Overview of Deep Learning

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September 9, 2024

- What is Deep Learning?
- Brief History of Neural Networks
- Perceptron
- Multilayer Perceptrons

Recap: What is AI?

- Artificial Intelligence (AI) is a broad field that focuses on creating systems capable of performing tasks that typically require human intelligence.
- To pass the (total) Turing Test, it needs:
 - Natural language processing (NLP) to enable it to communicate effectively;
 - Knowledge representation to store and retrieve information;
 - Automated reasoning to use the stored information to answer questions and to draw new conclusions;
 - Machine learning to recognize patterns from data and adapt to new situations;
 - Computer vision (CV) to perceive objects;
 - Robotics to manipulate and interact with the physical world.

Recap: What is ML?

• Machine learning (ML) is a subset of AI that focuses on developing algorithms and (statistical) models to learn from (training) data and generalize to unseen data.

Perceptron

- Commonly used algorithms and models are categorized into:
 - Supervised learning: linear/logistic regression, supper vector machines (SVM), decision trees, and neural networks
 - Unsupervised learning: k-means clustering, dimensionality reduction, Gaussian mixture models, generative models
 - Reinforcement learning: Q-Learning, policy gradient, deep Q-networks (DQN)

What is DL?

- Deep learning (DL) is a subset of ML that focuses on using deep neural networks (DNN) with many layers to learn representation in large datasets.
 - It is capable of automatically learning features from raw data, unlike other machine learning models that rely on manually crafted features.

Perceptron

- It learns the intricate structures from data by using backpropogation to update the parameters in DNN
- It encompasses various neural network architectures, including convolutional neural Networks (CNNs). recurrent neural networks (RNNs), transformers, and graph neural networks (GNNs), each tailored to specific tasks.
- It has led to significant breakthroughs in various applications, such as CV, NLP, speech recognition, and biomedical science.

- What is Deep Learning?
- Brief History of Neural Networks

Perceptron

Multilayer Perceptrons

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Early Beginnings and "Al Winters"

1940s: Early Beginnings

- In 1943, Warren McCulloch and Walter Pitts introduced the first mathematical model of a neuron, the McCulloch-Pitts Neuron Model.
- In 1949, Donald Hebb proposed Hebbian learning in his book The Organization of Behavior, summarized as "cells that fire together wire together."

1950s-1960s: Perceptron and the First "Al Winter"

- In 1958, Frank Rosenblatt proposed the perceptron, an early neural network model.
- In 1969, Marvin Minsky and Seymour Papert demonstrated that the perceptron could not solve non-linear problems, such as the XOR problem, leading to the first "AI winter."

1980s-1990s: Revival with Expert Systems and Backpropagation

- In 1980, XCON became one of the first commercially successful expert systems, marking a turning point for AI in the industry.
- In 1986, Geoffrey Hinton, David Rumelhart, and Ronald Williams popularized backpropagation in their Nature paper, "Learning Representations by Back-Propagating Errors."

1990s-2000s: The Second "Al Winter"

- The second "Al winter" occurred mainly due to the failure of **expert systems** to scale and generalize beyond narrow, rule-based tasks.
- Neural networks, despite the promise shown after the introduction of backpropagation, were still
 constrained by limited computational power, scalability issues, and insufficient data.

Emergence of Deep Learning

1990s-2000s: Advancements and the Emergence of Deep Learning

- In 1989, Yann LeCun et al. created the LetNet as an early example of a CNN, which became critical for image processing tasks.
- In 1997, the Long Short-Term Memory (LSTM) network was proposed by Sepp Hochreiter and Jürgen Schmidhuber that overcome the problem of vanishing gradients in RNNs

hat is Deep Learning?

Brief History of Neural Networks

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Multilayer Perceptron

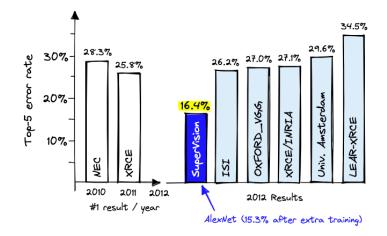
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Modern Era: AlexNet 2012

2010s-Present: Deep Learning Revolution

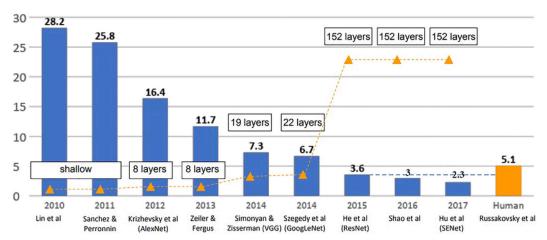
• In 2012, AlexNet trained using GPUs dominated the ImageNet competition



Modern Era: ResNet 2015

2010s-Present: Deep Learning Revolution

• In 2015, the introduction of skip connection in **ResNet** allowed the training of extremely ResNet, e.g., 152 layers, achieving **better-than-human** performance on ImageNet



Modern Era: AlphaGo 2016-2017

2010s-Present: Deep Learning Revolution

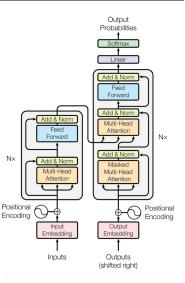
- In 2016, AlphaGo gained worldwide attention by defeating South Korean professional Go player Lee Sedol, one of the best players in the world, showing that AI can master complex and strategic games.
- In 2017, AlphaGo further cemented its dominance by defeating the world's number one Go player, Ke Jie of China, in a best-of-three match, winning all three games.





