## EE1390

Matrix Project

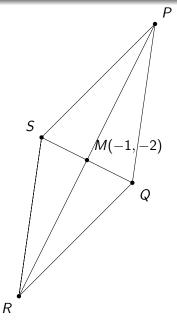
EE18BTECH11016 and EE18BTECH11025

## Question

Two sides of a rhombus are along the lines

$$(7-1)\mathbf{x} - 5 = 0$$
  
 $(1-1)\mathbf{x} + 1 = 0$ 

If its diagonals intersect at  $\begin{pmatrix} -1 \\ -2 \end{pmatrix}$ , find its vertices.



## Solution

Given the equations of two lines PQ and PS are :

$$(7-1)x - 5 = 0$$
  
 $(1-1)x + 1 = 0$ 

Solving these two equations, we get the point of intersection as P.

$$\begin{pmatrix} 7 & -1 \\ 1 & -1 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 5 \\ -1 \end{pmatrix}$$
$$\mathbf{x} = \begin{pmatrix} 1/6 & -1/6 \\ 1/6 & -7/6 \end{pmatrix} \begin{pmatrix} 5 \\ -1 \end{pmatrix}$$
$$\mathbf{x} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

So coordinates of P in matrix form are  $\binom{1}{2}$ 

Now to find coordinates of point R in matrix form, we need to use the mid-point formula.

Hence, 
$$M = (P+R)/2$$

where M = point of intersection of diagonals

$$= \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$R = 2M - P$$

$$R = \begin{pmatrix} -3 \\ -6 \end{pmatrix}$$

The direction vector of PR is  $\binom{2}{4}$  So, normal vector of PR is  $\binom{-4}{2}$ 

The equation of QS is 
$$(2 \ 4)(\mathbf{x} - {1 \choose -2}) = 0$$
  
 $(2 \ 4)\mathbf{x} + 10 = 0$ 

We can get the points Q by finding the intersection of PQ and QS;

(7 -1) 
$$\mathbf{x} - 5 = 0$$
  
(2 4)  $\mathbf{x} + 10 = 0$   
( $^{7}_{2 \ 4}^{-1}$ )  $\mathbf{x} = {5 \choose -10}$   
 $\mathbf{x} = {4/30 \ 1/30 \choose -2/30 \ 7/30} {5 \choose -10}$   
 $\mathbf{Q} = {1/3 \choose -8/3}$ 

Similarly for getting S, we find intersection of PS and QS

(1-1) 
$$\mathbf{x} + 1 = 0$$
  
(24)  $\mathbf{x} + 10 = 0$   
( $^{1}_{24}$ )  $\mathbf{x} = (^{-1}_{-10})$   
 $\mathbf{x} = (^{4/6}_{-2/6})^{1/6}_{1/6} (^{-1}_{-10})$   
 $\mathbf{S} = (^{-7/3}_{-4/3})$ 

