

## Topics: Descriptive Statistics and Probability

1. Look at the data given below. Plot the data, find the outliers and find out  $\mu, \sigma, \sigma^2$

Name of company	Measure X
Allied Signal	24.23%
Bankers Trust	25.53%
General Mills	25.41%
ITT Industries	24.14%
J.P.Morgan & Co.	29.62%
Lehman Brothers	28.25%
Marriott	25.81%
MCI	24.39%
Merrill Lynch	40.26%
Microsoft	32.95%
Morgan Stanley	91.36%
Sun Microsystems	25.99%
Travelers	39.42%
US Airways	26.71%
Warner-Lambert	35.00%

**Ans :**

Mean = 33.271333

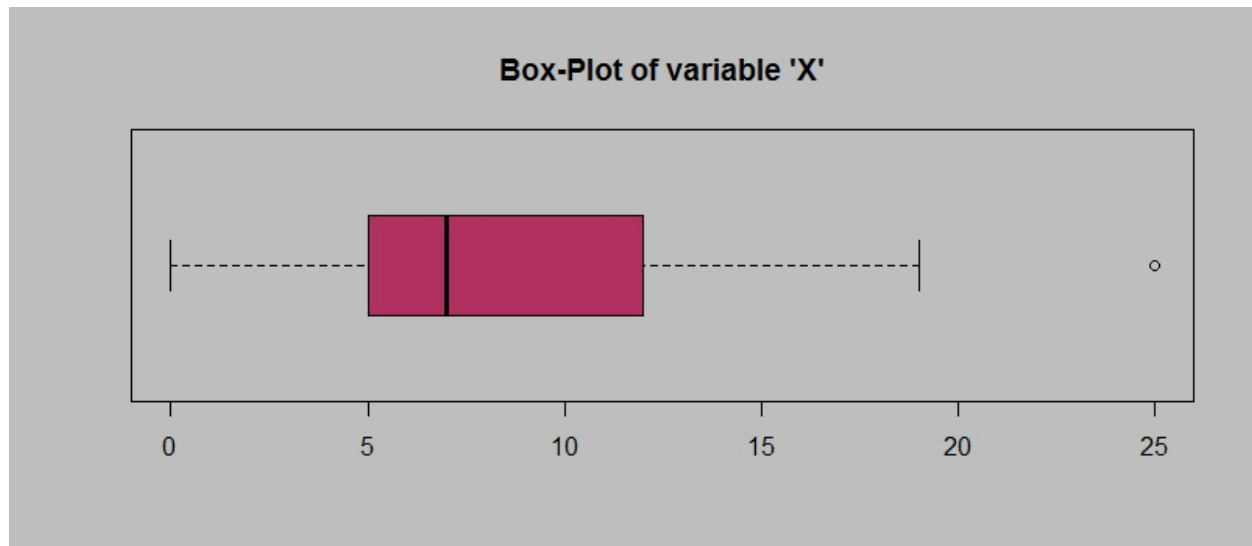
Var = 287.146612

std = 16.9454

Morgan Stanley measure is very distant from other measures .Outlier is = 91.36

(in ipnyb set1 Q1)

2.



Answer the following three questions based on the box-plot above.

- (i) What is inter-quartile range of this dataset? (please approximate the numbers) In one line, explain what this value implies.
- (ii) What can we say about the skewness of this dataset?
- (iii) If it was found that the data point with the value 25 is actually 2.5, how would the new box-plot be affected?

