**Supplemental Material**

**Supplemental Methods**

Simulation studies:

**Supplemental Figures**

For example, Fig. S1A displays the *complete collapsing* theme with window size equaling the length of the region, Fig. S1B displays a collapsing theme with windows of size 2 and Fig. S1C with windows of size 1 which degenerates to using the original haplotypes.