# 模板

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```

## 差分

```
题目大意:
   第一行n,m
   第二行n个整数
   接下来m行,每行三个正整数1,r,c
   表示对区间[1, r]每个数加c
   输出操作后的数列
输入样例:
6 3
1 2 2 1 2 1
1 3 1
3 5 1
1 6 1
输出样例:
3 4 5 3 4 2
#include <iostream>
using namespace std;
const int N = 100010;
int s[N], a[N];
void insert(int l, int r, int c)
```

```
a[1] += c;
    a[r+1] -= c;
}
int main()
   int n, m;
    cin >> n >> m;
    for (int i=1; i <= n; i++) scanf("%d", &s[i]), insert(i, i, s[i]);
    while (m--)
        int 1, r, c;
       scanf("%d %d %d", &l, &r, &c);
        insert(l, r, c);
    }
    for (int i=1; i <= n; i++) a[i] += a[i-1];
    for(int i=1;i<=n;i++) printf("%d ", a[i]);</pre>
    return 0;
}
/*
题目大意:
   第一行n,m,q
    接下来n行m列矩阵
   接下来q行x1,y1, x2,y2, c
    表示对子矩阵每个数加c,输出操作后的矩阵
输入样例:
3 4 3
1 2 2 1
3 2 2 1
1 1 1 1
1 1 2 2 1
1 3 2 3 2
3 1 3 4 1
输出样例:
2 3 4 1
4 3 4 1
2 2 2 2
*/
#include <iostream>
using namespace std;
const int N = 1010;
int n, m, q;
int a[N][N], b[N][N];
void insert(int x1, int y1, int x2, int y2, int c)
    b[x1][y1] += c;
   b[x2+1][y1] -= c;
```

```
b[x1][y2+1] -= c;
    b[x2+1][y2+1] += c;
}
int main()
    scanf("%d %d %d", &n, &m, &q);
    for (int i = 1; i \le n; i++)
        for (int j = 1; j \le m; j++)
            scanf("%d", &a[i][j]), insert(i, j, i, j, a[i][j]);
    while (q--)
        int x1, x2, y1, y2, c;
        scanf("%d %d %d %d %d", &x1, &y1, &x2, &y2, &c);
        insert(x1, y1, x2, y2, c);
    for(int i=1;i<=n;i++)</pre>
        for (int j=1; j <=m; j++)
            b[i][j] += b[i-1][j] + b[i][j-1] - b[i-1][j-1];
    for(int i=1;i<=n;i++)
        for(int j=1;j<=m;j++) printf("%d ", b[i][j]);
       puts("\b");
    }
    return 0;
```

#### **KMP**

```
#include <iostream>
using namespace std;

const int N = 1e5+10, M = 1e6+10;
int n, m;
char p[N], s[M];
int ne[N];

int main()
{
    cin >> n >> p + 1 >> m >> s + 1;
    for(int i=2, j=0;i<=n;i++)
    {
        while(j&&p[i]!=p[j+1]) j = ne[j];
        if(p[i] == p[j+1]) j ++;
        ne[i] = j;
    }

    for(int i=1, j=0;i<=m;i++)
    {
</pre>
```

```
while(j&&s[i]!=p[j+1]) j = ne[j];
if(s[i]==p[j+1]) j++;
if(j==n)
{
    printf("%d ", i - n);
    j = ne[j];
}
return 0;
}
```

### tire

```
#include <iostream>
using namespace std;
const int N = \frac{1e5+10}{};
int son[N][26], cnt[N], idx;
char str[N];
void insert(char str[])
   int p = 0;
    for(int i=0;str[i];i++)
        int u = str[i] - 'a';
       if(!son[p][u]) son[p][u] = ++ idx;
       p = son[p][u];
   cnt[p] ++;
}
int query(char str[])
    int p = 0;
    for(int i=0;str[i];i++)
        int u = str[i] - 'a';
       if(!son[p][u]) return 0;
       p = son[p][u];
    }
   return cnt[p];
}
int main()
    int n;
   cin >> n;
    while(n--)
```

```
char op[2];
    scanf("%s%s", op, str);
    if(op[0]=='I') insert(str);
    else printf("%d\n", query(str));
}
return 0;
}
```

