Digital Transmission - Homework 4

Andrea Dittadi, Davide Magrin, Michele Polese

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MATLAB code

DFE_filter

```
function [ Jmin, psi, r ] = DFE_filter(x, hi, N1, N2, est_sigmaw, D, M1, M2, coding, verb)
\% Function that performs DFE filtering. It needs
\mbox{\ensuremath{\upedge}{\%}} packet is the sequence of sent symbols
% x is the received samples vector in T, normalized by h0
\%\ h is the estimated impulse response in T, normalized by h0
\% N1 is the estimated number of precursors
% N2 is the estimated number of postcursors
% est_sigmaw is the estimated variance of the noise
% tO timing phase
\% D is the delay of the FF filter
                                                                                                             10
\% M1 is the number of coefficients of FF filter
\% M2 is the number of coefficients of FB filter, set to 0 to get LE
\% if verb is true then plots will be plotted
% Power of the input sequence
                                                                                                             15
sigma_a = 2;
% Zero padding of the i.r.
nb0 = 60;
nf0 = 60;
                                                                                                             20
hi = [zeros(nb0,1); hi; zeros(nf0,1)];
% Get the Weiner-Hopf solution
p = zeros(M1, 1);
for i = 0: (M1 - 1)
                                                                                                             25
    p(i+1) = sigma_a * conj(hi(N1+nb0+1+D-i));
R = zeros(M1);
for row = 0:(M1-1)
                                                                                                             30
    for col = 0:(M1-1)
        first_sum = (hi((nb0+1):(N1+N2+nb0+1)))., * ...
            conj(hi((nb0+1-(row-col)):(N1+N2+nb0+1-(row-col))));
        second_sum = (hi((N1+nb0+1+1+D-col):(N1+nb0+1+M2+D-col))).* * ...
            conj((hi((N1+nb0+1+1+D-row):(N1+nb0+1+M2+D-row))));
                                                                                                             35
        r_w = (row == col) * est_sigmaw; % This is a delta only if there is no g_M.
        R(row+1, col+1) = sigma_a * (first_sum - second_sum) + r_w;
    end
end
c_{opt} = R \setminus p;
Jmin = sigma_a*(1-c_opt.'* flipud(hi(N1+nb0+1+D-M1+1:N1+nb0+1+D)));
b = zeros(M2,1);
for i = 1:M2
    b(i) = -(fliplr(c_opt.')*hi((i+D+N1+nb0+1-M1+1):(i+D+N1+nb0+1)));
psi = conv(hi(nb0+1:nb0+1+N1+N2),c_opt);
```

```
if (verb == true)
    \% Plot hhat, c, psi=conv(h,c), b and get a sense of what is happening
                                                                                                              55
    figure
    subplot (4,1,1)
    stem(-N1:N2, abs(hi(nb0+1:nb0+1+N1+N2))), title('|h_{hat} normalized|'), xlim([-5 8]), ylim([0 1])
    subplot(4,1,2)
    stem(abs(c_opt)), title('|c|'), xlim([1 14]), ylim([0 1])
                                                                                                              60
    subplot (4,1,3)
    stem(-N1:-N1+length(psi)-1, abs(psi)), title('|psi|'), xlim([-N1 -N1+length(psi)]), ylim([0 1])
    subplot(4,1,4)
    stem(abs(b)), title('|b|'), xlim([1 14]), ylim([0 1])
end
                                                                                                              65
y = zeros(length(x) + D , 1); % output of ff filter
r = zeros(length(x) + D, 1);
detected = zeros(length(x) + D, 1); % output of td
for k = 0:length(x) - 1 + D
                                                                                                              70
    if (k < M1 - 1)
        xconv = [flipud(x(1:k+1)); zeros(M1 - k - 1, 1)];
    elseif k > length(x)-1 & k & k < length(x) - 1 + M1
        xconv = [zeros(k-length(x)+1, 1); flipud(x(end - M1 + 1 + k - length(x) + 1:end))];
    elseif k \ge length(x) - 1 + M1 \% just in case D is greater than M1
                                                                                                              75
        xconv = zeros(M1, 1);
    else
        xconv = flipud(x(k-M1+1 + 1:k + 1));
    end
                                                                                                              80
    if (k <= M2)
        a_old = [flipud(detected(1:k)); zeros(M2 - k, 1)];
        a_old = flipud(detected(k-M2+1:k));
                                                                                                              85
    y(k+1) = c_{opt}. *xconv;
    y(k+1) = y(k+1) / psi(D+1); % normalize y
                                                                                                              90
    r(k+1) = y(k+1) + b.**a_old;
    detected(k+1) = qpsk_td(r(k+1));
end
if (coding == true)
                                                                                                              95
   r = r(D+1:end);
else % if coding is not used return the decisions
   r = detected(D+1:end);
end
                                                                                                              100
end
```

LE_DFE_param_evaluator

```
%% This script performs parametric sweep on the parameters for DFE, for
% different SNR and the assigned channel

clear
close all
clc
rng default
snr_vec = [0, 14]; % dB

% From the assignment
t0 = 6;
N1 = 0;
N2 = 4;
N = N1 + N2 + 1;

%% DFE (parametric evaluation without channel coding)
```

```
printmsg_delete = ''; % Just to display progress updates
M1_max = N+30;
                                                                                                                20
D_{max} = M1_{max-1};
JminDFE = zeros(length(snr_vec), M1_max, D_max);
L_data = 128; % useless
bits = randi([0 1], 1, L_data);
symbols = bitmap(bits);
                                                                                                                25
for snr_i = 1:length(snr_vec)
    snr_ch = snr_vec(snr_i);
    % Create, send and receive data with the given channel
                                                                                                                30
    snrlin = 10^(snr_ch/10);
    [rcv_symb, sigma_w, h] = channel_output(symbols, snrlin, false);
    % Normalization!
    rcv_symb = rcv_symb(t0:end-7)/h(t0);
                                                                                                                35
    hi = h(t0-N1:t0+N2)/h(t0);
    %% Receiver: compute Jmin
    for M1_dfe = 1:M1_max;
                               % FF filter: equal to the span of h
                                                                                                                40
        for D_dfe = 1:D_max
             \% Print progress update
             printmsg = sprintf('for DFE, snr = %d, M1 = %d, D = %d\n', snr_ch, M1_dfe, D_dfe);
             fprintf([printmsg_delete, printmsg]);
             printmsg_delete = repmat(sprintf('\b'), 1, length(printmsg));
                                                                                                                45
             M2\_dfe = N2 + M1\_dfe - 1 - D\_dfe; % FB filter: one less than the FF filter [JminDFE(snr_i, M1_dfe, D_dfe), ~] = DFE_filter(rcv_symb, hi.', N1, N2, sigma_w, D_dfe,
                   M1_dfe, M2_dfe, false, false);
        end
    end
end
save('jmin_DFE', 'JminDFE')
for i = 1:length(snr_vec)
    figure, mesh(1:D_max, 1:M1_max, 10*log10(reshape(abs(JminDFE(i, :, :)), size(JminDFE(i, :, :), 2),
           size(JminDFE(i, :, :), 3)))
    title(strcat('Jmin for DFE, snr= ', num2str(snr_vec(i))))
    xlabel('D'), ylabel('M1'), zlabel('Jmin [dB]')
end
```

