

Motion, Tracking & Optical Flow II

Gary Overett (Slides adapted from CMU 16-720 2014)
Szeliski Chapter 8



Summary

- Using Gradients to Estimate Motion
- Ambiguities
- Constant Motion Assumption
- Affine Flow Assumption
- Planar Assumption
- Tracking Using Mean Shift
- Motion Segmentation
- Background Detection

Tracking Using Mean Shift



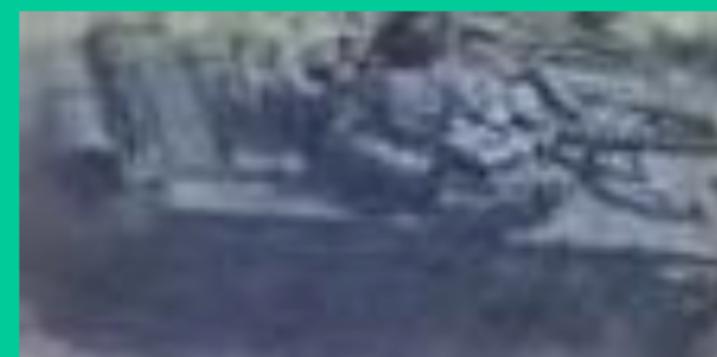
Tracking as “Hill Climbing”

**current frame +
previous location**



appearance model

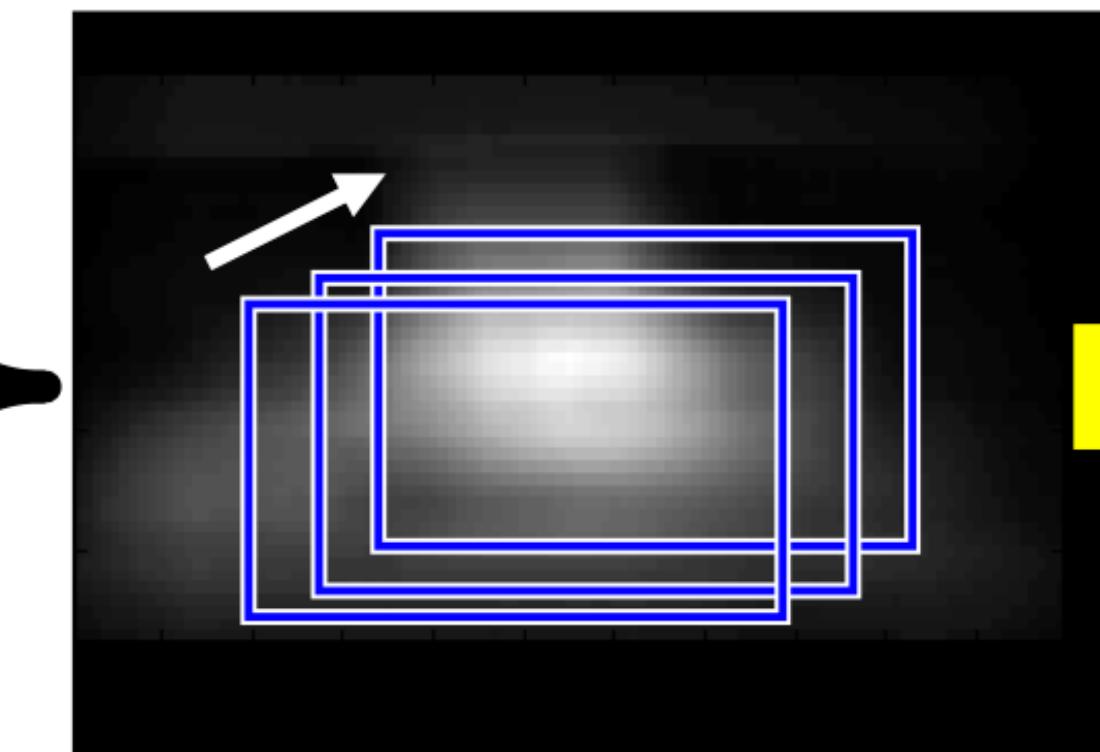
(e.g. image template, or



color; intensity; edge histograms)



Response map
(confidence map; likelihood image)



current location



Mode-Seeking

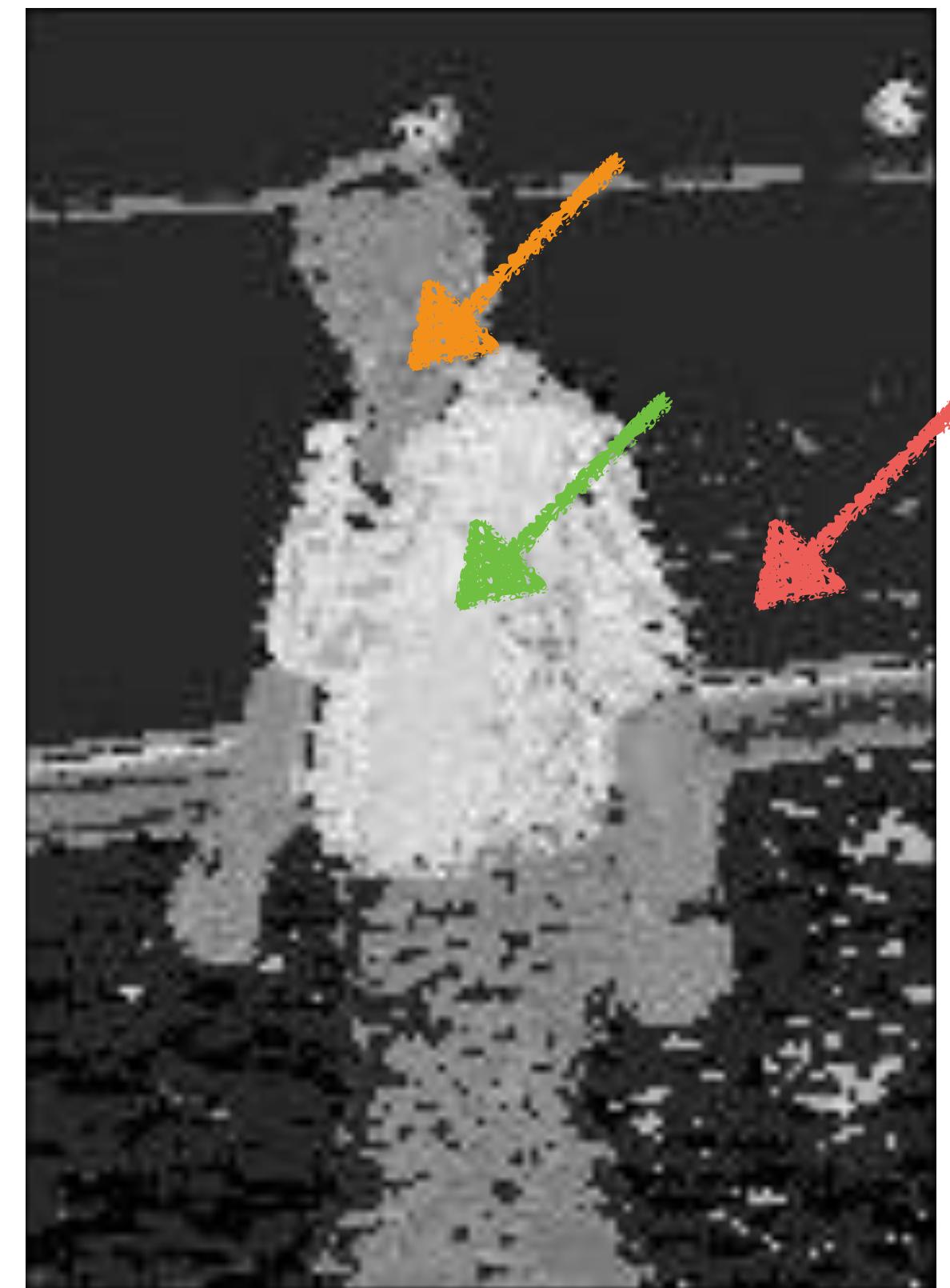
(e.g. mean-shift; Lucas-Kanade)

Mean-Shift Tracking

Create a response map with pixels weighted by “likelihood” that they belong to the object being tracked.
Perform mean- shift algorithm on pixels (weighted points) in that image.

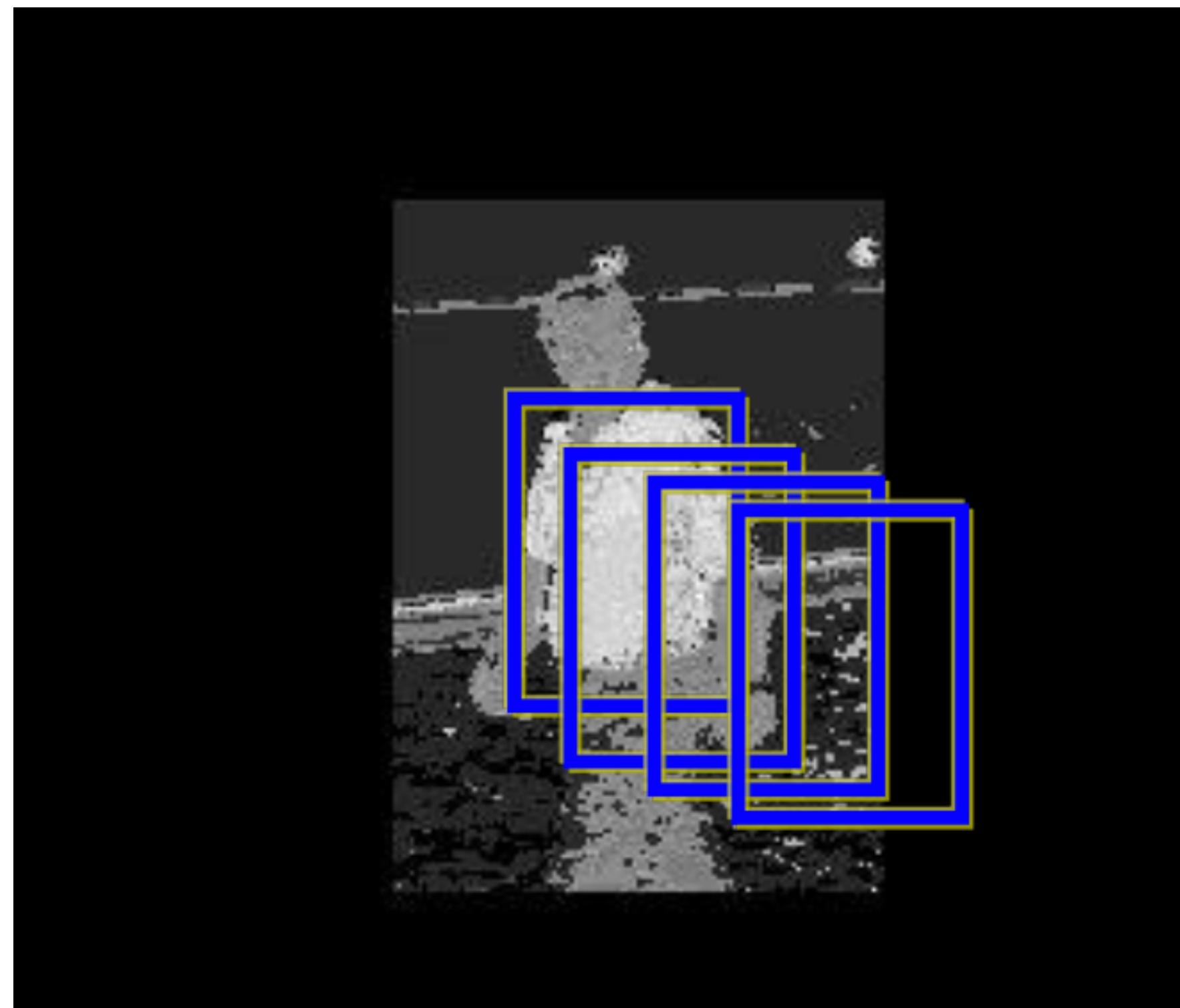
Computation of likelihood can be based on

- color
- texture
- shape (boundary)
- predicted location
- classifier outputs



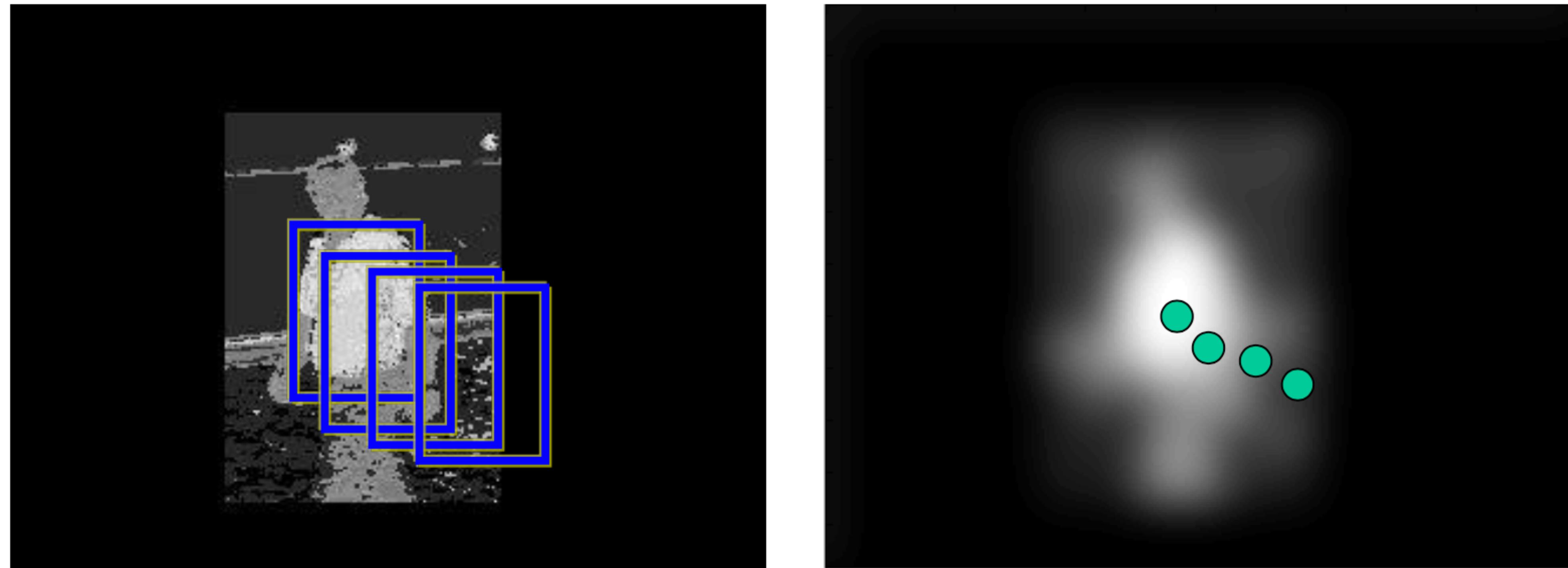
Mean-Shift on Weight Images

- The pixels form a uniform grid of data points, each with a weight (pixel value). Perform standard mean-shift algorithm using this weighted set of points.



Nice Property

- Running mean-shift with kernel K on weight image w is equivalent to performing gradient ascent in a (virtual) image formed by convolving w.



- The algorithm is performing hill-climbing on an implicit density function.

