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Resolutions of the ground ring

ResolutionAbelianGroup (G, n) Inputs a list $L := [m_1, m_2, ..., m_d]$ of nonnegative ResolutionAbelianGroup(L,n) ResolutionAlmostCrystalGroup (G, n) Inputs a positive integer n and an almost crystallographic pcp group G. It ret ResolutionAlmostCrystalQuotient(G,n,c) ResolutionAlmostCrystalQuotient(G,n,c,false) An almost ResolutionArtinGroup (D, n) Inputs a Coxeter diagram D and an integer n > 1. It returns n terms of a free ZG-resolutionArtinGroup (D, n) ResolutionAsphericalPresentation (F, R, n) Inputs a free group F, a set R of words in F which constitute an asph ResolutionBieberbachGroup(G) ResolutionBieberbachGroup (G, v) Inputs a Bieberbach group G (represented using AffineCrystGroupOnRight ResolutionDirectProduct (R, S, "internal") Inputs a ZG-resolution R and ResolutionDirectProduct(R,S) ResolutionExtension(g,R, S, "TestFiniteness") ResolutionExtension ResolutionExtension(q,R,S) ResolutionFiniteDirectProduct (R,S) ResolutionFiniteDirectProduct(R,S, "internal") Inputs a ZG ResolutionFiniteExtension(gensE,gensG,R,n) ResolutionFiniteExtension(gensE, gensG, R, n, true) ResolutionFiniteGroup(gens,n) ResolutionFiniteGroup(gens,n,true) ResolutionFiniteGroup(gens ResolutionFiniteSubgroup (R, gensG, gensK) Inputs a ZG-resolution for a ResolutionFiniteSubgroup(R,K) ResolutionGraphOfGroups(D,n) ResolutionGraphOfGroups (D, n, L) Inputs a graph of groups D and a position ResolutionNilpotentGroup(G,n) ResolutionNilpotentGroup(G, n, "TestFiniteness") Inputs a nilpotent ResolutionNormalSeries(L,n) ResolutionNormalSeries(L,n,true) ResolutionNormalSeries(L,n,fa ResolutionPrimePowerGroup (G, n, p) Inputs a p-group P and integer n > 0ResolutionPrimePowerGroup(P,n) ResolutionSmallFpGroup(G,n) ResolutionSmallFpGroup (G, n, p) Inputs a small finitely presented group GResolutionSubgroup (R, K) Inputs a ZG-resolution for an (infinite) group G and a subgroup K of finite index |G:K|. ResolutionSubnormalSeries (L, n) Inputs a positive integer n and a list $L = [L_1, \dots, L_k]$ of subgroups L_i of a finite TwistedTensorProduct (R, S, EhomG, GmapE, NhomE, NEhomN, EltsE, Mult, InvE) Inputs a ZG-resolution R, a ZN-re

Resolutions of modules

ResolutionFpGModule (M, n) Inputs an FpG-module M and a positive integer n. It returns n terms of a minimal free F

Induced equivariant chain maps

EquivariantChainMap(R,S,f) Inputs a ZG-resolution R, a ZG'-resolution S, and a group homomorphism $f:G\longrightarrow G$

Functors

HomToIntegers (X) Inputs either a ZG-resolution X=R, or an equivariant chain map $X=(F:R\longrightarrow S)$. It returns the HomToIntegersModP (R) Inputs a ZG-resolution R and returns the cochain complex obtained by applying HomZG(Z) HomToIntegralModule (R, f) Inputs a ZG-resolution R and a group homomorphism $f:G\longrightarrow GL_n(Z)$ to the group G LowerCentralSeriesLieAlgebra (G) LowerCentralSeriesLieAlgebra (f) Inputs a pcp group G. If each quot TensorWithIntegers (X) Inputs either a ZG-resolution X=R, or an equivariant chain map $X=(F:R\longrightarrow S)$. It ret TensorWithIntegersModP (X,p) Inputs either a ZG-resolution X=R, or an equivariant chain map $X=(F:R\longrightarrow S)$. TensorWithRationals (R) Inputs a ZG-resolution Z0 and returns the chain complex obtained by tensoring with the transfer of ZG1.