MLsequence

```
function [ p ] = MLsequence( L )
% Generate a Maximum Length Pseudo Noise sequence, using shift and xor
\mbox{\ensuremath{\mbox{\%}}} operators. L is the desired length of the resulting PN sequence.
% Extract r from the given L
r = log2(L+1);
p = zeros(L,1);
p(1:r) = ones(r,1); % Set arbitrary initial condition
for l = r+1:(L) % Skip the initial condition for the cycle
    switch L
                                                                                                               10
        case 3
            p(1) = xor(p(1-1), p(1-2));
        case 7
            p(1) = xor(p(1-2), p(1-3));
        case 15
                                                                                                               15
            p(1) = xor(p(1-3), p(1-4));
        case 31
            p(1) = xor(p(1-3), p(1-5));
        case 63
            p(1) = xor(p(1-5), p(1-6));
                                                                                                               20
        case 127
            p(1) = xor(p(1-6), p(1-7));
```

```
case 2^10 -1
            p(1) = xor(p(1-7), p(1-10));
        case 2^11 -1
                                                                                                          25
            p(1) = xor(p(1-9), p(1-11));
        case 2^12 -1
            p(1) = xor(xor(xor(p(1-2), p(1-10)), p(1-11)), p(1-12));
        case 2<sup>13</sup> -1
            p(1) = xor(xor(p(1-1), p(1-11)), p(1-12)), p(1-13));
                                                                                                          30
        case 2^14 -1
            p(1) = xor(xor(p(1-2), p(1-12)), p(1-13)), p(1-14));
        case 2^15 -1
           p(1) = xor(p(1-14), p(1-15));
        case 2^16 -1
                                                                                                          35
           p(1) = xor(xor(xor(p(1-11), p(1-13)), p(1-14)), p(1-16));
        case 2^18 -1
            p(1) = xor(p(1-11), p(1-18));
        case 2^19 -1
           p(1) = xor(xor(p(1-14), p(1-17)), p(1-18)), p(1-19));
                                                                                                          40
        case 2^20 -1
           p(1) = xor(p(1-17), p(1-20));
        otherwise
            p = [];
            disp('MLsequence: length not supported');
                                                                                                          45
    end
end
end
```

bitmap

```
function [output] = bitmap(input)
   % Check if the input array has even length
   L = length(input);
   if (mod(L, 2) ~= 0)
        disp('Must input an even length array');
                                                                                                           5
    output = zeros(L,1);
                                                                                                           10
   % Map each couple of values to the corresponding symbol
    for idx = 1:2:L-1
        if (isequal(input(idx:idx+1), [0; 0] ))
            output(idx) = -1-1i;
        elseif (isequal(input(idx:idx+1), [1; 0] ))
            output(idx) = 1-1i;
        elseif (isequal(input(idx:idx+1), [0; 1] ))
            output(idx) = -1+1i;
        elseif (isequal(input(idx:idx+1), [1; 1] ))
            output(idx) = +1+1i;
                                                                                                           20
        end
    end
    % Finally, only keep the useful values of the output
    output = output(1:2:end);
                                                                                                           25
end
```

channel_output

```
function [ r, sigma_w, h ] = channel_output( x, snr, OFDM)
% CHANNEL_OUTPUT Generates channel output (that is the desired signal)
% with an hard coded non varying channel.
% Returns the channel output r given the input parameters
% x is a column vector for consistency
% snr must be linear
h = [0,0,0,0,0,0.7*exp(-1i*2.57), 0.24*exp(1i*1.34), 0.15*exp(-1i*2.66), ...
```

```
0.58*exp(-1i*1.51), 0.4*exp(-1i*1.63), 0, 0, 0];
M = 512;

E_h = sum(abs(h).^2);
if (OFDM == true) % different definition of SNR Msigma_a E_h / sigma_w
    sigma_a = 2/M;
else
    sigma_a = 2; % for a QPSK
end
sigma_w = sigma_a*E_h/snr;

w = wgn(1, length(x) + length(h) - 1, 10*log10(sigma_w), 'complex');

r = conv(h, x) + w.';
end
```

decodeBits

```
function [decoded_bits] = decodeBits(bits)
   % Create the encoder
    warning('off', 'all');
    dec = fec.ldpcdec;
    dec.DecisionType = 'Hard Decision';
    dec.OutputFormat = 'Information Part';
    dec.NumIterations = 50;
    dec.DoParityChecks = 'Yes';
                                                                                                          10
   numInfoBits = dec.NumInfoBits; % Length of the info words
    if (mod(length(bits), numInfoBits) ~= 0)
        disp('Length of the input vector should be a multiple of 64800');
        return;
                                                                                                          15
    decoded_bits = zeros(length(bits)/2,1);
    % Iterate over the input info bits and encode them
    for idx = 0:(length(bits)/(2*numInfoBits))-1
                                                                                                          20
        current_bits = bits(2*idx*numInfoBits + 1 : 2*idx*numInfoBits + 2*numInfoBits);
        decoded_bits(idx*numInfoBits+1:idx*numInfoBits + numInfoBits) = decode(dec, current_bits);
    end
\verb"end"
```

deinterleaver

```
function [deinterleaved_bits] = deinterleaver(bits)
    % This function receives a sequence of bits and unscrambles it
   % INPUT:
   % bits: the bits to interleave
   % OUTPUT:
   \% deinterleaved_bits: the deinterleaved bits
   \% Input should be a multiple of 14061600 = lcm(rows*columns, 64800) bits
    if (mod(length(bits), 32400) ~= 0)
        disp('Length of the input vector should be a multiple of 14061600');
                                                                                                          10
        return;
    end
    deinterleaved_bits = zeros(1,length(bits));
                                                                                                          15
   % The deinterleaver is just an interleaver with rows and cols switched
    rows = 36;
    columns = 30;
   % We work with a rowsxcolumns matrix
                                                                                                          20
    for matrix = 0:(length(bits)/(rows*columns) - 1)
        curr_matrix = matrix * rows * columns;
```

encodeBits

```
function [encoded_bits] = encodeBits(bits)
   % Create the encoder
    warning('off', 'all');
    enc = fec.ldpcenc;
    numInfoBits = enc.NumInfoBits; % Length of the info words
    if (mod(length(bits), numInfoBits) ~= 0)
        disp('Length of the input vector should be a multiple of 32400');
        return;
    end
                                                                                                         10
    encoded_bits = zeros(2*length(bits),1);
    % Iterate over the input info bits and encode them
    for idx = 0:(ceil(length(bits)/numInfoBits))-1
        current_bits = bits(idx*numInfoBits+1:idx*numInfoBits + numInfoBits);
        encoded_bits(2*idx*numInfoBits+1:2*idx*numInfoBits + 2*numInfoBits) = encode(enc, current_bits
             ):
end
```

