ACM Preliminary Analysis

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Read in Data

```
data = as.tbl(read.csv("student-por.csv", sep=";", stringsAsFactors=TRUE))
```

Rename the Variables

```
rename_cols <- c(4:12,16:21,23:24,26:28,31:33)
colnames(data)[rename_cols] = c("urban_rural",
                                 "fam_size",
                                 "parents cohabit",
                                 "mom edu",
                                 "dad edu",
                                 "mom_job",
                                 "dad_job",
                                 "school_reason",
                                 "student_guardian",
                                 "extra_school_support",
                                 "fam_edu_support",
                                 "paid_extra_classes",
                                 "extracurricular_activities",
                                 "attended_nursery",
                                 "wants_higher_education",
                                 "has romantic_partner",
                                 "family_relationship",
                                 "going out amount",
                                 "weekday_alcohol_cons",
                                 "weekend_alcohol_cons",
                                 "grade one",
                                 "grade two",
                                 "final_grade")
```

Meaningful Variable Values

Regression Using Sex as a Variable

```
lm_sex <- lm(final_grade ~ sex, data = data)</pre>
summary(lm sex)
##
## Call:
## lm(formula = final_grade ~ sex, data = data)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -12.2533 -1.4060 -0.2533
                              1.7467
                                        7.5940
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
                           0.1638 74.795 < 2e-16 ***
## (Intercept) 12.2533
## sexM
               -0.8472
                           0.2559 -3.311 0.000982 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.206 on 647 degrees of freedom
## Multiple R-squared: 0.01666,
                                   Adjusted R-squared: 0.01514
## F-statistic: 10.96 on 1 and 647 DF, p-value: 0.0009815
```

The average grade for females is 12.25 whereas the average grade for Males is 11.40. The difference between the two is significant (p < 0.001); the R-squared is 0.015.

Regression Using Family/Home Attributes

fam_edu_supportTRUE

family_relationship

```
lm_family <- lm(final_grade ~ fam_size + parents_cohabit + fam_edu_support + family_relationship + mom_</pre>
summary(lm_family)
##
## Call:
## lm(formula = final_grade ~ fam_size + parents_cohabit + fam_edu_support +
##
       family_relationship + mom_edu + mom_job, data = data)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                             Max
                                2.0203
                       0.0319
                                         7.4870
## -13.3384 -1.6538
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
                             9.3701
## (Intercept)
                                        0.7137 13.129 < 2e-16 ***
## fam_size>3
                            -0.3588
                                        0.2796 -1.283 0.199911
## parents_cohabitTogether
                             0.1837
                                        0.3892
                                                0.472 0.637060
```

0.2558

0.1294

0.855 0.392604

1.510 0.131569

0.2188

0.1953

```
## mom edu
                            0.5132
                                       0.1416
                                                3.624 0.000314 ***
                                                1.774 0.076597 .
## mom_jobhealth
                            1.0470
                                       0.5903
                                                1.134 0.257024
## mom jobother
                            0.3878
                                       0.3418
                                       0.4124
## mom_jobservices
                            0.4969
                                                1.205 0.228669
## mom_jobteacher
                            0.8951
                                       0.5599
                                                1.599 0.110407
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.137 on 639 degrees of freedom
## Multiple R-squared: 0.07044,
                                   Adjusted R-squared: 0.05734
## F-statistic: 5.38 on 9 and 639 DF, p-value: 4.05e-07
```

Note that dad_edu and dad_job were not used since they are highly correlated to mom_edu and mom_job, respectively.

Out of the variables used, it looks like mom_edu has the only significant estimate. The estimate of 0.5132 suggests that each additional level of education reached by the mother corresponds with an additional 0.5132 points in the student's final grade in Portuguese.

Regression with Student Behaviors

```
lm_habits <- lm(final_grade ~ paid_extra_classes + extracurricular_activities + attended_nursery + want</pre>
summary(lm_habits)
##
## Call:
## lm(formula = final_grade ~ paid_extra_classes + extracurricular_activities +
       attended_nursery + wants_higher_education + has_romantic_partner +
       going_out_amount + weekday_alcohol_cons + weekend_alcohol_cons,
##
       data = data)
##
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -13.1748 -1.6646
                       0.1527
                                1.8600
                                         6.5574
##
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  10.231070
                                              0.588339 17.390 < 2e-16 ***
## paid_extra_classesTRUE
                                  -0.800661
                                              0.497388 - 1.610
                                                                 0.1079
## extracurricular_activitiesTRUE 0.386926
                                              0.237758
                                                        1.627
                                                                  0.1041
## attended_nurseryTRUE
                                  -0.003662
                                              0.297699 -0.012
                                                                 0.9902
## wants_higher_educationTRUE
                                                         8.186 1.47e-15 ***
                                   3.174917
                                              0.387856
## has_romantic_partnerTRUE
                                  -0.401965
                                              0.246684 -1.629
                                                                 0.1037
                                                                  0.7071
## going_out_amount
                                  -0.041095
                                              0.109327
                                                        -0.376
## weekday_alcohol_cons
                                  -0.369190
                                              0.163366
                                                        -2.260
                                                                 0.0242 *
## weekend_alcohol_cons
                                                                 0.0974 .
                                  -0.204184
                                              0.122994 - 1.660
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 2.997 on 640 degrees of freedom
Multiple R-squared: 0.1502, Adjusted R-squared: 0.1396
F-statistic: 14.14 on 8 and 640 DF, p-value: < 2.2e-16</pre>

Out of the variables used, it seems that only wanting a higher education (i.e. wants_higher_education) and weekday alcohol consumption (i.e. weekday_alchol_cons) were significant.

```
lm_habits2 <- lm(final_grade ~ wants_higher_education + weekday_alcohol_cons, data = data)
summary(lm_habits2)</pre>
```

```
##
## Call:
## lm(formula = final grade ~ wants higher education + weekday alcohol cons,
##
       data = data)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
##
  -12.5393 -1.5393
                       0.2858
                                1.7498
                                         6.6052
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
                                9.8587
                                           0.4337 22.732 < 2e-16 ***
## (Intercept)
## wants_higher_educationTRUE
                                3.2529
                                           0.3862
                                                    8.423 2.38e-16 ***
                                                  -4.442 1.05e-05 ***
## weekday alcohol cons
                               -0.5723
                                           0.1288
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.006 on 646 degrees of freedom
## Multiple R-squared: 0.1367, Adjusted R-squared: 0.134
## F-statistic: 51.15 on 2 and 646 DF, p-value: < 2.2e-16
```

The combined adjusted R-Squared id about 0.134 which is very low. However, the p-values for the two variables are both very low, suggesting that it is very unlikely that there is no relationship and the final score and either of those two variables. The strength of wanting higher education both has a larger slope estimate and a more significant p-value compared to weekday alcohol consumption. It is heartening to see that academic ambition corresponds strongly to academic achievement.

Regression with Hybrid Step-Wise Abroach