## hash

```
//拉链法
#include <iostream>
#include <cstring>
using namespace std;
const int N = 1e5+3;
int h[N], e[N], ne[N], idx;
void insert(int x)
   int k = (x % N + N) % N;
   e[idx] = x;
   ne[idx] = h[k];
   h[k] = idx ++;
}
bool find(int x)
{
   int k = (x % N + N) % N;
   for (int i = h[k]; i != -1; i = ne[i])
       if (e[i] == x)
           return true;
   return false;
}
int main()
   int n;
    cin >> n;
    memset(h, -1, sizeof(h));
    while (n--)
        string s;
        cin >> s;
        int x;
        cin >> x;
        if (s[0] == 'I') insert(x);
        else
```

```
if(find(x)) puts("Yes");
            else puts("No");
        }
   return 0;
//开放寻址法
#include <iostream>
#include <cstring>
using namespace std;
const int N = 2e5+3, null = 0x3f3f3f3f3f;
int h[N];
int find(int x)
{
   int k = (x % N + N) % N;
   while (h[k] != null && h[k] != x)
       k ++;
       if (k == N) k = 0;
   return k;
}
int main()
{
   int n;
   cin >> n;
    memset(h, 0x3f, sizeof(h));
    while (n--)
        string s;
        cin >> s;
        int x;
        cin >> x;
        int k = find(x);
        if(s[0] == 'I') h[k] = x;
        else
        {
           if (h[k] != null) puts("Yes");
           else puts("No");
        }
   return 0;
}
//字符串哈希
#include <iostream>
using namespace std;
typedef unsigned long long ll;
```

```
const int N = 1e5+10, P = 131;
int n, m;
char str[N];
ll h[N], p[N];
11 get(int l, int r)
   return h[r] - h[l-1] * p[r-l+1];
int main()
{
    cin >> n >> m >> str + 1;
   p[0] = 1;
    for (int i = 1; i \le n; i++)
       p[i] = p[i - 1] * P;
       h[i] = h[i - 1] * P + str[i];
    while (m--)
        int 11, r1, 12, r2;
        cin >> 11 >> r1 >> 12 >> r2;
        if(get(l1, r1) == get(l2, r2)) puts("Yes");
       else puts("No");
    }
   return 0;
```