Mean-Shift Tracking Example



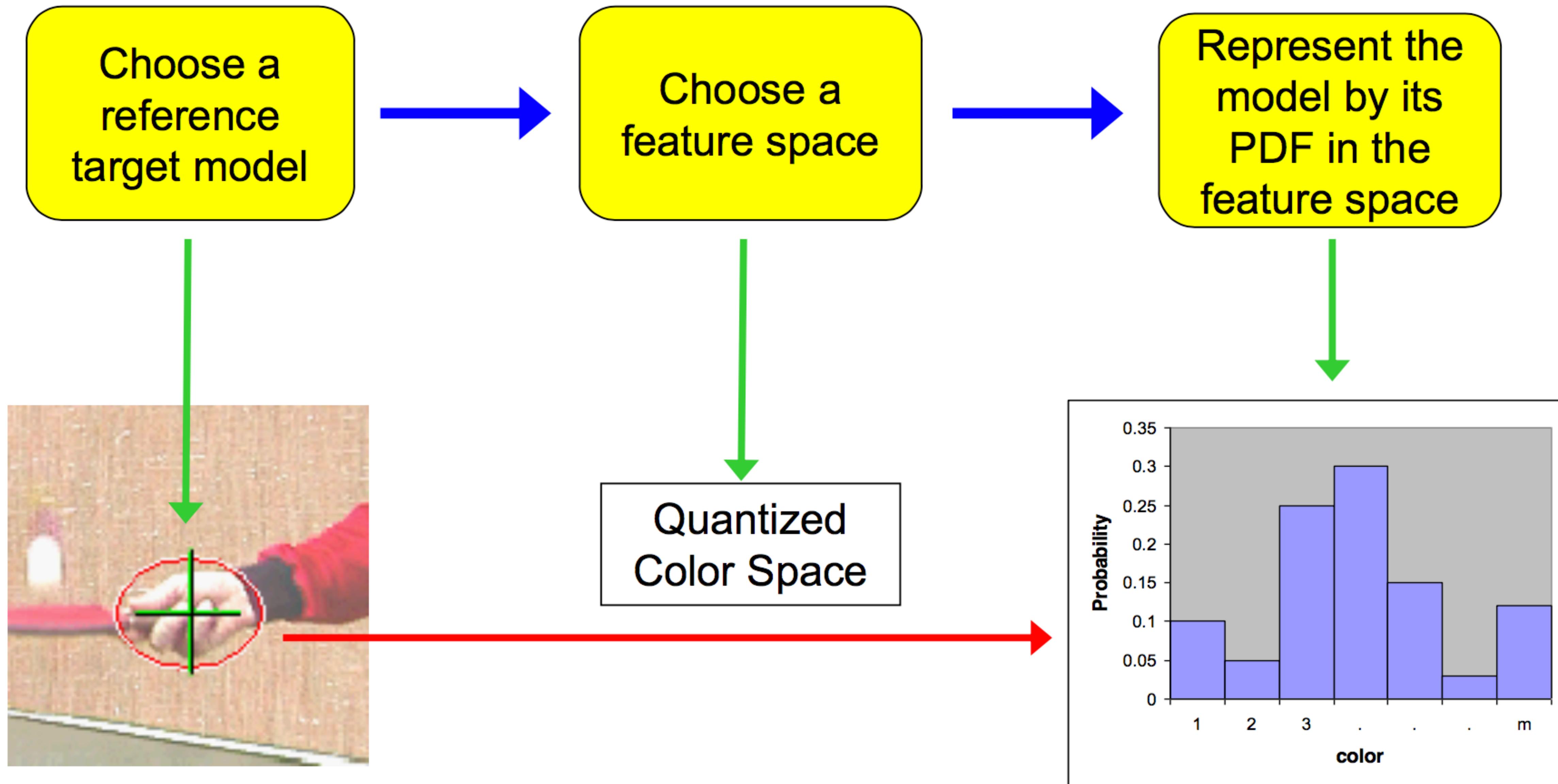
Mean-Shift Tracking Example



Using Mean-Shift on Color Models

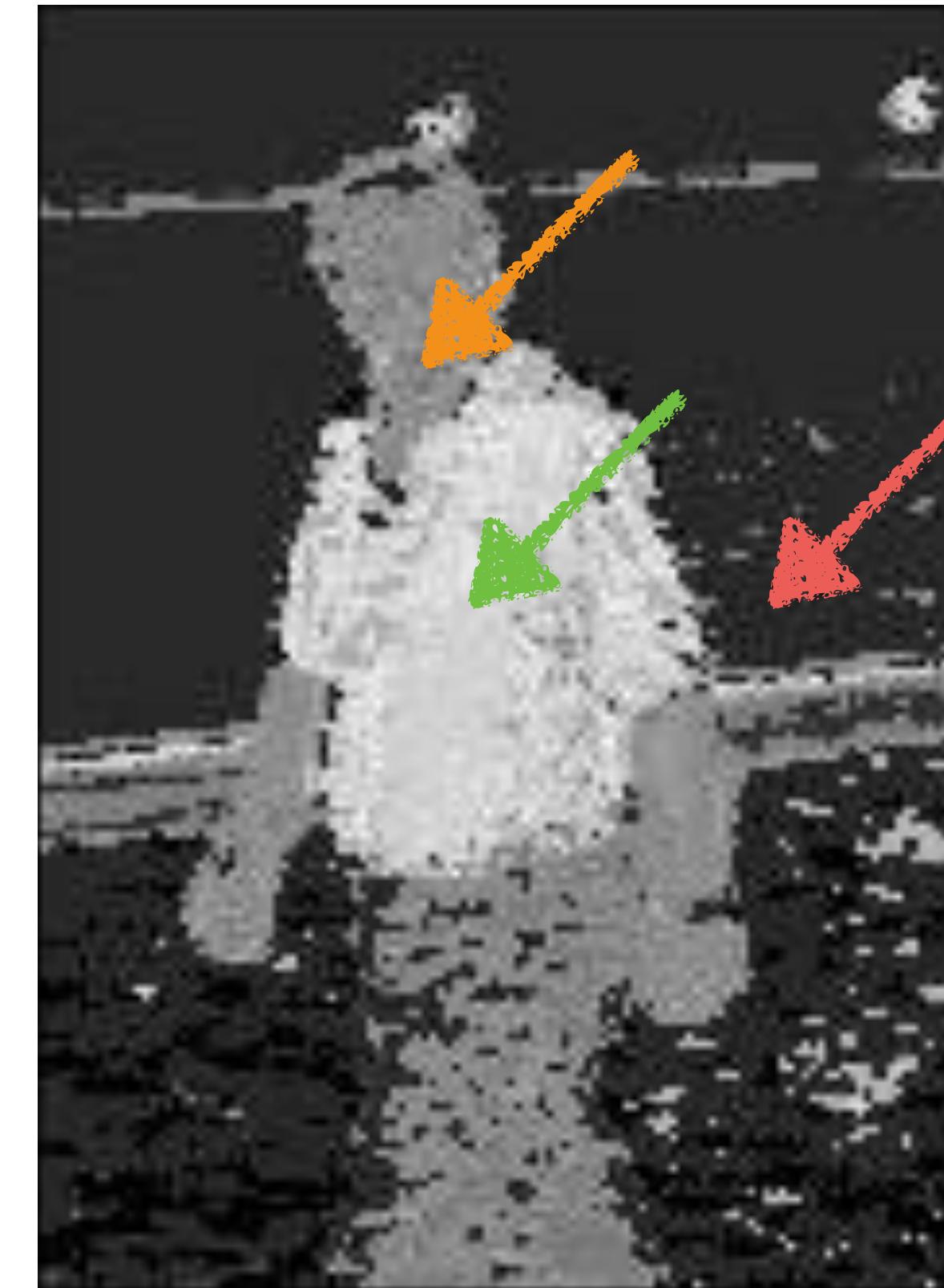
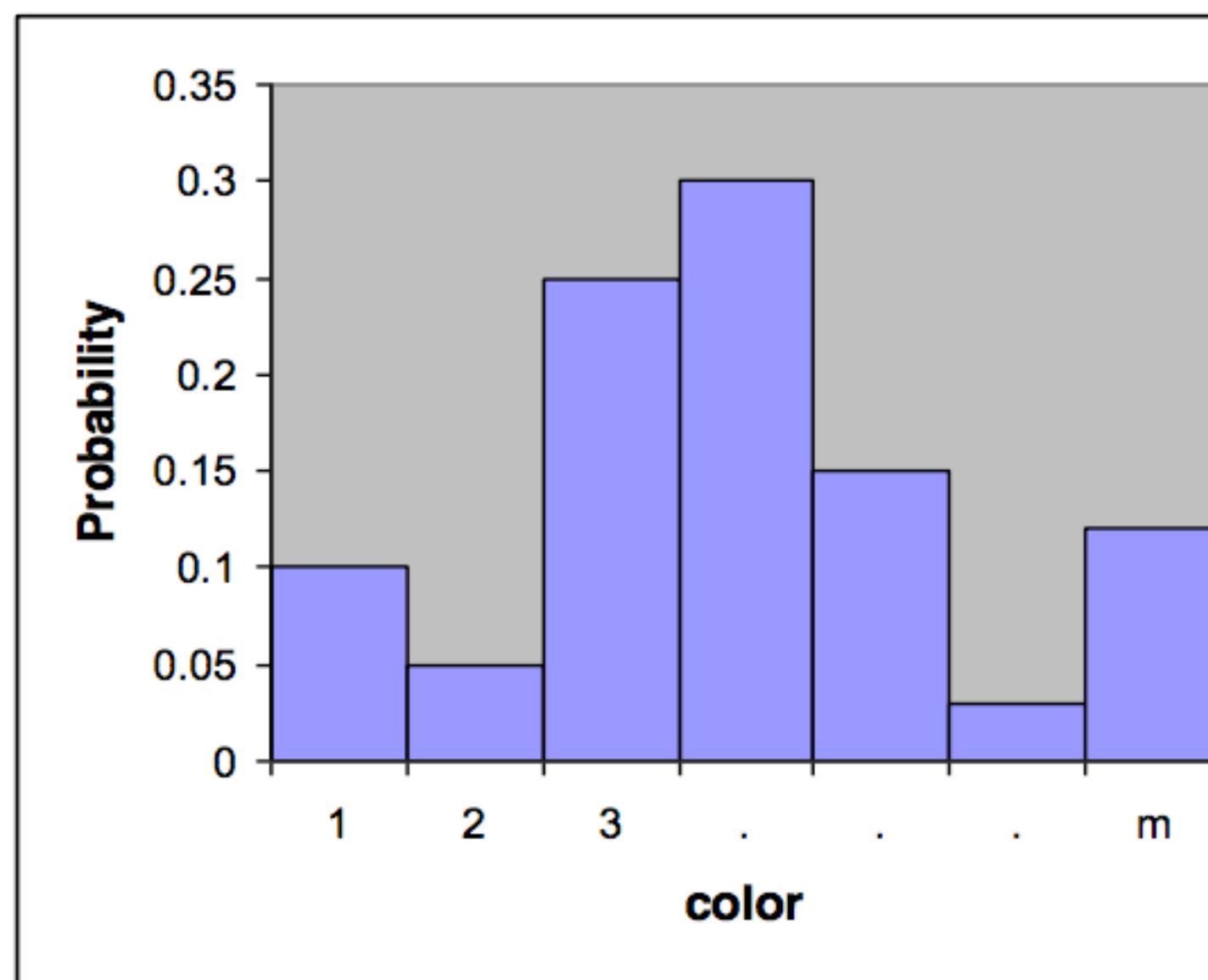
Two approaches:

- 1) Create a color “likelihood” image, with pixels weighted by similarity to the desired color (best for unicolored objects)
- 2) Represent color distribution with a histogram. Use mean-shift to find region that has most similar distribution of colors.