Chain complexes

ChevalleyEilenbergComplex (X, n) Inputs either a Lie algebra X = A (over the ring of integers Z or over a field K) LeibnizComplex (X, n) Inputs either a Lie or Leibniz algebra X = A (over the ring of integers Z or over a field K) or

Homology and cohomology groups

Cohomology (X) Inputs either a cochain complex X=C or a cochain map $X=(C\longrightarrow D)$ over the integers Z. If X=C CohomologyPrimePart (C, n, p) Inputs a cochain complex C in characteristic 0, a positive integer n, and a prime p. It regroupCohomology (X, n) GroupCohomology (X, n, p) Inputs a positive integer n and either a finite group X=G or a GroupHomology (X, n)

GroupHomology (X, n, p) Inputs a positive integer n and either a finite group X = G or a Coxeter diagram X = D represed Homology (X, n) Inputs either a chain complex X = C or a chain map $X = (C \longrightarrow D)$. If X = C then the torsion coefficient Homology (C, n) This is a back-up function which might work in some instances where Homology(C,n) fails. It is more Homology PrimePart (C, n, p) Inputs a chain complex C in characteristic 0, a positive integer n, and a prime p. It returns Leibniz Algebra Homology (A, n) Inputs a Lie or Leibniz algebra X = A (over the ring of integers Z or over a field K), to Lie Algebra Homology (A, n) Inputs a Lie algebra A (over the integers or a field) and a positive integer n. It returns the homology PrimePart Derived Functor (G, R, F, n) Inputs a finite group G, a positive integer n, at least n+1 terms of a ZP-resolut Rank Homology Proup (G, n) Rank Homology Proup (R, n) Rank Homology Proup (G, n, "empirical") Inputs a (small Rank Prime Homology (G, n) Inputs a (small sh) p-group G together with a positive integer n. It returns a function dim(k)

Poincare series

EfficientNormalSubgroups(G)

EfficientNormalSubgroups (G, k) Inputs a prime-power group G and, optionally, a positive integer k. The default is k ExpansionOfRationalFunction (f, n) Inputs a positive integer n and a rational function f(x) = p(x)/q(x) where the G

PoincareSeries (G, n) PoincareSeries (R, n)

PoincareSeries (L, n)

PoincareSeries (G) Inputs a finite p-group G and a positive integer n. It returns a quotient of polynomials f(x) = P0 PoincareSeriesPrimePart (G, p, n) Inputs a finite group G, a prime p, and a positive integer n. It returns a quotient of Prank (G) Inputs a p-group G and returns the rank of the largest elementary abelian subgroup.

Cohomology ring structure

IntegralCupProduct(R,u,v,p,q)

IntegralCupProduct (R, u, v, p, q, P, Q, N) (Various functions used to construct the cup product are also $CR_function$ IntegralRingGenerators (R, n) Inputs at least n+1 terms of a ZG-resolution and integer n>0. It returns a minimal ModPCohomologyRing (G, n)

ModPCohomologyRing (R) Inputs either a p-group G and positive integer n, or else n terms of a minimal Z_pG -resoluti ModPRingGenerators (A) Inputs a mod p cohomology ring A (created using the preceding function). It returns a generator P and P cohomology ring P coho

Commutator and nonabelian tensor computations

BaerInvariant (G, c) Inputs a nilpotent group G and integer c>0. It returns the Baer invariant $M^(c)(G)$ defined as for Coclass (G) Inputs a group G of prime-power order p^n and nilpotency class c say. It returns the integer r=n-c. EpiCentre (G, N)

EpiCentre (G) Inputs a finite group G and normal subgroup N and returns a subgroup $Z^*(G,N)$ of the centre of N. The NonabelianExteriorProduct (G, N) Inputs a finite group G and normal subgroup N. It returns a record E with the foll NonabelianTensorProduct (G, N) Inputs a finite group G and normal subgroup N. It returns a record E with the foll NonabelianTensorSquare (G)