```
fit = lm(final grade~.-grade one-grade two,data=data)
step = stepAIC(fit, direction="both")
## Start: AIC=1311.16
## final_grade ~ (school + sex + age + urban_rural + fam_size +
##
       parents_cohabit + mom_edu + dad_edu + mom_job + dad_job +
##
       school_reason + student_guardian + traveltime + studytime +
##
       failures + extra_school_support + fam_edu_support + paid_extra_classes +
##
       extracurricular_activities + attended_nursery + wants_higher_education +
       internet + has_romantic_partner + family_relationship + freetime +
##
       going_out_amount + weekday_alcohol_cons + weekend_alcohol_cons +
##
##
       health + absences + grade_one + grade_two) - grade_one -
##
       grade_two
##
##
                                Df Sum of Sq
                                                RSS
                                                        AIC
```

```
## - mom_job
                                       28.27 4354.4 1307.4
                                       17.47 4343.6 1307.8
## - school_reason
                                 3
## - fam_edu_support
                                       0.06 4326.2 1309.2
## - mom_edu
                                        0.39 4326.6 1309.2
                                 1
## - traveltime
                                 1
                                        1.10 4327.3 1309.3
                                       1.85 4328.0 1309.4
## - parents cohabit
                                 1
                                 2
                                     16.00 4342.2 1309.5
## - student_guardian
## - going_out_amount
                                 1
                                       2.68 4328.9 1309.6
## - weekend_alcohol_cons
                                 1
                                        3.36 4329.5 1309.7
## - attended_nursery
                                 1
                                       4.50 4330.7 1309.8
## - paid_extra_classes
                                 1
                                        4.61 4330.8 1309.8
                                        5.95 4332.1 1310.0
## - internet
                                 1
## - extracurricular_activities 1
                                        6.84 4333.0 1310.2
## - dad_edu
                                       10.42 4336.6 1310.7
## - freetime
                                       10.68 4336.9 1310.8
                                 1
## - urban_rural
                                 1
                                       10.79 4337.0 1310.8
                                       10.83 4337.0 1310.8
## - fam_size
                                 1
## - dad job
                                       52.76 4378.9 1311.0
## - weekday_alcohol_cons
                                       12.72 4338.9 1311.1
                                 1
## <none>
                                             4326.2 1311.2
## - family_relationship
                                 1
                                       13.75 4339.9 1311.2
## - age
                                       16.59 4342.8 1311.6
## - absences
                                       16.65 4342.8 1311.7
                                 1
                                       25.18 4351.4 1312.9
## - has romantic partner
                                 1
## - health
                                 1
                                       41.88 4368.1 1315.4
## - sex
                                 1
                                       45.54 4371.7 1316.0
## - studytime
                                       59.99 4386.2 1318.1
                                 1
## - extra_school_support
                                 1
                                      92.14 4418.3 1322.8
                                    143.23 4469.4 1330.3
## - school
                                 1
## - wants_higher_education
                                    145.64 4471.8 1330.7
                                 1
## - failures
                                 1
                                      338.75 4664.9 1358.1
##
## Step: AIC=1307.38
## final_grade ~ school + sex + age + urban_rural + fam_size + parents_cohabit +
##
       mom_edu + dad_edu + dad_job + school_reason + student_guardian +
##
       traveltime + studytime + failures + extra_school_support +
##
       fam_edu_support + paid_extra_classes + extracurricular_activities +
##
       attended_nursery + wants_higher_education + internet + has_romantic_partner +
##
       family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
##
       weekend_alcohol_cons + health + absences
##
                                Df Sum of Sq
##
                                                RSS
                                                       ATC
## - school reason
                                       17.69 4372.1 1304.0
## - fam_edu_support
                                        0.00 4354.4 1305.4
                                 1
## - traveltime
                                 1
                                        1.04 4355.5 1305.5
                                 2
                                       14.94 4369.4 1305.6
## - student_guardian
## - parents_cohabit
                                 1
                                       2.12 4356.6 1305.7
## - weekend_alcohol_cons
                                 1
                                       2.19 4356.6 1305.7
## - going_out_amount
                                 1
                                       2.54 4357.0 1305.8
## - attended_nursery
                                 1
                                       4.04 4358.5 1306.0
                                 4
                                     44.81 4399.3 1306.0
## - dad_job
## - paid_extra_classes
                                 1
                                       5.63 4360.1 1306.2
## - extracurricular_activities 1
                                       7.08 4361.5 1306.4
## - dad edu
                                        8.12 4362.6 1306.6
```

```
9.75 4364.2 1306.8
## - freetime
## - internet
                                        9.86 4364.3 1306.8
                                 1
## - mom edu
                                       10.06 4364.5 1306.9
## - family_relationship
                                       11.44 4365.9 1307.1
                                 1
## - urban_rural
                                 1
                                       12.56 4367.0 1307.2
                                       12.77 4367.2 1307.3
## - fam size
                                 1
## <none>
                                             4354.4 1307.4
                                       14.21 4368.7 1307.5
## - age
                                 1
## - weekday_alcohol_cons
                                 1
                                       15.98 4370.4 1307.8
## - absences
                                 1
                                       20.21 4374.6 1308.4
## - has_romantic_partner
                                 1
                                       25.93 4380.4 1309.2
                                       36.28 4390.7 1310.8
## - health
                                 1
## + mom_job
                                 4
                                       28.27 4326.2 1311.2
## - sex
                                 1
                                      43.82 4398.3 1311.9
## - studytime
                                     55.81 4410.2 1313.7
                                 1
                                   100.28 4454.7 1320.2
## - extra_school_support
                                 1
                                   150.86 4505.3 1327.5
## - school
                                 1
## - wants_higher_education
                                 1 154.58 4509.0 1328.0
## - failures
                                      328.04 4682.5 1352.5
                                 1
##
## Step: AIC=1304.02
## final_grade ~ school + sex + age + urban_rural + fam_size + parents_cohabit +
       mom_edu + dad_edu + dad_job + student_guardian + traveltime +
##
       studytime + failures + extra_school_support + fam_edu_support +
##
##
       paid_extra_classes + extracurricular_activities + attended_nursery +
      wants_higher_education + internet + has_romantic_partner +
##
       family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
       weekend_alcohol_cons + health + absences
##
##
                                Df Sum of Sq
                                                RSS
                                                       AIC
## - fam_edu_support
                                 1
                                        0.10 4372.2 1302.0
## - traveltime
                                 1
                                        0.73 4372.9 1302.1
## - weekend_alcohol_cons
                                       1.63 4373.8 1302.3
                                       1.64 4373.8 1302.3
## - parents_cohabit
                                 1
## - going_out_amount
                                 1
                                       2.62 4374.8 1302.4
                                 2
                                     17.30 4389.4 1302.6
## - student_guardian
## - attended nursery
                                1
                                      4.00 4376.1 1302.6
## - dad_job
                                 4
                                      45.90 4418.0 1302.8
## - paid_extra_classes
                                 1
                                       7.39 4379.5 1303.1
## - dad_edu
                                       8.07 4380.2 1303.2
                                 1
## - freetime
                                       9.05 4381.2 1303.4
                                 1
## - internet
                                       10.54 4382.7 1303.6
                                 1
## - extracurricular_activities 1
                                       10.57 4382.7 1303.6
## - mom_edu
                                       10.84 4383.0 1303.6
                                 1
## - family_relationship
                                 1
                                       11.25 4383.4 1303.7
                                       11.48 4383.6 1303.7
## - urban_rural
                                 1
## <none>
                                             4372.1 1304.0
                                       14.75 4386.9 1304.2
## - fam_size
                                 1
## - age
                                 1
                                       15.71 4387.8 1304.3
## - absences
                                 1
                                       18.39 4390.5 1304.7
                                       20.76 4392.9 1305.1
## - weekday_alcohol_cons
                                 1
## - has_romantic_partner
                                 1
                                     29.07 4401.2 1306.3
## + school_reason
                                 3
                                     17.69 4354.4 1307.4
## + mom job
                                 4
                                       28.49 4343.6 1307.8
```