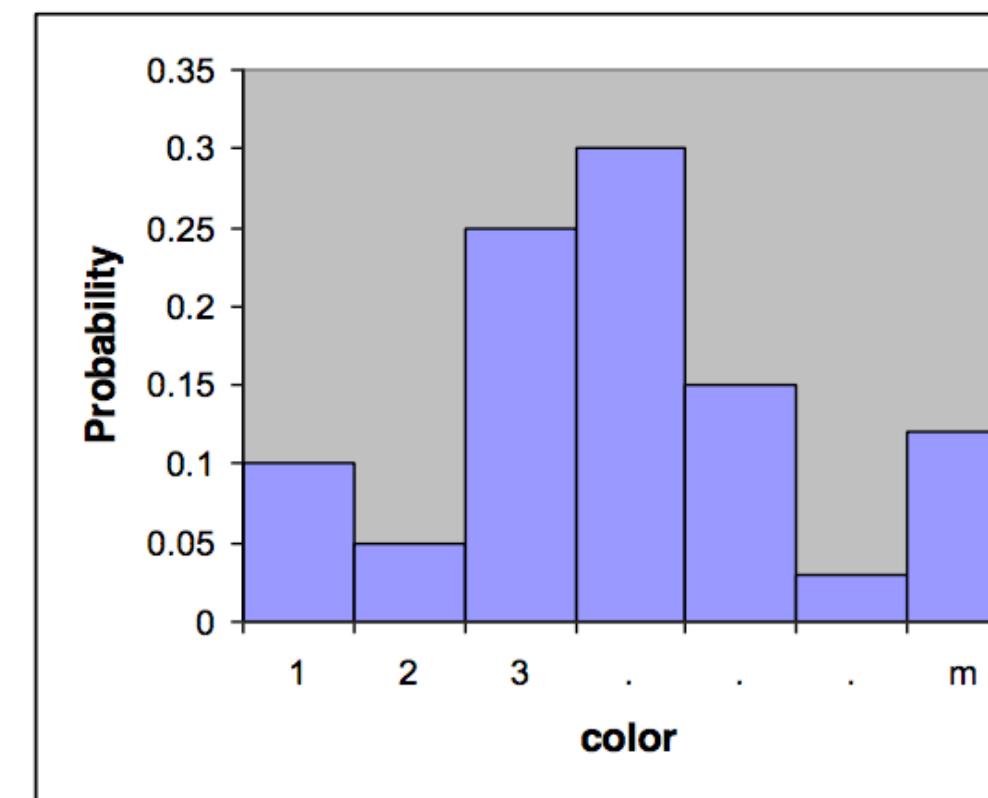


Kernel Based Object Tracking, by Comaniniu, Ramesh, Meer

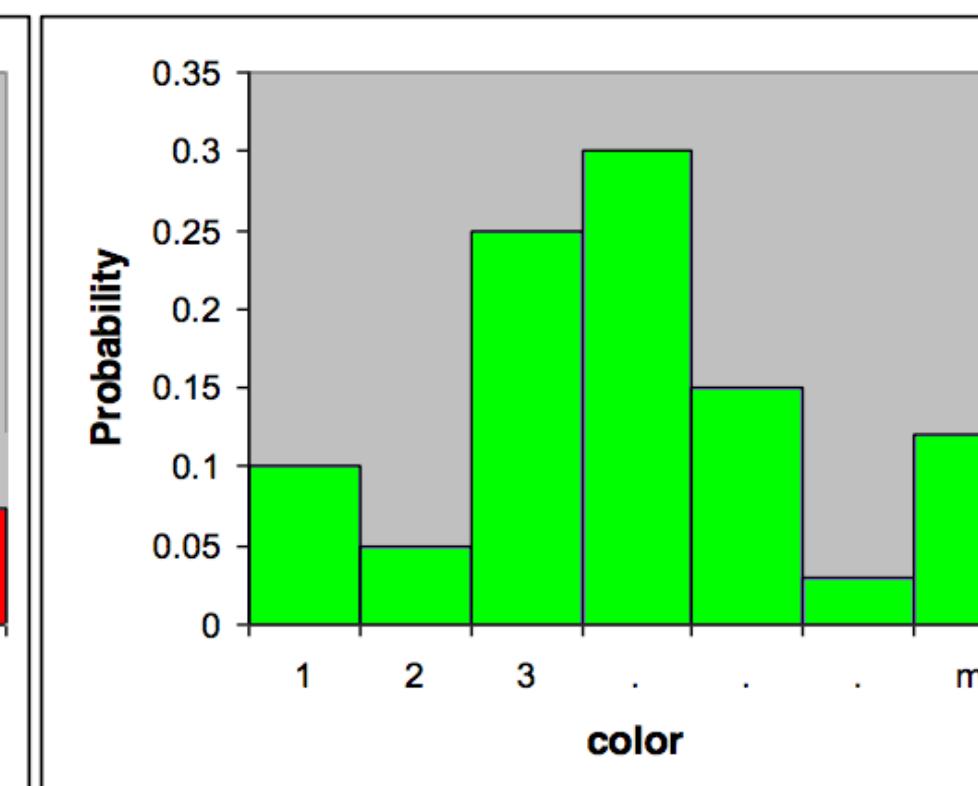
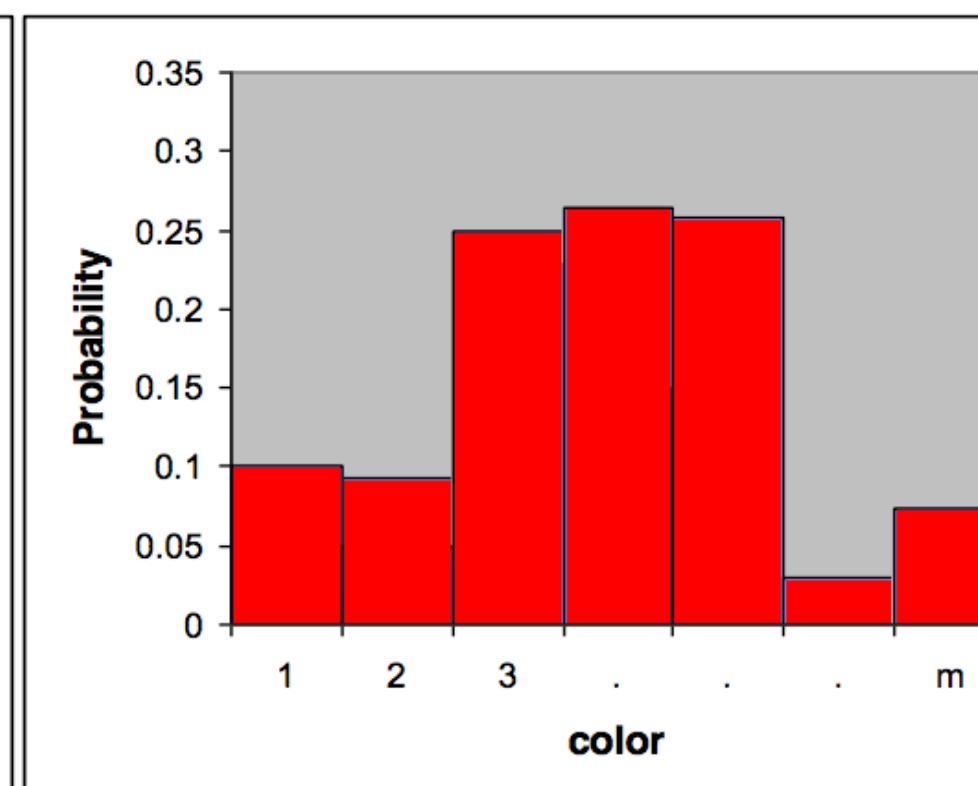
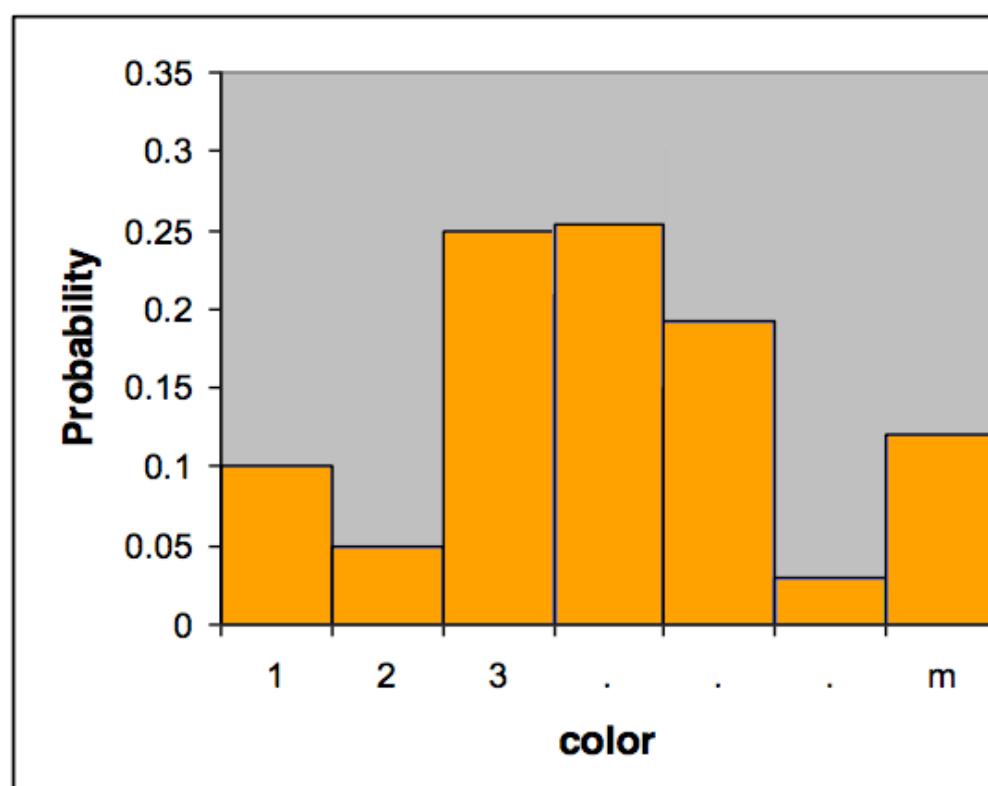
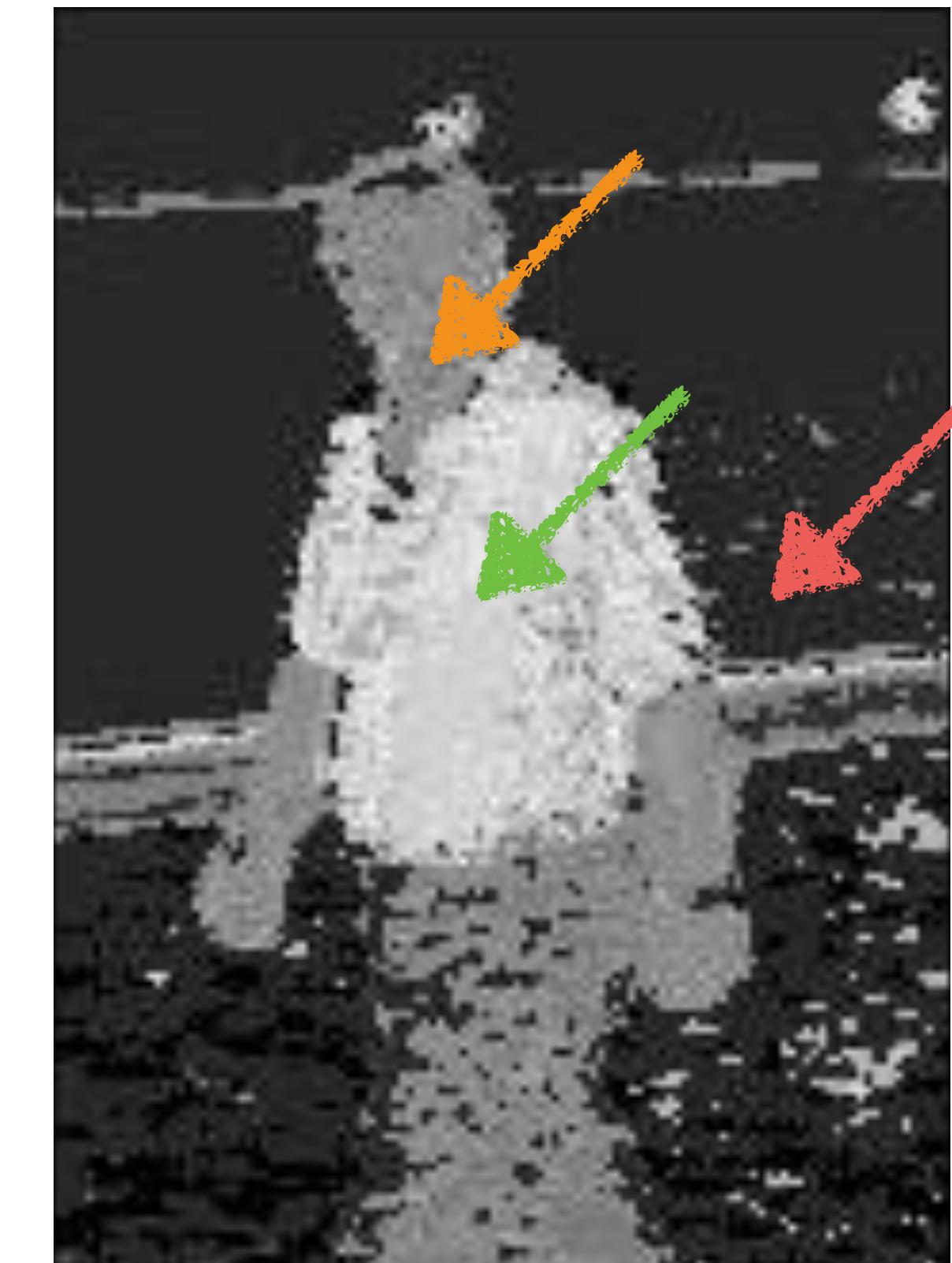
1) Color Likelihood Image



2) Color Distribution + Distance Metric



Distance between
Histograms

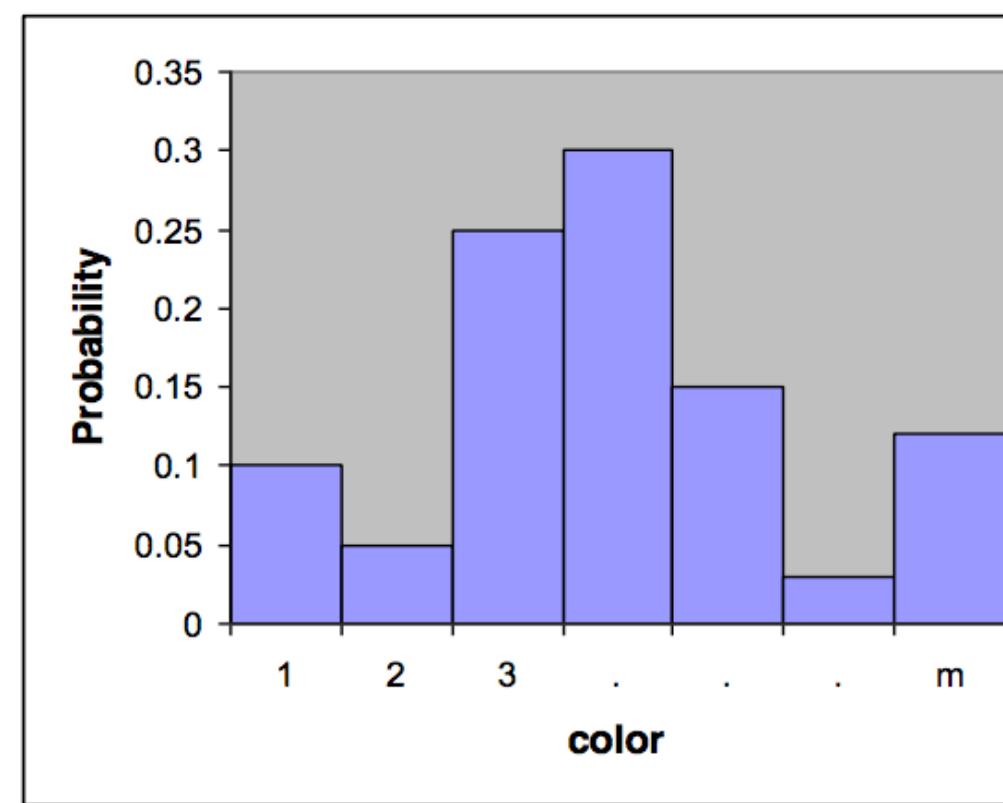


Using Mean-Shift on Color Models

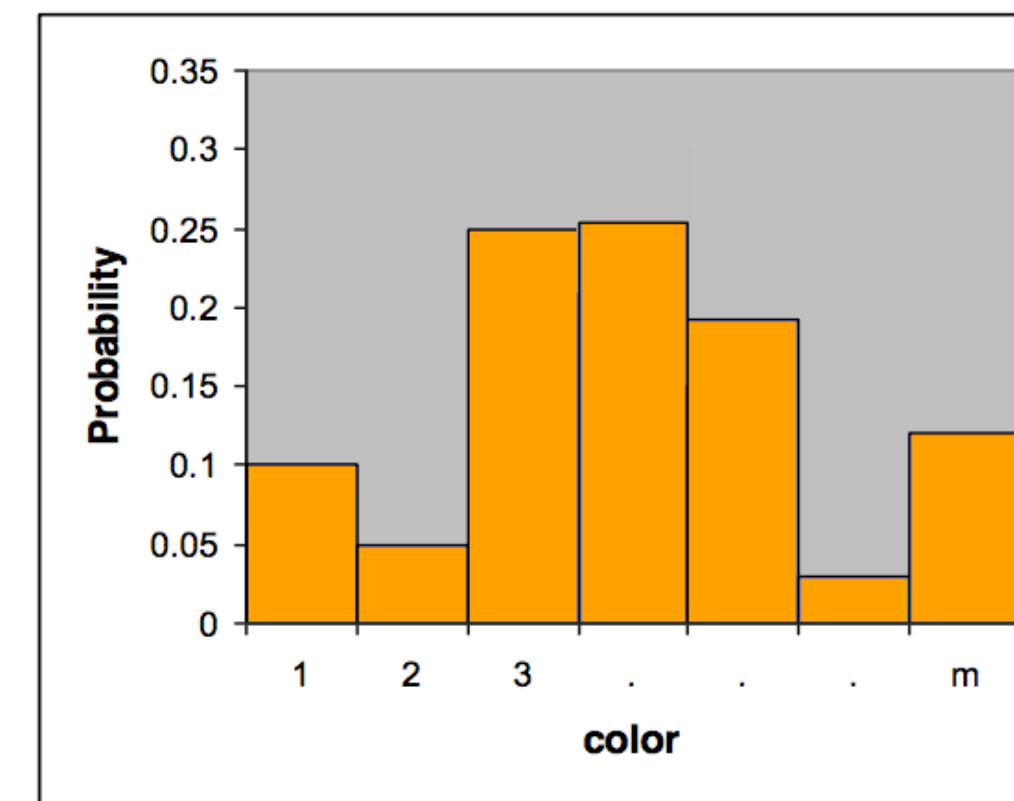
Two approaches:

- 1) Create a color “likelihood” image, with pixels weighted by similarity to the desired color (best for unicolored objects)
- 2) Represent color distribution with a histogram. Use mean-shift to find region that has most similar distribution of colors.
- Think about it... discuss the advantages of both, can you think of other color models that might be useful?

What Distance Metric?