NonabelianTensorSquare (G, m) Inputs a finite or nilpotent infinite group G and returns a record T with the following RelativeSchurMultiplier (G, N) Inputs a finite group G and normal subgroup N. It returns the homology group H_2 TensorCentre (G) Inputs a group G and returns the largest central subgroup N such that the induced homomorphism ThirdHomotopyGroupOfSuspensionB (G)

ThirdHomotopyGroupOfSuspensionB(G,m) Inputs a finite or nilpotent infinite group G and returns the abelian invar UpperEpicentralSeries(G,c) Inputs a nilpotent group G and an integer c. It returns the c-th term of the upper epic

Generators and relators of groups

CayleyGraphDisplay(G,X)

CayleyGraphDisplay (G, X, "mozilla") Inputs a finite group G together with a subset X of G. It displays the correst IsAspherical (F, R) Inputs a free group F and a set R of words in F. It performs a test on the 2-dimensional CW-spare PresentationOfResolution (R) Inputs at least two terms of a reduced ZG-resolution R and returns a record P with TorsionGeneratorsAbelianGroup (G) Inputs an abelian group G and returns a generating set $[x_1, \ldots, x_n]$ where no property of the set of th

Orbit polytopes and fundamental domains

FundamentalDomainAffineCrystGroupOnRight (v, G) Inputs a crystallographic group G (represented using AffineCorbitPolytope (G, v, L) Inputs a permutation group or matrix group G of degree n and a rational vector v of length n. The function uses Polymake software.

PolytopalComplex(G,v) PolytopalComplex(G,v,n)

Inputs a permutation group or matrix group G of degree n and a rational vector v of length n. In both cases there is a natural action of G on v. Let P(G,v) be the convex polytope arising as the convex hull of the Euclidean points in the orbit of v under the action of G. The cellular chain complex $C_* = C_*(P(G,v))$ is an exact sequence of (not necessarily free) ZG-modules. The function returns a component object R with components:

- R!.dimension(k) is a function which returns the number of G-orbits of the k-dimensional faces in P(G, v). If each k-face has trivial stabilizer subgroup in G then C_k is a free ZG-module of rank R.dimension(k).
- R!.stabilizer(k,n) is a function which returns the stabilizer subgroup for a face in the n-th orbit of k-faces.
- If all faces of dimension < k+1 have trivial stabilizer group then the first k terms of C_* constitute part of a free ZG-resolution. The boundary map is described by the function boundary(k,n). (If some faces have non-trivial stabilizer group then C_* is not free and no attempt is made to determine signs for the boundary map.)
- R!.elements, R!.group, R!.properties are as in a ZG-resolution.

If an optional third input variable n is used, then only the first n terms of the resolution C_* will be computed.

The function uses Polymake software.

PolytopalGenerators (G, v)

Inputs a permutation group or matrix group G of degree n and a rational vector v of length n. In both cases there is a natural action of G on v, and the vector v must be chosen so that it has trivial stabilizer subgroup in G. Let P(G, v) be the convex polytope arising as the convex hull of the Euclidean points in the orbit of v under the action of G. The function returns a record P with components:

- *P.generators* is a list of all those elements g in G such that $g \cdot v$ has an edge in common with v. The list is a generating set for G.
- *P.vector* is the vector *v*.
- *P.hasseDiagram* is the Hasse diagram of the cone at *v*.

The function uses Polymake software. The function is joint work with Seamus Kelly. VectorStabilizer(G, V)

Inputs a permutation group or matrix group G of degree n and a rational vector of degree n. In both cases there is a natural action of G on v and the function returns the group of elements in G that fix v.

Cocycles

CocycleCondition (R, n) Inputs a resolution R and an integer n>0. It returns an integer matrix M with the following StandardCocycle (R, f, n)

StandardCocycle (R, f, n, q) Inputs a ZG-resolution R (with contracting homotopy), a positive integer n and an integration R (with contracting homotopy) and a list g = [g[1], ..., g[n]] of elements in G. It is

Words in free ZG-modules

AddFreeWords (v, w) Inputs two words v, w in a free ZG-module and returns their sum v + w. If the characteristic of Z AddFreeWordsModP (v, w, p) Inputs two words v, w in a free ZG-module and the characteristic p of Z. It returns the superproduction (w)

AlgebraicReduction (w,p) Inputs a word w in a free ZG-module and returns a reduced version of the word in which Multiply Word (n, w) Inputs a word w and integer n. It returns the scalar multiple $n \cdot w$.