```
## - health
                                      41.35 4413.5 1308.1
## - sex
                                      44.49 4416.6 1308.6
                                 1
## - studytime
                                      63.36 4435.5 1311.3
## - extra_school_support
                                    101.65 4473.8 1316.9
                                1
## - wants_higher_education
                                1
                                   159.55 4531.7 1325.3
## - school
                                1
                                   176.15 4548.3 1327.7
## - failures
                                1
                                     336.69 4708.8 1350.2
##
## Step: AIC=1302.03
## final_grade ~ school + sex + age + urban_rural + fam_size + parents_cohabit +
       mom_edu + dad_edu + dad_job + student_guardian + traveltime +
       studytime + failures + extra_school_support + paid_extra_classes +
##
##
       extracurricular_activities + attended_nursery + wants_higher_education +
##
       internet + has_romantic_partner + family_relationship + freetime +
##
       going_out_amount + weekday_alcohol_cons + weekend_alcohol_cons +
##
       health + absences
##
##
                               Df Sum of Sq
                                               RSS
                                                       AIC
                                       0.74 4373.0 1300.1
## - traveltime
                                1
## - weekend alcohol cons
                                1
                                       1.67 4373.9 1300.3
## - parents_cohabit
                                1
                                       1.67 4373.9 1300.3
## - going_out_amount
                                      2.58 4374.8 1300.4
                                1
## - student_guardian
                                2
                                     17.45 4389.7 1300.6
## - attended nursery
                                      3.99 4376.2 1300.6
                                1
                                      45.92 4418.1 1300.8
                                4
## - dad job
## - paid_extra_classes
                                1
                                      7.31 4379.5 1301.1
                                       8.19 4380.4 1301.2
## - dad_edu
                                1
                                       9.03 4381.3 1301.4
## - freetime
                                1
## - extracurricular_activities 1
                                   10.51 4382.7 1301.6
## - internet
                                1
                                      10.67 4382.9 1301.6
## - mom_edu
                                 1
                                      10.96 4383.2 1301.7
## - family_relationship
                                1
                                      11.30 4383.5 1301.7
## - urban_rural
                                      11.43 4383.7 1301.7
## <none>
                                             4372.2 1302.0
## - fam size
                                1
                                      14.74 4387.0 1302.2
                                      15.65 4387.9 1302.3
## - age
                                1
## - absences
                                1
                                      18.30 4390.5 1302.7
## - weekday_alcohol_cons
                                1
                                      20.68 4392.9 1303.1
## + fam_edu_support
                                1
                                      0.10 4372.1 1304.0
## - has_romantic_partner
                                      29.17 4401.4 1304.3
                                1
## + school reason
                                3
                                      17.79 4354.4 1305.4
                                      28.57 4343.7 1305.8
## + mom job
                                4
                                      41.27 4413.5 1306.1
## - health
                                1
## - sex
                                1
                                      45.80 4418.0 1306.8
                                     64.64 4436.9 1309.5
## - studytime
                                1
                                1 101.57 4473.8 1314.9
## - extra_school_support
## - wants_higher_education
                                1 160.06 4532.3 1323.4
## - school
                                1 176.37 4548.6 1325.7
## - failures
                                1
                                     337.36 4709.6 1348.3
## Step: AIC=1300.14
## final_grade ~ school + sex + age + urban_rural + fam_size + parents_cohabit +
##
      mom_edu + dad_edu + dad_job + student_guardian + studytime +
##
      failures + extra_school_support + paid_extra_classes + extracurricular_activities +
```

```
##
       attended_nursery + wants_higher_education + internet + has_romantic_partner +
##
       family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
##
       weekend_alcohol_cons + health + absences
##
                                Df Sum of Sq
                                                RSS
## - weekend alcohol cons
                                        1.69 4374.7 1298.4
                                        1.71 4374.7 1298.4
## - parents_cohabit
                                        2.41 4375.4 1298.5
## - going_out_amount
                                 1
## - attended_nursery
                                 1
                                        3.87 4376.8 1298.7
                                 2
## - student_guardian
                                       17.98 4390.9 1298.8
## - dad_job
                                       46.64 4419.6 1299.0
## - paid_extra_classes
                                        7.51 4380.5 1299.2
                                 1
## - dad_edu
                                        8.02 4381.0 1299.3
                                 1
## - freetime
                                 1
                                        9.32 4382.3 1299.5
## - internet
                                       10.24 4383.2 1299.7
                                 1
## - mom_edu
                                       10.44 4383.4 1299.7
                                       10.48 4383.4 1299.7
## - extracurricular_activities 1
## - urban rural
                                       10.69 4383.7 1299.7
                                 1
## - family_relationship
                                       11.31 4384.3 1299.8
                                 1
## <none>
                                             4373.0 1300.1
## - fam_size
                                 1
                                       14.85 4387.8 1300.3
## - age
                                       15.38 4388.3 1300.4
                                       18.17 4391.1 1300.8
## - absences
                                 1
## - weekday alcohol cons
                                       20.35 4393.3 1301.2
                                 1
## + traveltime
                                 1
                                       0.74 4372.2 1302.0
## + fam_edu_support
                                 1
                                        0.10 4372.9 1302.1
## - has_romantic_partner
                                       29.33 4402.3 1302.5
                                 1
                                 3
                                       17.48 4355.5 1303.5
## + school_reason
                                 4
                                       28.49 4344.5 1303.9
## + mom_job
## - health
                                 1
                                       42.00 4415.0 1304.3
## - sex
                                 1
                                       45.18 4418.1 1304.8
## - studytime
                                 1
                                       64.88 4437.8 1307.7
## - extra_school_support
                                      102.16 4475.1 1313.1
                                      160.85 4533.8 1321.6
## - wants_higher_education
                                 1
## - school
                                 1
                                      175.97 4548.9 1323.7
## - failures
                                      336.67 4709.6 1346.3
##
## Step: AIC=1298.39
## final_grade ~ school + sex + age + urban_rural + fam_size + parents_cohabit +
       mom_edu + dad_edu + dad_job + student_guardian + studytime +
##
##
       failures + extra_school_support + paid_extra_classes + extracurricular_activities +
##
       attended_nursery + wants_higher_education + internet + has_romantic_partner +
       family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
##
##
       health + absences
##
                                Df Sum of Sq
##
                                                 RSS
                                                        AIC
## - parents_cohabit
                                 1
                                        1.55 4376.2 1296.6
                                        3.63 4378.3 1296.9
## - attended_nursery
                                 1
## - going_out_amount
                                 1
                                        4.42 4379.1 1297.0
## - student_guardian
                                 2
                                       18.88 4393.5 1297.2
                                        7.38 4382.0 1297.5
## - dad_edu
                                 1
## - paid_extra_classes
                                1
                                       7.51 4382.2 1297.5
## - freetime
                                 1
                                       8.91 4383.6 1297.7
## - dad_job
                                 4
                                       49.72 4424.4 1297.7
```