q



$p(y)$

Bhattacharyya Distance

$$f(q, p(y)) = \sum_u \sqrt{q_u p_u(y)}$$



From Comaniciu, Ramesh, Meer

Feature space: $16 \times 16 \times 16$ quantized RGB

Target: manually selected on 1st frame

Average mean-shift iterations: 4



Partial occlusion



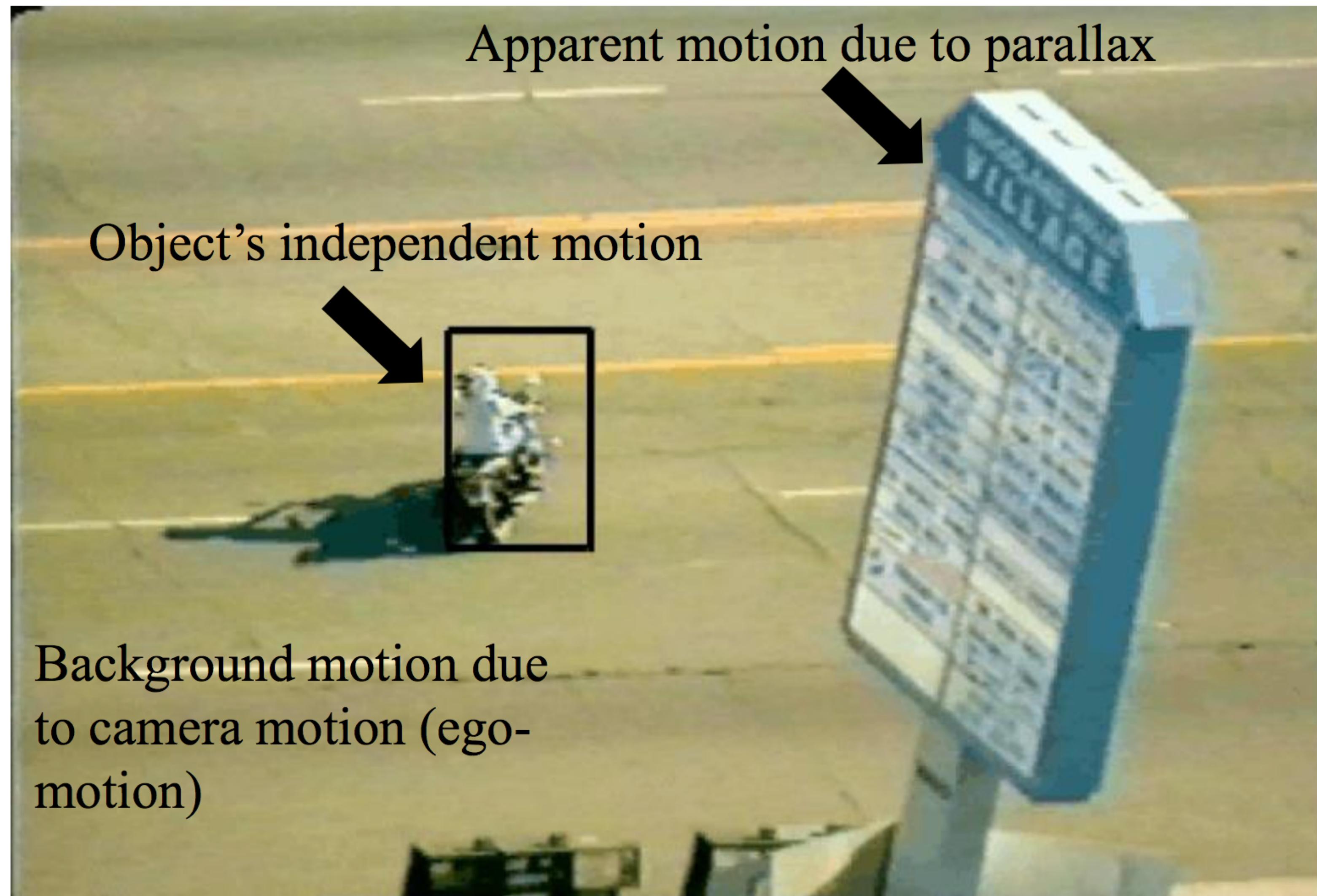
Distraction



Motion blur

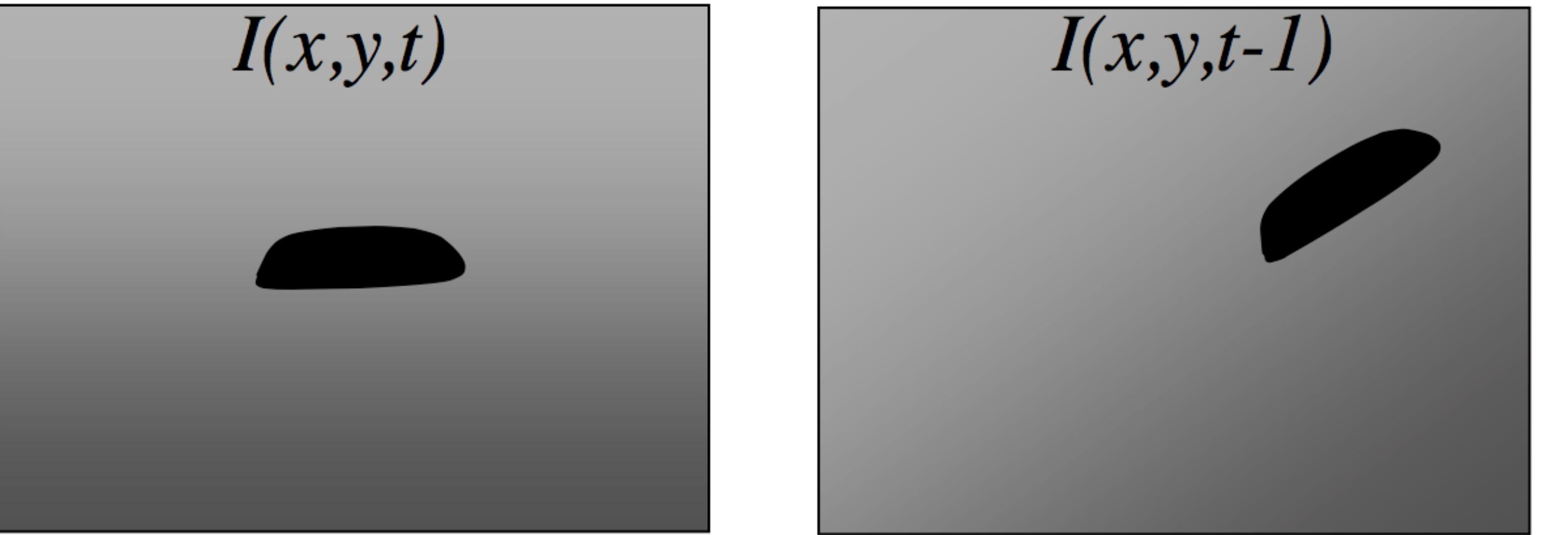
Motion Segmentation

Motion Segmentation

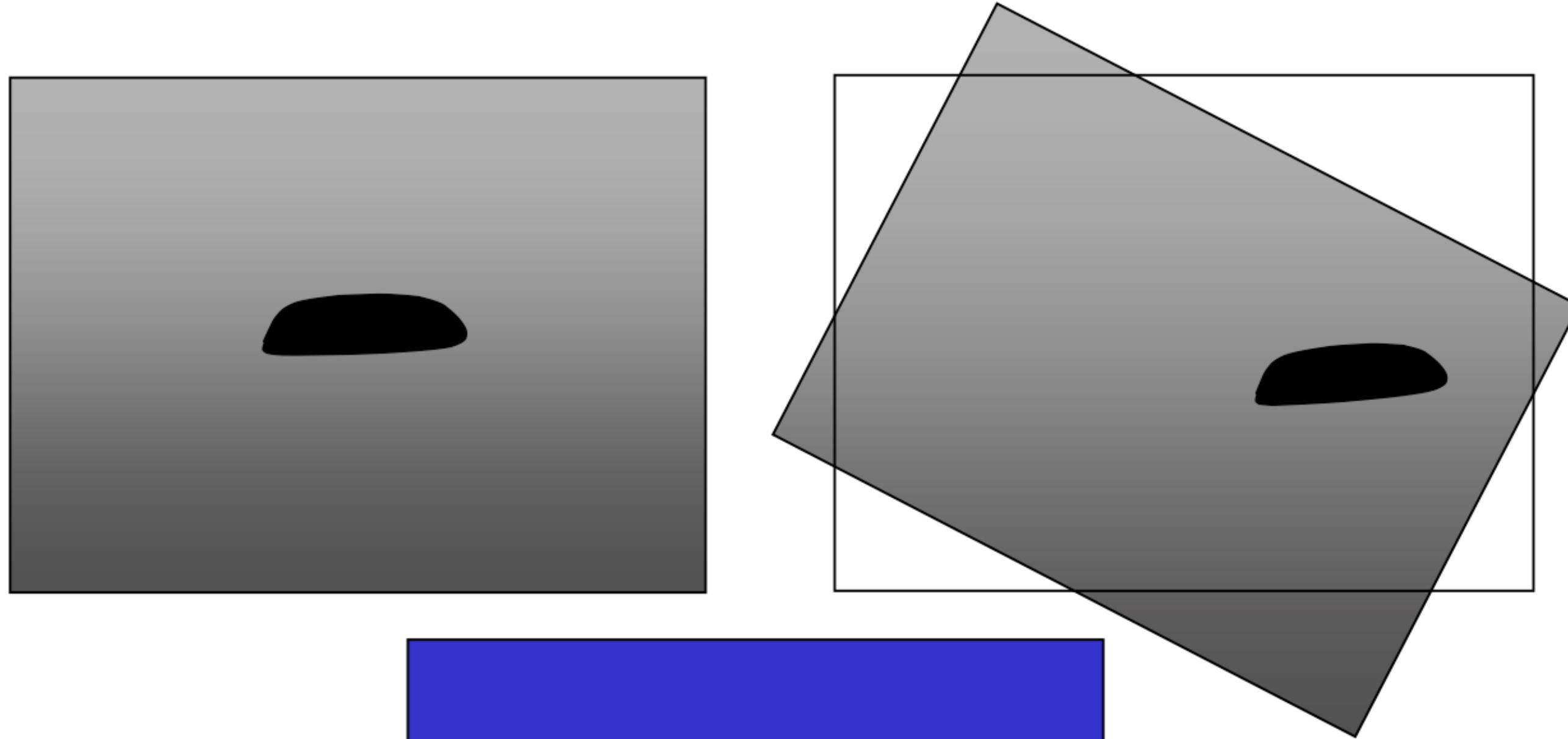


Separating Motion

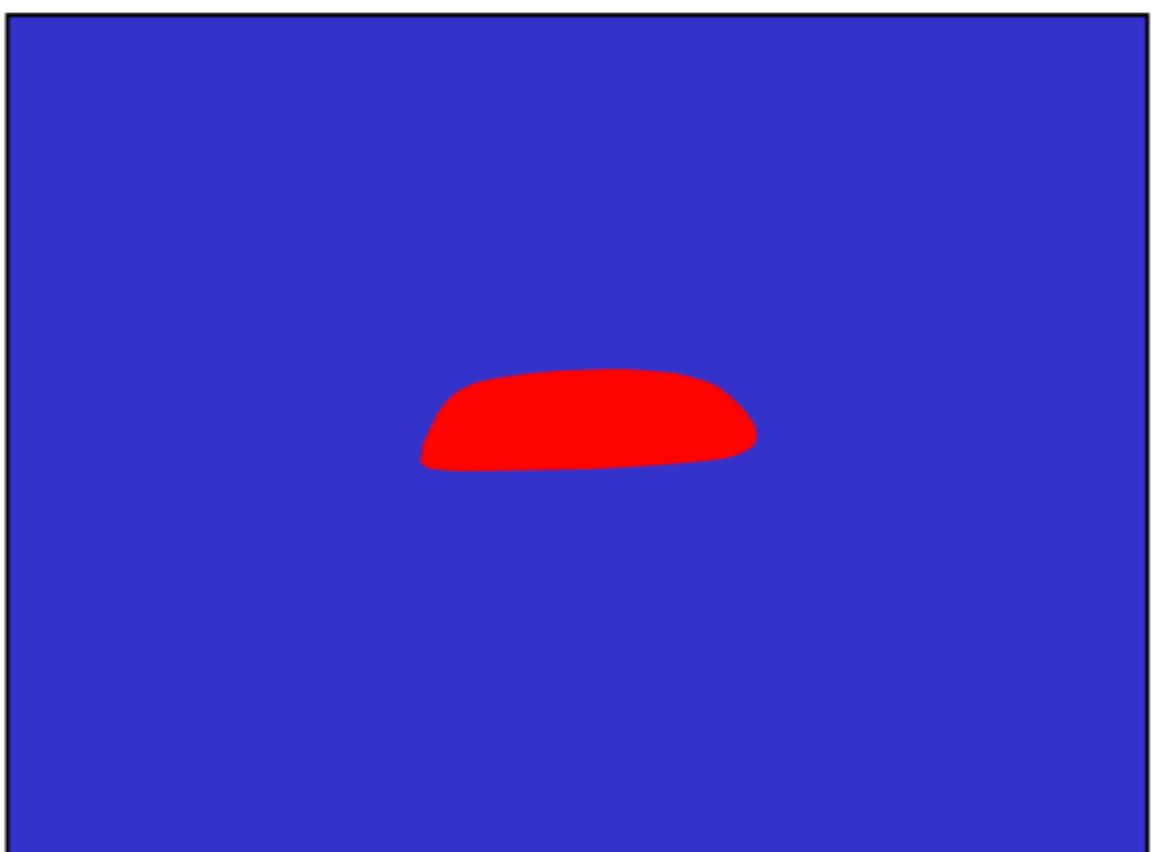
- Consider removing the dominant motion in the image as “background”
 - Assumes a large static “background” + “small” moving objects
- How about segmentation from independent motion and parallax: i.e. “Layered” representations



Compute flow
($u(x,y), v(x,y)$)