Modern Era: The Transformer and Attention 2017-2022

2010s-Present: Deep Learning Revolution



- In 2017, the Transformer architecture and attention mechanism were introduced, revolutionizing NLP with superior performance in sequence-based tasks.
- In 2018, BERT and GPT emerged as foundational pre-trained models in NLP, significantly improving performance across a wide range of downstream tasks.
- In 2020, OpenAI developed GPT-3 as the largest language model at time with 175 billion parameters, trained on 499 billion tokens (approximately 570 GB of text) using around 10,000 GPUs over several months.
- In 2022, ChatGPT was released by OpenAI, based on the GPT-3.5 model. It quickly gained widespread attention for its ability to generate human-like text.

Modern Era: Generative Al 2021-Present

2010s-Present: Deep Learning Revolution

- In 2021, Diffusion models like Denoising Diffusion Probabilistic Models (DDPM)
 became prominent for generating high-quality images, challenging the dominance of GANs.
- In 2022, Stability AI released Stable
 Diffusion, allowing users to generate images from text prompts based on diffusion models.
- In 2024, OpenAI introduced Sora, a text-to-video model based on diffusion models that can generate about 1 minute of high-quality video from text prompts.



Applications of Deep Learning

- Computer Vision
- Natural Language Processing (NLP)
- Speech Recognition and Generation
- Biomedical Science and Healthcare
- Self-Driving Vehicles
- Recommendation Systems
- Finance and Fraud Detection
- Medical Imaging and Diagnostics
- Robotics and Automation
- Music Technology and Audio Processing
- Climate Science and Environmental Monitoring
- Biological Sciences and Bioinformatics

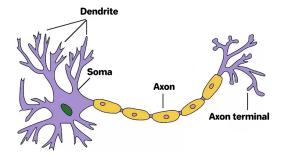
- Agricultural Technology
- Meteorology and Weather Prediction
- Cloud Computing and Data Centers
- Smart Manufacturing and Industry 4.0
- Logistics and Supply Chain Optimization
- Food Security and Sustainable Agriculture
- Cybersecurity and Threat Detection
- Software Engineering and DevOps
- Materials Science and Engineering
- Mechanical Engineering and System Design
- Digital Media, Filmmaking, and Animation
- User Interface and User Experience (UI/UX)
 Development

What is Deep Learning?

- Perceptron

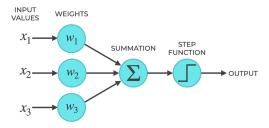
Multilayer Perceptrons

Biological Neuron



- Dendrite: Receives signals from other neurons
- Soma: Processes the information
- Axon: Transmits signals away from Soma
- Axon terminal: Send signals to other neurons

Perceptron



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- Each input x_i is multiplied by its corresponding weight w_i
- The weighted inputs are summed together (along with the bias b).
- The sum is passed through a step function to produce the estimated output.

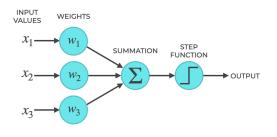
Mathematical Form of Perceptron:

$$\hat{y} = \phi \left(\sum_{i=1}^{n} w_i x_i + b \right)$$

• x_i are the input, w_i are the weights, b is the bias, \hat{y} is the prediction, ϕ is the step function:

$$\phi(z) = \begin{cases} 1, & \text{if } z \ge 0 \\ 0, & \text{if } z < 0 \end{cases}$$

Perceptron Example



Consider

• Inputs: $x_1, x_2 \in \{0, 1\}$ are binary values

• Weights: $w_1 = 1$, $w_2 = 1$

• Bias: h = -1.5

The perceptron output is computed as:

$$\hat{y} = \phi(w_1 x_1 + w_2 x_2 + b) = \phi(1 \cdot x_1 + 1 \cdot x_2 - 1.5)$$

• Input:
$$x_1 = 0, x_2 = 0$$
; Output: $z = 1 \cdot 0 + 1 \cdot 0 - 1.5 = -1.5$ \Rightarrow $\hat{y} = \phi(z) = 0$.

