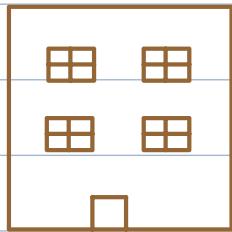


Hotel



← & Vishal

301

Key

Unique

Room	Available
1	✓
2	✗
3	✓
⋮	
301	✓

Value

, capacity, AC, etc

Multiple

Notebook

Hash Map

Q → Store population of every country →
country name → population
string → long

Q → Store # states of every country →
country name → # states
string → int

Q → Store name of all states of every country →
country name → list of states
string → list of string

Q → Store population of each state in every country →
country name → (state → population)
string → HM < string, int >

< Key, Null > → < Key > Hash Set

✓ Hash Set / Hash Map → Hashing $TC = O(1)$ → Store Keys in random order.

Tree Set / Tree Map → Maintain Keys in Sorted Order

(use balanced BST internally) $TC = O(\log N)$

LinkedHashMap / LinkedHashSet → Maintain Keys in order of insertion.

Operations

To update → insert the same key again.

HashMap

- 1) insert(key, value) / put(key, value)
 - 2) size()
 - 3) delete(key) / remove(key)
 - 4) get(key)
 - 5) containsKey(key)
 - ⋮
- $TC = O(1)$

HashSet

- 1) insert(key) / add(key)
 - 2) size()
 - 3) delete(key) / remove(key)
 - 4) contains(key)
 - ⋮
- $TC = O(1)$

$Q \rightarrow$ Given N elements & Q queries.

Find frequency of an element for multiple queries.

(Ans)

	0	1	2	3	4	5	6	7	
A = [2	6	3	6	3	8	2	6]]
Query	Frequency								
6						3			

Bruteforce \rightarrow \forall query, travel & find frequency.

8	1
5	0

$$TC = O(Q \times N) \quad SC = O(1)$$

Frequency Array \rightarrow $F[i]$ \rightarrow frequency of i

```
for i → 0 to (N-1) {  
    | F[A[i]] ++  
    }  
}
```

$\|$ Find freq. of $x \rightarrow F[x]$

$SC = O(\text{Range of } A[i])$

0	1	2	3	4	5	6	7
✓	✓	✓	✓	✓	✓	✓	✓

$A = [2, 1, 3, 3, 0, 3, 2, 2]$

$F = [1, 1, 3, 3]$

Hash Map \rightarrow $\langle \text{int}, \text{int} \rangle$

$A[i] \rightarrow$ frequency of $A[i]$

```
for i → 0 to (N-1) {  
    | if (hm. containsKey(A[i])) {  
    |     | v = hm.get(A[i])  
    |     | hm.put(A[i], v+1)  
    | } else {  
    |     | hm.put(A[i], 1)  
    }  
}
```

```

for i → 0 to (Q-1) {
    x = B[i] // B → queries
    if (hm.containskey(x))
        print (hm.get(x))
    else
        print (0)
}

```

$hm.getOrDefault(x, 0)$

$$TC = \underline{O(N+Q)} \quad SC = \underline{O(N)}$$

\rightarrow Given N integers, find first non-repeating value.
 Return -1 if all elements are repeating.

$$N = 6 \quad A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 1 & 3 & 5 & 1 & 2 & 3 \end{bmatrix}$$

$\xrightarrow{\quad}$

$Ans = \underline{5}$

$$N = 5 \quad A = \begin{bmatrix} 2 & 3 & 2 & 4 & 4 \end{bmatrix} \quad Ans = \underline{3}$$

Bruteforce → \forall elements check if that element is repeating in future. $TC = \underline{O(N^2)} \quad SC = \underline{O(1)}$

Sol → 1) store frequency $\forall A[i]$.

2)

```

for i → 0 to (N-1) {
    if (hm.get(A[i]) == 1)
        return A[i]
}

```

$$TC = \underline{O(N)} \quad SC = \underline{O(N)}$$

Q → Find the count of distinct elements in A[].

$$A = [\begin{smallmatrix} 0 & 1 & 2 & 3 & 4 \\ 3 & 5 & 6 & 5 & 6 \end{smallmatrix}] \quad \{3, 5, 6\}$$

Ans = 3

$$A = [\begin{smallmatrix} 0 & 1 & 2 \\ 5 & 5 & 5 \end{smallmatrix}] \quad \text{Ans} = \underline{1}$$

for $i \rightarrow 0$ to $(N-1)$ {
 hs.add(A[i])
}

return hs.size()

TC = $O(N)$ SC = $O(N)$

Q → Given an integer array, check if there exist a subarray with 0 sum.

