

# 화일처리 보고서

## B-Tree 삭제

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강의 슬라이드를 참조하였습니다.

## 1 출력 결과

output.txt

File Processing		B-Tree																																																						
M = 3																																																								
Delete 66		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	20	22	24	25	28	30	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55														
		56	57	58	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																												
Delete 10		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	30	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56														
		57	58	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																													
Delete 22		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	30	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57														
		58	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																														
Delete 30		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58														
		59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																															
Delete 44		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59														
		60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																																
Delete 55		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	45	46	47	48	49	50	51	52	53	54	56	57	58	59	60														
		61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																																	
Delete 50		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	60	61														
		62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																																		
Delete 60		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62														
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Delete 100		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	28	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62														
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Delete 28		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63														
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Delete 18		1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64														
		65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																																						
Delete 9		1	2	3	4	5	6	7	8	11	12	13	14	15	16	17	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64															
		65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																																						
Delete 5		1	2	3	4	6	7	8	11	12	13	14	15	16	17	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65															
		67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																																							
Delete 17		1	2	3	4	6	7	8	11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67															
		68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																																								
Delete 6		1	2	3	4	7	8	11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68															
		69	70	73	75	77	80	81	82	83	84	88	89	90	99																																									
Delete 3		1	2	4	7	8	11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68																
		69	70	73	75	77	80	81	82	83	84	88	89	90	99																																									
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		73	75	77	80	81	82	83	84	88	89	90	99																																											
Delete 7		8	11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68	69	70	73																	
		75	77	80	81	82	83	84	88	89	90	99																																												
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Delete 73		11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68	69	70	75	77																	
		80	81	82	83	84	88	89	90	99																																														
Delete 12		11	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68	69	70	75	77	80																	
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Delete 13		11	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65	67	68	69	70	75	77	80	81																	
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Delete 14		11	15	16	20	24	25																																																	

Delete 66	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	20	22	24	25	28	30	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56				
Delete 10	56	57	58	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																			
Delete 22	1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	30	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57				
Delete 30	58	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																					
Delete 44	1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58				
Delete 55	59	60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																						
Delete 50	1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	56	57	58	59	60			
Delete 60	61	62	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																								
Delete 100	1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	56	57	58	59	61	62		
Delete 28	63	64	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99	100																										
Delete 18	1	2	3	4	5	6	7	8	9	11	12	13	14	15	16	17	18	20	22	24	25	28	33	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	56	57	58	59	61	62	63	64
Delete 9	65	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																													
Delete 5	1	2	3	4	6	7	8	11	12	13	14	15	16	17	20	24	25	33	40	41	42	43	45	46	47	48	49	51	52	53	54	56	57	58	59	61	62	63	64	65						
Delete 17	67	68	69	70	73	75	77	80	81	82	83	84	88	89	90	99																														
Delete 6	1	2	3	4	6	7	8	11	12	13	14	15	16	20	24	25	33	40	41	42	43	45	46	47	48	49	51																			

## 2 소스 코드

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```
1  #include <iostream>
2  #include <vector>
3  #include <stack>
4  #include <algorithm>
5  using namespace std;
6
7  enum FLAG {LEFT, RIGHT, MERGE};
8
9  class BTreeNode {
10 public:
11     BTreeNode(int key) {
12         keys.push_back(key);
13         childs.assign(2, nullptr);
14         n = 1;
15     }
16     BTreeNode(const BTreeNode *node) : n(node->n), keys(node->keys), childs(node->childs) {}
17     ~BTreeNode() {
18         for (auto child : childs) delete child;
19     }
20     void insertKey(int newKey, BTreeNode *newChild=nullptr, int newChildPos=RIGHT) {
21         keys.push_back(newKey);
22         childs.push_back(newChild);
23         int i = ++n - 1;
24         while (i > 0 && keys[i] < keys[i-1]) {
25             swap(keys[i], keys[i-1]);
26             swap(childs[i], childs[i+1]);
27             i--;
28         }
29         if (newChildPos == LEFT) swap(childs[i], childs[i+1]);
30     }
31
32     bool deleteKey(int oldKey, int oldChildPos=RIGHT) {
33         int i = 0;
34         while (i < n && oldKey > keys[i]) i++;
35         if (keys[i] != oldKey) return false;
36         keys.erase(keys.begin() + i);
37         if (oldChildPos == RIGHT) i++;
38         childs.erase(childs.begin() + i);
39         n--;
40         return true;
41     }
42
43     int n = 0;
44     vector<int> keys;
45     vector<BTreeNode*> childs;
46     static int M;
47 };
48
49 int BTreeNode::M = 3;
50
51 bool insertBT(BTreeNode *&T, int newKey) {
52     if (T == nullptr) {
53         T = new BTreeNode(newKey);
54         return true;
55     }
```