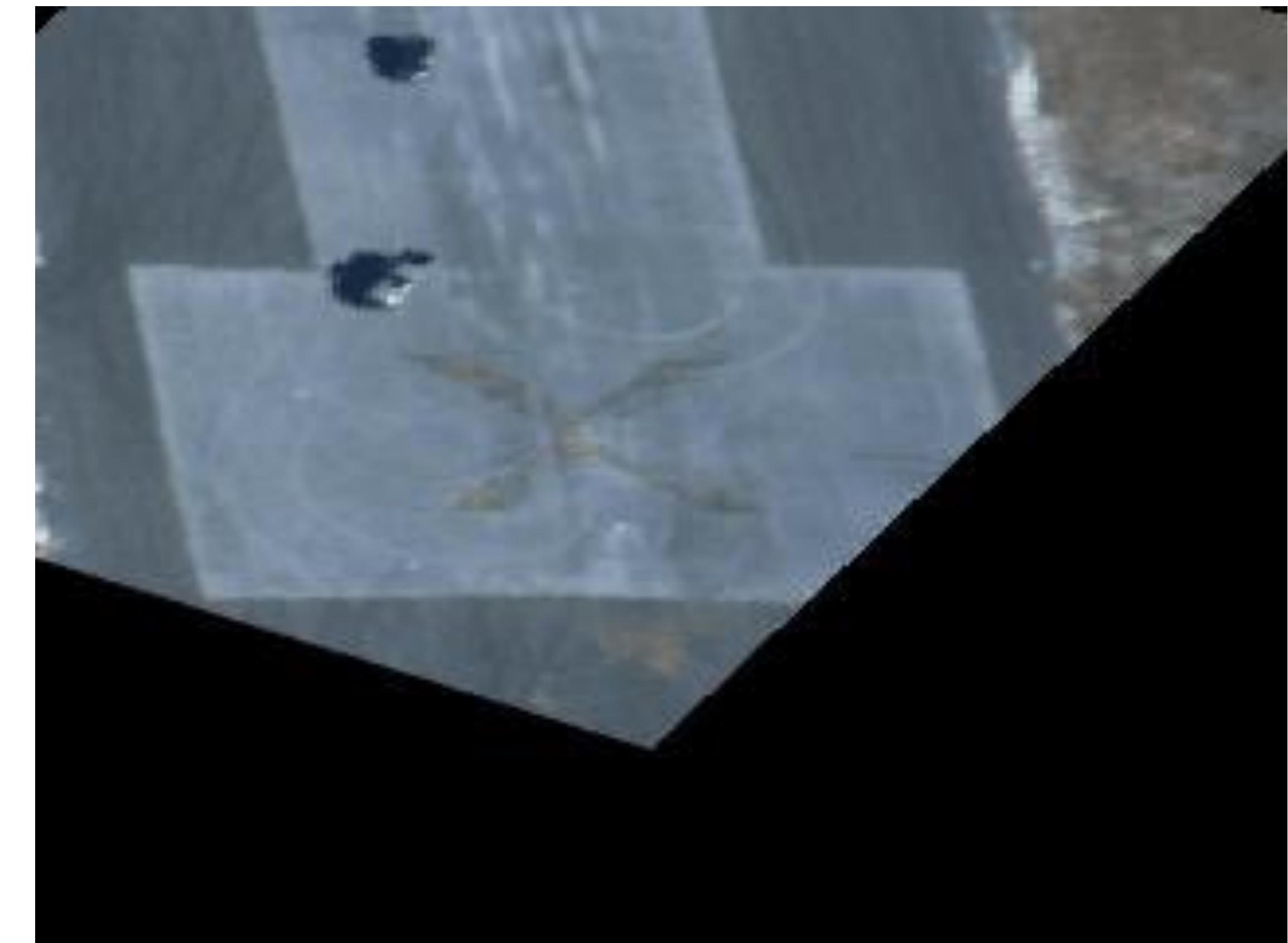


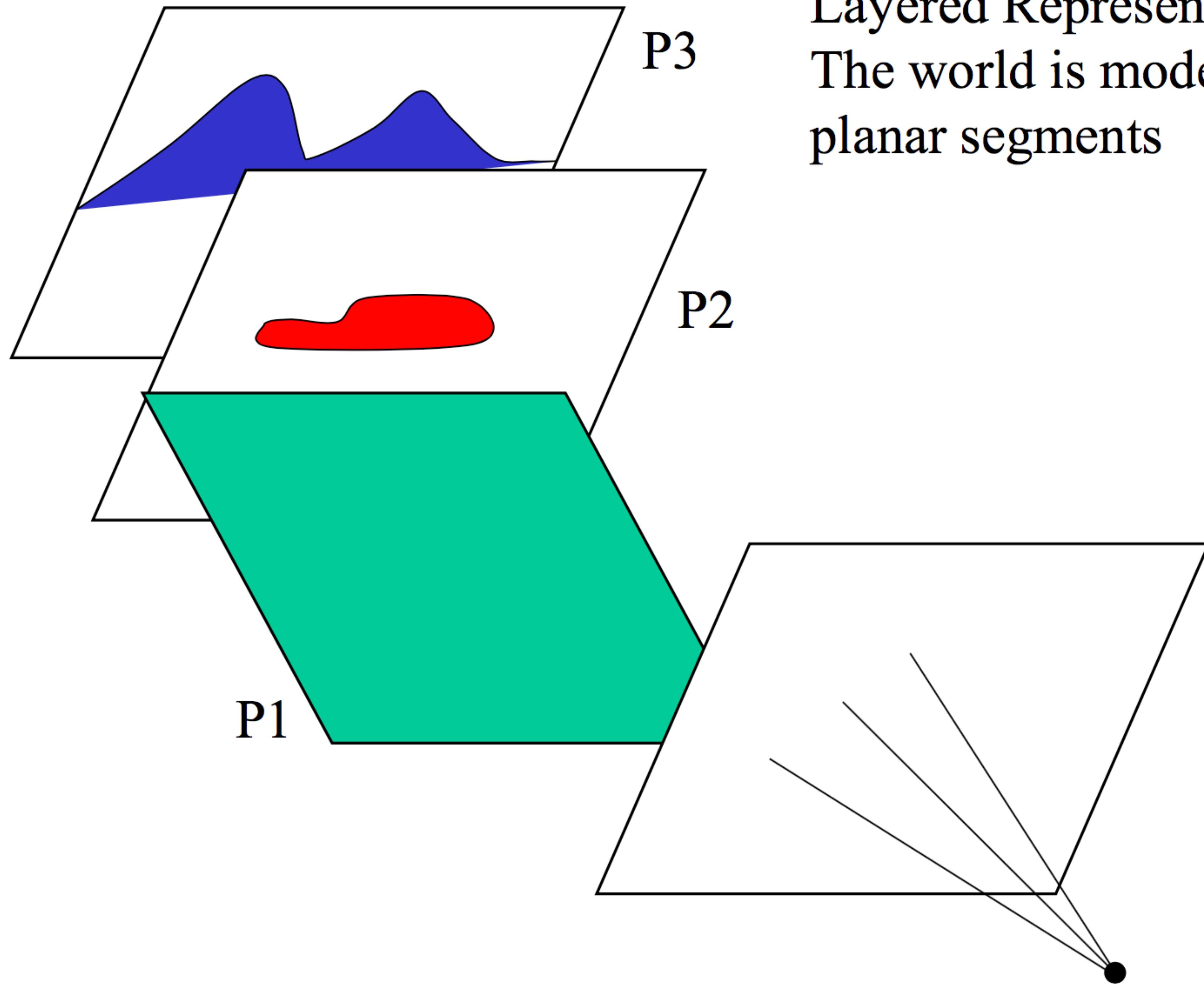
Warp image



Compare images

Warp/align the dominant background



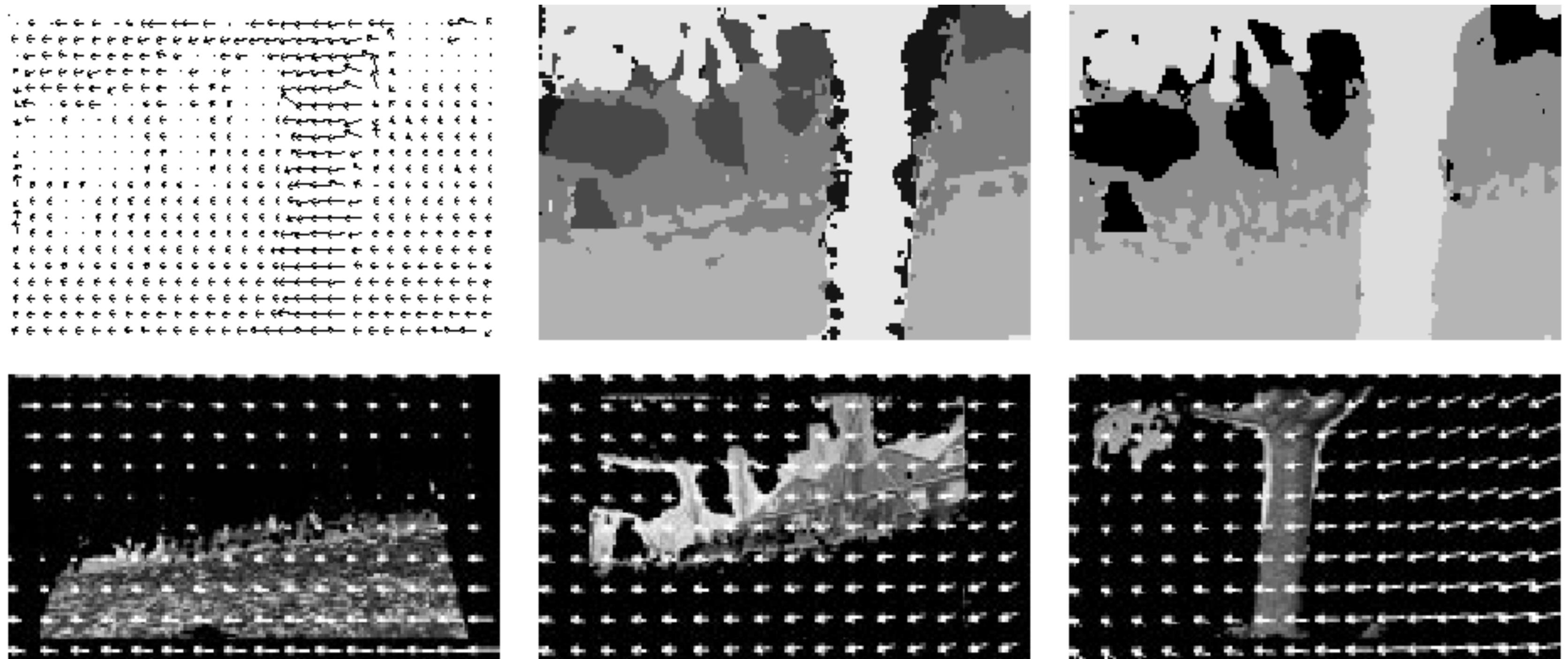


Layered Representation:
The world is modeled as a set of
planar segments

Layered Representations : Outline

- Estimate the dominant motion a over the entire image.
- Warp the images according to the dominant motion.
- Extract the regions that do not agree with the dominant motion.
- For each region:
 - Estimate the dominant motion again over that region
 - Extract the moving objects in the region by warping and differencing.
- This assumes that there is a dominant motion, i.e., one region is very large relative to the others. This might not be the case, so another approach is to first divide into K different motion models and find the corresponding pixels. A sketch of the algorithm is:
 - Estimate the motion in local blocks (e.g., $N \times N$ windows in the image)
 - Each window produces a vector representing the estimate motion (e.g. 6-dim if affine model)
 - Cluster the vectors into K clusters (corresponding to K motions) Assign each pixel to the cluster that best agrees with the local motion
 - Re-estimate the motion in each cluster and iterate

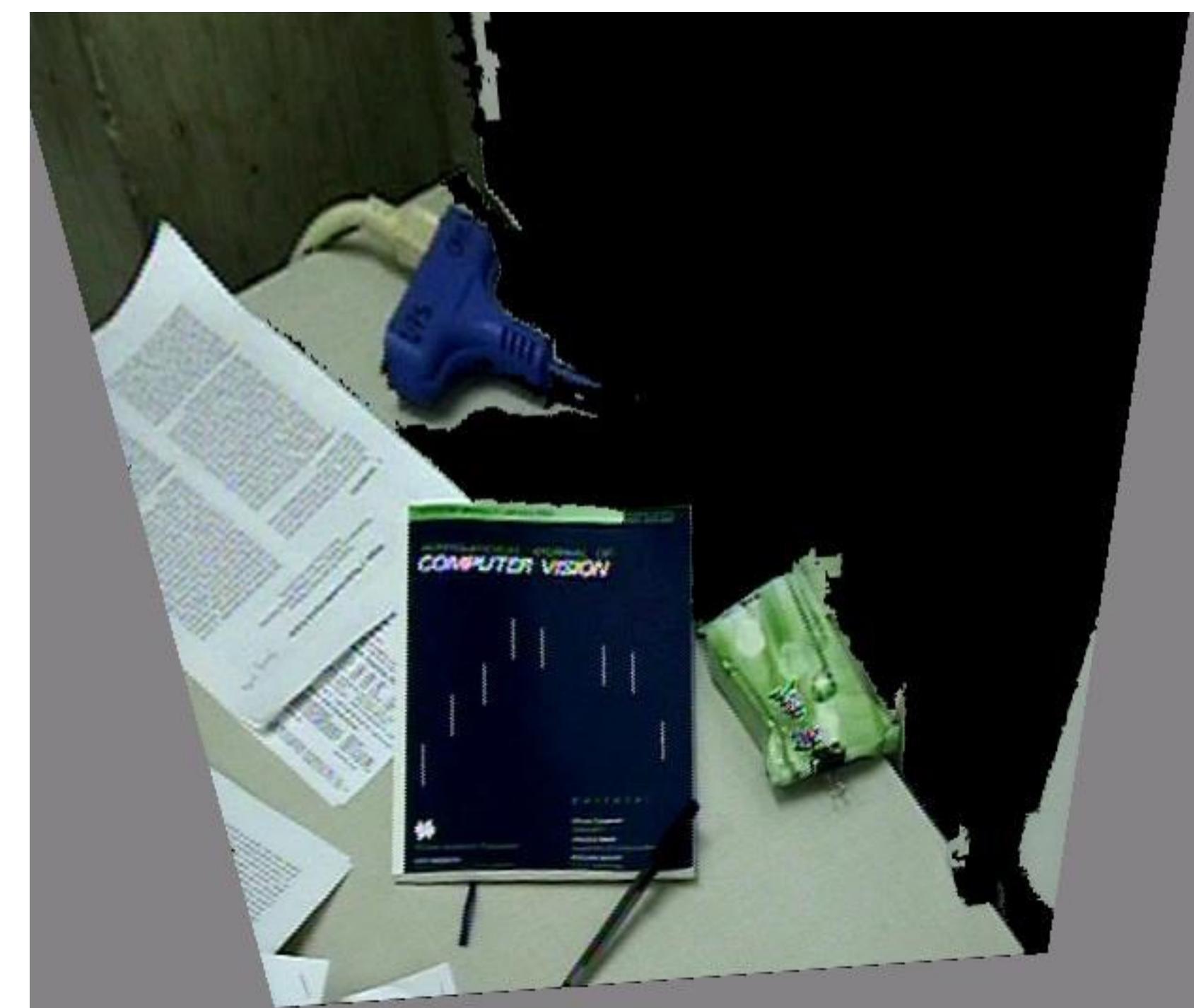
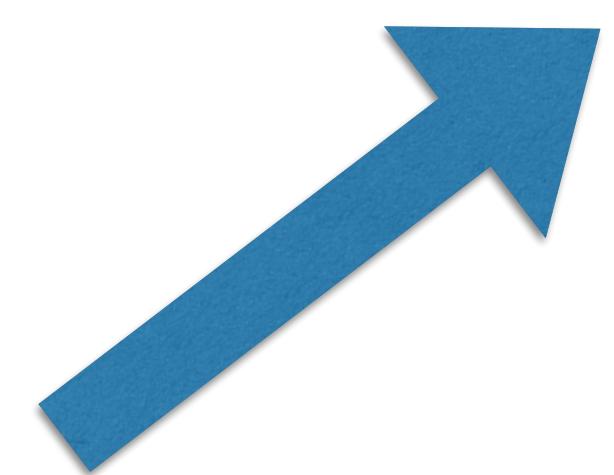
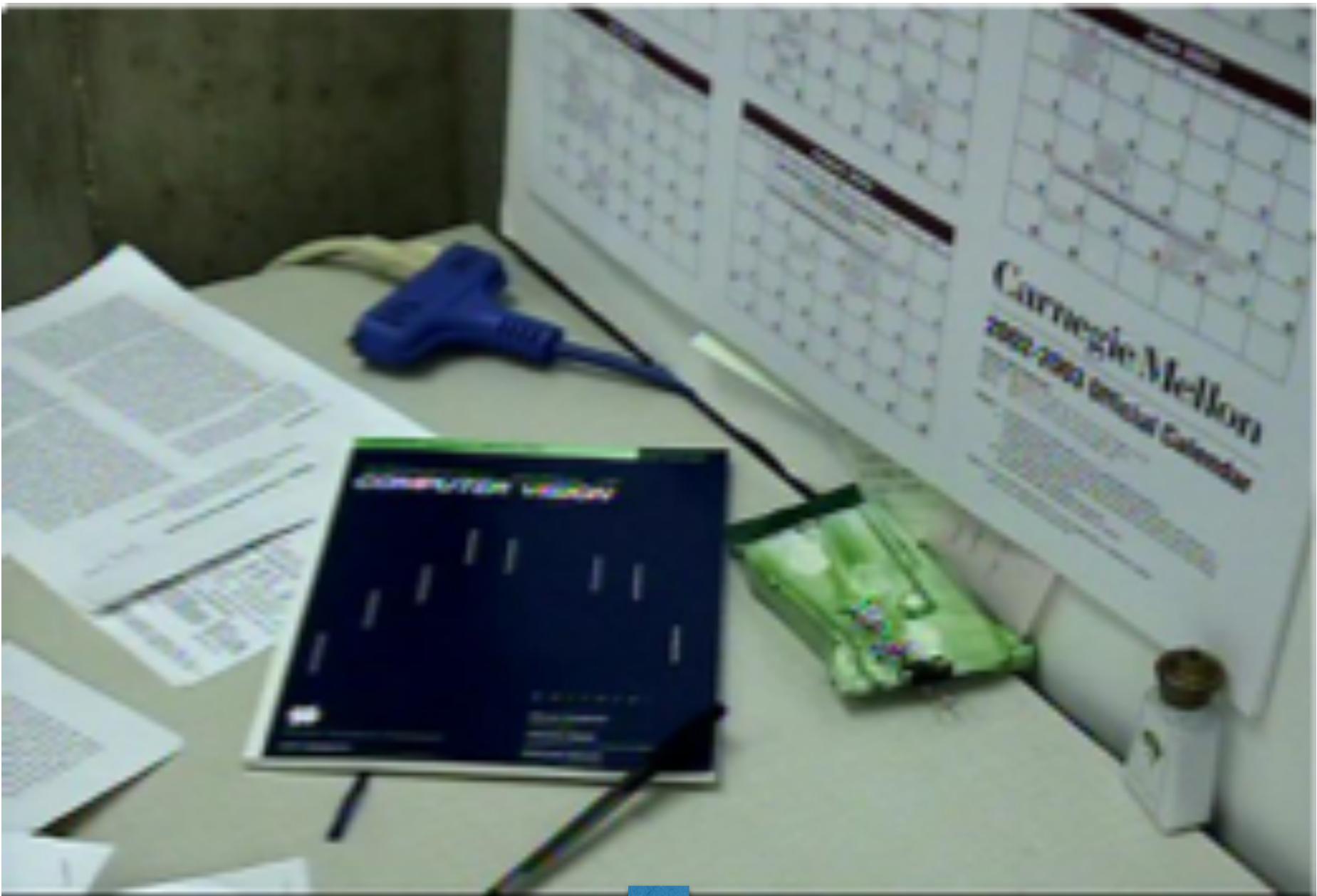
Motion Segmentation in Layers



Example from Adelson et al.



From M. Irani, Weizmann Inst.



Q. Ke & T. Kanade

Side Note

- Drone footage as which is currently a huge expansion area in computer vision is particularly well suited to exploring these techniques.

