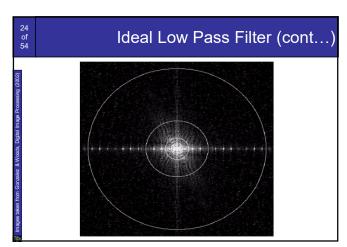
$$H(u,v) = \begin{cases} 1 & \text{if } D(u,v) \le D_0 \\ 0 & \text{if } D(u,v) > D_0 \end{cases}$$

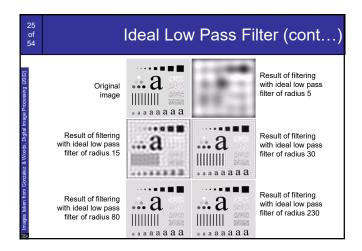
where D(u,v) is given as:

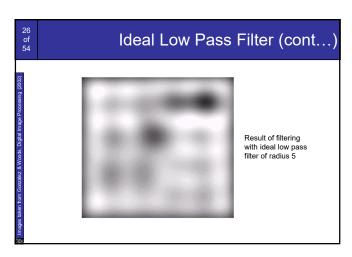
$$D(u,v) = [(u - M/2)^{2} + (v - N/2)^{2}]^{1/2}$$

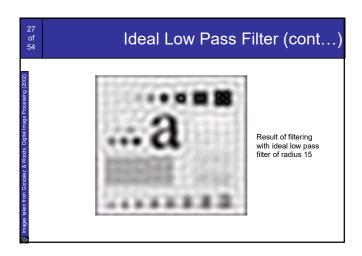


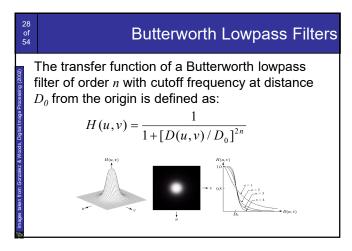


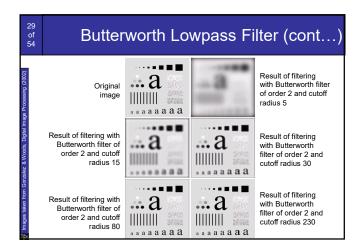


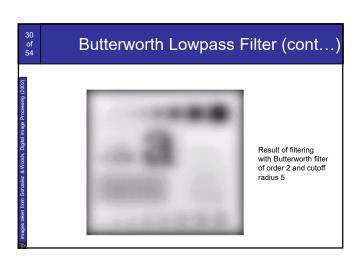


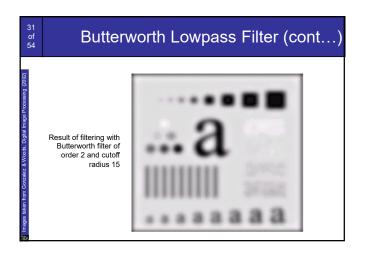


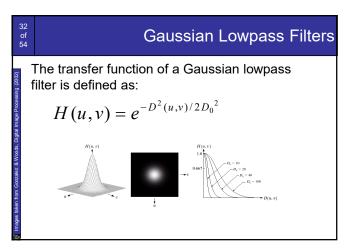


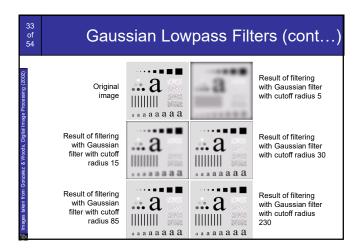


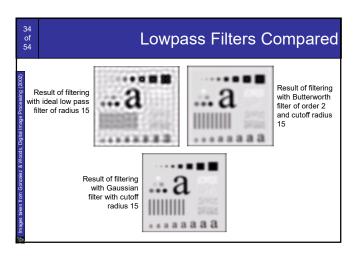


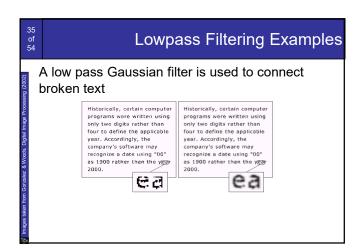


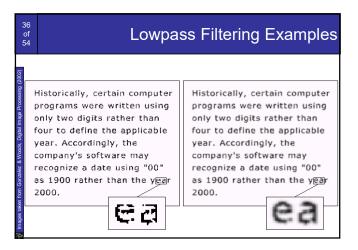


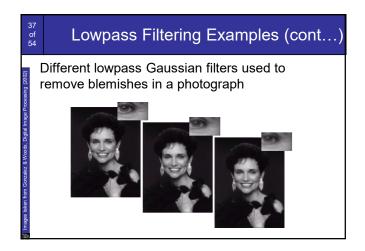


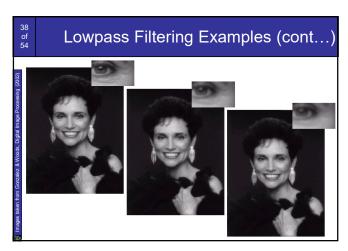


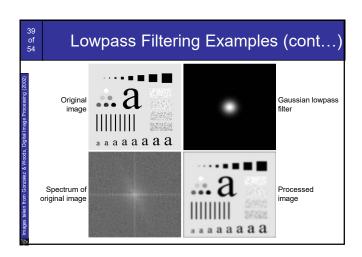


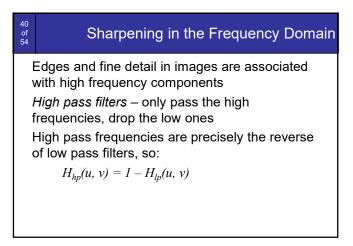