$$A = [\begin{smallmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 2 & 2 & 1 & -3 & 4 & 3 \end{smallmatrix}] \quad \text{Ans} = \underline{\text{true}}$$

Bruteforce → ∀ subarray, calculate sum &
check if sum = 0.

$$\frac{N \times (N+1)}{2} \quad \text{TC} = O(N^3) \rightarrow \underline{O(N^2)}$$

SC = $O(1)$

subarray sum → prefix sum

subarray sum $l \dots r \Rightarrow P[r] - P[l-1] \quad // l > 0$

$$P[r] - P[l-1] = 0 \quad \text{if } (l == 0) \rightarrow P[r]$$
$$\Rightarrow P[r] = P[l-1] \quad P[r] = 0$$

$$P[0] = A[0]$$

$$P[i] = A[0] + A[1] + \dots + A[i]$$

if ($P[0] == 0$) return true

hs.add($P[0]$)

for $i \rightarrow 1$ to $(N-1)$ {

$$P[i] = P[i-1] + A[i]$$

if ($P[i] == 0$) return true

hs.add($P[i]$)

}

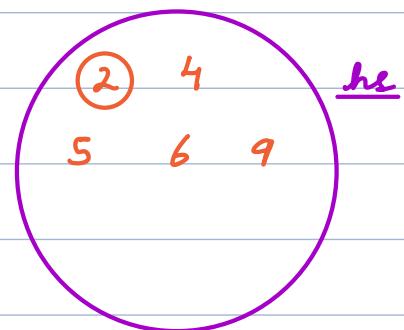
if ($hs.size() == N$) return false

else return true

$$TC = \underline{O(N)} \quad SC = \underline{O(N)}$$

$$A = [\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 2 & 2 & 1 & -3 & 4 & 3 \end{matrix}]$$

$$P = \begin{matrix} 2 & 4 & 5 & 2 & 6 & 9 \end{matrix}$$



Value

contest — learner_id \rightarrow not attempted / score
key \downarrow int
-1

\Rightarrow Given an integer array, check if there exist a pair (i, j) s.t $A[i] + A[j] = K \ \& \ i \neq j$

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 8 & 9 & 1 & -2 & 4 & 5 & 11 & -6 & 4 \end{bmatrix}$$

$$K = 6 \quad A[2] + A[5] = 6 \quad \text{Ans} = \text{true}$$

$$K = 22 \quad \text{Ans} = \text{false}$$

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 3 & 5 & 1 & 2 & 1 & 2 \end{bmatrix} \quad K = 7 \quad \text{Ans} = \text{true}$$

$$K = 10 \quad \text{Ans} = \text{false}$$

Bruteforce $\rightarrow \forall i, j$ check if $\text{sum} = K \ \& \ i \neq j$.

$$TC = \underline{O(N^2)} \quad SC = \underline{O(1)}$$

for $i \rightarrow 1$ to $(N-1)$ {

 for $j \rightarrow 0$ to $(i-1)$ {
 if $(A[i] + A[j]) == K)$
 return true
 }

$$A[i] + A[j] = A[j] + A[i]$$

} return false

$$TC = \underline{O(N^2)} \quad SC = \underline{O(1)}$$

$i < j$ or $i > j$

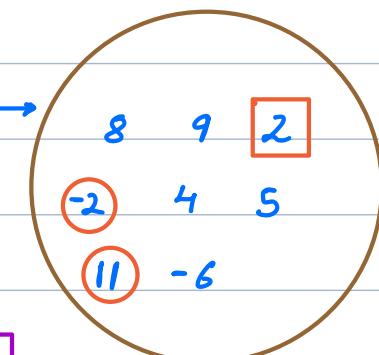
check if there exist

$A[j]$ st. $A[j] = K - A[i]$.

} Hash Set

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 8 & 9 & 2 & -2 & 4 & 5 & 11 & -6 & 4 \end{bmatrix}$$

i i i



search $K - A[i]$ \rightarrow complete array

$$K = 6$$

$$6 - 8 = -2$$

$$\text{Ans} = \text{true}$$

K = 9

$$9 - 8 = 1 \quad x$$

$$9 - 9 = 0 \quad x$$

$$9 - 2 = 7 \quad x$$

$$9 - (-2) = 11 \quad \checkmark \quad \text{Ans} = \text{true}$$

K = 4

$$4 - 8 = -4$$

$$4 - 9 = -5$$

$$4 - 2 = 2 \quad \text{Ans} = \text{true} \rightarrow \text{false}$$

$$(i == j)$$

Hashset should contain values from 0 to (i-1).

