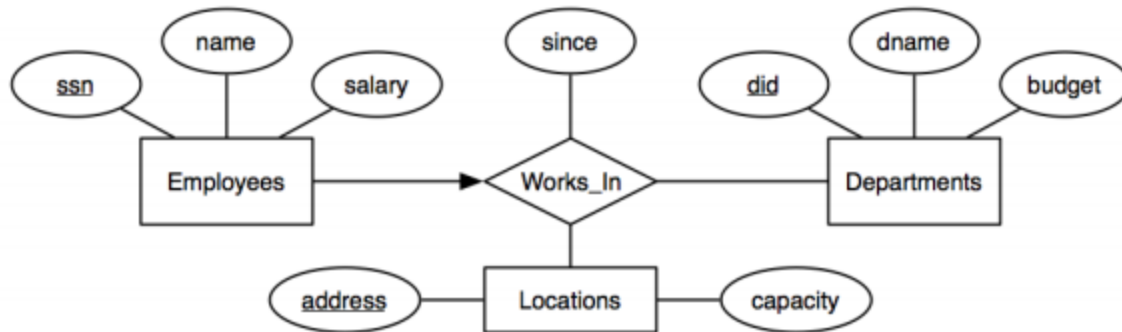


CS186 Week 13 - ER & Functional Dependencies

ER to SQL



```
CREATE TABLE Employees(  
    _____'  
    _____'  
    _____'  
    _____') ;
```

```
CREATE TABLE Departments(  
    _____'  
    _____'  
    _____'  
    _____') ;
```

```
CREATE TABLE Locations(  
    _____'  
    _____'  
    _____') ;
```

```
CREATE TABLE Works_In(  
    _____'  
    _____'  
    _____'  
    _____'  
    _____'  
    _____'  
    _____') ;
```

Functional Dependencies Review

Function Dependency: $X \rightarrow Y$

- Given any two tuples in r , if the X values are the same, then the Y values must also be the same, but not vice versa.
- An FD is a statement about *all* allowable relations and is identified based on *application semantics*. Given some instance $r1$ of R , we can check if $r1$ violates some FD f , but we cannot determine if f holds over R .

FDs vs. Keys

- If " $K \rightarrow$ all attributes of R ", then K is a *superkey* for R (does not require K to be *minimal*.)
- FDs are a generalization of keys.

FD Closure: $F^+ =$ closure of $F =$ set of all FDs that are implied by F , including "trivial dependencies"

Armstrong's Axioms

- Reflexivity: if $X \supseteq Y$, then $X \rightarrow Y$
- Augmentation: if $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z
- Transitivity: if $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

Useful rules (can be derived from AA)

- Union: if $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
- Decomposition: if $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$

Common mistake (!): if $XA \rightarrow YA$, you CAN'T infer $X \rightarrow Y$

Attribute Closure X^+ : what attributes can X determine?

- initialize $X^+ := X$
- Repeat until no change:
 - if $U \rightarrow V$ in F such that U is in X^+ , then add V to X^+
- Example: $R = ABCDE$, $F = \{ B \rightarrow CD, D \rightarrow E, B \rightarrow A, E \rightarrow C, AD \rightarrow B \}$
 - $B \rightarrow B \rightarrow BCD \rightarrow BCDA \rightarrow BCDAE$
 - $B^+ = \{ABCDE\}$, which means B is a key of R !

Boyce-Codd Normal Form

- Definition: Relation R with FDs F is in BCNF if, for all $X \rightarrow A$ in F^+
 - A belongs to X (called a trivial FD), or
 - X is a superkey for R .
- i.e. R is in BCNF if the only non-trivial FDs over R are the key constraints.

Decomposing a schema into BCNF

- What is the motivation of decomposing a schema into BCNF?
- If $X \rightarrow A$ is a FD that violates BCNF, then decompose R into $R - A$ and XA
- Repeat if necessary.
- Example: $R = ABCEG$; $F = \{ AB \rightarrow C, AC \rightarrow B, BC \rightarrow A, E \rightarrow G \}$.

Decompose R into BCNF.

- $AB \rightarrow C \Rightarrow$ Decompose $ABCEG$: $ABEG$, ABC
- $E \rightarrow G \Rightarrow$ Decompose $ABEG$: ABE , EG
- Final relations: ABE , EG , ABC

Decomposition properties

- Lossless-join
- Dependency preserving

FD Problem 1

Consider the **Works_In**(Ssn, Lot, Did, sInce) relation from our previous example. If **S** (ssn) is a key for this relationship, what is the functional dependency we can infer from that? Abbreviate the attribute with the bolded/capitalized letter.

If employees in the same department are given the same parking lot, what additional functional dependency can we infer?

FD Problem 2

*Abbreviate attributes with the bolded/capitalized letter (e.g. F = Flight_no)

Flight schema

Flights(Flight_no, Date, fRom, To, Plane_id), ForeignKey(Plane_id)

Planes(Plane_id, tYpe)

Seat(Seat_no, Plane_id, Legroom), ForeignKey(Plane_id)

1. Find the set of functional dependencies.

2. Expand the FDs found above using Armstrong's axioms (you can omit the trivial and non interesting dependencies).

FD Problem 3

1. Now consider the attribute set $R = ABCDE$ and the FD set $F = \{AB \rightarrow C, A \rightarrow D, D \rightarrow E, AC \rightarrow B\}$. Compute the attribute closure for each of A, AB, B, and D.

- A:
- AB:
- B:
- D:

2. Decompose $R = ABCDEFG$ into BCNF, given the functional dependency set $F = \{AB \rightarrow CD, C \rightarrow EF, G \rightarrow A, G \rightarrow F, CE \rightarrow F\}$.