```

55     }
56     stack<BTreeNode*> st;
57     BTreeNode *x = T;
58     while (x != nullptr) {
59         int i = 0;
60         while (i < x->n && newKey > x->keys[i]) i++;
61         if (i < x->n && newKey == x->keys[i]) return false;
62         st.push(x);
63         x = x->childs[i];
64     }
65
66     BTreeNode *newChild = nullptr;
67     while (true) {
68         x = st.top(); st.pop();
69         x->insertKey(newKey, newChild);
70         if (x->n < BTreeNode::M) break;
71         newKey = x->keys[x->n/2];
72         newChild = new BTreeNode(x);
73         x->keys.resize(x->n/2);
74         x->childs.resize(x->n/2+1);
75         x->n /= 2;
76         newChild->keys.erase(newChild->keys.begin(), newChild->keys.begin() + newChild->n/2+1);
77         newChild->childs.erase(newChild->childs.begin(), newChild->childs.begin() + newChild->n/2+1);
78         newChild->n -= newChild->n / 2 + 1;
79         if (st.empty()) {
80             T = new BTreeNode(newKey);
81             T->childs[0] = x;
82             T->childs[1] = newChild;
83             break;
84         }
85     }
86
87     return true;
88 }
89
90 bool deleteBT(BTreeNode *&T, int oldKey) {
91     stack<BTreeNode*> st;
92     BTreeNode *x = T;
93     while (x != nullptr) {
94         int i = 0;
95         while (i < x->n && oldKey > x->keys[i]) i++;
96         if (i < x->n && oldKey == x->keys[i]) break;
97         st.push(x);
98         x = x->childs[i];
99     }
100     if (x == nullptr) return false; // Search Fail
101     if (x->childs[0] != nullptr) { // if x is Internal Node
102         BTreeNode *internalNode = x;
103         st.push(x);
104         x = x->childs[find(x->keys.begin(), x->keys.end(), oldKey) - x->keys.begin()+1];
105         while (x != nullptr) {
106             st.push(x);
107             x = x->childs[0];
108         }
109         x = st.top(); st.pop();
110         *find(internalNode->keys.begin(), internalNode->keys.end(), oldKey) = x->keys[0];

```