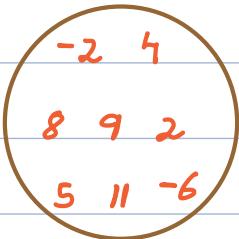
For i, \Rightarrow Search for $K - A[i] \checkmark$

\Rightarrow Insert A[i] in Hashset \checkmark ($j < i$)

$$A = [\begin{array}{cccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 8 & 9 & 2 & -2 & 4 & 5 & 11 & -6 & 4 \end{array}]$$

$\downarrow \downarrow \downarrow \downarrow \downarrow$

$i \quad i \quad i \quad i$



K = 4

$K - A[i]$

$$4 - 8 = -4$$

$$4 - 5 = -1$$

$$4 - 9 = -5$$

$$4 - 11 = -7$$

$$4 - 2 = 2$$

$$4 - (-6) = 10$$

$$4 - (-2) = 6$$

$$4 - 4 = 0$$

Ans = false \checkmark

$$4 - 4 = 0$$

K = 7

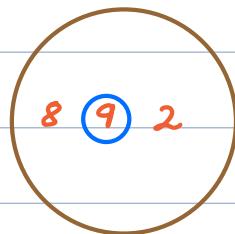
$$7 - 8 = -1$$

$$7 - (-2) = 9$$

$$7 - 9 = -2$$

Ans = true

$$7 - 2 = 5$$



TC = O(N)

SC = O(N)

$i \setminus j$	0	1	2	3	4
0					
1					
2					
3					
4					

$$N = 5$$

$$i \neq j$$

$$i < j$$

$$i > j$$

\rightarrow count pairs with sum = K .

$$i \neq j \text{ & } (i, j) = (j, i).$$

$$A = [\begin{array}{cccccc} 0 & 1 & 2 & 3 & 4 & 5 \\ 3 & 5 & 1 & 2 & 1 & 2 \end{array}] \quad K = 3$$

i	j
2	3
2	5
3	4
4	5

$$\text{Ans} = 4$$

Find # times a value is present

\Rightarrow Hash Map (freq.)

$$A = [\begin{array}{cccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 8 & 9 & 2 & -2 & 4 & 5 & -2 & 5 & 2 \end{array}]$$

$\langle A[i], \text{freq.} \rangle$

$$K = 7$$

$$K - A[i]$$

$$\text{count} = 0$$

$$7 - 8 = -1$$

$$+ 1$$

$$7 - 9 = -2$$

$$+ 1$$

$$7 - 2 = 5$$

$$+ 1$$

$$7 - (-2) = 9$$

$$+ 1$$

$8 \rightarrow 1$	$4 \rightarrow 1$
$9 \rightarrow 1$	$5 \rightarrow 2$
$2 \rightarrow 1$	
$-2 \rightarrow 2$	

$$7 - 4 = 3$$

$$\underline{+2}$$

$$7 - 5 = 2$$

$$\underline{6} \text{ (Ans)}$$

$$7 - (-2) = 9$$

$$7 - 5 = 2$$

$$7 - 2 = 5$$

$$TC = \underline{O(N)} \quad SC = \underline{O(N)}$$

Q → check if there exist a subarray with sum K .

$$A = [2 \ \underline{3 \ 9} \ -4 \ 1 \ 5] \quad K = 8 \quad \text{Ans} = \text{true}$$

$$K = 12 \quad \text{Ans} = \text{true}$$

$$A = [5 \ 10 \ 20 \ 100 \ 105] \quad K = \underline{110} \quad \text{Ans} = \text{false}$$

subarray sum \Rightarrow prefix sum

$$i \rightarrow j$$

$$P[j] - P[i-1] = K$$

$$i \leq j$$

$$\Rightarrow P[i-1] = P[j] - K$$

$$(i == 0)$$

$$P[j]$$

$\forall j$, check $P[j] - K$ is present in prefix sum

or $P[j] = K$ ✓

$$A = [2 \ 3 \ 9 \ -4 \ 1]$$

$$P \rightarrow 2 \ 5 \ 14$$

$$K = 12$$

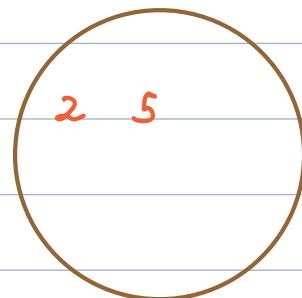
$$\text{Ans} = \text{true}$$

$$\underline{P[j] - K}$$

$$2 - 12 = -10$$

$$5 - 12 = -7$$

$$14 - 12 = 2 \checkmark \quad \text{Ans} = \text{true}$$



Hash Set (prefix sum)