• Input:
$$x_1 = 0, x_2 = 1$$
; Output: $z = 1 \cdot 0 + 1 \cdot 1 - 1.5 = -0.5 \quad \Rightarrow \quad \hat{y} = \phi(z) = 0.$

• Input:
$$x_1 = 1, x_2 = 0$$
; Output: $z = 1 \cdot 1 + 1 \cdot 0 - 1.5 = -0.5$ \Rightarrow $\hat{y} = \phi(z) = 0.$

• Input:
$$x_1 = 1, x_2 = 1$$
; Output: $z = 1 \cdot 1 + 1 \cdot 1 - 1.5 = 0.5$ \Rightarrow $\hat{y} = \phi(z) = 1$.

Conclusion

The perceptron correctly implements the **AND** operator.

$$\hat{y} = \phi \left(\sum_{i=1}^{n} x_i w_i + b \right)$$

• Define vectors x, $w \in \mathbb{R}^n$:

$$m{x} = egin{bmatrix} x_1 \ x_2 \ dots \ x_n \end{bmatrix}, \quad m{w} = egin{bmatrix} w_1 \ w_2 \ dots \ w_n \end{bmatrix}$$

• The perceptron can be defined in vector form:

$$\hat{y} = \phi(\boldsymbol{w}^{\top} \boldsymbol{x} + b),$$

where the inner or dot product of w and x is given by

$$oldsymbol{w}^{ op}oldsymbol{x} = \sum_{i=1}^n w_i x_i$$

Using Perceptrons to Implement Logical Operators

Logical operators such as AND (\land), OR (\lor), and NOT (\neg):

- \bullet \land : the result is true if both x_1 and x_2 are
- ullet \vee : the result is true if either x_1 and x_2 is
- ¬: the result is true if the input is not

x_1	x_2	$x_1 \wedge x_2$	$x_1 \vee x_2$	$\neg x_1$
0	0	0	0	1
0	1	0	1	1
1	0	0	1	0
1	1	1	1	0

Table: Boolean table illustrating \land , \lor , and \neg operations with x_1 and x_2

Perceptron can be used to implement them:

$$\hat{y} = \phi(\boldsymbol{w}^{\top}\boldsymbol{x} + b) = \phi(w_1x_1 + w_2x_2 + b)$$

- \wedge : w = [1, 1] and b = -1.5
- \vee : $\mathbf{w} = [1, 1]$ and b 0.5
- \bullet \neg : w=-1 and b=0.5

Limitations of Perceptron

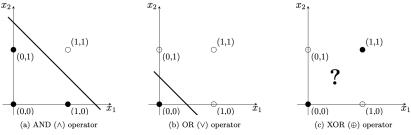
The perceptron cannot solve **nonlinear** problems such as the logical operator XOR (\oplus) :

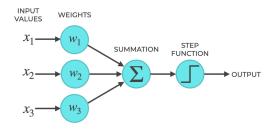
ullet \oplus : the result is true if x_1 and x_2 are different

x_1	x_2	$x_1 \wedge x_2$	$x_1 \vee x_2$	$\neg x_1$	$x_1 \oplus x_2$
0	0	0	0	1	0
0	1	0	1	1	1 1
1	0	0	1	0	1 1
1	1	1	1	0	0

Table: Boolean table illustrating \land , \lor , and \oplus operations with x_1 and x_2

The perceptron can only solve **linearly** separable data:





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The perceptron is defined as:

$$\hat{y} = \phi(\boldsymbol{w}^{\top} \boldsymbol{x} + b),$$

- Mathematical Model: It computes the weighted sum of the inputs along with the bias term
- Activation: The perceptron (or neuron) is activated by the step (activation) function if the weighted sum exceeds a certain threshold.
- Linear Separability: The perceptron can classify linearly separable data, e.g., \wedge , \vee , and \neg .
- **Limitation**: It cannot solve **nonlinear** problems, *e.g.*, \oplus .



- What is Deep Learning?
- 2 Brief History of Neural Networks

Perceptron

Multilayer Perceptrons

Why Multilayer Perceptrons (MLP)?

Recap: A single perceptron can implement AND, OR, and NOT, but **not** XOR **However**, XOR can be implemented by **multiple** percetrons.