## 最短路

```
//dijkstra
//O(n^2)
//n = 500, m = 1e5, 适合稠密图,无负权边
#include <iostream>
#include <cstring>
#include <algorithm>
using namespace std;
const int N = 510;
int n, m, g[N][N], dist[N];
bool st[N];

int dijkstra()
{
    memset(dist, 0x3f, sizeof(dist));
    dist[1] = 0;
    for (int i = 0; i < n; i++)
    {
```

```
int t = -1;
        for (int j = 1; j \le n; j ++)
            if(!st[j] \&\& (t == -1 || dist[t] > dist[j]))
                t = j;
        //if(t == n) break;
        st[t] = true;
        for (int j = 1; j \le n; j + +)
            dist[j] = min(dist[j], dist[t]+g[t][j]);
    if(dist[n] == 0x3f3f3f3f) return -1;
    return dist[n];
}
int main()
{
   scanf("%d %d", &n, &m);
    memset(g, 0x3f, sizeof(g));
    while (m--)
        int a, b, c;
        scanf("%d %d %d", &a, &b, &c);
        g[a][b] = min(g[a][b], c);
    int t = dijkstra();
    printf("%d\n", t);
   return 0;
//dijkstra
//O(mlogn)
//n, m = 1e5, 适合稀疏图
#include <iostream>
#include <cstring>
#include <algorithm>
#include <queue>
using namespace std;
const int N = 1e5+10;
int n, m, h[N], e[N], ne[N], dist[N], w[N], idx;
bool st[N];
typedef pair<int, int> PII;
void add(int a, int b, int c)
{
    e[idx] = b;
   ne[idx] = h[a];
   w[idx] = c;
   h[a] = idx ++;
}
int dijkstra()
{
   memset(dist, 0x3f, sizeof(dist));
    dist[1] = 0;
    priority queue<PII, vector<PII>, greater<PII>> heap;
    heap.push(\{0, 1\});
    while(heap.size())
```

```
auto t = heap.top();
        heap.pop();
        int ver = t.second, distance = t.first;
        if(st[ver]) continue;
        for (int i=h[ver];i!=-1;i=ne[i])
        {
            int j = e[i];
            if(dist[j] > distance + w[i])
                dist[j] = distance + w[i];
               heap.push({dist[j], j});
        st[ver] = true;
    if(dist[n] == 0x3f3f3f3f) return -1;
    return dist[n];
int main()
   scanf("%d %d", &n, &m);
    memset(h, -1, sizeof(h));
    while (m--)
        int a, b, c;
        scanf("%d %d %d", &a, &b, &c);
        add(a, b, c);
    }
    int t = dijkstra();
    printf("%d\n", t);
    return 0;
//bellman ford
//O(nm)
//可以处理负权边
#include <iostream>
#include <cstring>
#include <algorithm>
using namespace std;
const int N = 510, M = 10010;
int n, m, k;
int dist[N], backup[N];
struct Edge
   int a, b, w;
}edges[N];
int bellman ford()
   memset(dist, 0x3f, sizeof(dist));
    dist[1] = 0;
    for (int i = 0; i < k; i++)
        memcpy(backup, dist, sizeof(dist));
        for (int j = 0; j < m; j++)
```

```
int a = edges[j].a, b = edges[j].b, w = edges[j].w;
            dist[b] = min(dist[b], backup[a] + w);
        }
    if (dist[n] > 0x3f3f3f3f / 2) return -1;
    return dist[n];
int main()
    scanf("%d %d %d", &n, &m, &k);
    for (int i = 0; i < m; i++)
    {
        int a, b, w;
        scanf("%d %d %d", &a, &b, &w);
        edges[i] = \{a, b, w\};
    int t = bellman ford();
    if (t == -1) puts("impossible");
    else printf("%d\n", t);
   return 0;
//spfa
//O(m)最坏O(nm)
#include <iostream>
#include <cstring>
#include <algorithm>
#include <queue>
using namespace std;
const int N = 1e5+10;
int n, m, h[N], e[N], ne[N], dist[N], w[N], idx;
bool st[N];
typedef pair<int, int> PII;
void add(int a, int b, int c)
{
   e[idx] = b;
   ne[idx] = h[a];
   w[idx] = c;
   h[a] = idx ++;
}
int spfa()
    memset(dist, 0x3f, sizeof(dist));
   dist[1] = 0;
   queue<int> q;
    q.push(1);
    st[1] = true;
    while (q.size())
        int t = q.front();
        q.pop();
```

```
st[t] = false;
        for (int i = h[t]; i != -1; i = ne[i])
            int j = e[i];
            if (dist[j] > dist[t] + w[i])
            {
                dist[j] = dist[t] + w[i];
                if (!st[j])
                    q.push(j);
                   st[j] = true;
               }
            }
       }
    if (dist[n] == 0x3f3f3f3f) return -1;
   return dist[n];
}
int main()
{
   scanf("%d %d", &n, &m);
   memset(h, -1, sizeof(h));
    while (m--)
    {
       int a, b, c;
       scanf("%d %d %d", &a, &b, &c);