// Hash Set → hs

$$p = 0$$

for $i \rightarrow 0$ to $(N-1)$ do

$$p^+ = A[i]$$

$$P[j] - P[i-1] = K$$

$$\Rightarrow P[j] = K + P[i-1]$$

$$\Rightarrow P[i] - K = P[i-1]$$

if ($p == K$) return True

if (hs. contains (p - K)) returns true

hs. add (p)

7

return false

$$TC = \underline{O(N)}$$

$$SC = \underline{o(N)}$$

(he)

HW → Count subarrays with sum = K.

Q → Given an array, find count of distinct elements in every window of size K.

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 1 & 3 & 4 & 2 & 3 \end{bmatrix} \quad K = 4$$

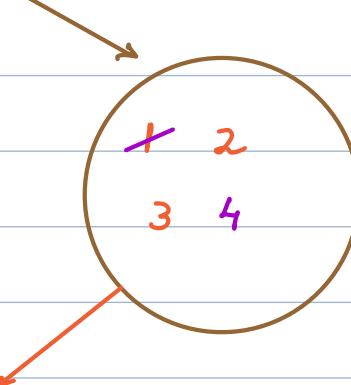
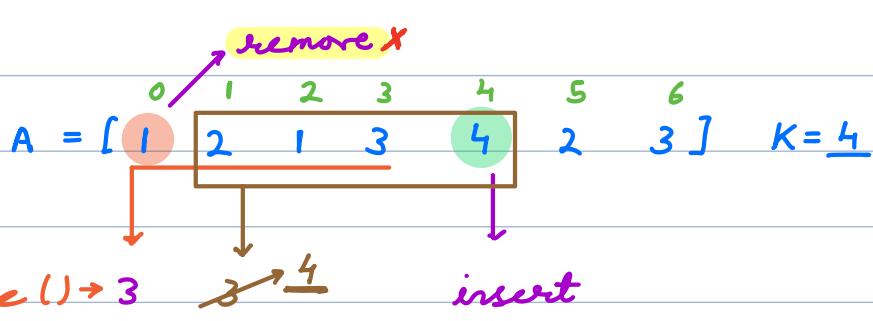
Ans → 3 4 4 3

✓ { fixed size subarray \Rightarrow sliding window
distinct elements in array \Rightarrow

1) Insert all elements in hashset

⇒ Ans = hs.size()

Sliding window + Hashset

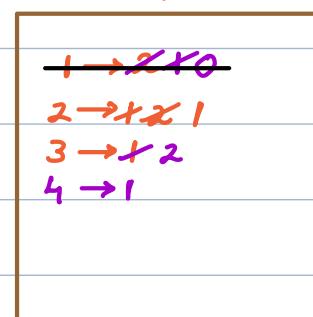
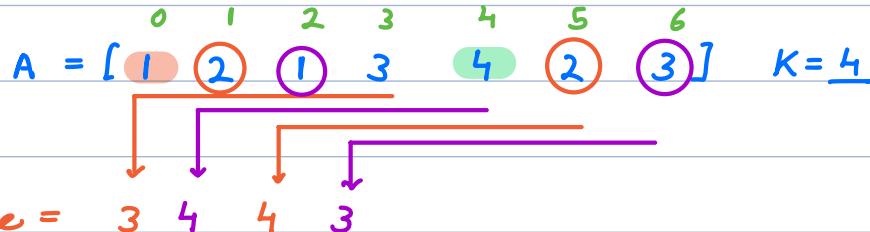


removing from hashset removes all occurrences.

HashMap with freq. of elements.

Sliding Window + HashMap

$\langle A[i], freq. \rangle$



for $i \rightarrow 0$ to $(K-1)$ {

$f = hm.\text{getOrDefault}(A[i], 0)$
 $hm.\text{put}(A[i], f + 1)$

}

 print($hm.\text{size}()$)

for $i \rightarrow K$ to $(N-1)$ { // window $(i-K+1) \dots i$

$f = hm.\text{getOrDefault}(A[i], 0)$ add $A[i]$
 $hm.\text{put}(A[i], f + 1)$ remove $A[i-K]$

$f = hm.\text{get}(A[i-K])$

 if ($f == 1$) $hm.\text{remove}(A[i-K])$

 else $hm.\text{put}(A[i-K], f - 1)$

 print($hm.\text{size}()$)

}

$TC = O(N)$

$SC = O(K)$