get_channel_info

```
function [ h_i, est_sigmaw ] = get_channel_info( r, N1, N2 )
%GET_CHANNEL_INFO
L = 31;
Nseq = 7;
trainingsymbols = ts_generation(L, Nseq);
\% --- Estimate impulse response h @T and compute estimated noise power
N = N1 + N2 + 1:
                                                                                                            10
x_for_ls = trainingsymbols(end - (L+N-1) + 1 : end);
\% r is in T
d_for_ls = r(end - (L+N-1) + 1 - N1 : end - N1); % is -N1 correct?
[h_i, r_hat] = h_estimation_onebranch(x_for_ls, d_for_ls, L, N);
d_{no\_trans} = d_{for\_ls(N : N+L-1)};
                                                                                                            15
est_sigmaw = sum(abs(r_hat - d_no_trans).^2)/length(r_hat);
h_i = h_i.'; % for convenience
end
                                                                                                            20
```

h_estimation_onebranch

```
function [ h_hat, d_hat ] = h_estimation_onebranch( x, d, L, N )
% This function performs the estimation of the h coefficients, given the
% input sequence, the output of the channel and the number of coefficients
% to estimate. Additionally, the function outputs d_hat, i.e. the output of
% a channel that would have the estimated coefficients as impulse response.

% In this case the estimation cannot be performed.
if N > L
   h_hat = [];
   d_hat = [];
```

```
return
%% Estimate h
\% Using the data matrix (page 246), easier implementation
h_{hat} = zeros(1,N);
I = zeros(L,N);
for column = 1:N
                                                                                                               20
    I(:,column) = x(N-column+1:(N+L-column));
end
o = d(N:N + L - 1);
\% Compute the Phi matrix and the theta vector
                                                                                                               25
Phi = I'*I;
theta = I'*o;
h_hat(1, 1:N) = Phi \setminus theta;
                                                                                                               30
%% Compute d_hat
d_hat = conv(x, h_hat);
d_hat = d_hat(N : N+L-1);
                                                                                                               35
```

ibmap

```
function [output] = ibmap(input)
   % Check if the input array has even length
    L = length(input);
    output = zeros(2*L,1);
                                                                                                             5
    \% Map each couple of values to the corresponding symbol
    \% The real part gives the bit
    for k = 1:2:length(output)-1
        symbol = input((k+1)/2);
                                                                                                             10
        if (real(symbol) == 1)
           b2k = 1;
        else
           b2k = 0;
        end
        if (imag(symbol) == 1)
            b2k1 = 1;
        else
            b2k1 = 0;
                                                                                                             20
        end
        output(k) = b2k;
        output(k+1) = b2k1;
    end
                                                                                                             25
end
```

interleaver

```
function [interleaved_bits] = interleaver(bits)
    % This function receives a sequence of bits and scrambles it
    % INPUT:
    % bits: the bits to interleave
    % OUTPUT:
    % interleaved_bits: the interleaved bits

% Input should be a multiple of 14061600 = lcm(rows*columns, 64800) bits
    if (mod(length(bits), 32400) ~= 0)
```

```
disp('Length of the input vector should be a multiple of 14061600');
                                                                                                          10
    end
    interleaved_bits = zeros(1,length(bits));
                                                                                                           15
    columns = 36:
   % We work with a rowsxcolumns matrix
    for matrix = 0:(length(bits)/(rows*columns) - 1)
                                                                                                           20
        curr_matrix = matrix * rows * columns;
        for col = 0:(columns-1)
            interleaved_bits(curr_matrix + col * rows + 1 : curr_matrix + col * rows + rows) = ...
                bits(curr_matrix + col + 1 : columns : curr_matrix + col + columns * rows);
        end
                                                                                                           25
    end
end
```

problem_1

```
% This script solves the first problem.
clear
close all
clc
                                                                                                          5
rng default
%parpool(15);
% data
                                                                                                          10
sigma_a = 2;
%% Get optimal number of bits
desired_bits = 2^24;
% Compute the closest number of bits that both interleaver and encoder will like
                                                                                                          15
search_step = 32400;
bit_number = ceil(desired_bits / search_step) * search_step;
%% Estimate Pbit for ideal channel without encoding
snr_vec = 0:0.5:14;
                                                                                                          20
Pbit_noenc = zeros(1,length(snr_vec));
parfor curr_snr = 1:length(snr_vec)
  disp(curr_snr);
   snrdb = snr_vec(curr_snr);
                                                                                                          25
  % Simulate Pbit for the ideal channel, no encoding
  bits = randi([0 1], 1, bit_number);
  symbols = bitmap(bits.');
  % Send stuff through
                                                                                                          30
  snrlin = 10^(snrdb/10);
  Eh = 1; \% Energy of the ideal channel ir
  sigma_w = sigma_a*Eh/snrlin;
  w = wgn(length(symbols), 1, 10*log10(sigma_w), 'complex');
  rcv_bits = symbols + w;
                                                                                                          35
  % Threshold the bits
   decided_symbols = zeros(1, length(rcv_bits));
  for idx = 1:length(rcv_bits)
      decided_symbols(idx) = qpsk_td(rcv_bits(idx)); % TODO modify qpsk_td to handle vectors
                                                                                                          40
  decided_bits = ibmap(decided_symbols);
  % Estimate pbit
                                                                                                          45
  Pbit_noenc(curr_snr) = sum(xor(decided_bits.', bits))/length(bits);
end
```

```
%% Estimate Pbit for ideal channel with encoding
                                                                                                          50
snr_vec_enc = 0:0.02:1;
Pbit_enc = zeros(1,length(snr_vec_enc));
parfor curr_snr = 1:length(snr_vec_enc)
   disp(snr_vec_enc(curr_snr));
   snrdb = snr_vec_enc(curr_snr);
  bits = randi([0 1], 1, bit_number);
   enc_bits = encodeBits(bits);
   int_enc_bits = interleaver(enc_bits); % Interleave the encoded bits
  symbols = bitmap(int_enc_bits.');
  % Send stuff through
  snrlin = 10^(snrdb/10);
  Eh = 1:
  sigma_w = sigma_a*Eh/snrlin;
  w = wgn(length(symbols), 1, 10*log10(sigma_w), 'complex');
  rcv_bits = symbols + w;
                                                                                                          70
  % Compute Log Likelihood Ratio
  llr = zeros(2*length(symbols),1);
  llr(1:2:end) = -2*real(rcv_bits)/(sigma_w/2);
  llr(2:2:end) = -2*imag(rcv_bits)/(sigma_w/2);
                                                                                                          75
  % Decode the bits
  llr = deinterleaver(llr); % Deinterleave the loglikelihood ratio first
  dec_bits = decodeBits(llr).';
  Pbit_enc(curr_snr) = sum(xor(dec_bits, bits))/length(bits);
                                                                                                          80
end
%% Save results
save('Problem1', 'snr_vec', 'snr_vec_enc', 'bit_number', 'Pbit_noenc', 'Pbit_enc');
                                                                                                          85
%% Plot results
load ('Problem1');
semilogy(snr_vec, Pbit_noenc), hold on,
semilogy(snr_vec_enc, Pbit_enc)
                                                                                                          90
ylim([10^-5, 10^-1]), xlim([0, 14]), grid on
xlabel('\Gamma (dB)')
ylabel('Pbit')
legend('Uncoded QPSK', 'Coded QPSK')
title('Bit Error Rate for uncoded and coded QPSK');
                                                                                                          95
```