Negate ([i, j]) Inputs a pair [i, j] of integers and returns [-i, j].

NegateWord (w) Inputs a word w in a free ZG-module and returns the negated word -w.

PrintZGword(w, elts) Inputs a word w in a free ZG-module and a (possibly partial but sufficient) listing elts of the G-module. The function returns a set S of words in a free ZG-module, and a word w in the module. The function returns a set S-module.

FpG-modules

DirectSumOfFpGModules(M,N)

DirectSumOfFpGModules([M[1], M[2], ..., M[k]])) Inputs two FpG-modules M and N with common group FpGModule(A,P)

FpgModule (A, G, p) Inputs a p-group P and a matrix A whose rows have length a multiple of the order of G. It returns FpgModuleDualBasis (M) Inputs an FpG-module M. It returns a record R with two components: R. f reeM odule is the FpgModuleHomomorphism (M, N, A)

FpGModuleHomomorphismNC (M, N, A) Inputs FpG-modules M and N over a common p-group G. Also inputs a list A DesuspensionFpGModule (M, n)

DesuspensionFpGModule (R, n) Inputs a positive integer n and and FpG-module M. It returns an FpG-module D^nM RadicalOfFpGModule (M) Inputs an FpG-module M with G a p-group, and returns the Radical of M as an FpG-module GeneratorsOfFpGModule (M) Inputs an FpG-module M and returns a matrix whose rows correspond to a minimal gradient in the second sec

Meataxe modules

DesuspensionMtxModule (M) Inputs a meataxe module M over the field of p elements and returns an FpG-module DM FpG-to_MtxModule (M) Inputs an FpG-module M and returns an isomorphic meataxe module.

 $\texttt{GeneratorsOfMtxModule} \ (\texttt{M}) \ \ \textbf{Inputs a meataxe module} \ \textit{M} \ \ \textbf{acting on, say, the vector space} \ \textit{V}. \ \ \textbf{The function returns a module} \ \textit{M} \ \ \textbf{M} \ \ \ \textbf{M} \ \ \textbf{$

Coxeter diagrams and graphs of groups

CoxeterDiagramComponents (D) Inputs a Coxeter diagram D and returns a list $[D_1,...,D_d]$ of the maximal connected CoxeterDiagramDegree (D, v) Inputs a Coxeter diagram D and vertex v. It returns the degree of v (i.e. the number of CoxeterDiagramDisplay (D)

CoxeterDiagramFpArtinGroup (D) Inputs a Coxeter diagram D and returns the corresponding finitely presented Art CoxeterDiagramFpCoxeterGroup (D) Inputs a Coxeter diagram D and returns the corresponding finitely presented CoxeterDiagramIsSpherical (D) Inputs a Coxeter diagram D and returns "true" if the associated Coxeter groups is CoxeterDiagramMatrix (D) Inputs a Coxeter diagram D and returns a matrix representation of it. The matrix is give CoxeterSubDiagram (D, V) Inputs a Coxeter diagram D and a subset V of its vertices. It returns the full sub-diagram CoxeterDiagramVertices (D) Inputs a Coxeter diagram D and returns its set of vertices.

EvenSubgroup (G) Inputs a group G and returns a subgroup G^+ . The subgroup is that generated by all products xy where G is G is G in G.

GraphOfGroupsDisplay (D, "web browser") Inputs a graph of groups D and displays it as a .gif file. It uses the Mo GraphOfGroupsTest (D) Inputs an object D and itries to test whether it is a Graph of Groups. However, it DOES NO

Some functions for accessing basic data

BoundaryMap(C) Inputs a resolution, chain complex or cochain complex C and returns the function C!.boundary. BoundaryMatrix(C,n) Inputs a chain or cochain complex C and integer n>0. It returns the n-th boundary map of C Dimension(C)

Dimension (M) Inputs a resolution, chain complex or cochain complex C and returns the function C!. dimension. Alte EvaluateProperty (X, "name") Inputs a component object X (such as a ZG-resolution or chain map) and a string "n GroupOfResolution (R) Inputs a ZG-resolution R and returns the group G.

