
$$E = \frac{mc^2}{\sqrt{1 - \frac{v^2}{c^2}}}$$

GENEROVÁNÍ KÓDU

6. VÝBĚR INSTRUKCÍ: GRAHAM-GLANVILLOVA METODA, VYHLEDÁVÁNÍ VZORKŮ A DYNAMICKÉ PROGRAMOVÁNÍ, MAXIMAL MUNCH



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GRAHAM-GLANVILLE METHOD IN DETAILS

Graham-Glanville technique -recapitulation

- The basic method which uses context-free grammars.
- Grammar rules are constructed for prefix notations of patterns of all machine instructions.
- LR(0) parser for the grammar is constructed.
- Reduction by a rule means that the corresponding instruction is selected.
- The created grammar is unambiguous, which means that the constructed LR(0) parser contains many parse conflicts (nondeterminisms).
- The conflicts are resolved by some heuristics so that the minimal number of target instructions would be generated.

Example, contd.

- The IR from our example in prefix notation:

`:= + A D1 + | + | + P D1 B | + C D1`

Note. Symbol `|` represents indirection.

- A context-free translation grammar which corresponds to the tree patterns is constructed:

<code>Null</code>	<code>-></code>	<code>:= + const R2 R1</code>	<code>{ ST const (R2) , R1 }</code>	
<code>Null</code>	<code>-></code>	<code>:= + R2 const R1</code>	<code>{ ST const (R2) , R1 }</code>	<code>; commutative!</code>
<code>Null</code>	<code>-></code>	<code>:= const R1</code>	<code>{ ST const , R1 }</code>	
<code>Null</code>	<code>-></code>	<code>:= R2 R1</code>	<code>{ ST 0 (R2) , R1 }</code>	

Example, contd.

R1 -> := const	{ LD #const, R1 }
R1 -> + const R2	{ LD const (R2) , R1 }
R1 -> + R2 const	{ LD const (R2) , R1 }
R2 -> := R1	{ LR R2, R1 }
R1 -> + + const R2 R1	{ ADD const (R2) , R1 }
R1 -> + + R2 const R1	{ ADD const (R2) , R1 }
R1 -> + R1 + const R2	{ ADD const (R2) , R1 }
R1 -> + R1 + R2 const	{ ADD const (R2) , R1 }
R1 -> + const R1	{ ADD #const, R1 }
R1 -> + R1 const	{ ADD #const, R1 }
R1 -> + R2 R1	{ ADD R2, R1 }
R1 -> + R1 R2	{ ADD R2, R1 }

+rules for the other registers

Example, contd.



- LR(0) parser is constructed.
- For the construction of LR(0) parser, see additional slides (see subject MI-SYP).
- The resulting parser contains conflicts.

Resolving conflicts

- The conflicts are resolved so that a minimal number of instructions would be generated. Therefore, if there is a conflict (ie. more instructions can be selected) the instruction with the biggest pattern is preferred.
- **In case of shift-reduce conflict: shift is preferred.**
- **In case of reduce-reduce conflict: an instruction with the biggest right-hand side is preferred.**

Example, contd.

String := + A D1 + | + | + P D1 B | + C D1 **is read. The following sequence of transitions is performed:**

(pushdown store, input)

(# ,	:=	+	A	D1	+		+		+	P	D1	B		+	C	D1)	
(#	:= ,	+	A	D1	+		+		+	P	D1	B		+	C	D1)	
(#	:= + ,	A	D1	+		+		+	P	D1	B		+	C	D1)		
(#	:= + A ,	D1	+		+		+	P	D1	B		+	C	D1)			
(#	:= + A D1 ,	+		+		+	P	D1	B		+	C	D1)				
(#	:= + A D1 + ,		+		+	P	D1	B		+	C	D1)					
(#	:= + A D1 + ,	+		+	P	D1	B		+	C	D1)						
(#	:= + A D1 + + ,		+	P	D1	B		+	C	D1)							
(#	:= + A D1 + + ,	+	P	D1	B		+	C	D1)								
(#	:= + A D1 + + + ,	P	D1	B		+	C	D1)									

Example, contd.

```

(# := + A D1 + | + | + P, D1 B | + C D1) ⊢
(# := + A D1 + | + | + P D1, B | + C D1) ⊢ ; LD P(D1), R1
(# := + A D1 + | + R1, B | + C D1) ⊢
(# := + A D1 + | + R1 B, | + C D1) ⊢
(# := + A D1 + | + R1 B |, + C D1) ⊢
(# := + A D1 + | + R1 B | +, C D1) ⊢
(# := + A D1 + | + R1 B | + C, D1) ⊢
(# := + A D1 + | + R1 B | + C D1, ε) ⊢ ; LD C(D1), R2
(# := + A D1 + | + R1 B R2, ε) ⊢ ; ADD B(R1), R2
(# := + A D1 R2, ε) ⊢ ; ST A(D1), R2
(# Null, ε)

```

Example, contd.