problem_2

```
% This script solves the second problem.
clear, clc, close all
rng default
\% Initialize parameters based on the assigned channel
t0 = 5;
N1 = 0;
N2 = 4;
M1_dfe = 15;
D_dfe = M1_dfe - 1;
                                                                                                          10
M2_dfe = N2 + M1_dfe - 1 - D_dfe;
parpool(15);
%% Known channel, DFE, uncoded data (HW3)
                                                                                                          15
snr_vec_knownch_uncoded = 0:14;
seq_lengths_knownch_uncoded = 2.^[13 13 13 13 13 13 15 18 18 20 20 22 23 23];
Pbit_knownch_uncoded = zeros(length(snr_vec_knownch_uncoded),1);
```

```
20
parfor snr_idx = 1:length(snr_vec_knownch_uncoded)
    curr_snr = snr_vec_knownch_uncoded(snr_idx);
    fprintf('Known channel, uncoded, snr = %.2f\n', curr_snr);
    % Generate the current needed sequence
                                                                                                             25
    bits = randi([0 1], 1, seq_lengths_knownch_uncoded(snr_idx));
    symbols = bitmap(bits.');
    % Send through the channel
    [rcv_symb, sigma_w, h] = channel_output(symbols, 10^(curr_snr/10), false);
                                                                                                             30
    rcv_symb = rcv_symb(t0+1 : end-7)/h(t0+1);
    hi = h(t0+1-N1:t0+1+N2)/h(t0+1);
    % Receiver: filter with DFE
    [", rcv_symb] = DFE_filter(rcv_symb, hi.', N1, N2, sigma_w, D_dfe, M1_dfe, M2_dfe, false, false);
    rcv_bits = ibmap(rcv_symb);
    % Compute the Pbit and store it
    Pbit_knownch_uncoded(snr_idx) = sum(xor(rcv_bits.', bits))/length(bits);
                                                                                                             40
end
% Save current results
save('Problem2_knownch_uncoded', 'snr_vec_knownch_uncoded', ...
    'seq_lengths_knownch_uncoded', 'Pbit_knownch_uncoded');
                                                                                                             45
%% Known channel, DFE, coded data
% Get optimal number of bits
desired_bits = 2^2;
                                                                                                             50
% Compute the closest number of bits that both interleaver and encoder will like
search_step = 32400;
bit_number = ceil(desired_bits / search_step) * search_step;
snr_vec_knownch_coded = [1, 1.5, 2:0.02:2.4];  % Pbit falls at 2.2 dBs
seq_lengths_knownch_coded = bit_number*ones(1, length(snr_vec_knownch_coded));
Pbit_knownch_coded = zeros(length(snr_vec_knownch_coded),1);
parfor snr_idx = 1:length(snr_vec_knownch_coded)
    curr_snr = snr_vec_knownch_coded(snr_idx);
                                                                                                             60
    fprintf('Known channel, coded, snr = %.2f\n', curr_snr);
    \% Generate the current needed sequence
    bits = randi([0 1], 1, seq_lengths_knownch_coded(snr_idx));
                                                                                                             65
    enc_bits = encodeBits(bits);
    int_enc_bits = interleaver(enc_bits);  % Interleave the encoded bits
    symbols = bitmap(int_enc_bits.');
    \% Send through the channel
                                                                                                             70
    [rcv_symb, sigma_w, h] = channel_output(symbols, 10^(curr_snr/10), false);
    rcv_symb = rcv_symb(t0+1 : end-7)/h(t0+1);
    hi = h(t0+1-N1:t0+1+N2)/h(t0+1);
    \% Receiver: filter with DFE
    [~, rcv_symb] = DFE_filter(rcv_symb, hi.', N1, N2, sigma_w, D_dfe, M1_dfe, M2_dfe, true, false);
    % Compute Log Likelihood Ratio
    llr = zeros(2*length(symbols),1);
    llr(1:2:end) = -2*real(rcv_symb)/(sigma_w/2);
                                                                                                             80
    11r(2:2:end) = -2*imag(rcv_symb)/(sigma_w/2);
    % Decode the bits
    llr = deinterleaver(llr); % Deinterleave the loglikelihood ratio first
    dec_bits = decodeBits(llr).';
                                                                                                             85
    \% Compute the Pbit and store it
    Pbit_knownch_coded(snr_idx) = sum(xor(dec_bits, bits))/length(bits);
end
                                                                                                             90
```

```
% Save current results
save('Problem2_knownch_coded', 'snr_vec_knownch_coded', ...
   'seq_lengths_knownch_coded', 'Pbit_knownch_coded');
%% Estimated channel, DFE, uncoded data
L = 31:
Nseq = 7;
snr_vec_estch_uncoded = 0:14;
seq_lengths_estch_uncoded = 2.^[13 13 13 13 13 13 13 13 14 15 15 18 18 18] -1;
Pbit_estch_uncoded = zeros(length(snr_vec_estch_uncoded),1);
parfor snr_idx = 1:length(snr_vec_estch_uncoded)
                                                                                                      105
   curr_snr = snr_vec_estch_uncoded(snr_idx);
   fprintf('Estimated channel, uncoded, snr = %.2f\n', curr_snr);
   % Send through the channel
   [packet, rcv_symb, sigma_w] = txrc(seq_lengths_estch_uncoded(snr_idx), curr_snr);
                                                                                                      110
   % Perform estimation
   [h, est_sigma_w] = get_channel_info(rcv_symb(t0+1:t0+L+Nseq), N1, N2);
   rcv_symb = rcv_symb(t0+1:end-7)/h(N1+1);
                                                                                                      115
   hi = h / h(N1+1);
   % Receiver: filter with DFE
    [~, rcv_symb] = DFE_filter(rcv_symb, hi, N1, N2, est_sigma_w, D_dfe, M1_dfe, M2_dfe, false)
   rcv_bits = ibmap(rcv_symb);
                                                                                                      120
   packet = ibmap(packet);
   % Compute the Pbit and store it
   Pbit_estch_uncoded(snr_idx) = sum(xor(rcv_bits, packet))/length(packet);
end
% Save current results
save('Problem2_estch_uncoded', 'snr_vec_estch_uncoded', ...
    'seq_lengths_estch_uncoded', 'Pbit_estch_uncoded');
%% Estimated channel, DFE, coded data
\% In this section we don't use the txrc function for now. This is because
% txrc only accepts L_data such that an ML sequence can be directly
% created.
                                                                                                      135
L = 31;
Nseq = 7;
% Get optimal number of bits
                                                                                                      140
desired_bits = 2^22;
% Compute the closest number of bits that both interleaver and encoder will like
search_step = 32400;
bit_number = ceil(desired_bits / search_step) * search_step;
                                                                                                      145
numsim = 10;
seq_lengths_estch_coded = bit_number*ones(1, length(snr_vec_estch_coded));
Pbit_estch_coded = zeros(length(snr_vec_estch_coded),numsim);
                                                                                                      150
for sim = 1:numsim
   parfor snr_idx = 1:length(snr_vec_estch_coded)
        curr_snr = snr_vec_estch_coded(snr_idx);
       fprintf('Estimated channel, coded, snr = %.2f\n', curr_snr);
                                                                                                      155
       % Generate the current needed sequence
       packet = randi([0 1], 1, seq_lengths_estch_coded(snr_idx));
       enc_packet = encodeBits(packet);
                                                                                                      160
```

```
int_enc_packet = interleaver(enc_packet);  % Interleave the encoded bits
         symbols = [ts_generation(L, Nseq); bitmap(int_enc_packet.')];
        % Send through the channel
                                                                                                                 165
         [rcv_symb, sigma_w, ~] = channel_output(symbols, 10^(curr_snr/10), false);
        % Perform estimation
         [h, est_sigma_w] = get_channel_info(rcv_symb(t0+1:t0+L+Nseq), N1, N2);
                                                                                                                 170
        rcv_symb = rcv_symb(t0+1:end-7)/h(N1+1);
        hi = h / h(N1+1);
        % Receiver: filter with DFE
        [~, rcv_symb] = DFE_filter(rcv_symb, hi, N1, N2, est_sigma_w, D_dfe, M1_dfe, M2_dfe, true,
                                                                                                                 175
               false):
        % Compute Log Likelihood Ratio
        llr = zeros(2*length(packet),1);
        llr(1:2:end) = -2*real(rcv_symb(L+Nseq+1:end))/(est_sigma_w/2);
        llr(2:2:end) = -2*imag(rcv_symb(L+Nseq+1:end))/(est_sigma_w/2);
                                                                                                                  180
        llr = deinterleaver(llr); % Deinterleave the loglikelihood ratio first
        dec_packet = decodeBits(llr).';
                                                                                                                  185
        % Compute the Pbit and store it
        Pbit_estch_coded(snr_idx, sim) = sum(xor(dec_packet, packet))/length(packet);
    end
end
                                                                                                                  190
% Save current results
save('Problem2_estch_coded', 'snr_vec_estch_coded', ...
    'seq_lengths_estch_coded', 'Pbit_estch_coded');
%% Plot BER graphs
load('Problem2_estch_uncoded.mat');
load('Problem2_estch_coded.mat');
load('Problem2_knownch_uncoded.mat');
load('Problem2_knownch_coded.mat');
                                                                                                                 200
figure, semilogy(snr_vec_knownch_uncoded, Pbit_knownch_uncoded), hold on
semilogy(snr_vec_knownch_coded, Pbit_knownch_coded), hold on
semilogy(snr_vec_estch_uncoded, Pbit_estch_uncoded, '--')
semilogy(snr_vec_estch_coded, Pbit_estch_coded, '--')
                                                                                                                 205
xlabel('\Gamma [dB]'), ylabel('Pbit'), grid on
ylim([10^-5, 10^-1])
xlim([0, 14])
legend('Known channel, uncoded', 'Known channel, coded', ...
'Estimated channel, uncoded', 'Estimated channel, coded');
                                                                                                                 210
title('Bit Error Rate for a DFE receiver')
%% Clean parpool
delete(gcp)
```