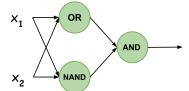
• NAND ↑: the result is false if both inputs are true

x_1	x_2	$x_1 \wedge x_2$	$x_1 \uparrow x_2$
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0

- \bullet A single perceptron can implement NAND with $\boldsymbol{w}=[-1,-1]\text{,}$ and b=1.5
- We can express XOR in terms of AND, OR, and NAND as follows

$$x_1 \oplus x_2 = (x_1 \vee x_2) \wedge (x_1 \uparrow x_2).$$

This forms a **2-layer network**:



MLP for XOR

The XOR function can be computed using MLP as follows:

• Define logical operators using single perceptrons:

$$h_i(\boldsymbol{x}) = \phi(\boldsymbol{w}_i^{\top} \boldsymbol{x} + b_i), \quad \forall i \in \{1, 2, 3\},$$

where the weight and biases are:

OR:
$$\mathbf{w}_1 = [1, 1], b_1 = -0.5$$

NAND:
$$w_2 = [-1, -1], b_2 = 1.5$$

AND:
$$w_3 = [1, 1], b_3 = -1.5$$

ullet Define the **activation vector** $a\in\mathbb{R}^2$ as the intermediate results from the first layer:

$$oldsymbol{a} = egin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

where $a_1 = h_1(\boldsymbol{x})$ from the OR output and $a_2 = h_2(\boldsymbol{x})$ from the NAND output.

ullet Compute the estimated output \hat{y} using the activation vector $oldsymbol{a}$ from the first layer:

$$\hat{y} = h_3(\boldsymbol{a}) = \phi(\boldsymbol{w}_3^{\top} \boldsymbol{a} + b_3)$$

where h_3 represents the AND operation on the outputs of OR and NAND.

Structure of MLP

For each hidden layer in a multi-layer perceptron:

- ullet The input vector $x\in\mathbb{R}^d$ is obtained from the previous layer (or from the input data for the first layer).
- We define n perceptrons, each with independent **weights** $w_i \in \mathbb{R}^d$ and a **bias** $b_i \in \mathbb{R}$ for $i \in [n] := \{1, 2, \dots, n\}$:

$$h_i(\boldsymbol{x}) = \phi(\boldsymbol{w}_i^{\top} \boldsymbol{x} + b_i)$$

where ϕ is the activation function.

• The computed outputs $h_i(x)$ are stacked into an activation vector $a \in \mathbb{R}^n$, representing the output of this layer:

$$\boldsymbol{a} = \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{bmatrix}$$

where $a_i = h_i(\boldsymbol{x})$ for each i.

To rewrite the MLP in matrix-vector form for each layer ℓ :

• Define the weight matrix $W \in \mathbb{R}^{n \times d}$ and the bias vector $b \in \mathbb{R}^n$:

$$oldsymbol{W} = egin{bmatrix} oldsymbol{w}_1^{\intercal} \ dots \ oldsymbol{w}_n^{\intercal} \end{bmatrix}, \quad oldsymbol{b} = egin{bmatrix} b_1 \ dots \ b_n \end{bmatrix}$$

where each $w_i \in \mathbb{R}^d$ and b_i represents the weights and bias for the *i*-th perceptron.

ullet Define the **pre-activation vector** $oldsymbol{z} \in \mathbb{R}^n$ as:

$$oldsymbol{z} = oldsymbol{W} oldsymbol{x} + oldsymbol{b} = egin{bmatrix} oldsymbol{w}_1^{ op} oldsymbol{x} + b_1 \ oldsymbol{z} \ oldsymbol{w}_n^{ op} oldsymbol{x} + b_n \end{bmatrix}$$

This combines the weighted sum of the inputs from the previous layer.

• Apply the activation function ϕ element-wise to z to obtain the activation vector $a \in \mathbb{R}^n$:

$$oldsymbol{a} = \phi(oldsymbol{z}) = egin{bmatrix} \phi(oldsymbol{w}_1^{ op} oldsymbol{x} + b_1) \ dots \ \phi(oldsymbol{w}_n^{ op} oldsymbol{x} + b_n) \end{bmatrix}$$

where ϕ is applied to each element of the pre-activation vector ${m z}.$

Summary of MLP

An MLP with L layers can be defined in a recurrent manner: for each layer $\ell \in [L]$,

$$egin{aligned} oldsymbol{z}^\ell &= oldsymbol{W}^\ell oldsymbol{x}^{\ell-1} + oldsymbol{b}^\ell, \ oldsymbol{x}^\ell &= \phi(oldsymbol{z}^\ell), \end{aligned}$$

where $m{x}^\ell = m{a}^\ell$ serves as the input to the next layer, and the initial input is $m{x}^0 = m{x}$.

- The MLP is also called a feed-forward network because the data flows from the input layer to the output layer through hidden layers without any feedback loops.
- **②** Each hidden layer consists of n_{ℓ} perceptrons (or neurons), where n_{ℓ} is referred to as the **width** of the network at layer ℓ .
- lacktriangle The total number of layers L defines the **depth** of the network.
- **①** The final estimated output $\hat{y} = x^L$ can have **multiple dimensions**, depending on the task (e.g., classification or regression).
- The width and depth are hyperparameters chosen by the network designer.
- **o** An MLP is capable of solving **nonlinear problems** that a single perceptron cannot handle.

Question

How do we effectively select the weights $oldsymbol{W}^\ell$ and biases $oldsymbol{b}^\ell$?