```
## - internet
                                       10.11 4384.8 1297.9
                                       10.55 4385.2 1298.0
## - extracurricular_activities 1
## - urban rural
                                       10.78 4385.4 1298.0
## - mom_edu
                                       11.16 4385.8 1298.0
                                 1
## - family_relationship
                                       12.96 4387.6 1298.3
                                             4374.7 1298.4
## <none>
                                       14.30 4389.0 1298.5
## - fam size
## - age
                                 1
                                       15.24 4389.9 1298.7
## - absences
                                 1
                                       18.68 4393.3 1299.2
## + weekend_alcohol_cons
                                 1
                                       1.69 4373.0 1300.1
## + traveltime
                                 1
                                        0.76 4373.9 1300.3
## + fam_edu_support
                                        0.13 4374.5 1300.4
                                 1
## - has_romantic_partner
                                 1
                                       28.95 4403.6 1300.7
## - weekday_alcohol_cons
                                      36.97 4411.6 1301.8
                                 1
                                 3
                                      16.95 4357.7 1301.9
## + school_reason
## + mom_job
                                 4
                                       27.44 4347.2 1302.3
## - health
                                      44.59 4419.3 1303.0
                                 1
## - sex
                                      49.74 4424.4 1303.7
                                 1
                                      68.35 4443.0 1306.5
## - studytime
                                 1
## - extra_school_support
                                 1
                                      100.96 4475.6 1311.2
                                    160.26 4534.9 1319.7
## - wants_higher_education
                                 1
## - school
                                    175.03 4549.7 1321.8
                                 1
## - failures
                                      337.10 4711.8 1344.6
                                 1
## Step: AIC=1296.62
## final_grade ~ school + sex + age + urban_rural + fam_size + mom_edu +
##
       dad_edu + dad_job + student_guardian + studytime + failures +
##
       extra_school_support + paid_extra_classes + extracurricular_activities +
##
       attended_nursery + wants_higher_education + internet + has_romantic_partner +
##
       family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
##
       health + absences
##
##
                                Df Sum of Sq
                                                RSS
                                                        AIC
                                        3.65 4379.9 1295.2
## - attended_nursery
                                 1
## - going_out_amount
                                        4.36 4380.6 1295.3
                                 1
                                 2
                                       19.26 4395.5 1295.5
## - student_guardian
## - dad edu
                                       7.22 4383.4 1295.7
## - paid_extra_classes
                                        7.47 4383.7 1295.7
                                 1
## - dad job
                                 4
                                       48.90 4425.1 1295.8
## - freetime
                                       8.87 4385.1 1295.9
                                 1
## - urban_rural
                                       10.16 4386.4 1296.1
                                 1
## - mom edu
                                       10.69 4386.9 1296.2
                                 1
## - internet
                                 1
                                       10.90 4387.1 1296.2
## - extracurricular_activities
                                       11.42 4387.6 1296.3
                                 1
## - fam_size
                                       12.83 4389.0 1296.5
                                 1
## - family_relationship
                                       13.06 4389.3 1296.5
                                 1
## <none>
                                             4376.2 1296.6
## - age
                                 1
                                       15.91 4392.1 1297.0
## - absences
                                       19.97 4396.2 1297.6
                                 1
## + parents_cohabit
                                 1
                                        1.55 4374.7 1298.4
                                       1.53 4374.7 1298.4
## + weekend_alcohol_cons
                                 1
## + traveltime
                                 1
                                       0.81 4375.4 1298.5
## + fam_edu_support
                                       0.16 4376.1 1298.6
                                 1
## - has romantic partner
                                 1
                                       29.76 4406.0 1299.0
```

```
## - weekday_alcohol_cons
                                      36.40 4412.6 1300.0
                                1
                                      16.56 4359.6 1300.2
## + school_reason
                                3
## + mom job
                                4
                                      27.63 4348.6 1300.5
## - health
                                      44.50 4420.7 1301.2
                                1
## - sex
                                1
                                      48.91 4425.1 1301.8
                                    68.18 4444.4 1304.7
## - studytime
                                1
                                   101.47 4477.7 1309.5
## - extra_school_support
                                1
## - wants_higher_education
                                   161.03 4537.2 1318.1
                                1
## - school
                                1
                                     175.84 4552.1 1320.2
## - failures
                                1
                                     337.85 4714.1 1342.9
##
## Step: AIC=1295.16
## final_grade ~ school + sex + age + urban_rural + fam_size + mom_edu +
##
      dad_edu + dad_job + student_guardian + studytime + failures +
##
      extra_school_support + paid_extra_classes + extracurricular_activities +
##
      wants_higher_education + internet + has_romantic_partner +
##
      family_relationship + freetime + going_out_amount + weekday_alcohol_cons +
##
      health + absences
##
##
                               Df Sum of Sq
                                               RSS
## - going_out_amount
                                1
                                       4.60 4384.5 1293.8
## - student_guardian
                                      20.31 4400.2 1294.2
                                       7.14 4387.0 1294.2
## - dad edu
                                1
                                       7.71 4387.6 1294.3
## - paid_extra_classes
                                1
## - dad job
                                4
                                      49.58 4429.4 1294.5
## - freetime
                                1
                                      8.86 4388.7 1294.5
## - mom_edu
                                       9.57 4389.4 1294.6
                                1
                                   10.21 4390.1 1294.7
## - urban_rural
                                1
                                   11.03 4390.9 1294.8
## - extracurricular_activities 1
## - internet
                                1
                                     11.36 4391.2 1294.8
                                    11.54 4391.4 1294.9
## - fam_size
                                1
## - family_relationship
                                1
                                      12.69 4392.6 1295.0
## <none>
                                            4379.9 1295.2
## - age
                                      15.47 4395.3 1295.5
                                1
## - absences
                                      19.80 4399.7 1296.1
                                1
                                      3.65 4376.2 1296.6
## + attended_nursery
                                1
## + parents cohabit
                               1
                                      1.58 4378.3 1296.9
## + weekend_alcohol_cons
                                      1.31 4378.6 1297.0
                               1
## + traveltime
                                1
                                       0.68 4379.2 1297.1
## + fam_edu_support
                                      0.15 4379.7 1297.1
                                1
                                      29.59 4409.5 1297.5
## - has_romantic_partner
                                1
## - weekday_alcohol_cons
                                      35.14 4415.0 1298.3
                                1
## + school_reason
                                3
                                      16.58 4363.3 1298.7
## + mom_job
                                4
                                    27.27 4352.6 1299.1
## - health
                                1
                                    44.73 4424.6 1299.8
## - sex
                                      47.87 4427.7 1300.2
                                1
## - studytime
                                1
                                     67.89 4447.8 1303.2
## - extra_school_support
                                1 102.61 4482.5 1308.2
## - wants_higher_education
                                1 161.63 4541.5 1316.7
## - school
                                1
                                     177.12 4557.0 1318.9
## - failures
                                     336.05 4715.9 1341.1
                                1
##
## Step: AIC=1293.84
## final grade ~ school + sex + age + urban rural + fam size + mom edu +
```