qpsk_td

```
function [ out ] = qpsk_td( in )
% Threshold detector for QPSK
if (real(in) > 0)
    if (imag(in) > 0)
        out = 1+1i;
    else
        out= 1-1i;
    end
else
    if (imag(in) > 0)
        out = -1+1i;
```

```
else
    out = -1-1i;
end
end
end
```

transmitter

```
% This script converts bits into symbols, using the encoder + interleaver +
% bitmap setup.
clear
close all
clc
rng default
% The design of the DFE equalizer has to be carried out assuming the
% channel is known
\% From the assigned impulse response
                                                                                                           10
t0 = 6;
N1 = 0;
N2 = 4;
\%\% Get optimal number of bits
desired_bits = 2^18;
                                                                                                           15
% Compute the closest number of bits that both interleaver and encoder will
% like
found = false;
bit_number = 0;
while (~found)
                                                                                                           20
    search_step = 32400;
    bit_number = bit_number + search_step;
    if (bit_number > desired_bits)
        found = true;
                                                                                                           25
end
%% Generate and encode bits
bits = randi([0 1], 1, bit_number);
                                                                                                           30
enc_bits = encodeBits(bits);
int_enc_bits = interleaver(enc_bits); % Interleave the encoded bits
coding = true;
symbols = bitmap(int_enc_bits.');
%% Send stuff through
snrdb = 2.15;
snrlin = 10^(snrdb/10);
                                                                                                           40
[rcv_symb, sigma_w, h] = channel_output(symbols, snrlin, false);
% Normalization!
rcv_symb = rcv_symb(t0:end-7)/h(t0);
hi = h(t0-N1:t0+N2)/h(t0);
%% Receiver: filter with DFE
M1_dfe = 15;
D_dfe = M1_dfe - 1;
M2\_dfe = N2 + M1\_dfe - 1 - D\_dfe;
[", rcv_bits] = DFE_filter(rcv_symb, hi.', N1, N2, sigma_w, D_dfe, M1_dfe, M2_dfe, coding, false);
%% Compute Log Likelihood Ratio
11r = zeros(2*length(symbols),1);
llr(1:2:end) = -2*real(rcv_bits)/(sigma_w/2);
                                                                                                           55
11r(2:2:end) = -2*imag(rcv_bits)/(sigma_w/2);
\%\% Decode the bits
llr = deinterleaver(llr); % Deinterleave the loglikelihood ratio first
                                                                                                           60
```

```
dec_bits = decodeBits(llr).';
Pbit = sum(xor(dec_bits, bits))/length(bits);
```

ts_generation

```
function [ trainingsymbols ] = ts_generation( L, Nseq )
% Training sequence generation
% This function outputs a partially repeated ML sequence in which the
mlseq = MLsequence(L); % Get the 0-1 ML sequence
% Replace every 0 with two 0s and every 1 with two 1s
mlseqdouble = zeros(2*L,1);
for i = 1:L
                                                                                              10
   switch mlseq(i)
       case 0
          mlseqdouble(2*i-1) = 0;
          mlseqdouble(2*i) = 0;
       case 1
                                                                                              15
          mlseqdouble(2*i-1) = 1;
          mlseqdouble(2*i) = 1;
   end
end
                                                                                              20
\% Repeat the sequence and bitmap it to get the symbols
trainingseq = [mlseqdouble; mlseqdouble(1:2*Nseq)];
trainingsymbols = bitmap(trainingseq);
```

txrc

```
function [packet, r, sigma_w] = txrc(L_data, snr)
\% This script produces an output given by the 50 bit of ML training sequence and
% L_data bit computed with an MLsequence (therefore L_data has to be 2 smth
                                                                                                           5
%% Packet generation w/ ts, data
L = 31;
Nseq = 7;
                                                                                                           10
trainingsymbols = ts_generation(L, Nseq);
MAX_ML = 2^20 - 1;
if (L_data > MAX_ML)
    dataseq = MLsequence(MAX_ML);
    dataseq = repmat(dataseq, ceil(L_data / MAX_ML), 1);
    dataseq = dataseq(1:L_data);
else
    dataseq = MLsequence(L_data);
end
{\tt datasymbols = bitmap(dataseq(1 : end - mod(L_data, 2)));}
% QPSK requires an even number of bits
packet = [trainingsymbols; datasymbols];
%% Generate the channel output
snr_lin = 10^(snr/10);
[r, sigma_w, ~] = channel_output(packet, snr_lin, false);
end
```