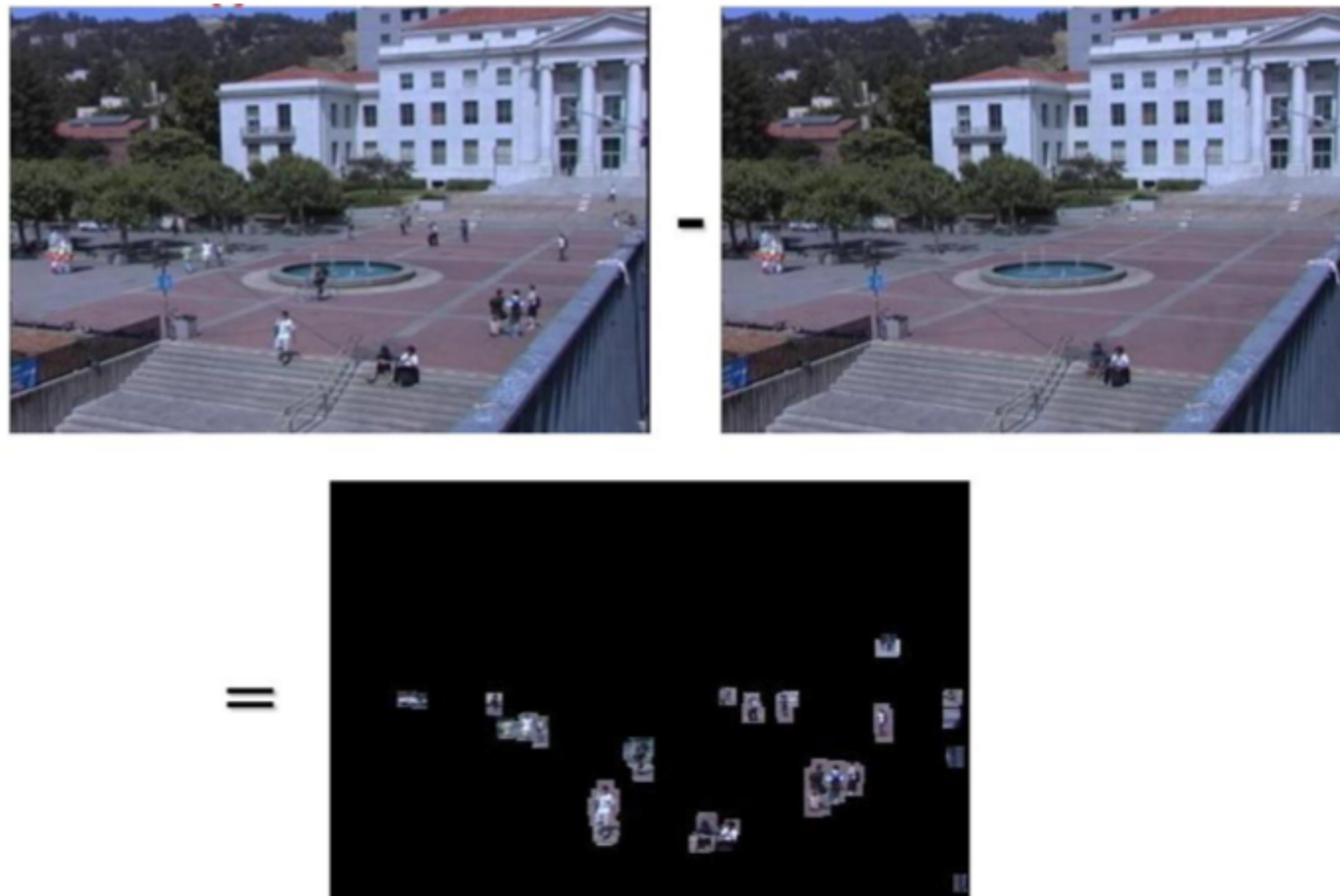
Change Detection/Background Models

Simple Background Subtraction



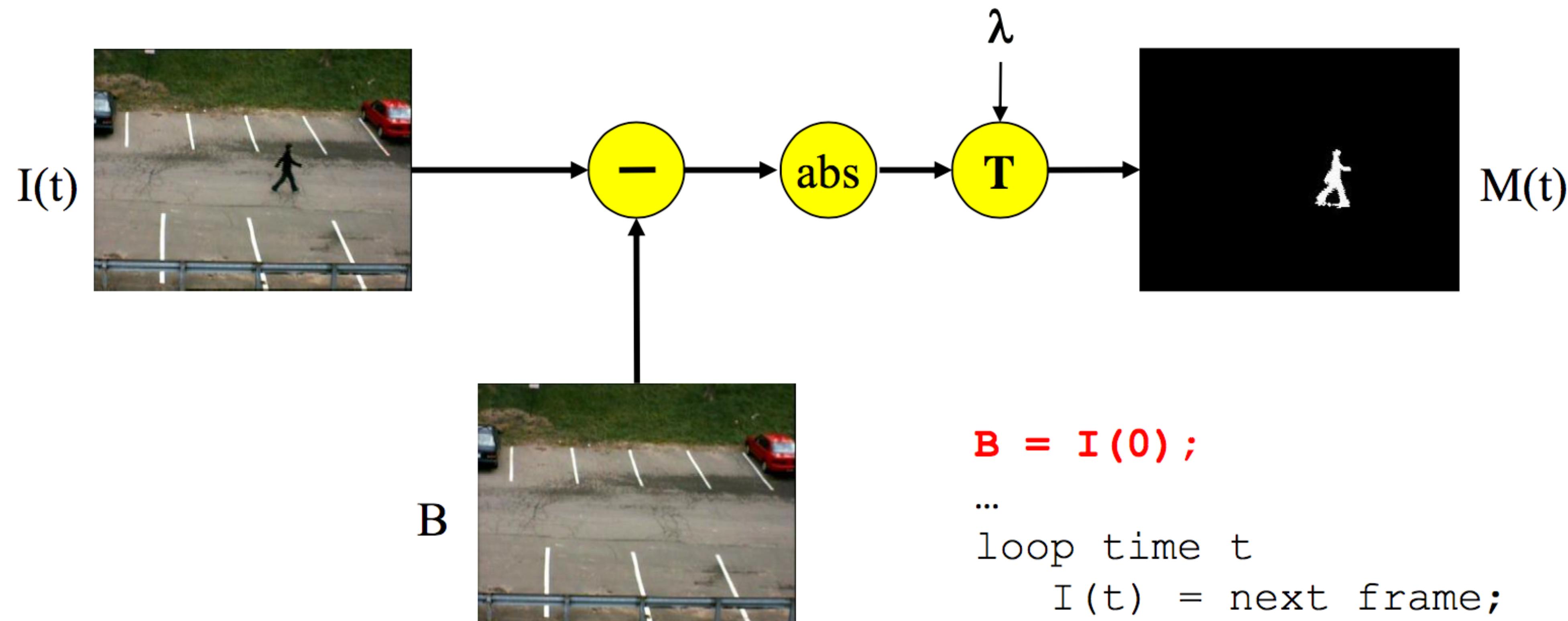
$$|I(x,y) - I_b(x,y)| > \tau ??$$

Simple Background Subtraction



Example from A. Efros

Simple Background Subtraction

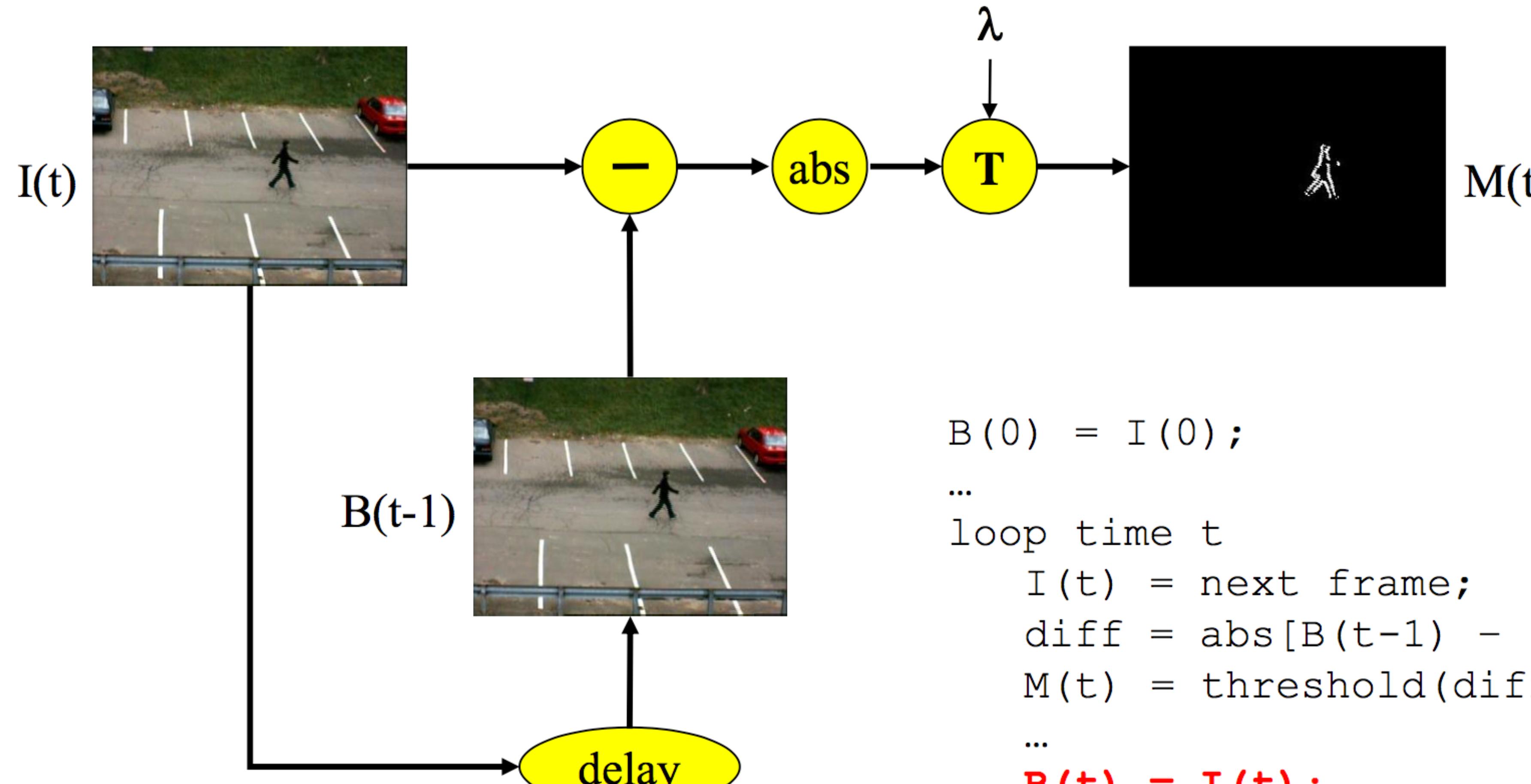


- Background model is a static image (assumed to have no objects present).
- Pixels are labeled as object (1) or not object (0) based on thresholding the absolute intensity difference between current frame and background.

```
B = I(0);  
...  
loop time t  
    I(t) = next frame;  
    diff = abs[B - I(t)];  
    M(t) = threshold(diff, λ);  
    ...  
end
```

Slide adapted from B. Collins

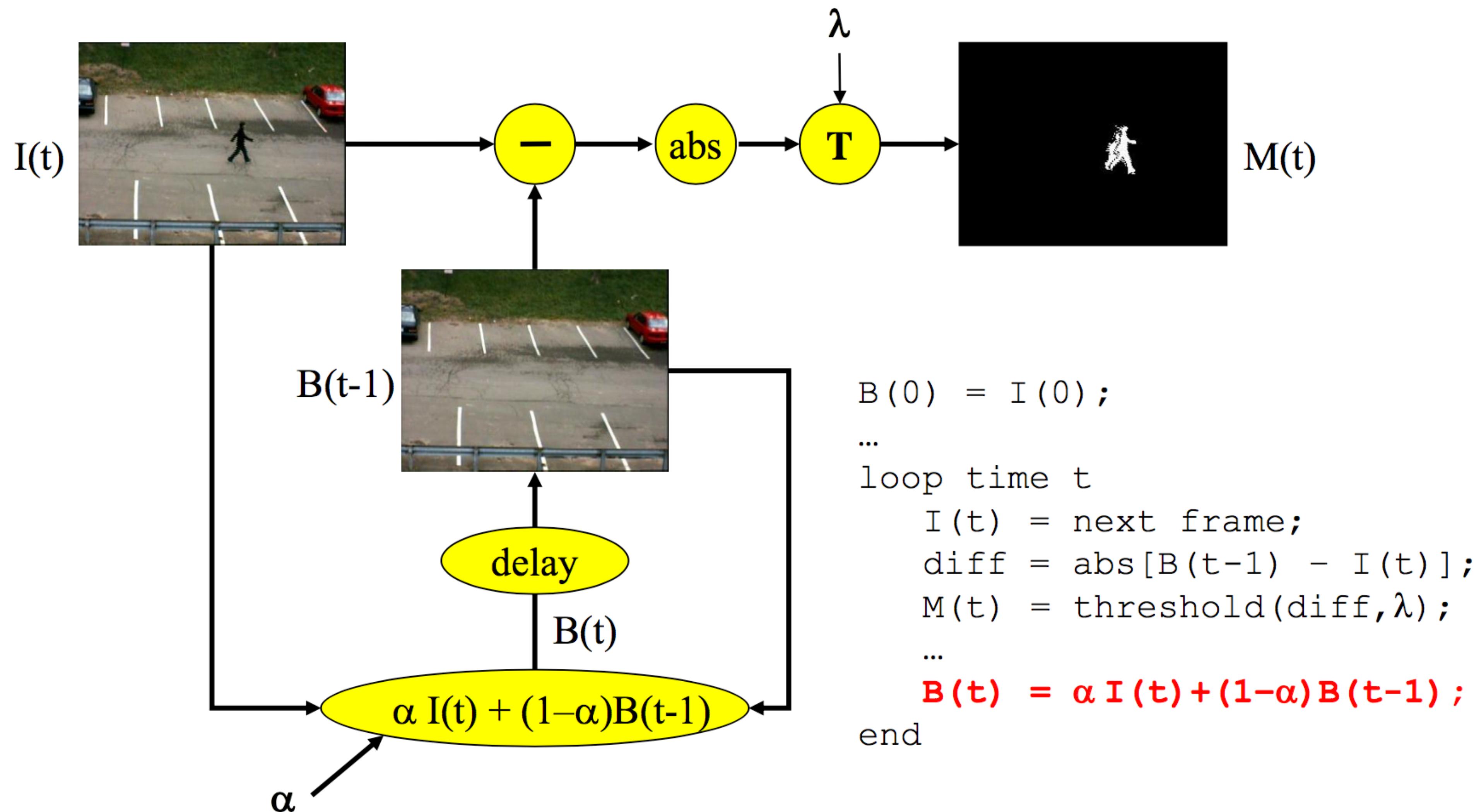
Simple Frame Differencing



- Background model is replaced with the previous image.

Credit: B. Collins

Adaptive Background Subtraction

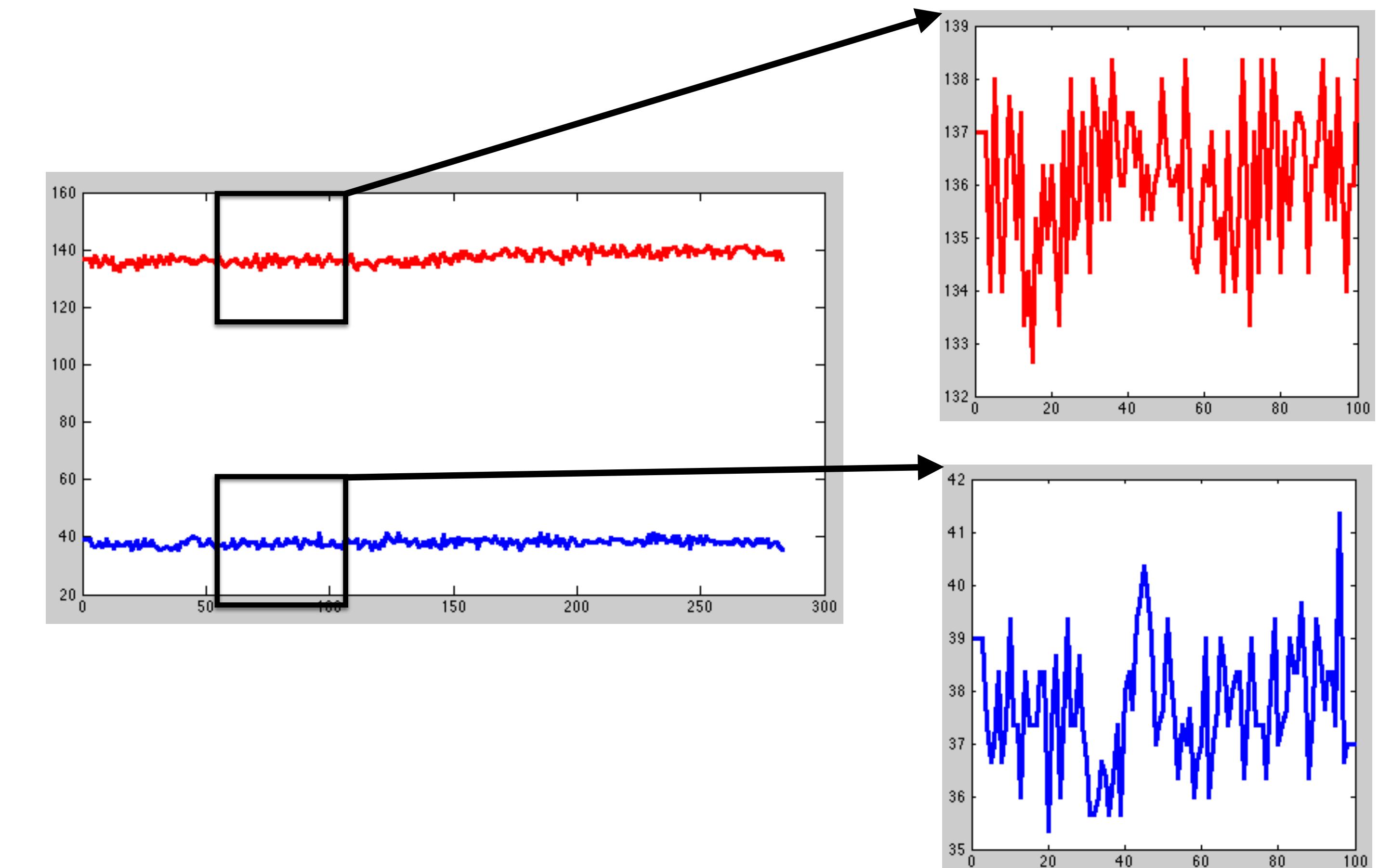
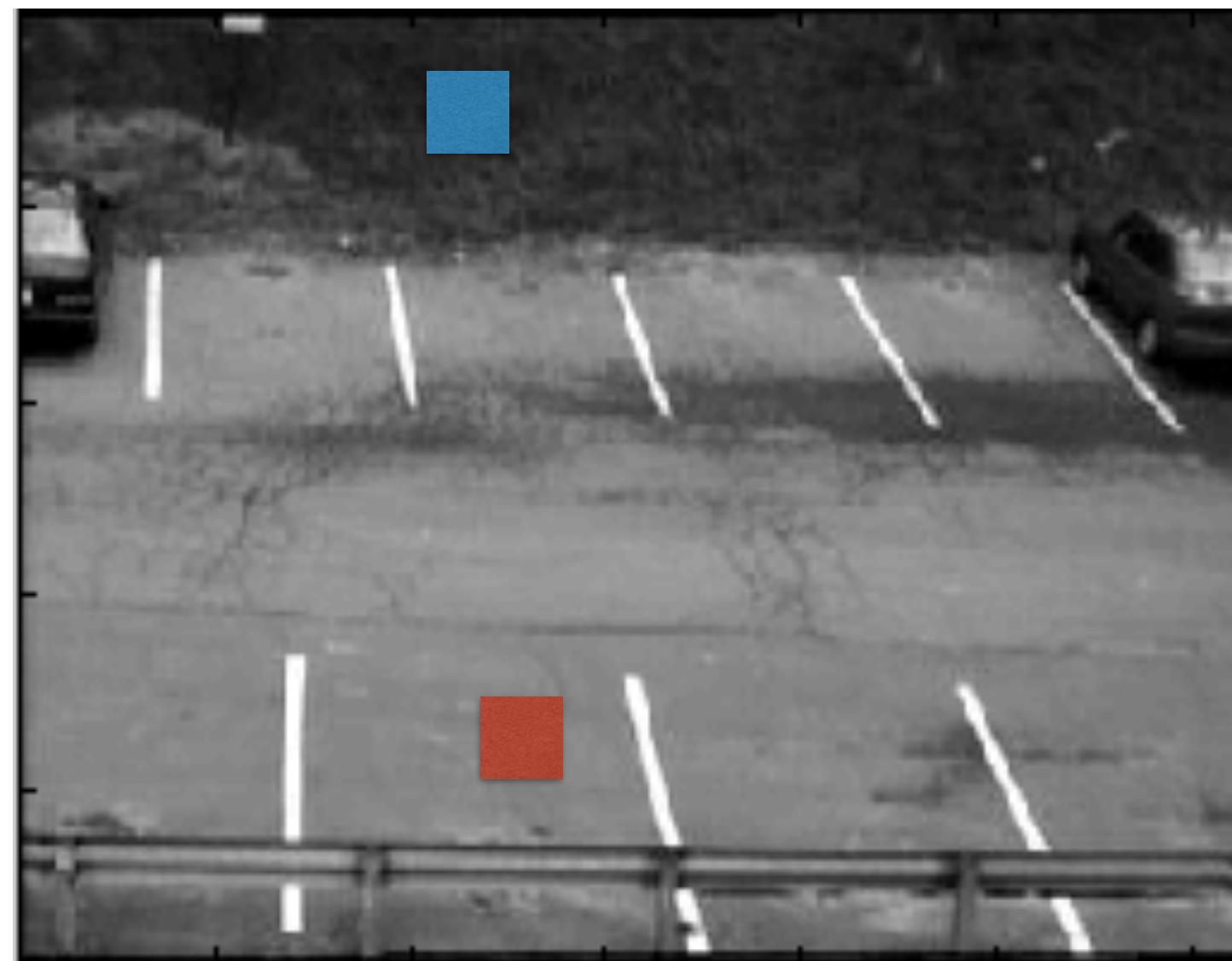