```

111     x->keys[0] = oldKey;
112 }
113 x->deleteKey(oldKey);
114 BTreeNode *y, *leftSibling, *rightSibling;
115 while (x->n < (BTreeNode::M+1)/2-1 && !st.empty()) { // While Underflow
116     y = st.top(); st.pop();
117     int idx = find(y->childs.begin(), y->childs.end(), x) - y->childs.begin();
118     if (x == y->childs[0]) leftSibling = nullptr;
119     else leftSibling = y->childs[idx-1];
120     if (x == y->childs.back()) rightSibling = nullptr;
121     else rightSibling = y->childs[idx+1];
122     int flag;
123     if (leftSibling == nullptr || rightSibling == nullptr) {
124         if (leftSibling == nullptr) {
125             if (rightSibling->n > (BTreeNode::M-1)/2) flag = RIGHT;
126             else flag = MERGE;
127         }
128         else {
129             if (leftSibling->n > (BTreeNode::M-1)/2) flag = LEFT;
130             else flag = MERGE;
131         }
132     }
133     else {
134         if (leftSibling->n >= rightSibling->n && leftSibling->n > (BTreeNode::M-1)/2) flag = LEFT;
135         else if (rightSibling->n > leftSibling->n) flag = RIGHT;
136         else flag = MERGE;
137     }
138     if (flag == LEFT) { // Get key from left sibling
139         x->insertKey(y->keys[idx-1], leftSibling->childs.back(), LEFT);
140         y->keys[idx-1] = leftSibling->keys.back();
141         leftSibling->deleteKey(leftSibling->keys.back());
142     }
143     else if (flag == RIGHT) { // Get key from right sibling
144         x->insertKey(y->keys[idx], rightSibling->childs[0], RIGHT);
145         y->keys[idx] = rightSibling->keys[0];
146         rightSibling->deleteKey(rightSibling->keys[0], LEFT);
147     }
148     else { // Merge
149         if (leftSibling == nullptr) {
150             idx++;
151             leftSibling = x;
152             x = rightSibling;
153         }
154         leftSibling->keys.push_back(y->keys[idx-1]);
155         leftSibling->n++;
156         y->deleteKey(y->keys[idx-1], RIGHT);
157         leftSibling->keys.insert(leftSibling->keys.end(), x->keys.begin(), x->keys.end());
158         leftSibling->childs.insert(leftSibling->childs.end(), x->childs.begin(), x->childs.end());
159         leftSibling->n += x->n;
160         x->childs.clear();
161         delete x;
162     }
163     x = y;
164 }
165 if (T->n == 0) {
166     y = T;

```

```

167         T = T->childs[0];
168         y->childs.clear();
169         delete y;
170     }
171
172     return true;
173 }
174
175 void inorderBT(BTreeNode *T) {
176     if (T == nullptr) return;
177     for (int i=0;i<T->n;++i) {
178         inorderBT(T->childs[i]);
179         cout << T->keys[i] << ' ';
180     }
181     inorderBT(T->childs[T->n]);
182 }
183
184 int main() {
185     cout << " File Processing " << endl;
186     cout << "      B-Tree" << endl;
187     cout << "===== " << endl;
188
189     int insertKeys[] = {
190         40, 11, 77, 33, 20, 90, 99, 70, 88, 80,
191         66, 10, 22, 30, 44, 55, 50, 60, 100, 28,
192         18, 9, 5, 17, 6, 3, 1, 4, 2, 7,
193         8, 73, 12, 13, 14, 16, 15, 25, 24, 28,
194         45, 49, 42, 43, 41, 47, 48, 46, 63, 68,
195         61, 62, 64, 69, 67, 65, 54, 59, 58, 51,
196         53, 57, 52, 56, 83, 81, 82, 84, 75, 89
197     };
198
199     int deleteKeys[] = {
200         66, 10, 22, 30, 44, 55, 50, 60, 100, 28,
201         18, 9, 5, 17, 6, 3, 1, 4, 2, 7,
202         8, 73, 12, 13, 14, 16, 15, 25, 24, 28,
203         40, 11, 77, 33, 20, 90, 99, 70, 88, 80,
204         45, 49, 42, 43, 41, 47, 48, 46, 63, 68,
205         53, 57, 52, 56, 83, 81, 82, 84, 75, 89,
206         61, 62, 64, 69, 67, 65, 54, 59, 58, 51
207     };
208
209     BTreeNode *root = nullptr;
210
211     BTreeNode::M = 3;
212     cout << "M = 3" << endl;
213     for (int key : insertKeys) insertBT(root, key);
214
215     for (int key : deleteKeys) {
216         cout << "Delete " << key << '\t';
217         deleteBT(root, key);
218         inorderBT(root);
219         cout << endl;
220     }
221
222     delete root;

```

```
223     root = nullptr;
224
225     cout << "=====" << endl;
226     BTreeNode::M = 4;
227     cout << "M = 4" << endl;
228     for (int key : insertKeys) insertBT(root, key);
229
230     for (int key : deleteKeys) {
231         cout << "Delete " << key << '\t';
232         deleteBT(root, key);
233         inorderBT(root);
234         cout << endl;
235     }
236
237     delete root;
238
239     return 0;
240 }
```

---