OFDM_choose_N2

```
%% Channel ESTIMATION for OFDM
\% Send one block of data with symbols spaced of 16 channels
clear, close all
OFDM = true;
                                                                                                            5
M = 512;
allowed_symb = 32;
spacing = M/allowed_symb;
Npx = 7;
t0 = 5;
                                                                                                            10
block = ones(M, 1)*(-1-1i);
ts = ts_generation(allowed_symb-1, 1) * sqrt(2);
init\_step = 1; % < 16
                                                                                                            15
indices = init_step : spacing : init_step + spacing*(allowed_symb-1);
block(indices) = ts;
% Compute IDFT, add prefix, P/S
A = ifft(block);
                                                                                                            20
A_pref = [A(end-Npx + 1:end); A];
s = reshape(A_pref, [], 1);
%% CHANNELIZATION
                                                                                                            25
snr = 6; %dB
snr_lin = 10^(snr/10);
% Send over the noisy channel
[r, sigma_w, g] = channel_output(s, snr_lin, OFDM);
g = g(1+t0 : end); % Take t0 into account (just to plot stuff)
                                                                                                            30
G = fft(g, 512);
G = G(:);
%% Process at the receiver
                                                                                                            35
r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
\% Perform the DFT
r_matrix = reshape(r, M+Npx, []);
                                                                                                            40
r_matrix = r_matrix(Npx + 1:end, :);
x_matrix = fft(r_matrix);
% Select useful samples
x_rcv = x_matrix(indices, 1);
                                                                                                            45
x_known = diag(ts);
\% Compute G_est by dividing the received symbol by the transmitted one
G_{est} = x_{rcv} ./ ts;
                                                                                                            50
\% Solve LS for F*g=G_est where g is an 8x1 vector: do it for different values of N2
F_complete = dftmtx(M);
for N2 = 1:Npx
  F = F_complete(indices, 1:N2+1);
   g_{hat} = (F' * F) \setminus (F' * G_{est});
   g_est = ifft(G_est);
   G_hat = fft(g_hat, M);
  % Noise estimation
                                                                                                            60
   xhat = x_known * G_hat(indices);
   E = sum(abs(xhat - x_rcv).^2)/length(xhat);
   est_sigma_w(N2) = E/M; %#ok<SAGROW>
                                                                                                            65
%% Plot
```

OFDM_channel_estimation

```
function [G_hat, est_sigma_w] = OFDM_channel_estimation(snr, Npx, N2, t0)
%% Channel ESTIMATION for OFDM
% Send one block of data with symbols spaced of 16 channels
                                                                                                           5
OFDM = true;
M = 512;
allowed_symb = 32;
spacing = M/allowed_symb;
                                                                                                           10
block = ones(M, 1)*(-1-1i);
% Remember: for the symbols on which the estimation is performed, for a
% given snr (computed with the usual sigma_a^2 = 2), the power of the
% "estimation symbols" is doubled (-> better snr)
                                                                                                           15
\% Note that the variance of the noise at the receiver, after the DFT, is
\% multplied by M, therefore it could be high
ts = ts_generation(allowed_symb-1, 1) * sqrt(2);
init_step = 1; % < 16
indices = init_step : spacing : init_step + spacing*(allowed_symb-1);
                                                                                                           20
\% Scale in order to double the power of tx symbols
% TODO What should we set the other symbols to?
block(indices) = ts;
% Compute IDFT, add prefix, P/S
                                                                                                           25
A = ifft(block);
A_pref = [A(end-Npx + 1:end); A];
s = reshape(A_pref, [], 1);
%% CHANNELIZATION
                                                                                                           30
\% Do our own transmission and reception of the training sequence
snr_lin = 10^(snr/10);
[r, ~, ~] = channel_output(s, snr_lin, OFDM);
%% Process at the receiver
r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
                                                                                                           40
\% Perform the DFT
r_matrix = reshape(r, M+Npx, []);
r_matrix = r_matrix(Npx + 1:end, :);
x_matrix = fft(r_matrix);
% Select useful samples
x_rcv = x_matrix(init_step:spacing:end, 1);
X_known = diag(ts)*sqrt(2);
\% Compute G_est by dividing the received symbol by the transmitted one
G_{est} = x_{rcv} ./ ts;
\% Solve LS for F*g=G_est where g is an 8x1 vector
F = dftmtx(M);
F = F(indices, 1:N2+1);
                                                                                                           55
g_hat = (F' * F) \ (F' * G_est);
G_hat = fft(g_hat, M);
% Noise estimation
                                                                                                           60
```

```
xhat = X_known * G_hat(init_step : spacing : end);
E = sum(abs(xhat - x_rcv).^2)/length(xhat);
est_sigma_w = E/M;
end
65
```