The produced code:

```
LD P(D1), R1
LD C(D1), R2
ADD B(R1), R2
ST A(D1), R2
```

However, it is not optimal (we use two registers, one register suffices):

```
LD P(D1), R1
LD B(R1), R1
ADD C(D1), R1
ST A(D1), R1
```



SELECTING INSTRUCTIONS BY TREE PATTERN MATCHING AND DYNAMIC PROGRAMMING

Introduction

- Code selection problem has been presented as a problem of tiling an IR tree by tree patterns, which correspond to particular machine instructions.
- As we have seen, we can assign **a cost** to each pattern.
- Graham-Glanville technique tries to cover the tree by a largest possible patterns and therefore to generate minimal number of instructions. But it does not follow an optimal tiling.
- The computing of tiling a tree with the minimal cost (**the total cost of all used patterns is to be the minimal one**) can be done by combination of tree pattern matching and dynamic programming:

Introduction



- Another bottom-up method
- **Produces optimal tiling**
- **Suitable for CISC processors, which has rather complicated instructions**

Note on tree pattern matching

- The task of tree pattern matching (TPM) is **to find all occurrences of given tree patterns in an input subject tree.**

Many TPM methods have been proposed:

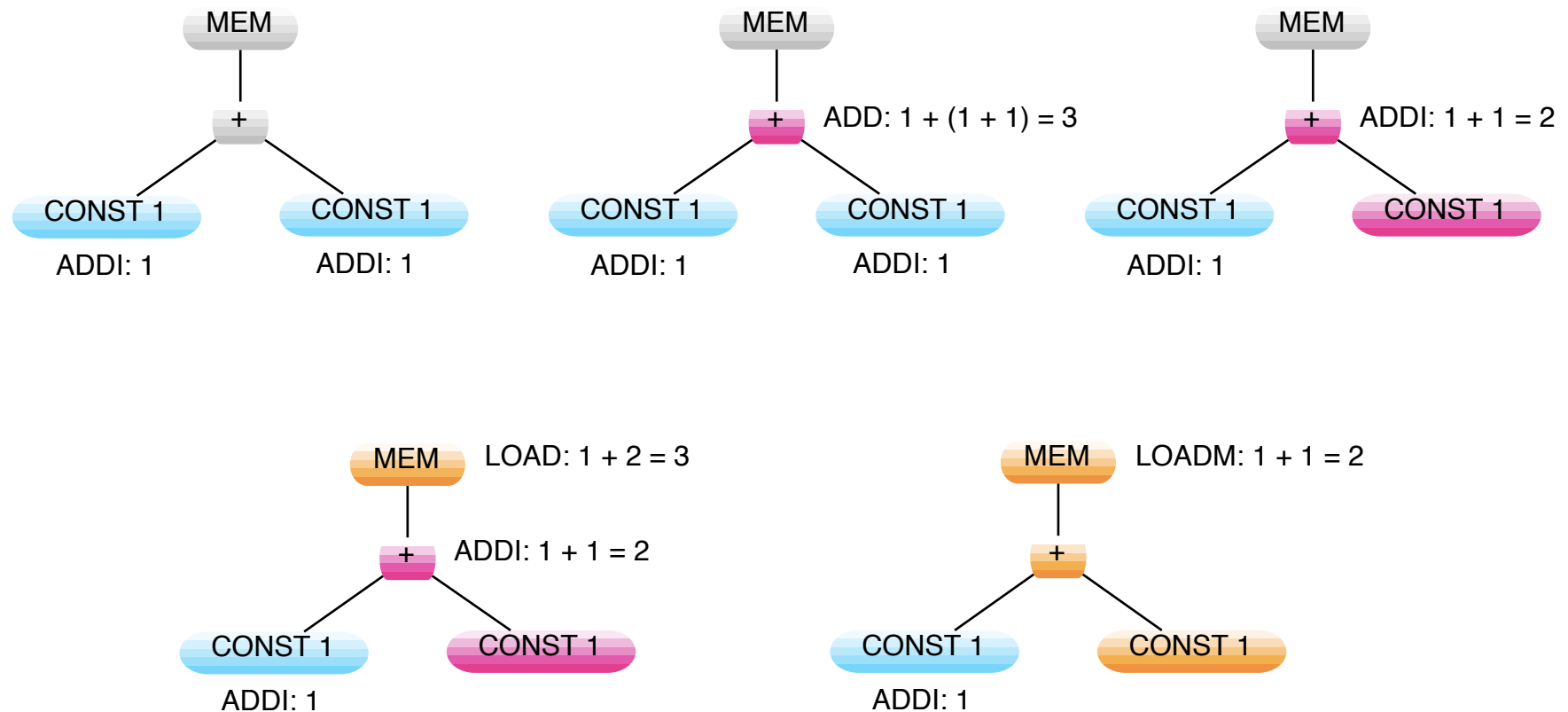
- Basic TPM algorithms: Hofmann, ODonell 1982
- TPM using automata:
 - Finite tree automata
 - Standard pushdown automata reading a linear notation of the tree (arbology)
- All these methods can be used in the selection code method in question