       add(a, b, c);
    }
    int t = spfa();
    if (t == -1) puts("impossible");
   else printf("%d\n", t);
   return 0;
}
//spfa判负环
//O(m)最坏O(nm)
#include <iostream>
#include <cstring>
#include <algorithm>
#include <queue>
using namespace std;
const int N = 1e5+10;
int n, m, h[N], e[N], ne[N], dist[N], w[N], idx;
int cnt[N];
bool st[N];
typedef pair<int, int> PII;
void add(int a, int b, int c)
   e[idx] = b;
   ne[idx] = h[a];
   w[idx] = c;
   h[a] = idx ++;
```

```
bool spfa()
{
    queue<int> q;
    for(int i=1;i<=n;i++)
        st[i] = true;
       q.push(i);
    }
    st[1] = true;
    while (q.size())
        int t = q.front();
        q.pop();
        st[t] = false;
        for (int i = h[t]; i != -1; i = ne[i])
            int j = e[i];
            if (dist[j] > dist[t] + w[i])
                dist[j] = dist[t] + w[i];
                cnt[j] = cnt[t] + 1;
                if(cnt[j]>=n) return true;
                if (!st[j])
                {
                   q.push(j);
                   st[j] = true;
           }
       }
    }
    return false;
}
int main()
{
    scanf("%d %d", &n, &m);
    memset(h, -1, sizeof(h));
    while (m--)
    {
        int a, b, c;
        scanf("%d %d %d", &a, &b, &c);
        add(a, b, c);
    if(spfa()) puts("Yes");
    else puts("No");
   return 0;
}
//floyd
//o(n^3)
```

```
#include <iostream>
 using namespace std;
 const int N = 210, INF = 1e9;
 int n, m, Q;
 int d[N][N];
 void floyd()
     for (int k=1; k \le n; k++)
         for(int i=1;i<=n;i++)
             for(int j=1;j<=n;j++)
                 d[i][j] = min(d[i][j], d[i][k]+d[k][j]);
 }
 int main()
     scanf("%d %d %d", &n, &m, &Q);
     for(int i=1; i<=n; i++)
         for(int j=1; j<=n; j++)
             if(i == j) d[i][j] = 0;
             else d[i][j] = INF;
     while (m--)
     {
         int a, b, w;
         scanf("%d %d %d", &a, &b, &w);
        d[a][b] = min(d[a][b], w);
     }
     floyd();
     while (Q--)
     {
         int a, b;
         scanf("%d %d", &a, &b);
         if(d[a][b] > INF / 2) puts("impossible");
         else printf("%d\n", d[a][b]);
     }
     return 0;
    return 0;
 }
 //prim
 //0(n^2)
 #define inf 0x3f3f3f3f
 #include <iostream>
 #include <cstring>
 #include <algorithm>
 using namespace std;
 const int N = 510;
 int n, m;
```

```
int g[N][N];
int dist[N];
bool st[N];
int prim()
{
    memset(dist, 0x3f, sizeof(dist));
    int res = 0;
    dist[1] = 0;
    for (int i = 0; i < n; i++)
        int t = -1;
        for (int j=1; j \le n; j++)
            if(!st[j] \&\& (t == -1 || dist[t] > dist[j]))
                t = j;
        if(dist[t] == inf) return inf;
        res += dist[t];
        for (int j=1; j \le n; j++) dist[j] = min(dist[j], g[t][j]);
        st[t] = true;
    }
    return res;
}
int main()
{
    scanf("%d %d", &n, &m);
    memset(g, 0x3f, sizeof(g));
    while (m--)
        int a, b, c;
        scanf("%d %d %d", &a, &b, &c);
        g[a][b] = g[b][a] = min(g[a][b], c);
    }
    int t = prim();
    if(t == inf) puts("impossible");
    else cout << t << endl;</pre>
   return 0;
}
//kruskal
//O(mlogm)
#include <iostream>
#include <algorithm>
using namespace std;
const int N = 2e5+10;
int n, m;
int p[N];
int cnt, res;
struct Edge
{
  int a, b, w;
```

```
bool operator< (const Edge &W) const
       return w < W.w;
    }
}edges[N];
int find(int x)
   if (p[x] != x) p[x] = find(p[x]);
   return p[x];
}
int main()
{
    scanf("%d %d", &n, &m);
   for (int i = 0; i < m; i++)
        int a, b, c;
        scanf("%d %d %d", &a, &b, &c);
        edges[i] = \{a, b, c\};
    }
    sort(edges, edges+m);
    for (int i=1; i <= n; i++) p[i] = i;
    for (int i = 0; i < m; i++)
        int a = edges[i].a, b = edges[i].b, w = edges[i].w;
        a = find(a), b = find(b);
        if(a != b)
        {
            p[a] = b;
            res += w;
            cnt ++;
    if(cnt < n-1)puts("impossible");</pre>
    else cout << res << endl;</pre>
    return 0;
}
```