OFDM_channel_estimation_comparison

```
%% Channel ESTIMATION for OFDM (second method)
\% Send one block of data using 8 equally spaced groups of 4
% adjacent subchannels.
%#ok<*SAGROW>
clear, close all
numsim = 500;
OFDM = true;
M = 512;
                                                                                                           10
allowed_symb = 32;
Npx = 7;
N2 = 4;
t0 = 5;
                                                                                                           15
snr_vec = 0:2:22;
block = ones(M, 1)*(-1-1i);
\% Scale in order to double the power of tx symbols
ts = ts_generation(allowed_symb-1, 1) * sqrt(2);
                                                                                                           20
sigma_ts = 4;
%% First method
                                                                                                           25
indices = 1 : M/allowed_symb : M;
block(indices) = ts;
\% Compute IDFT, add prefix, P/S
A = ifft(block);
                                                                                                           30
A_pref = [A(end-Npx + 1:end); A];
s = reshape(A_pref, [], 1);
for snr_i = 1:length(snr_vec)
   for sim=1:numsim
      snr = snr_vec(snr_i); %dB
      snr_lin = 10^(snr/10);
                                                                                                           40
      \% --- Send over the noisy channel
      [r, sigma_w(snr_i), g] = channel_output(s, snr_lin, OFDM);
      g = g(1+t0 : end);
                          % Take t0 into account (just to plot stuff)
      G = fft(g, 512);
      G = G(:);
      % --- Process at the receiver
      r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
      \% Perform the DFT
      r_matrix = reshape(r, M+Npx, []);
      r_matrix = r_matrix(Npx + 1:end, :);
      x_matrix = fft(r_matrix);
                                                                                                           55
      % Select useful samples
      x_rcv = x_matrix(indices, 1);
      x_known = diag(ts);
                                                                                                           60
```

```
% Compute G_est by dividing the received symbol by the transmitted one
      G_{est} = x_{rcv} ./ ts;
      % Solve LS for F*g=G_est where g is an 8x1 vector
      F = dftmtx(M);
     F = F(indices, 1:N2+1);
      g_hat = (F' * F) \ (F' * G_est);
      g_est = ifft(G_est);
      G_hat = fft(g_hat, M);
                                                                                                          70
     % Noise estimation original
      xhat = x_known * G_hat(indices);
      E = sum(abs(xhat - x_rcv).^2)/length(xhat);
      est_sigma_w(sim, snr_i) = E/M;
                                                                                                          75
      % Error on the estimate of G
      est_err(sim, snr_i) = sum(abs(G_hat - G).^2);
   end
                                                                                                          80
end
% Save simulation results
meanest1 = mean(est_sigma_w);
ciest1 = 1.96 * std(est_sigma_w) / sqrt(numsim);
                                                                                                          85
meanesterr = mean(est_err);
ciesterr = 1.96 * std(est_err) / sqrt(numsim);
%% Second method
                                                                                                          90
nsamples = 8;
symbpersegment = allowed_symb / nsamples;
indices = reshape(1:M, M/nsamples, nsamples);
indices = reshape(indices(1:symbpersegment, :), size(indices, 2)*symbpersegment, 1); % Second way
                                                                                                          95
block(indices) = ts;
% Compute IDFT, add prefix, P/S
A = ifft(block);
A_pref = [A(end-Npx + 1:end); A];
                                                                                                          100
s = reshape(A_pref, [], 1);
% CHANNELIZATION
for snr_i = 1:length(snr_vec)
                                                                                                           105
   for sim=1:numsim
      snr = snr_vec(snr_i); %dB
      snr_lin = 10^(snr/10);
      % Send over the noisy channel
      [r, sigma_w(snr_i), g] = channel_output(s, snr_lin, OFDM);
      g = g(1+t0 : end);
                          % Take t0 into account (just to plot stuff)
      G = fft(g, 512);
      G = G(:);
                                                                                                           115
      % --- Process at the receiver
     r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
                                                                                                           120
      % Perform the DFT
      r_matrix = reshape(r, M+Npx, []);
      r_matrix = r_matrix(Npx + 1:end, :);
      x_matrix = fft(r_matrix);
                                                                                                           125
     % Select useful samples
      x_rcv = x_matrix(indices, 1);
      x_known = diag(ts);
      % Compute G_est by dividing the received symbol by the transmitted one
                                                                                                          130
      G_est = x_rcv ./ ts;
```

```
% Solve LS for F*g=G_est where g is an 8x1 vector
      F = dftmtx(M);
      F = F(indices, 1:N2+1);
                                                                                                           135
      g_{hat} = (F' * F) \setminus (F' * G_{est});
      g_est = ifft(G_est);
      G_hat = fft(g_hat, M);
      % Noise estimation new method
                                                                                                           140
      est_sigma_w(sim, snr_i) = 0;
      for j=0:nsamples-1
         tempGest = G_est((j*symbpersegment + 1) : (j*symbpersegment + 1)+3);
         est_sigma_w(sim, snr_i) = est_sigma_w(sim, snr_i) + var(tempGest);
                                                                                                           145
      est_sigma_w(sim, snr_i) = est_sigma_w(sim, snr_i) / nsamples / M * sigma_ts;
      % Error on the estimate of G
      est_err(sim, snr_i) = sum(abs(G_hat - G).^2);
   end
end
% Save simulation results
meanest2 = mean(est_sigma_w);
ciest2 = 1.96 * std(est_sigma_w) / sqrt(numsim);
meanesterr2 = mean(est_err);
ciesterr2 = 1.96 * std(est_err) / sqrt(numsim);
                                                                                                            160
%% Plots
figure, hold on
errorbar(snr_vec, meanest1, ciest1)
errorbar(snr_vec, meanest2, ciest2)
plot(snr_vec, sigma_w)
hold off
grid on, box on, set(gca, 'yscale', 'log')
legend('Original method', 'Second method', 'Actual \sigma_w')
xlim([snr_vec(1), snr_vec(end)])
                                                                                                           170
ax = gca; ax.XTick = snr_vec;
xlabel('SNR (dB)')
title('Comparison of estimates of \sigma_w')
figure, hold on
                                                                                                           175
errorbar(snr_vec, meanesterr, ciesterr)
errorbar(snr_vec, meanesterr2, ciesterr2)
hold off
grid on, box on, set(gca, 'yscale', 'log')
legend('Original method', 'Second method')
                                                                                                           180
xlim([snr_vec(1), snr_vec(end)])
ax = gca; ax.XTick = snr_vec;
xlabel('SNR (dB)')
title('Estimation error on G')
                                                                                                           185
% Plots for second method
% figure, hold on
% stem(0:Npx, abs(g))
                                                                                                           190
% stem(0:N2, abs(g_hat), 'x')
% stem(0:15, abs(g_est(1:16)), '^')
% legend('Actual g', 'g_hat', 'IDFT of G_est')
% figure,
                                                                                                            195
% subplot 211
% plot(real(G)), hold on
% plot(real(G_hat))
% plot(indices, real(G_est), '^')
% title(strcat('Comparison between estimated - LS+interpol - and real at ', num2str(snr), ' dB'))
                                                                                                           200
\% legend('real(G)', 'real(G_hat)', 'real(G_{est})'), xlabel('i - subchannels'), ylabel('Real(G)'),
% grid on, xlim([1, M])
```

```
% subplot 212
% plot(imag(G)), hold on
% plot(imag(G_hat))
% plot(indices, imag(G_est), '^')
% title(strcat('Comparison between estimated - LS+interpol - and real at ', num2str(snr), 'dB'))
% legend('imag(G)', 'imag(G_hat)', 'imag(G_{est})'), xlabel('i - subchannels'), ylabel('imag(G)'),
% grid on, xlim([1, M])
```