```
##
       dad_edu + dad_job + student_guardian + studytime + failures +
##
       extra_school_support + paid_extra_classes + extracurricular_activities +
##
       wants_higher_education + internet + has_romantic_partner +
       family_relationship + freetime + weekday_alcohol_cons + health +
##
##
       absences
##
                                Df Sum of Sq
##
                                                 RSS
## - dad edu
                                        6.76 4391.2 1292.8
## - paid_extra_classes
                                 1
                                        7.72 4392.2 1293.0
## - student_guardian
                                 2
                                        21.67 4406.1 1293.0
## - dad_job
                                  4
                                       49.79 4434.3 1293.2
                                        9.55 4394.0 1293.3
## - urban_rural
                                  1
## - mom_edu
                                        9.76 4394.2 1293.3
                                  1
## - extracurricular_activities
                                       10.27 4394.7 1293.4
## - internet
                                       10.59 4395.1 1293.4
                                  1
## - family_relationship
                                  1
                                       11.63 4396.1 1293.6
                                       11.83 4396.3 1293.6
## - fam_size
                                  1
## <none>
                                              4384.5 1293.8
                                       13.99 4398.5 1293.9
## - age
                                 1
## - freetime
                                       14.90 4399.4 1294.0
## - absences
                                 1
                                       20.88 4405.4 1294.9
## + going_out_amount
                                        4.60 4379.9 1295.2
                                 1
## + attended_nursery
                                        3.90 4380.6 1295.3
                                 1
## + weekend alcohol cons
                                        3.19 4381.3 1295.4
                                 1
## + parents_cohabit
                                 1
                                        1.51 4383.0 1295.6
## + traveltime
                                 1
                                        0.46 4384.0 1295.8
## + fam_edu_support
                                        0.10 4384.4 1295.8
                                  1
                                       28.43 4412.9 1296.0
## - has_romantic_partner
                                 1
## + school_reason
                                       16.39 4368.1 1297.4
                                 3
## + mom_job
                                  4
                                       26.37 4358.1 1297.9
## - weekday_alcohol_cons
                                  1
                                       43.01 4427.5 1298.2
## - health
                                  1
                                       43.07 4427.5 1298.2
## - sex
                                       46.28 4430.7 1298.7
                                       69.33 4453.8 1302.0
## - studytime
                                  1
## - extra_school_support
                                      101.44 4485.9 1306.7
                                 1
                                      161.61 4546.1 1315.3
## - wants_higher_education
                                  1
## - school
                                      181.25 4565.7 1318.1
## - failures
                                  1
                                      333.96 4718.4 1339.5
##
## Step: AIC=1292.84
## final_grade ~ school + sex + age + urban_rural + fam_size + mom_edu +
##
       dad_job + student_guardian + studytime + failures + extra_school_support +
       paid_extra_classes + extracurricular_activities + wants_higher_education +
##
##
       internet + has_romantic_partner + family_relationship + freetime +
       weekday_alcohol_cons + health + absences
##
##
##
                                Df Sum of Sq
                                                 RSS
## - paid_extra_classes
                                        6.79 4398.0 1291.8
## - urban_rural
                                        9.60 4400.8 1292.3
                                  1
## - extracurricular_activities 1
                                        10.30 4401.5 1292.4
                                       10.82 4402.1 1292.4
## - internet
                                  1
## - fam_size
                                  1
                                       11.47 4402.7 1292.5
## - family_relationship
                                       11.59 4402.8 1292.5
                                 1
## - student guardian
                                       25.38 4416.6 1292.6
```

```
4391.2 1292.8
## <none>
## - freetime
                                       13.83 4405.1 1292.9
                                1
## - age
                                       13.90 4405.1 1292.9
## - dad_job
                                4
                                       54.97 4446.2 1292.9
## - absences
                                1
                                      19.15 4410.4 1293.7
## + dad edu
                                       6.76 4384.5 1293.8
                               1
                                      4.23 4387.0 1294.2
## + going out amount
                               1
                               1
                                      3.81 4387.4 1294.3
## + attended_nursery
## + weekend_alcohol_cons
                               1
                                      2.28 4389.0 1294.5
## + parents_cohabit
                                1
                                      1.36 4389.9 1294.6
## + traveltime
                                1
                                       0.33 4390.9 1294.8
                                       0.21 4391.0 1294.8
## + fam_edu_support
                                 1
## - mom_edu
                                1
                                      30.06 4421.3 1295.3
                                1 30.32 4421.6 1295.3
## - has_romantic_partner
                                3 16.63 4374.6 1296.4
1 41.93 4433.2 1297.0
4 24.46 4366.8 1297.2
## + school_reason
## - health
## + mom_job
## - weekday_alcohol_cons
                                1
                                   43.41 4434.6 1297.2
                                      47.03 4438.3 1297.8
## - sex
                                1
## - studytime
                                1
                                      67.85 4459.1 1300.8
## - extra_school_support
                                1 101.36 4492.6 1305.7
## - wants_higher_education
                                1 166.30 4557.5 1315.0
                                1 183.71 4574.9 1317.4
## - school
## - failures
                                      340.22 4731.5 1339.3
##
## Step: AIC=1291.85
## final_grade ~ school + sex + age + urban_rural + fam_size + mom_edu +
       dad_job + student_guardian + studytime + failures + extra_school_support +
##
##
       extracurricular_activities + wants_higher_education + internet +
##
      has_romantic_partner + family_relationship + freetime + weekday_alcohol_cons +
##
       health + absences
##
##
                                Df Sum of Sq
                                                RSS
                                                       AIC
                                       9.50 4407.5 1291.2
## - extracurricular_activities 1
## - urban_rural
                                       10.24 4408.3 1291.4
## - internet
                                      10.53 4408.6 1291.4
                                1
## - family relationship
                                      11.02 4409.0 1291.5
## - freetime
                                      12.19 4410.2 1291.6
                                1
## - fam_size
                                      12.51 4410.5 1291.7
                                1
## - student_guardian
                                       26.17 4424.2 1291.7
                                             4398.0 1291.8
## <none>
## - age
                                      14.45 4412.5 1292.0
                                1
                                       56.61 4454.6 1292.2
## - dad_job
                                4
## - absences
                                1
                                      18.09 4416.1 1292.5
## + paid_extra_classes
                               1
                                       6.79 4391.2 1292.8
                                      5.83 4392.2 1293.0
## + dad_edu
                                1
## + going_out_amount
                                1
                                       4.26 4393.8 1293.2
## + attended_nursery
                                1
                                       4.05 4394.0 1293.2
## + weekend_alcohol_cons
                                1
                                      2.33 4395.7 1293.5
## + parents_cohabit
                                1
                                       1.34 4396.7 1293.7
## + traveltime
                                       0.47 4397.6 1293.8
                                1
                               1 27.00 4425.0 1293.8
## - mom_edu
## + fam_edu_support
                               1
                                     0.05 4398.0 1293.8
## - has romantic partner
                               1
                                      29.97 4428.0 1294.2
```