## 二分图

```
//O(n+m)
#include <iostream>
#include <cstring>
#include <algorithm>
using namespace std;
const int N = 1e5+10, M = 2e5+10;
int n, m;
int h[N], e[M], ne[M], idx;
int color[N];
```

```
void add(int a, int b)
   e[idx] = b, ne[idx] = h[a], h[a] = idx++;
bool dfs(int u, int c)
    color[u] = c;
    for(int i=h[u];~i;i=ne[i])
        int j = e[i];
        if(!color[j])
           if(!dfs(j, 3-c)) return false;
        else if(color[j] == c) return false;
   return true;
}
int main()
    scanf("%d %d", &n, &m);
    memset(h, -1, sizeof(h));
    while (m--)
        int a, b;
       scanf("%d %d", &a, &b);
        add(a, b), add(b, a);
    bool flag = true;
    for(int i=1;i<=n;i++)
    {
        if(!color[i])
        {
            if(!dfs(i, 1))
                flag = false;
               break;
           }
       }
    if(flag) puts("Yes");
    else puts("No");
    return 0;
}
//匈牙利算法
//O(mn)
#include <iostream>
#include <cstring>
using namespace std;
const int N = 510, M = 1e5 + 10;
```

```
int n1, n2, m;
 int h[N], e[M], ne[M], idx;
 int match[N];
 bool st[N];
 void add(int a, int b)
    e[idx] = b, ne[idx] = h[a], h[a] = idx ++;
 bool find(int x)
     for(int i=h[x];~i;i=ne[i])
         int j = e[i];
         if(!st[j])
         {
             st[j] = true;
             if(match[j] == 0 || find(match[j]))
                 match[j] = x;
                 return true;
             }
     }
    return false;
 }
 int main()
     scanf("%d %d %d", &n1, &n2, &m);
     memset(h, -1, sizeof(h));
     while (m--)
        int a, b;
        scanf("%d %d", &a, &b);
        add(a, b);
     }
     int res = 0;
     for(int i=1;i<=n1;i++)
        memset(st, false, sizeof st);
        if(find(i)) res ++;
     cout << res << endl;</pre>
    return 0;
 }
```