OFDM_channel_estimation_2

```
function [G_hat, est_sigma_w] = OFDM_channel_estimation_2(snr, Npx, N2, t0)
%% Channel ESTIMATION for OFDM (second method)
\% Send one block of data using 8 equally spaced groups of 4
% adjacent subchannels.
OFDM = true;
M = 512;
allowed_symb = 32;
                                                                                                           10
block = ones(M, 1)*(-1-1i);
% Scale in order to double the power of tx symbols
ts = ts_generation(allowed_symb-1, 1) * sqrt(2);
sigma_ts = 4;
                                                                                                           15
nsamples = 8;
symbpersegment = allowed_symb / nsamples;
indices = reshape(1:M, M/nsamples, nsamples);
indices = reshape(indices(1:symbpersegment, :), size(indices, 2)*symbpersegment, 1); % Second way
                                                                                                           20
block(indices) = ts;
% Compute IDFT, add prefix, P/S
A = ifft(block);
A_pref = [A(end-Npx + 1:end); A];
                                                                                                           25
s = reshape(A_pref, [], 1);
%% CHANNELIZATION
snr_lin = 10^(snr/10);
                                                                                                           30
% Send over the noisy channel
[r, ~, ~] = channel_output(s, snr_lin, OFDM);
% --- Process at the receiver
                                                                                                           35
r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
\% Perform the DFT
r_matrix = reshape(r, M+Npx, []);
                                                                                                           40
r_matrix = r_matrix(Npx + 1:end, :);
x_matrix = fft(r_matrix);
% Select useful samples
x_rcv = x_matrix(indices, 1);
\% Compute G_est by dividing the received symbol by the transmitted one
G_{est} = x_{rcv} ./ ts;
% Solve LS for F*g=G_{est} where g is an (N2+1)x1 vector
F = dftmtx(M);
F = F(indices, 1:N2+1);
g_hat = (F' * F) \ (F' * G_est);
G_hat = fft(g_hat, M);
\% Noise estimation new method
est_sigma_w = 0;
for j=0:nsamples-1
```

```
tempGest = G_est((j*symbpersegment + 1) : (j*symbpersegment + 1)+3);
  est_sigma_w = est_sigma_w + var(tempGest);
end
est_sigma_w = est_sigma_w / nsamples / M * sigma_ts;
end
end
```

OFDM_BER

```
function [ BER, G ] = OFDM_BER( M, Npx, N2, t0, desired_bits, snr, coding, chIsKnown, varargin )
%This function performs the transmission and reception of bits with ODFM,
%with or without encoding
%
   It needs
    - M block length
%
   - Npx prefix length
%
   - the number of desired bits
%
    - the snr
%
   - the option coding to be set either true or false
%
    - the estimation method (1 standard, 2 8 points+noise) - optional, if
                                                                                                          10
%
   not indicated the classic is used
%
    It returns
%
    - the BER
    - the channel frequency response
%
%
   This implementation doesn't rescale the power of sent symbols after the
%
   IFFT operation, therefore sigma_s^2 = sigma_a^/M
if (length(varargin) == 1)
    if (varargin{1} == 1)
        fprintf('Use classic estimation method \n')
        estMethod = 1;
    elseif (varargin{1} == 2)
        fprintf('Use new estimation method \n')
        estMethod = 2;
    end
                                                                                                          25
else
    fprintf('Use classic estimation method \n')
    estMethod = 1;
                                                                                                          30
warning('off', 'all');
OFDM = true;
% Compute the optimal number of bits
fprintf('Start transmission...\n');
                                                                                                          35
if (coding == true)
    % Compute the closest number of bits that both interleaver and encoder will like
    search_step = 32400;
    bit_number = ceil(desired_bits / search_step) * search_step;
else
                                                                                                          40
    bit_number = desired_bits;
end
\% Generate and encode bits
bits = randi([0 1], 1, bit_number).';
                                                                                                          45
if (coding == true)
    enc_bits = encodeBits(bits.');
    int_enc_bits = interleaver(enc_bits); % Interleave the encoded bits
    a = bitmap(int_enc_bits.');
                                                                                                          50
else
    a = bitmap(bits);
% Create data blocks
                                                                                                          55
% perform a padding of the last symbols in order to have blocks of 512 symbols: we use
% -1-j to perform the padding
a_pad = [a; ones(M - mod(length(a), M), 1) * (-1-1i)];
```

```
a_matrix = reshape(a_pad, M, []); % it should mantain columnwise order
                                                                                                           60
\% compute the ifft of blocks of 512 symbols
% http://it.mathworks.com/matlabcentral/newsreader/view_thread/17104
% it should be a columnwise operation!
A_matrix = ifft(a_matrix);
                                                                                                           65
\% add the preamble to each column
A_matrix = [A_matrix(M-Npx+1:M, :); A_matrix]; % very powerful operation
% serialize in order to call channel output
                                                                                                           70
s = reshape(A_matrix, [], 1);
fprintf('Symbols are pushed into the channel...\n');
\% Send over the noisy channel
snr_lin = 10^(snr/10);
                                                                                                           75
[r, sigma_w, g] = channel_output(s, snr_lin, OFDM);
if (chIsKnown)
   g = g(1+t0 : end);
   G = fft(g, 512);
   G = G(:);
                                                                                                           80
else
    if(estMethod == 1)
        [G, sigma_w] = OFDM_channel_estimation(snr, Npx, N2, t0);
    elseif(estMethod == 2)
        [G, sigma_w] = OFDM_channel_estimation_2(snr, Npx, N2, t0);
                                                                                                           85
    end
end
% Process at the receiver
% consider the effect of the convolution at the end should be easy,
                                                                                                           90
\% since the resulting data should have a length which is a multiple of M +
fprintf('Symbols received, processing begins...\n');
r = r(1+t0 : end - mod(length(r), M+Npx) + t0);
% perform the DFT
r_matrix = reshape(r, M+Npx, []);
r_matrix = r_matrix(Npx + 1:end, :);
G_{inv} = G.^{(-1)};
x_matrix = fft(r_matrix);
y_matrix = bsxfun(@times, x_matrix, G_inv);
\% Detect and compute BER
                                                                                                           105
if (coding == true)
    % sigma_i after the DFT and the scaling by G_i of each branch
    sigma_i = 0.5*sigma_w*M*abs(G_inv).^2;
    % Compute Log Likelihood Ratio
    % It is different for each branch
                                                                                                           110
   llr_real = -2*bsxfun(@times, real(y_matrix), sigma_i.^(-1));
    llr_imag = -2*bsxfun(@times, imag(y_matrix), sigma_i.^(-1));
    llr_real_ar = reshape(llr_real, [], 1);
    llr_imag_ar = reshape(llr_imag, [], 1);
    llr = zeros(numel(llr_real) + numel(llr_imag), 1);
                                                                                                           115
    llr(1:2:end) = llr_real_ar;
    llr(2:2:end) = llr_imag_ar;
   % Drop the zero padding
    llr = llr(1:length(enc_bits));
    % Decode the bits
                                                                                                           120
   llr = deinterleaver(llr); % Deinterleave the loglikelihood ratio first
    dec_bits = decodeBits(llr).';
else
    y = reshape(y_matrix, [], 1);
    \% drop the zero padding
                                                                                                           125
   y = y(1:length(a));
    decision = zeros(length(y), 1);
    for k = 1:length(y)
        decision(k) = qpsk_td(y(k));
                                                                                                          130
```

```
dec_bits = ibmap(decision);
end

% make dec_bits a column even if it is already
dec_bits = dec_bits(:);

BER = sum(xor(dec_bits, bits))/length(bits);
fprintf('End, the BER is %d \n', BER);

% my_llr_linear = 10.^(llr(1:100)/10);
% my_dec_bits = dec_bits(1:100);
% my_p = 1 ./ (1 + my_llr_linear);
% figure, stem(my_p), hold on, stem(my_dec_bits)
end
```