```
## + school reason
                                      18.06 4380.0 1295.2
                                4
                                      25.67 4372.4 1296.0
## + mom_job
## - health
                                      43.92 4441.9 1296.3
## - weekday_alcohol_cons
                                      45.18 4443.2 1296.5
                                1
## - sex
                                1
                                     49.12 4447.1 1297.1
## - studytime
                                    67.75 4465.8 1299.8
                                1
## - extra school support
                                1 104.21 4502.2 1305.0
## - wants_higher_education
                                1 165.15 4563.2 1313.8
                                   185.06 4583.1 1316.6
## - school
                                1
## - failures
                                1
                                     350.17 4748.2 1339.6
##
## Step: AIC=1291.25
## final_grade ~ school + sex + age + urban_rural + fam_size + mom_edu +
      dad_job + student_guardian + studytime + failures + extra_school_support +
##
##
      wants_higher_education + internet + has_romantic_partner +
##
      family_relationship + freetime + weekday_alcohol_cons + health +
##
      absences
##
                               Df Sum of Sq
##
                                            RSS
                                                      AIC
## - urban rural
                                      9.14 4416.7 1290.6
## - freetime
                                1
                                      9.71 4417.2 1290.7
## - internet
                                      11.28 4418.8 1290.9
                                1
## - student_guardian
                                2
                                    25.04 4432.6 1290.9
## - family relationship
                                      11.63 4419.2 1291.0
                                1
## - fam size
                                1
                                      12.19 4419.7 1291.0
## - age
                                1
                                     13.32 4420.8 1291.2
## <none>
                                            4407.5 1291.2
                                    56.35 4463.9 1291.5
## - dad_job
                                      9.50 4398.0 1291.8
## + extracurricular_activities 1
## - absences
                                    18.49 4426.0 1292.0
                                1
## + paid_extra_classes
                                1
                                      5.99 4401.5 1292.4
## + dad_edu
                                1
                                      5.91 4401.6 1292.4
## + attended_nursery
                               1
                                      3.64 4403.9 1292.7
                                      3.55 4404.0 1292.7
## + going_out_amount
                                1
## + weekend alcohol cons
                                1
                                      2.19 4405.3 1292.9
                                     2.08 4405.4 1292.9
## + parents_cohabit
                                1
## + traveltime
                               1
                                     0.48 4407.1 1293.2
## + fam_edu_support
                                      0.02 4407.5 1293.2
                                1
                                   27.59 4435.1 1293.3
## - has_romantic_partner
                                1
                                    29.44 4437.0 1293.6
## - mom_edu
                                1
                                3
                                     21.20 4386.3 1294.1
## + school reason
                                     26.19 4381.3 1295.4
## + mom job
                                4
                                     44.30 4451.8 1295.7
## - health
                                1
## - weekday_alcohol_cons
                                1 45.25 4452.8 1295.9
                                    45.30 4452.8 1295.9
## - sex
                                1
                                    72.41 4479.9 1299.8
## - studytime
                                1
                                1 106.45 4514.0 1304.7
## - extra_school_support
## - wants_higher_education
                                1 167.43 4575.0 1313.4
## - school
                                1
                                   192.29 4599.8 1317.0
## - failures
                                1
                                     346.56 4754.1 1338.4
##
## Step: AIC=1290.59
## final_grade ~ school + sex + age + fam_size + mom_edu + dad_job +
      student_guardian + studytime + failures + extra_school_support +
```

```
##
       wants_higher_education + internet + has_romantic_partner +
##
       family_relationship + freetime + weekday_alcohol_cons + health +
##
       absences
##
                                Df Sum of Sq
                                                 RSS
## - freetime
                                        9.93 4426.6 1290.0
## - family_relationship
                                       10.54 4427.2 1290.1
                                 1
## - student_guardian
                                       25.07 4441.7 1290.3
                                 2
## - internet
                                 1
                                       13.19 4429.9 1290.5
## - fam_size
                                 1
                                       13.43 4430.1 1290.6
## <none>
                                              4416.7 1290.6
                                       13.96 4430.6 1290.6
## - age
                                  1
## - dad_job
                                  4
                                       55.23 4471.9 1290.7
                                       17.98 4434.6 1291.2
## - absences
                                        9.14 4407.5 1291.2
## + urban_rural
                                  1
## + extracurricular_activities 1
                                        8.40 4408.3 1291.4
                                        6.61 4410.1 1291.6
## + paid_extra_classes
                                 1
## + dad edu
                                        5.91 4410.8 1291.7
                                        3.69 4413.0 1292.0
## + attended_nursery
                                 1
## + going out amount
                                 1
                                        3.03 4413.6 1292.2
## + weekend_alcohol_cons
                                 1
                                        2.17 4414.5 1292.3
## + parents_cohabit
                                        1.36 4415.3 1292.4
                                 1
## + traveltime
                                        0.01 4416.7 1292.6
                                 1
## + fam edu support
                                        0.00 4416.7 1292.6
                                 1
                                       27.79 4444.5 1292.7
## - has_romantic_partner
                                 1
## - mom edu
                                 1
                                       32.46 4449.1 1293.3
## + school_reason
                                 3
                                       20.00 4396.7 1293.7
                                       27.47 4389.2 1294.5
## + mom_job
                                 4
## - health
                                       44.28 4460.9 1295.1
                                 1
## - sex
                                       45.49 4462.2 1295.2
                                 1
## - weekday_alcohol_cons
                                 1
                                       47.17 4463.8 1295.5
## - studytime
                                 1
                                       72.12 4488.8 1299.1
## - extra_school_support
                                      107.52 4524.2 1304.2
                                      168.49 4585.2 1312.9
## - wants_higher_education
                                 1
## - school
                                  1
                                       241.06 4657.7 1323.1
## - failures
                                  1
                                       346.10 4762.8 1337.5
##
## Step: AIC=1290.05
## final_grade ~ school + sex + age + fam_size + mom_edu + dad_job +
##
       student_guardian + studytime + failures + extra_school_support +
##
       wants higher education + internet + has romantic partner +
##
       family_relationship + weekday_alcohol_cons + health + absences
##
##
                                Df Sum of Sq
                                                 RSS
                                                        AIC
## - family_relationship
                                 1
                                        8.16 4434.8 1289.2
## - dad_job
                                       52.57 4479.2 1289.7
## - internet
                                 1
                                       11.47 4438.1 1289.7
                                        26.48 4453.1 1289.9
## - student_guardian
## <none>
                                              4426.6 1290.0
## - fam_size
                                 1
                                       14.21 4440.8 1290.1
                                       15.81 4442.4 1290.4
## - age
                                 1
                                       16.86 4443.5 1290.5
## - absences
                                1
## + freetime
                                1
                                        9.93 4416.7 1290.6
## + urban rural
                                 1
                                        9.36 4417.2 1290.7
```