The Dynamic Programming Algorithm

- We compute a minimal **cost** to every node in the tree in a bottom-up fashion.
- **Bottom-up traversal:**
 - for each tile t of cost c that matches at node n
 - c_i = cost of each subtree corresponding to the leaves of t
 - cost of $n = c + \sum c_i$
- **2nd traversal:**

Traverse the tree using costs and associated instructions to generate the target code.

Dynamic programming - example





MAXIMAL MUNCH METHOD

Maximal munch method



- Construct tree patterns for each machine instruction
- Order pattern trees by size, largest first
- Top-down method, starting at the root node, find the largest pattern that fits.
- Cover the root node, and perhaps several other nodes, with this tile. Repeat for each subtree.
- Traverse tree top-down and emit instructions (in reverse order)

Maximal munch

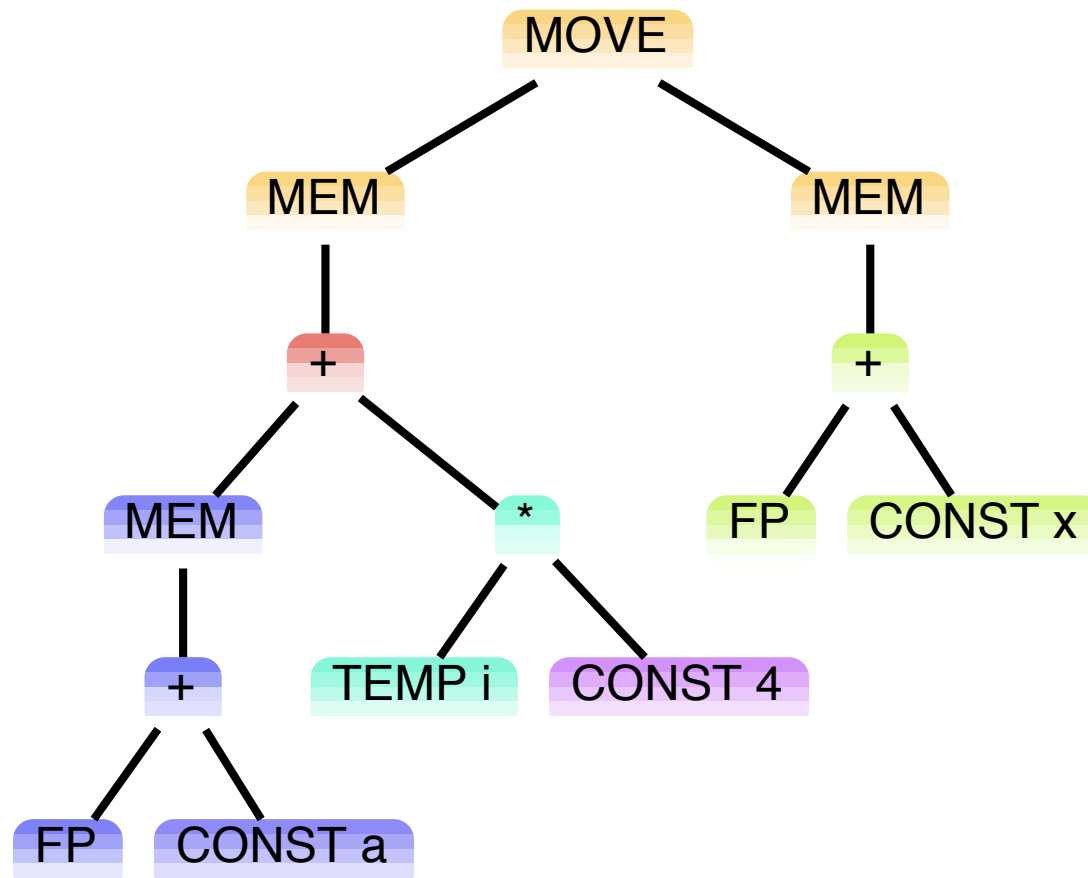


- Easy to understand and to implement (pattern matching).
- top-down method
- Fast method, good result with a RISC instruction set, but does not produce an optimal tiling in general.

Maximal munch - example



Maximal munch - example



- $r_1 \leftarrow M[fp + a]$
- $r_2 \leftarrow r_0 + 4$
- $r_2 \leftarrow r_i \times r_2$
- $r_1 \leftarrow r_1 + r_2$
- $r_2 \leftarrow fp + x$
- $M[r_1] \leftarrow M[r_2]$