- Current image is “blended” into the background model with parameter a
- $a = 0$ yields simple background subtraction, $a = 1$ yields frame differencing

Credit: B. Collins

Background Models

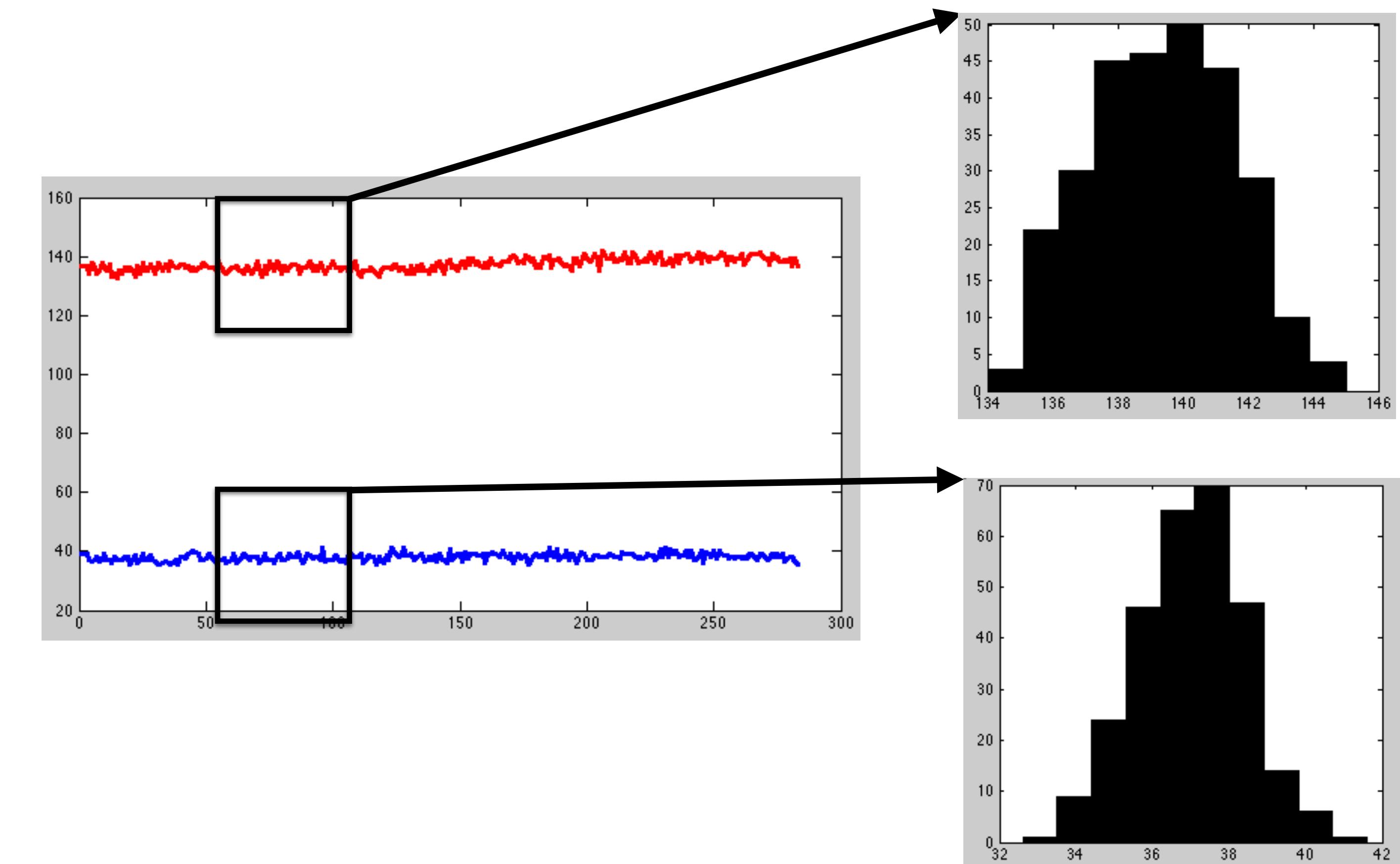
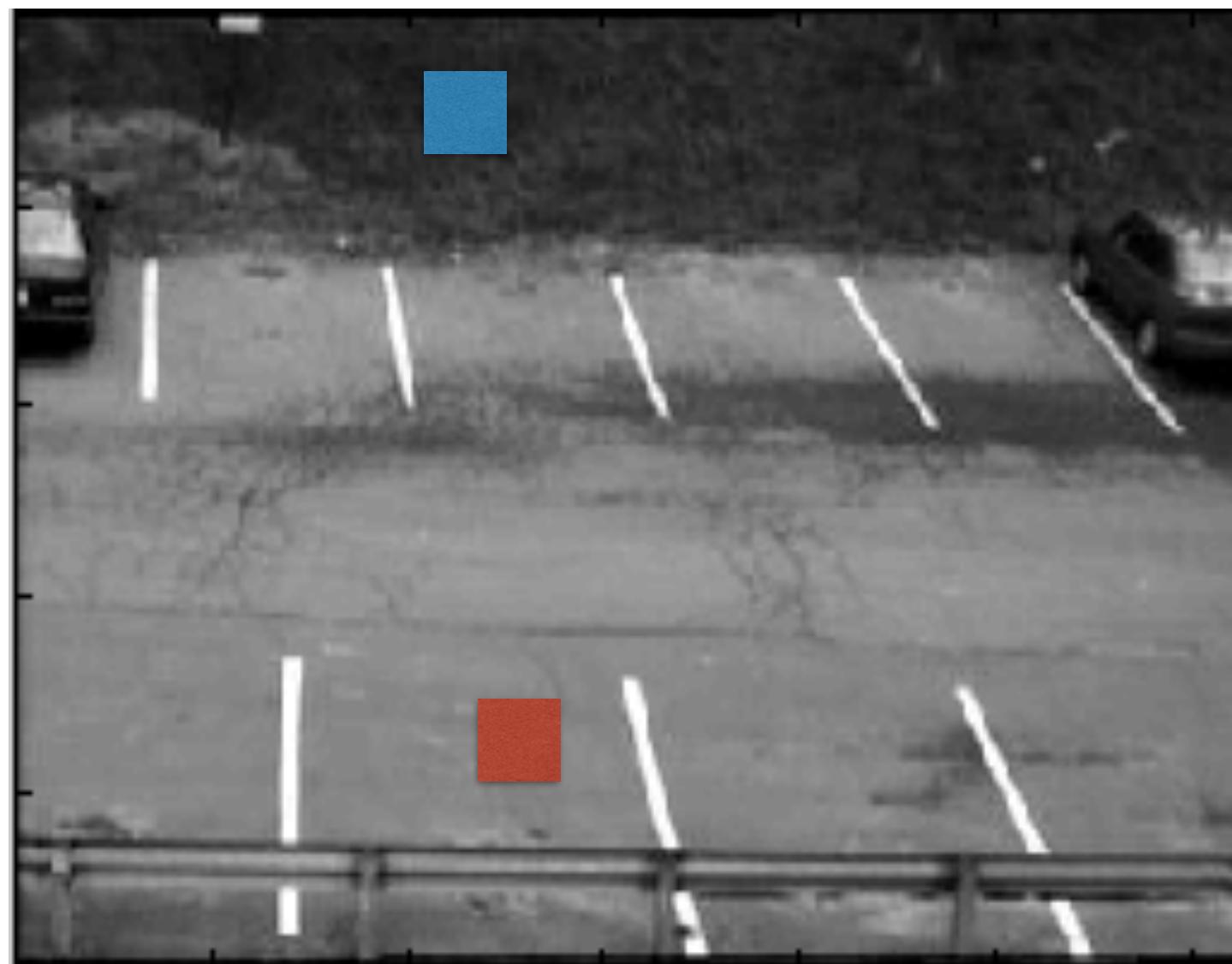
- What is a good statistical model of the value of a pixel in the unchanging background?



Credit: B. Collins

Background Models

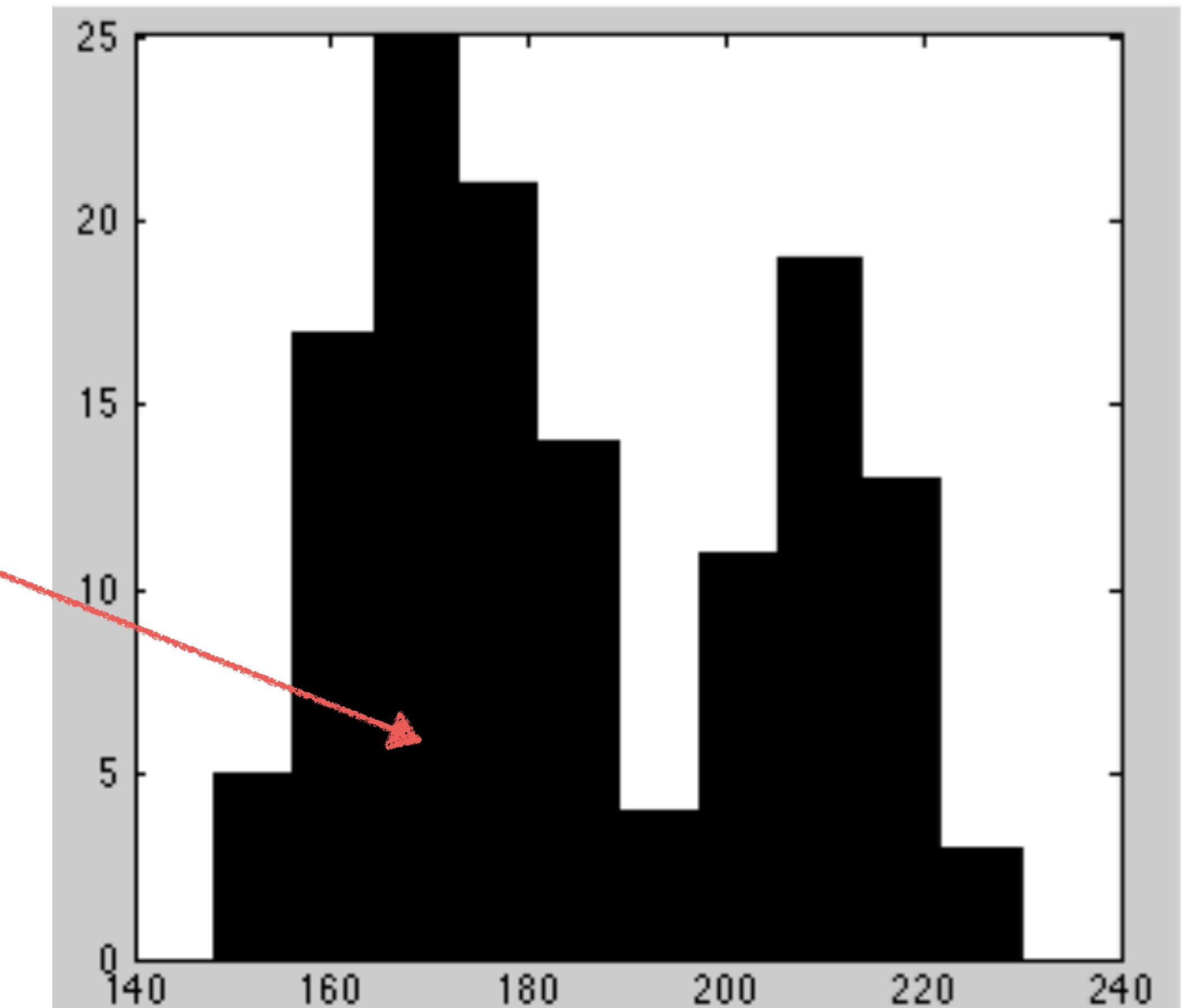
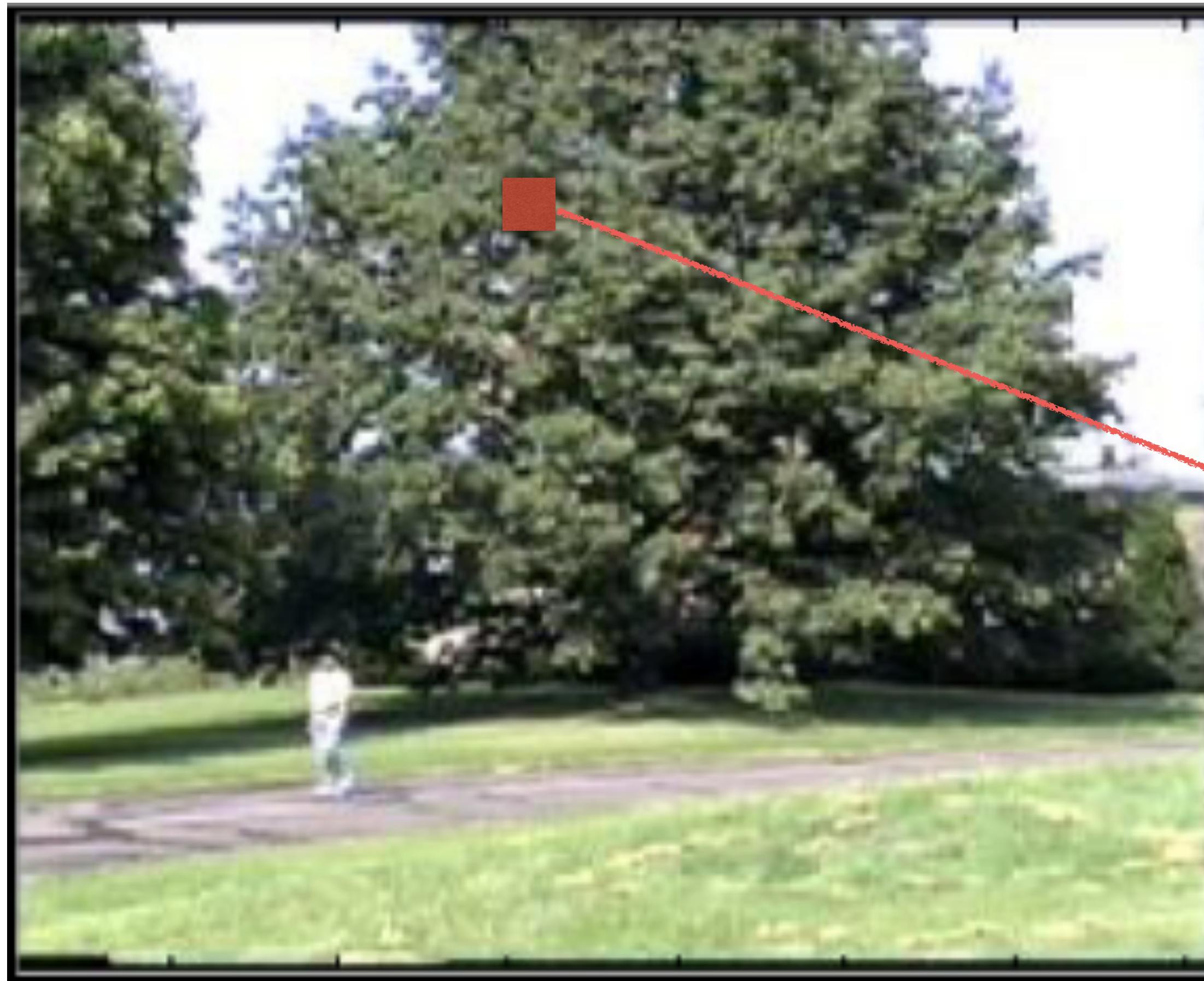
- What is a good statistical model of the value of a pixel in the unchanging background?