```
## + going_out_amount
                                       7.18 4419.4 1291.0
                                1
## + extracurricular_activities 1
                                       6.06 4420.5 1291.2
## + paid_extra_classes
                                       5.22 4421.4 1291.3
## + dad_edu
                                       5.14 4421.5 1291.3
                                 1
## + attended nursery
                                1
                                       3.84 4422.8 1291.5
## + weekend alcohol cons
                                       2.79 4423.8 1291.6
                                1
## + parents cohabit
                                      1.21 4425.4 1291.9
                                1
## + fam_edu_support
                                1
                                       0.00 4426.6 1292.0
## + traveltime
                                1
                                       0.00 4426.6 1292.0
## - has_romantic_partner
                                 1
                                       28.78 4455.4 1292.3
## - mom_edu
                                1
                                       33.16 4459.8 1292.9
                                3
                                       18.34 4408.3 1293.4
## + school_reason
## + mom_job
                                4
                                       25.86 4400.7 1294.2
## - health
                                 1
                                      46.55 4473.1 1294.8
## - sex
                                   50.03 4476.6 1295.3
                                 1
## - weekday_alcohol_cons
                                 1
                                      51.28 4477.9 1295.5
                                      72.24 4498.8 1298.6
## - studytime
                                 1
## - extra_school_support
                                1 107.23 4533.8 1303.6
                                   175.02 4601.6 1313.2
## - wants_higher_education
                                1
                                    244.99 4671.6 1323.0
## - school
                                 1
## - failures
                                 1
                                      359.02 4785.6 1338.7
##
## Step: AIC=1289.25
## final_grade ~ school + sex + age + fam_size + mom_edu + dad_job +
##
       student_guardian + studytime + failures + extra_school_support +
       wants_higher_education + internet + has_romantic_partner +
##
       weekday_alcohol_cons + health + absences
##
##
                               Df Sum of Sq
                                                RSS
                                                       AIC
## - dad_job
                                       49.66 4484.4 1288.5
## - student_guardian
                                       26.31 4461.1 1289.1
## - internet
                                1
                                       13.01 4447.8 1289.2
## <none>
                                             4434.8 1289.2
                                       14.04 4448.8 1289.3
## - fam_size
                                1
## - age
                                       16.80 4451.6 1289.7
## - absences
                                       18.43 4453.2 1289.9
                                1
## + urban rural
                                       8.35 4426.4 1290.0
## + family_relationship
                                       8.16 4426.6 1290.0
                                1
## + freetime
                                       7.55 4427.2 1290.1
                                 1
## + extracurricular_activities 1
                                       6.76 4428.0 1290.3
## + going out amount
                                       5.46 4429.3 1290.5
                                1
## + dad edu
                                       5.22 4429.5 1290.5
                                1
## + paid_extra_classes
                                       4.90 4429.9 1290.5
                                1
## + weekend_alcohol_cons
                                       3.91 4430.9 1290.7
                                1
## + attended_nursery
                                1
                                       3.47 4431.3 1290.7
                                       1.35 4433.4 1291.0
## + parents_cohabit
                                 1
## + fam_edu_support
                                 1
                                       0.00 4434.8 1291.2
## + traveltime
                                 1
                                       0.00 4434.8 1291.2
## - has_romantic_partner
                                 1
                                       29.32 4464.1 1291.5
## - mom_edu
                                1
                                       32.88 4467.6 1292.0
## + school_reason
                                3
                                       18.26 4416.5 1292.6
## - health
                                1
                                      43.06 4477.8 1293.5
## + mom job
                                4
                                      23.94 4410.8 1293.7
## - sex
                                1
                                       46.93 4481.7 1294.1
```

```
## - weekday_alcohol_cons
                                      55.75 4490.5 1295.3
                                1
                                      71.60 4506.4 1297.6
## - studytime
                                1
## - extra school support
                                     107.16 4541.9 1302.7
## - wants_higher_education
                                   175.85 4610.6 1312.5
                                1
## - school
                                1
                                      245.45 4680.2 1322.2
## - failures
                                      364.95 4799.7 1338.6
                                 1
## Step: AIC=1288.47
## final_grade ~ school + sex + age + fam_size + mom_edu + student_guardian +
##
       studytime + failures + extra_school_support + wants_higher_education +
##
       internet + has_romantic_partner + weekday_alcohol_cons +
##
      health + absences
##
                               Df Sum of Sq
##
                                                RSS
                                                       AIC
                                       8.61 4493.0 1287.7
## - internet
                                1
## - fam_size
                                       11.44 4495.9 1288.1
                                       27.12 4511.5 1288.4
## - student_guardian
## <none>
                                             4484.4 1288.5
                                       10.48 4473.9 1289.0
## + dad edu
                                1
## - absences
                                1
                                       17.44 4501.9 1289.0
## - age
                                1
                                      18.53 4502.9 1289.2
## + dad_job
                                      49.66 4434.8 1289.2
## + urban_rural
                                       7.40 4477.0 1289.4
                                1
## + weekend alcohol cons
                                       7.36 4477.1 1289.4
                                1
## + extracurricular_activities 1
                                       6.82 4477.6 1289.5
## + paid_extra_classes
                          1
                                       6.47 4478.0 1289.5
## + freetime
                                       5.70 4478.7 1289.7
                                1
## + going_out_amount
                                1
                                       5.32 4479.1 1289.7
                                      5.25 4479.2 1289.7
## + family_relationship
                                1
## + attended_nursery
                                      4.27 4480.1 1289.8
                                1
                                    25.41 4509.8 1290.1
## - has_romantic_partner
                                1
## + parents_cohabit
                                1
                                     0.69 4483.7 1290.4
## + traveltime
                                1
                                       0.12 4484.3 1290.5
                                       0.03 4484.4 1290.5
## + fam_edu_support
                                1
## + school reason
                                3
                                      18.35 4466.1 1291.8
## - health
                                      40.61 4525.0 1292.3
                                1
## - sex
                                1
                                      46.24 4530.7 1293.1
## + mom_job
                                4
                                   18.46 4466.0 1293.8
## - mom_edu
                                1
                                      55.25 4539.7 1294.4
                                      64.29 4548.7 1295.7
## - weekday_alcohol_cons
                                1
## - studytime
                                      64.75 4549.2 1295.8
                                1
## - extra_school_support
                                      95.20 4579.6 1300.1
                                1
## - wants_higher_education
                                1
                                     171.89 4656.3 1310.9
## - school
                                      258.16 4742.6 1322.8
                                 1
## - failures
                                      379.10 4863.5 1339.1
##
## Step: AIC=1287.72
## final_grade ~ school + sex + age + fam_size + mom_edu + student_guardian +
##
       studytime + failures + extra_school_support + wants_higher_education +
##
       has_romantic_partner + weekday_alcohol_cons + health + absences
##
##
                               Df Sum of Sq
                                                RSS
                                                       AIC
## - fam size
                                1
                                       11.71 4504.7 1287.4
## <none>
                                             4493.0 1287.7
```