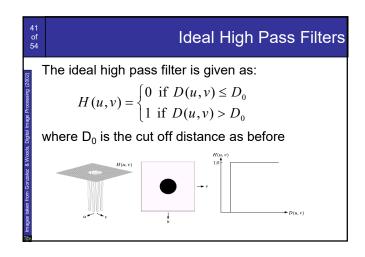


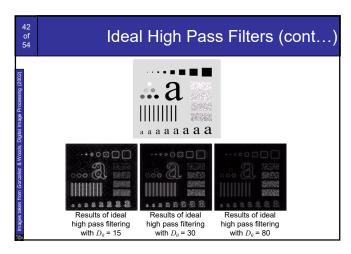


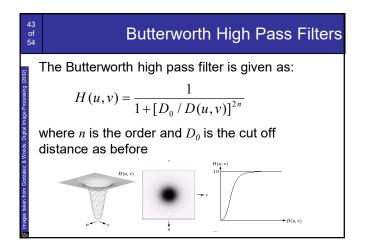


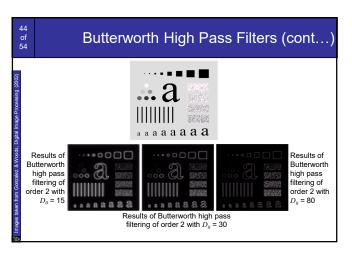


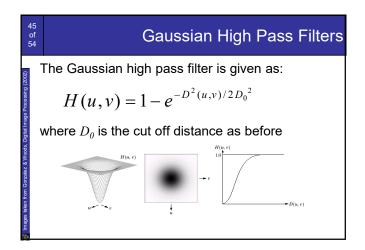


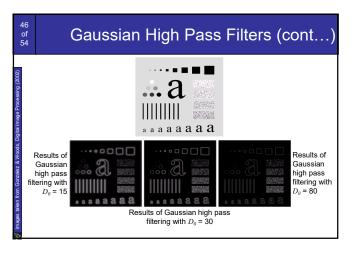


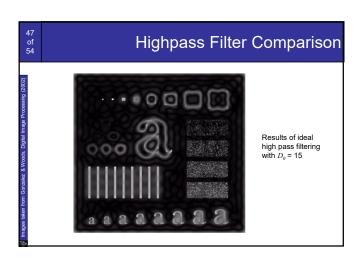


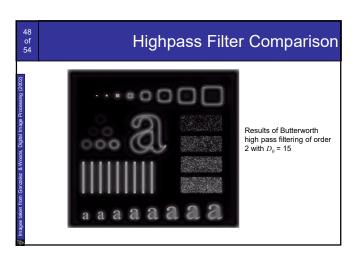


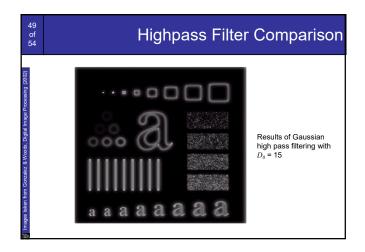


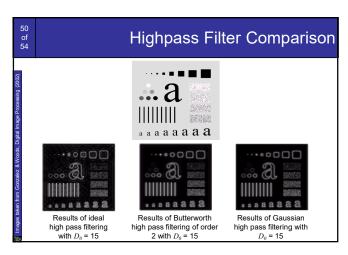


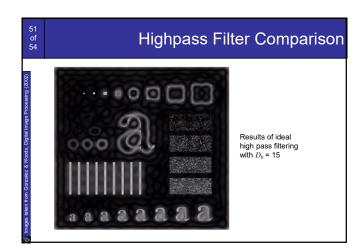


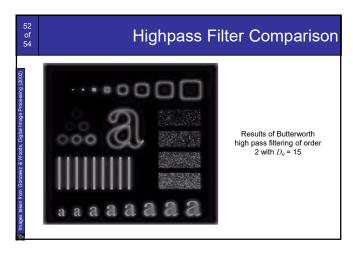


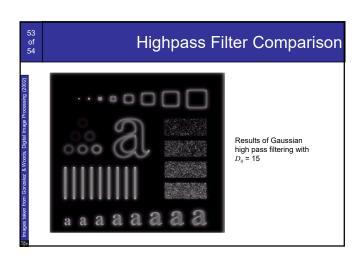


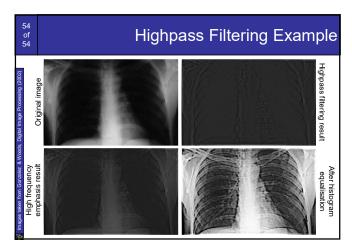




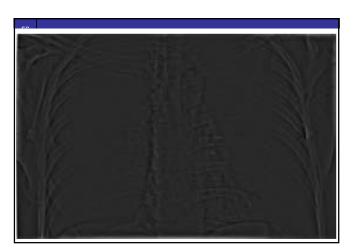


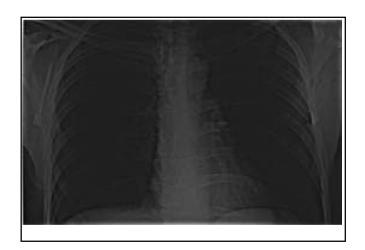


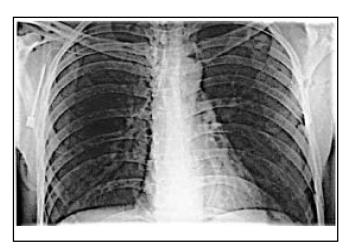


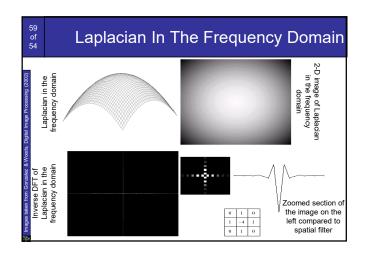


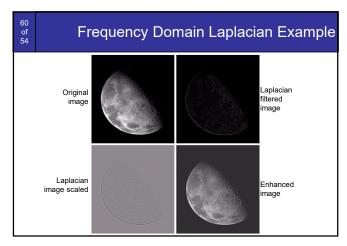












Fast Fourier Transform

The reason that Fourier based techniques have become so popular is the development of the Fast Fourier Transform (FFT) algorithm

Allows the Fourier transform to be carried out in a reasonable amount of time

Reduces the amount of time required to perform a Fourier transform by a factor of 100 – 600 times!

Frequency Domain Filtering & Spatial
Domain Filtering

Similar jobs can be done in the spatial and frequency domains

Filtering in the spatial domain can be easier to understand

Filtering in the frequency domain can be much faster – especially for large images

Summary

In this lecture we examined image enhancement in the frequency domain

- The Fourier series & the Fourier transform
- Image Processing in the frequency domain
 - Image smoothing
 - · Image sharpening
- Fast Fourier Transform

Next time we will begin to examine image restoration using the spatial and frequency based techniques we have been looking at