## manacher

```
//acwing 3188
#include <iostream>
#include <cstring>
using namespace std;
const int N = 3e7+10;
char str[N], tmp[N/2];
int ne[N];
int main()
   scanf("%s", tmp);
    str[0] = '\$', str[1] = '#';
    int length1 = 2;
    for (int i=0; tmp[i]; i++)
        str[length1++] = tmp[i];
        str[length1++] = '#';
    str[length1++] = '^';
    int mr = 0, ml = 0;
    for(int i=1;str[i]!='^';i++)
        if(i < mr) ne[i] = min(ne[2*ml-i], mr - i);
        else ne[i] = 1;
        while(str[i+ne[i]]==str[i-ne[i]]) ne[i] ++;
        if(ne[i]+i > mr)
           mr = ne[i] + i;
           ml = i;
    }
    int res = 0;
    for(int i=1;i<=length1;i++)</pre>
       res = max(res, ne[i]);
    printf("%d", res-1);
   return 0;
}
```

## 数学

#### 质数筛

```
//线性筛
#include <iostream>
using namespace std;
const int N=1000010;
int cnt,primes[N];
```

```
bool st[N];
void get prime(int n)
    for(int i=2;i<=n;i++)
         if(!st[i])
             primes[cnt++]=i;
         for (int j=0; primes [j] \le n/i; j++)
             st[primes[j]*i]=true;
            if(i% primes[j]==0) break;
         }
   }
}
int main()
    int n;
    cin>>n;
    get_prime(n);
    cout << cnt << endl;</pre>
    return 0;
```

### 约数个数

```
$$N = p_1^{\alpha _1}p_2^{\alpha _2}\cdots p_k^{\alpha _k}$$ N的约数个数 $$(\alpha _1+1) (\alpha _2+2)\cdots(\alpha _k+1) $$
```

#### 约数之和

```
 $$N = p_1^{\alpha_1}p_2^{\alpha_2}\cdot p_k^{\alpha_k} $$ (p_1^0+p_1^1+\cdot p_1^1+cdots+p_1^{\alpha_1})\cdot (p_k^0+p_k^1+\cdot p_k^{\alpha_k}) $$
```

#### 欧拉函数

```
#include <iostream>
using namespace std;
#define ll long long

const int mod=le9+7;
int main()
{
   int t;
```

```
cin>>t;
    while(t--)
        int n;
        cin>>n;
        int res=n;
        for (int i=2; i <= n/i; i++)
            if(n\%i==0)
                res=res/i*(i-1);
                while (n\%i==0) n/=i;
        }
        if (n>1) res=res/n* (n-1);
        cout<<res<<endl;</pre>
    return 0;
//欧拉函数定义:对于整数n,在1~n-1中与n互质的数的个数
#include <iostream>
using namespace std;
#define 11 long long
const int N=1000010;
int cnt,primes[N];
int phi[N];
bool st[N];
11 get eulers(int n)
    phi[1]=1;
    for(int i=2;i<=n;i++)
        if(!st[i])
        {
            primes[cnt++]=i;
            phi[i]=i-1;//质数p的欧拉函数为p-1
        for (int j=0; primes [j] \le n/i; j++)
            st[primes[j]*i]=true;
            if(i% primes[j] == 0)
                phi[i*primes[j]]=primes[j]*phi[i];
                break;
            phi[i*primes[j]]=phi[i]*(primes[j]-1);
    11 \text{ res}=0;
```

```
for(int i=1;i<=n;i++) res+=phi[i];
    return res;
}

int main()
{
    int n;
    cin>>n;

    cout<<get_eulers(n)<<endl;
    return 0;
}</pre>
```

## 快速幂

```
#include <iostream>
using namespace std;
#define ll long long
ll quick_pow(ll a,ll k,ll p)
{
    ll res=1%p;
    while(k)
        if(k&1) res=res*a%p;
       k >> = 1;
        a=a*a%p;
    return res;
}
int main()
{
   int t;
    cin>>t;
    while(t--)
       ll a,b,c;
        cin>>a>>b>>c;
       cout<<quick_pow(a,b,c)<<endl;</pre>
    return 0;
```

