Poof. David Salac.

1.b

From the question we have

$$y' = \begin{cases} y(-2) + \frac{1}{4} \\ 1 \end{cases}, \quad y \neq 0$$

9) (5-1) x 1 (0)

For \$ 70, we have

$$\frac{y}{y} = \left(-2t + \frac{1}{t}\right)$$

$$2) \int y' = \int \left(24 + \frac{1}{4}\right) dt$$

2) 
$$lm y = -1^2 + lm + C$$

Again, on differentiating both oides, we get  $\frac{dy}{dt} = t(-24)e^{-t^2+c} + e^{-t^2+c}$ j = (1-242)6-42+C Putting initial condition  $\dot{y}(0) = 1$  and solving ÿ(0)=1 => (1-0)(e-0+c)=1 2) e =1 2) C=0 (1 115) US 16 . . De have  $\dot{y} = (1-2t^2)e^{-t^2}$ and  $y = \pm e^{-t^2} \quad \text{(last page)}$ and 5 to tal gar 511 " " " " J. J. C. 21.1

1.(c) Using 
$$y = \pm e^{-t^2}$$
 from part (b), we get  $y = \pm e^{-t^2}$   $y(1) = 1 \cdot e^{-t} = 0.03$   
= 0.3678

rightly from me and

The position of point p is given by

 $x = L_1 cos o_1 + L_2 cos o_2$   $h = L_1 sin o_1 + L_2 sin o_2$ 

As  $0, L_1, L_2$  and h are given, the only unknown we have is  $0_2$  and a . To convert it into a root problem let's form a system of equations and get  $f(x, o_2): 0$ 

The system of non-linear equations we get are:

h = Li sino, + Lo sinoo

$$sin\theta_2 = h - L_1 sin\theta_1$$

$$L_2$$

$$\frac{1}{2} = \sin^{-1}\left(\frac{h - L_1 \sin \theta_1}{L_2}\right)$$

and the other equation is: 2 = 1,0000, + 120000 Now our not problem is:

$$L_{1} \cos \theta_{1} + L_{2} \cos \theta_{2} - 2 = 0$$
  
 $\sin^{-1} \left( \frac{h - L_{1} \sin \theta_{1}}{L_{2}} \right) - \theta_{2} = 0$ 

After odwing these equations, we'll get 02 & 2,

I have simply to make with the mapped of the

$$x = L_1 \cos O_1 + L_2 \cos \left( \sinh^{-1} \left( \frac{h - L_1 \sin O_1}{L_2} \right) \right)$$

the sea problems and a problems of

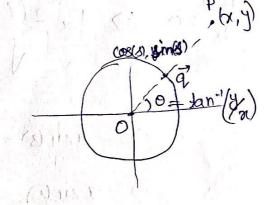
one I gon , I A

in the same

 $\left(\frac{1211}{5}\frac{\mu I\cdot A}{5}\right)^{\prime}m = 20$ 

some of the contract

- 03. The Junction which is at a q minimum when q is the closest to point \$\bar{p}\$ to \$|\bar{q} - \bar{p}|\\ \end{p}
- (b) We know that point à lies on the circumference of the circle with radius 1 so its magnitude will be 1



Also, its very easy to infer from the diagram that point  $\vec{p}$ ,  $\vec{q}$  and center  $\vec{0}$  of the circle will be Lotline co-linear, hence the angle that point q makes with x-axis can be given as  $0 = \tan^{-1}(y)$ , (a,y) is posint  $\overrightarrow{P}$ . took of well offer and Almander trades or work

Therefore point q can be given as:  $(1\times \cos 0, 1\times \sin 0) \equiv (\frac{\chi}{\sqrt{\chi^2 + H^2}}, \frac{\chi}{\sqrt{\chi^2 + H^2}})$ 

O To show the result of (b), we can write the distance between points 789 as:  $d = \sqrt{(x - \cos(\omega))^2 + (y - \sin(\omega))^2}$ 

To minimize d, we set:

$$\frac{d(d)}{ds} = 0 \implies \frac{1}{2} \times 2 \frac{((\alpha - \cos(s)) \cdot \sin(s)) + 2(y + \sin(s))(-\cos(s))}{\sqrt{(\alpha - \cos(s))^2 + (y - \sin(s))^2}} = 0$$

Leinbor dienselmin !!  $\Rightarrow$   $x \sin(8) - \sin(8)\cos(8) - y\cos(6) + \sin(8)\cos(6) = 0$  $\Rightarrow$   $x \sin(8) = y\cos(8)$ 

Janes Janes & Janes Bolding

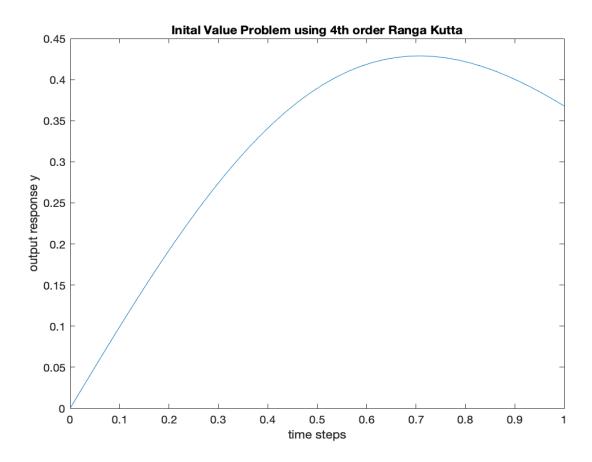
od dlin oliviosides - fan- (4) / m p - 1 / m

with the horar , hence the orgle that pent Here we see that point of on the interface is at minimum distance from point p when 8: lan' (%)