```
## - student_guardian
                                      28.93 4522.0 1287.9
                                      16.84 4509.9 1288.2
## - absences
                                1
## + dad edu
                                      10.47 4482.6 1288.2
## + urban_rural
                                       8.63 4484.4 1288.5
                                1
## + internet
                                1
                                       8.61 4484.4 1288.5
## - age
                                     19.81 4512.8 1288.6
                                1
                                     7.48 4485.6 1288.6
## + extracurricular_activities 1
## + weekend_alcohol_cons
                                1
                                      6.56 4486.5 1288.8
## + family_relationship
                                1
                                     6.39 4486.6 1288.8
## + paid_extra_classes
                                1
                                      6.25 4486.8 1288.8
## + attended_nursery
                                1
                                       4.64 4488.4 1289.0
                                       4.53 4488.5 1289.1
## + freetime
                                1
## + going_out_amount
                                1
                                       4.09 4488.9 1289.1
                                      45.26 4447.8 1289.2
## + dad_job
                                    24.08 4517.1 1289.2
## - has_romantic_partner
                                1
                                   1.19 4491.8 1289.5
## + parents_cohabit
                                1
                                      0.10 4492.9 1289.7
## + fam_edu_support
                                1
## + traveltime
                                1
                                      0.00 4493.0 1289.7
                                3
                                     19.18 4473.9 1290.9
## + school_reason
## - health
                                1
                                      42.09 4535.1 1291.8
## - sex
                                1
                                      45.32 4538.4 1292.2
## + mom job
                                      21.82 4471.2 1292.6
                                   62.77 4555.8 1294.7
## - weekday_alcohol_cons
                                1
                                      64.25 4557.3 1294.9
## - studytime
                                1
## - mom edu
                                1
                                    67.59 4560.6 1295.4
## - extra_school_support
                                1
                                      96.78 4589.8 1299.5
## - wants_higher_education
                                   173.21 4666.2 1310.3
                                1
## - school
                                1
                                     284.88 4777.9 1325.6
## - failures
                                     387.58 4880.6 1339.4
                                 1
##
## Step: AIC=1287.41
## final_grade ~ school + sex + age + mom_edu + student_guardian +
##
       studytime + failures + extra_school_support + wants_higher_education +
##
       has_romantic_partner + weekday_alcohol_cons + health + absences
##
                               Df Sum of Sq
                                               RSS
##
                                                      ATC
## <none>
                                            4504.7 1287.4
## - student_guardian
                                      28.07 4532.8 1287.4
## + fam size
                                      11.71 4493.0 1287.7
                                1
## - absences
                                      16.60 4521.3 1287.8
                                1
## + urban rural
                                      9.86 4494.9 1288.0
                                1
## + dad edu
                                       9.54 4495.2 1288.0
                                1
## + internet
                                1
                                       8.88 4495.9 1288.1
## - age
                                      20.20 4524.9 1288.3
                                1
## + paid_extra_classes
                                1
                                       7.12 4497.6 1288.4
## + extracurricular_activities 1
                                       7.06 4497.7 1288.4
## + family_relationship
                                1
                                       6.32 4498.4 1288.5
## + weekend_alcohol_cons
                                 1
                                       5.92 4498.8 1288.5
## + freetime
                                1
                                       5.01 4499.7 1288.7
## + going_out_amount
                                1
                                       4.42 4500.3 1288.8
                                      3.13 4501.6 1289.0
## + attended_nursery
                                1
                               1 25.09 4529.8 1289.0
## - has_romantic_partner
## + dad job
                                4
                                    42.64 4462.1 1289.2
## + fam edu support
                                1
                                      0.06 4504.7 1289.4
```

```
0.03 4504.7 1289.4
## + parents_cohabit
                                  1
## + traveltime
                                         0.00 4504.7 1289.4
                                  1
                                        21.43 4483.3 1290.3
## + school reason
                                  3
## - sex
                                  1
                                        41.67 4546.4 1291.4
## - health
                                  1
                                        42.42 4547.2 1291.5
## + mom job
                                  4
                                        23.75 4481.0 1292.0
## - weekday alcohol cons
                                  1
                                        60.73 4565.5 1294.1
## - studytime
                                  1
                                        65.05 4569.8 1294.7
## - mom_edu
                                  1
                                        65.71 4570.5 1294.8
## - extra_school_support
                                  1
                                        99.72 4604.5 1299.6
## - wants_higher_education
                                       173.42 4678.2 1309.9
                                  1
## - school
                                  1
                                       281.95 4786.7 1324.8
## - failures
                                       400.80 4905.5 1340.7
```

summary(step)

```
##
## Call:
## lm(formula = final_grade ~ school + sex + age + mom_edu + student_guardian +
##
       studytime + failures + extra_school_support + wants_higher_education +
##
      has_romantic_partner + weekday_alcohol_cons + health + absences,
##
       data = data)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -12.1548 -1.3687
                       0.0072
                                1.5292
                                         7.2845
##
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                          1.75710
                                                   5.068 5.28e-07 ***
                               8.90516
## schoolMousinho da Silveira -1.51318
                                          0.24021
                                                   -6.299 5.59e-10 ***
## sexM
                              -0.57091
                                          0.23574
                                                  -2.422 0.015726 *
                                                   1.686 0.092231
## age
                               0.16711
                                          0.09910
## mom_edu
                               0.30127
                                          0.09906
                                                    3.041 0.002454 **
## student_guardianmother
                              -0.45308
                                          0.25282
                                                  -1.792 0.073592
## student_guardianother
                               0.03407
                                          0.51153
                                                   0.067 0.946911
## studytime
                               0.40872
                                          0.13508
                                                   3.026 0.002580 **
## failures
                              -1.48437
                                          0.19764 -7.511 2.01e-13 ***
## extra_school_supportTRUE
                              -1.33575
                                          0.35655
                                                  -3.746 0.000196 ***
## wants_higher_educationTRUE 1.86377
                                          0.37726
                                                    4.940 9.99e-07 ***
                              -0.42199
## has_romantic_partnerTRUE
                                          0.22456
                                                  -1.879 0.060679 .
## weekday_alcohol_cons
                              -0.35842
                                          0.12260
                                                   -2.924 0.003584 **
## health
                              -0.17961
                                          0.07351
                                                   -2.443 0.014826 *
## absences
                              -0.03687
                                          0.02412 -1.529 0.126848
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.666 on 634 degrees of freedom
## Multiple R-squared: 0.3339, Adjusted R-squared: 0.3192
## F-statistic: 22.7 on 14 and 634 DF, p-value: < 2.2e-16
```

The hybrid step-wise linear regression model builder results in 14 different variables. There are 4 variables with higher statistical significance than the others, the school the student attended, the number of previous

failures the student has, whether or not the student had extra educational support, and whether or not the student wants a higher education. Among these, the one that has the highest estimate on the influence is whether or not the student wants higher education, although all 4 variables have fairly similar estimates. That is also the only predictor that has a positive relationship with the final score. All the other predictors, including, surprisingly whether a sudent has extra educational support, have negative relationships.

Sadly, the adjusted R-squared is 0.3192. This is low enough that we cannot make good predictions, even if we can identify influential factors.