### 高斯消元

```
#include <cmath>
#include <iostream>
#include <algorithm>
using namespace std;
const int N = 110;
const double eps = 1e-6;
int n;
double a[N][N];
int gauss()
{
   int c, r;
    for (c=0, r=0; c< n; c++)
    {
        int t = r;
        for (int i=r; i<n; i++)
            if(fabs(a[i][c]) > fabs(a[t][c]))
                t = i; //找到绝对值最大的一列
        if(fabs(a[t][c]) < eps) continue;//是零就下一列
        for(int i=c;i<=n;i++) swap(a[t][i], a[r][i]);//交换绝对值最大的行与当前
行
        for(int i=n;i>=c;i--) a[r][i] /= a[r][c];//当前行第一个数变成1
        for(int i=r+1; i<n; i++)
            if(fabs(a[i][c]) > eps)
                for(int j=n; j>=c; j--)
                    a[i][j] -= a[r][j] * a[i][c];//把c下面每个数变成0,就是减去
当前行的a[i][c]倍
       r++;
    if(r < n)
        for(int i=r;i<n;i++)</pre>
           if(fabs(a[i][n]) > eps)
               return <mark>2;</mark>//无解
       return 1; //无穷多解
    for (int i=n-1; i>=0; i--)
       for(int j=i+1; j<n; j++)
            a[i][n] -= a[i][j] * a[j][n];//算出答案
    return 0;//唯一解
}
int main()
    cin >> n;
    for (int i = 0; i < n; i++)
       for (int j = 0; j < n+1; j++)
           cin >> a[i][j];
    int t = gauss();
    if(t == 0) for (int i=0; i < n; i++)
```

```
double ans = a[i][n];
   if (fabs(ans) < eps) ans = 0;
   printf("%.2f\n", ans);
else if(t == 1) puts("Infinite group solutions");
else puts("No solution");
return 0;
```

## st表,树状数组与线段树

### st表

```
#include <iostream>
#include <cmath>
\#define lowbit(x) (x & -x)
using namespace std;
const int N = 1e5+10;
int f[N][25], g[N][25];
int lg[N];
int n, q;
int main()
{
                lg[1] = 0, lg[2] = 1;
                for (int i=3; i<N; i++) if (lowbit(i) == i) lg[i] = lg[i-1] + 1; else lg[i]
= \lg[i-1];
                cin >> n >> q;
                 for(int i=1;i<=n;i++)
                  {
                                 int x;
                                scanf("%d", &x);
                                 f[i][0] = g[i][0] = x;
                 int ed = 25;
                 for(int j=1;j<=ed;j++)
                                 for (int i=1; i+(1<<j)-1 <= n; i++)
                                                 f[i][j] = \max(f[i][j-1], f[i+(1<<(j-1))][j-1]);
                                                 g[i][j] = min(g[i][j-1], g[i+(1<<(j-1))][j-1]);
                                 }
                while (q--)
                                 int a, b;
                                 scanf("%d %d", &a, &b);
                                 int s = \lg[b-a+1];
                                 printf("%d\n", max(f[a][s], f[b-(1<<s)+1][s]) - min(g[a][s], g[b-(1<<s)+1][s]) - min(g[a][s], g[a][s], g[a][s]) - min(g[a][s], g[a][s], g[a][s]) - min(g[a][s], g[a][s], g[a][s]) - min(g[a][s], g[a][s], g[a][s], g[a][s]) - min(g[a][s][s], g[a][s], g[a][s], g[a][s]) - min(g[a][s][s], g[a][s], g[a][s
 (1 << s) + 1] [s]));
```

```
return 0;
}
```

#### 树状数组

```
#include <iostream>
#include <cstring>
\#define lowbit(x) (x & -x)
using namespace std;
const int N = 1e5+10;
int tr[N];
int n;
void add(int x, int c)
   for(int i=x;i<=n;i+=lowbit(i)) tr[i] += c;</pre>
char str[20];
int sum(int x)
   int res = 0;
   for(int i=x;i;i-=lowbit(i)) res += tr[i];
   return res;
}
int main()
   int t, cnt = 0;
   cin >> t;
    while (t--)
    {
        cnt ++;
        printf("Case %d:\n", cnt);
        memset(tr, 0, sizeof(tr));
        scanf("%d", &n);
        for(int i=1;i<=n;i++)
        {
            int x;
            scanf("%d", &x);
           add(i, x);
        }
        while (1)
            scanf("%s", str);
            char op = str[0];
            if(op == 'E') break;
            int i, j;
            scanf("%d %d", &i, &j);
            if(op == 'A') add(i, j);
            else if(op == 'S') add(i, -j);
            else printf("%d\n", sum(j)-sum(i-1));
```

```
return 0;
}
```