Credit: B. Collins

Limitation of Gaussian Assumption

- There is a problem with multimodal pixels
- Examples: trees in the wind; rippling water



Credit: B. Collins

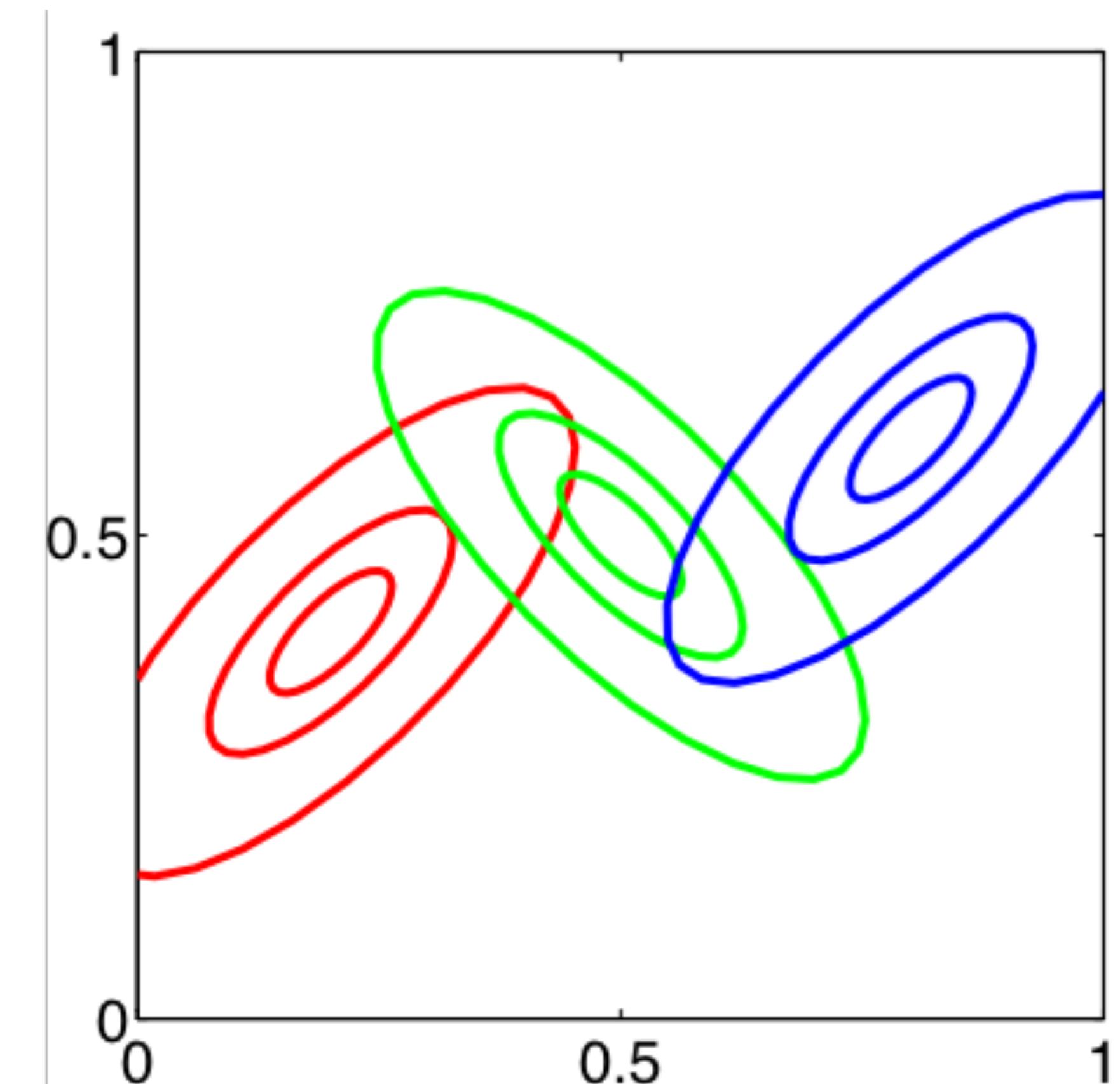
Use a Mixture of Gaussians!

- Linear combination of Gaussians

$$p(\mathbf{x}) = \sum_{k=1}^K \pi_k \mathcal{N}(\mathbf{x} | \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

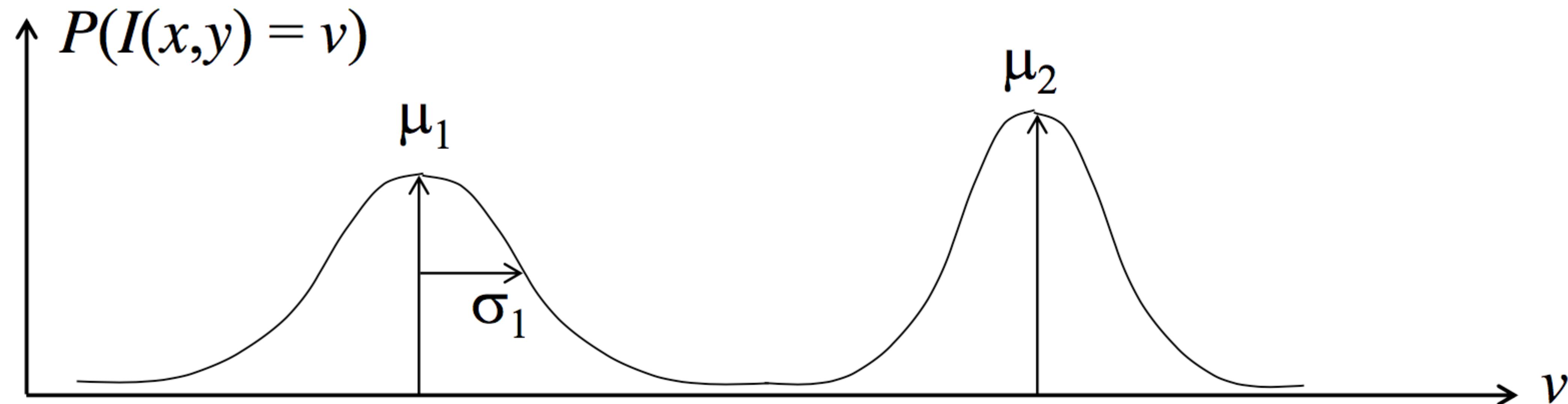
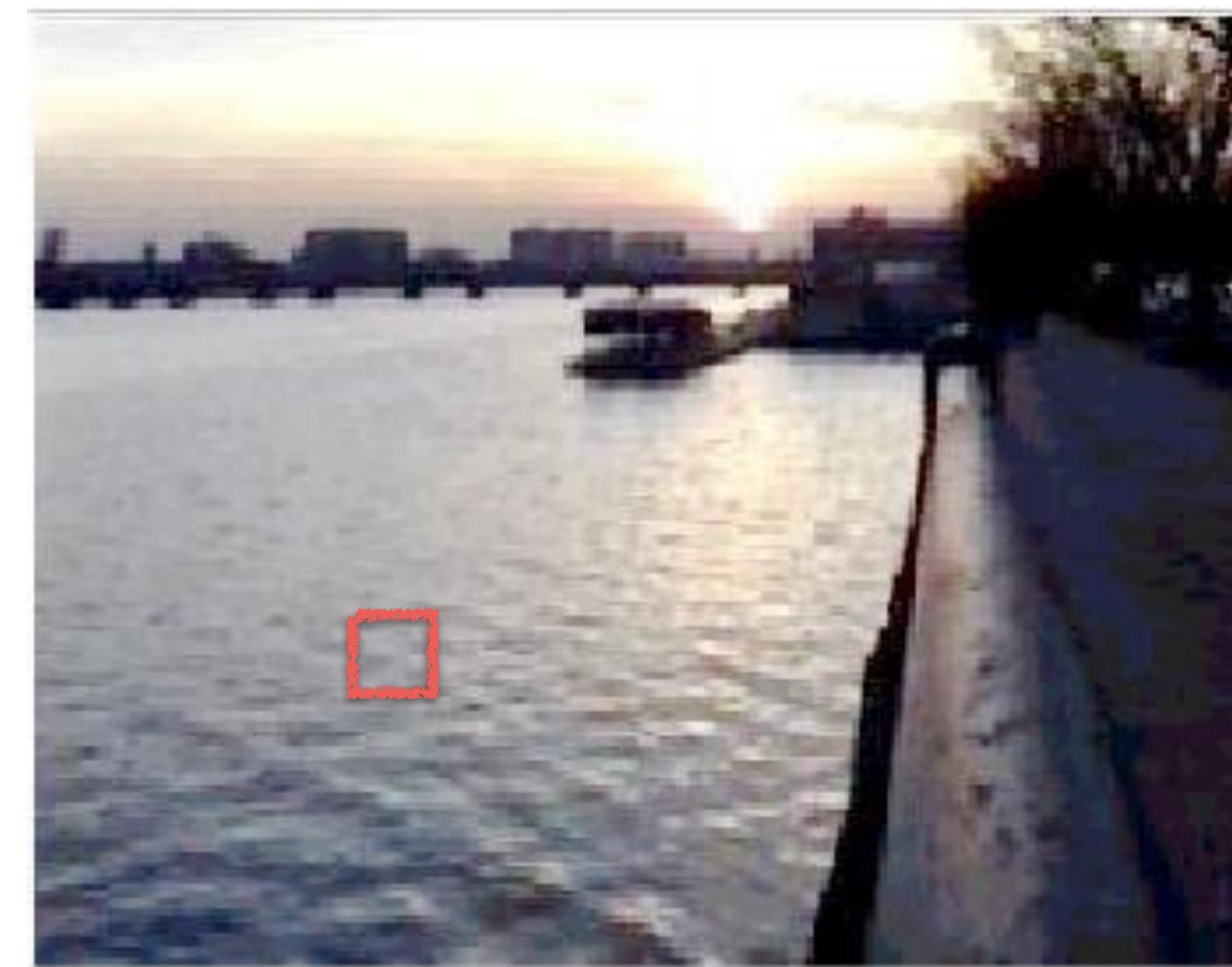
- Normalization and positivity requirements

$$\sum_{k=1}^K \pi_k = 1 \quad 0 \leq \pi_k \leq 1$$



Credit: B. Collins

Use a Mixture of Gaussians!



Persistent Frame Differencing

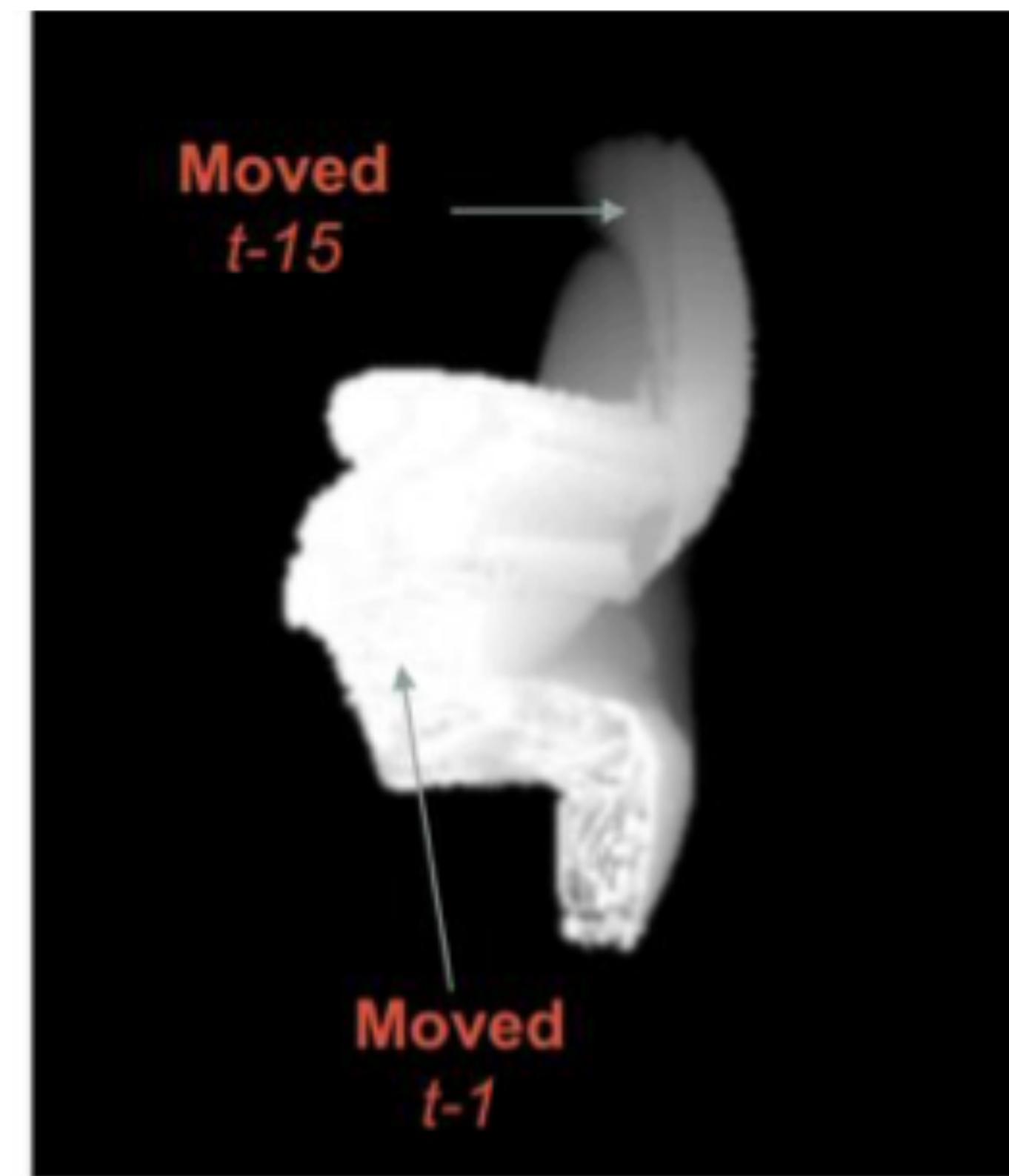
- Motion history images are a different function of temporal volume.
- Pixel operator is replacement decay:

if moving $I_\tau(x,y,t) = \tau$

otherwise

$$I_\tau(x,y,t) = \max(I_\tau(x,y,t-1)-1, 0)$$

- Trivial to construct $I_{\tau-k}(x,y,t)$ from $I_\tau(x,y,t)$ so can process multiple time window lengths without more search.
- MEI is thresholded MHI



Persistent Frame Differencing