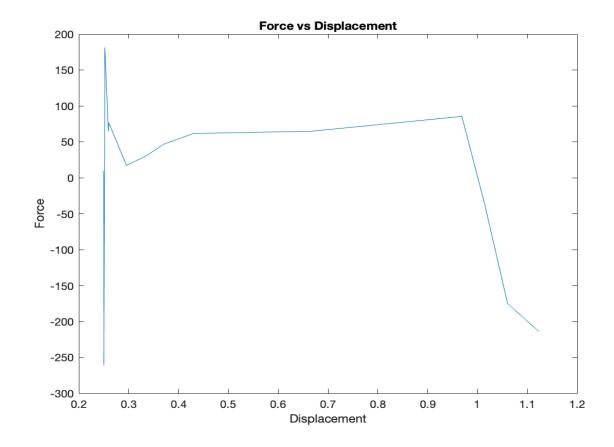
which is consistent with the angle O we had assumed in part (b).

# Plots and diagrams

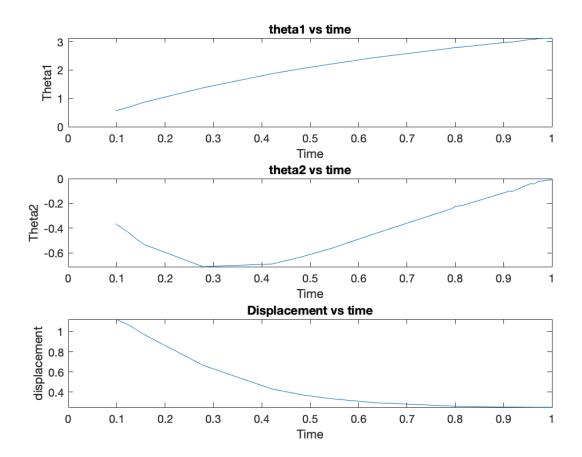
#### 1. A) Solution to ODE



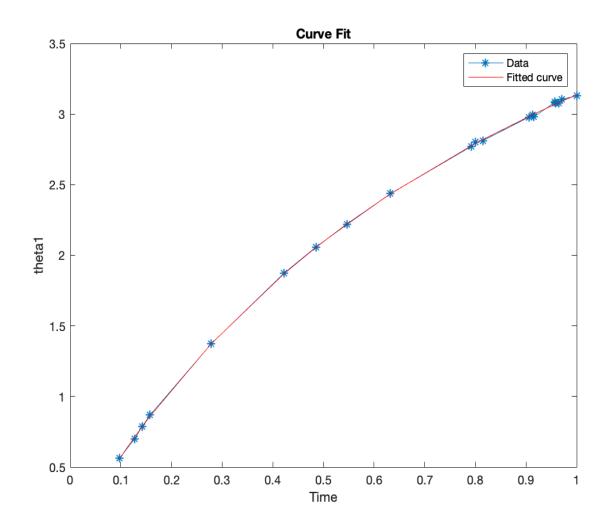
#### 2. A) Force Vs Displacement



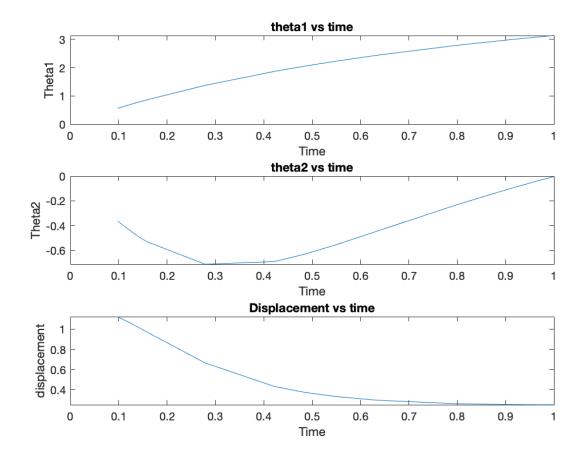
# B. $heta_1$ , $heta_2$ and displacement vs time



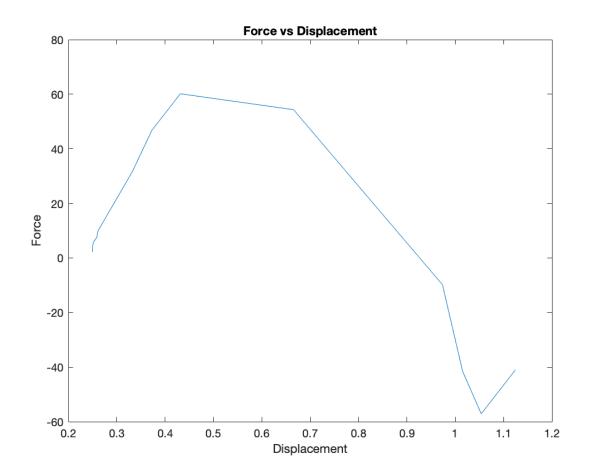
#### C. Fitting non-linear system of equation



# D. $\theta_1$ , $\theta_2$ and displacement vs time for given theta



### E. Force vs Displacement for the given theta



### 3. Plot of interface with calculated minimum distant point q from point p