**Ans :**

I . From the boxplot  $Q1 = 5$  ,  $Q3 = 12$

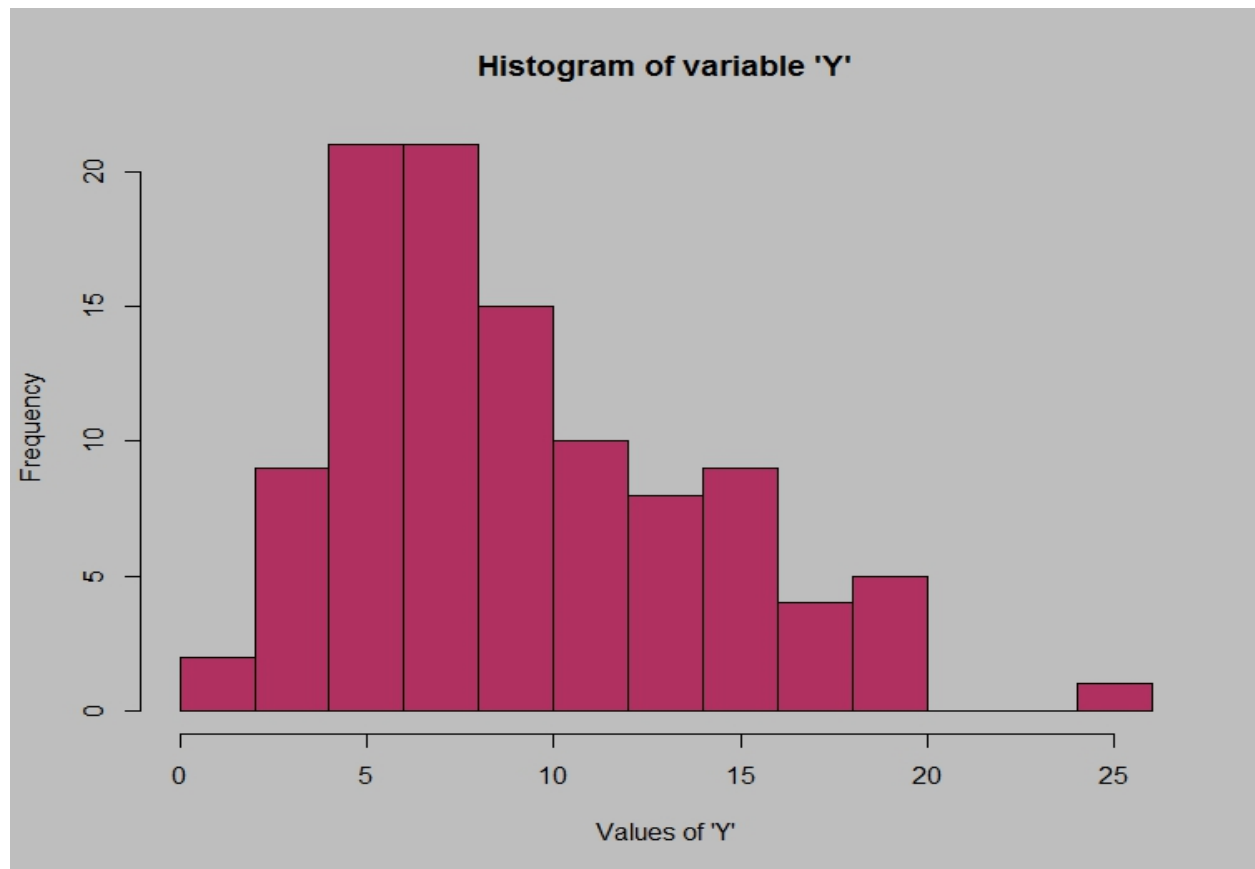
$$IQR = (Q3 - Q1) = 7$$

II . Right skewed

III . From , boxplot 25 observation is outlier

New boxplot will start from 0 and till 20

3.



Answer the following three questions based on the histogram above.

- (i) Where would the mode of this dataset lie?
- (ii) Comment on the skewness of the dataset.
- (iii) Suppose that the above histogram and the box-plot in question 2 are plotted for the same dataset. Explain how these graphs complement each other in providing information about any dataset.

**Ans :**

- I . From histogram the Mode is the range between 4 and 8  
Mode = (4,8)
- II . In histogram most values are concentrated in left side so right skewed
- III . Both histogram and boxplot are having right skewed and the same outlier ( i.e., 25<sup>th</sup> )  
And both are having 50% of observation the range between 5 and 12 .

4. AT&T was running commercials in 1990 aimed at luring back customers who had switched to one of the other long-distance phone service providers. One such commercial shows a businessman trying to reach Phoenix and mistakenly getting Fiji, where a half-naked native on a

beach responds incomprehensibly in Polynesian. When asked about this advertisement, AT&T admitted that the portrayed incident did not actually take place but added that this was an enactment of something that “could happen.” Suppose that one in 200 long-distance telephone calls is misdirected. What is the probability that at least one in five attempted telephone calls reaches the wrong number? (Assume independence of attempts.)

**Ans :**

misdirecting calls = 200

Probability of call misdirecting  $P = (1 / 200)$

Probability of call not misdirecting  $q = (199 / 200)$

number of calls  $n = 5$

$$P(x) = {}^nC_x p^x q^{n-x}$$

At least one in five attempted telephone calls reaches the wrong number

$$P(x) = 1 - \text{none of the call reaches the wrong number}$$

$$P(x) = 1 - 5C_0 (1 / 200)^0 (199 / 200)^{5-0}$$

$$P(x) = 1 - (199 / 200)^5 = 0.02475$$

$$P(x) = 0.02475$$

5. Returns on a certain business venture, to the nearest \$1,000, are known to follow the following probability distribution

x	P(x)
-2,000	0.1
-1,000	0.1
0	0.2
1000	0.2
2000	0.3
3000	0.1

- (i) What is the most likely monetary outcome of the business venture?
- (ii) Is the venture likely to be successful? Explain
- (iii) What is the long-term average earning of business ventures of this kind? Explain
- (iv) What is the good measure of the risk involved in a venture of this kind? Compute this measure

**Ans :**

I . Most likely monetary outcome of the business venture is 2000\$ as it has maximum

$$\text{Probability} = 0.3 \implies 2000 * 0.3 = 600$$

X	P(x)	X * P (x)
- 2000	0.1	- 200
- 1000	0.1	- 100
0	0.2	0
1000	0.2	200
2000	0.3	600
3000	0.1	300
	0.8	800

Expected value = 800

II . so venture is successfully we have to launch

III . long term average earning of business ventures = 800 \$

IV . risk =  $(1 - 0.8) = 0.2 = 20\%$