### 线段树

```
#include <iostream>
using namespace std;
const int N = 2e5+10;
int m, p;
struct Node
   int l, r;
   int v;
}tr[N*4];
void pushup(int u)
   tr[u].v = max(tr[u << 1].v, tr[u << 1|1].v);
}
void build(int u, int l, int r)
{
   tr[u] = \{1, r\};
    if(l == r) return;
    int mid = l + r \gg 1;
   build(u << 1, 1, mid), build(u << 1 | 1, mid+1, r);
int query(int u, int l, int r)
    if(tr[u].l >= l \&\& tr[u].r <= r) return tr[u].v;
    int mid = tr[u].l + tr[u].r >> 1;
    int v = 0;
    if (1 \le mid) v = query(u \le 1, 1, r);
    if (r > mid) v = max(v, query(u << 1 | 1, 1, r));
   return v;
void modify(int u, int x, int v)
    if(tr[u].l == x \&\& tr[u].r == x) tr[u].v = v;
    else
    {
        int mid = tr[u].l + tr[u].r >> 1;
        if (x \le mid) modify(u \le 1, x, v);
        else modify(u << 1 | 1, x, v);
        pushup(u);
   }
```

```
int main()
{
    int n = 0, last = 0;
    scanf("%d %d", &m, &p);
    build(1, 1, m);
    int x;
    char op[2];
    while (m--)
        scanf("%s %d", op, &x);
        if(*op == 'Q')
        {
            last = query(1, n-x+1, n);
           printf("%d\n", last);
        else
           modify(1, n+1, (last+x)%p);
           n ++;
        }
   return 0;
}
//AcWing 243
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <iostream>
#define int long long
using namespace std;
const int N = \frac{1e5+10}{};
int n, m;
int w[N];
struct Node
   int 1, r;
   int sum, add;
}tr[N * 4];
void pushdown(int u)
    auto &root = tr[u], &left = tr[u << 1], &right = tr[u << 1 | 1];
   if(root.add)
        left.add += root.add, left.sum += (left.r - left.l + 1) * root.add;
        right.add += root.add, right.sum += (right.r - right.l + 1) *
root.add;
       root.add = 0;
   }
void pushup(int u)
```

```
tr[u].sum = tr[u << 1].sum + tr[u << 1 | 1].sum;
void build(int u, int l, int r)
    if (1 == r) tr[u] = \{1, r, w[r], 0\};
    else
         tr[u] = \{1, r\};
         int mid = 1 + r \gg 1;
         build(u << 1, l, mid), build(u << 1 | 1, mid + 1, r);
         pushup(u);
    }
void modify(int u, int l, int r, int d)
    if(tr[u].l >= l && tr[u].r <= r)
     {
         tr[u].sum += (tr[u].r - tr[u].l + 1) * d;
        tr[u].add += d;
     else
        pushdown(u);
         int mid = tr[u].l + tr[u].r >> 1;
         if (1 \le mid) modify (u \le 1, 1, r, d);
         if (r > mid) modify (u << 1 | 1, 1, r, d);
         pushup(u);
     }
int query(int u, int l, int r)
    if(tr[u].l >= l \&\& tr[u].r <= r) return tr[u].sum;
    pushdown(u);
    int mid = tr[u].l + tr[u].r >> 1;
     int sum = 0;
     if (1 \le mid) sum = query(u << 1, 1, r);
     if (r > mid) sum += query(u << 1 | 1, 1, r);
    return sum;
 }
signed main()
 {
     scanf("%lld %lld", &n, &m);
    for(int i=1;i<=n;i++) scanf("%lld", &w[i]);</pre>
     build(1, 1, n);
     char op[2];
     int 1, r, d;
     while (m--)
         scanf("%s %lld %lld", op, &l, &r);
         if(*op == 'C')
         {
            scanf("%lld", &d);
            modify(1, l, r, d);
```

```
else printf("%lld\n", query(1, 1, r));
}
return 0;
}
```