

PHY F242 : QUANTUM MECHANICS-I

Assignment-1

Total Marks: 20

1. A wavefunction  $\psi_0$  is expressed as:

$$\psi_0(x) = A x e^{-ax^2/2}, x \in (-\infty, \infty)$$

where A and a are constants.

- i. Find A such that  $\psi_0$  represents a normalized wavefunction.
- ii. If a particle of mass  $m$  has state  $\psi_0$  at a particular time instance, calculate the expected value of the kinetic energy  $\langle T \rangle$  of the particle at that time instance.

[3+4]

2. Given that  $\hat{p} = \frac{\hbar}{i} \frac{\partial}{\partial x}$  and  $V$  is the potential energy function of the system, prove that

$$\frac{d\langle p \rangle}{dt} = \left\langle -\frac{\partial V}{\partial x} \right\rangle$$

[4]

3. A particle at time  $t=0$  is represented by the state:

$$\psi_0(x) = \begin{cases} A(x - x^3) & -1 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

- i. Find A such that  $\psi_0$  is normalized
- ii. Calculate the expectation values,  $\langle x \rangle$  and  $\langle x^2 \rangle$
- iii. Calculate the expectation values,  $\langle p \rangle$  and  $\langle p^2 \rangle$
- iv. Find  $\sigma_x$  and  $\sigma_p$ . Is their product consistent with the uncertainty principle?

[1+3+3+2]