Length (R) Inputs a resolution R and returns its length (i.e. the number of terms of R that HAP has computed).

Map (f) Inputs a chain map, or cochain map or equivariant chain map f and returns the mapping function (as opposed Source (f) Inputs a chain map, or cochain map, or equivariant chain map, or FpG-module homomorphism f and return Target (f) Inputs a chain map, or cochain map, or equivariant chain map, or FpG-module homomorphism f and return the following specific content of the following specific conte

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Parallel Computation - Core Functions

```
ChildProcess()
ChildProcess("computer.ac.wales") This starts a GAP session as a child process and returns a stream to the child process and returns a stream
```

- ssh-keygen -t dsa
- scp *.pub user@remotehost: /
- ssh remotehost -l user
- cat $id_r sa.pub >> .ssh/authorized_k eys$
- cat $id_d sa.pub >> .ssh/authorized_k eys$
- rm $id_r sa.pubid_d sa.pub$
- exit

You should now be able to connect from "thishost" to "remotehost" without a password prompt.)

ChildClose(s) This closes the stream s to a child GAP process.

ChildCommand ("cmd;",s) This runs a GAP command "cmd;" on the child process accessed by the stream s. Here "cm NextAvailableChild(L) Inputs a list L of child processes and returns a child in L which is ready for computation (as IsAvailableChild(s) Inputs a child process s and returns true if s is currently available for computations, and false the ChildPut(A, "B",s) This copies a GAP object A on the parent process to an object B on the child process s. (The cop ChildGet("A",s) This functions copies a GAP object A on the child process s and returns it on the parent process. (The cope childGet("A",s) This functions copies a GAP object A on the child process s and returns it on the parent process.

Parallel Computation - Extra Functions

ChildFunction("function(arg);",s) This runs the GAP function "function(arg);" on a child process accessed by the ChildRead(s) This returns, as a string, the output of the last application of ChildFunction("function(arg);",s). ChildReadEval(s) This returns, as an evaluated string, the output of the last application of ChildFunction("function(arg);",s). ParallelList(I,fn,L) Inputs a list I, a function fn such that fn(x) is defined for all x in I, and a list of children L. It

Topological Data Analysis

ReadImageFile("file.png", n) Inputs an image file ("file.png", "file.eps", "file.bmp" etc) and an integer n between BettiNumbersOfMatrix(A) Inputs a 1/0 integer matrix A representing a black/white version of an image. It returns a MatrixToChainComplex(A) Inputs a 1/0 integer matrix A representing a black/white version of an image and returns t ContractMatrix(A) Inputs a 1/0 integer matrix A representing a black/white version of an image and modifies A so the ThickenedMatrix(A) ThickenedMatrix(A, n) Inputs a 1/0 integer matrix A and returns a 1/0 matrix B. If an entry is the second of the second of

Pseudo lists

Add (L, x) Let L be a pseudo list of length n, and x an object compatible with the entries in L. If x is not in L then this of Append (L, K) Let L be a pseudo list and K a list whose objects are compatible with those in L. This operation applies L ListToPseudoList (L) Inputs a list L and returns the pseudo list representation of L.

Miscellaneous

BigStepLCS (G, n) Inputs a group G and a positive integer n. It returns a subseries $G = L_1 > L_2 > \dots L_k = 1$ of the lower Compose (f, g) Inputs two FpG-module homomorphisms $f: M \longrightarrow N$ and $g: L \longrightarrow M$ with Source(f) = Target(g). HAPcopyright () This function provides details of HAP'S GNU public copyright licence.

IsLieAlgebraHomomorphism(f) Inputs an object f and returns true if f is a homomorphism $f:A\longrightarrow B$ of Lie algebraHomomorphism $f:A\longrightarrow B$ o

PermToMatrixGroup (G, n) Inputs a permutation group G and its degree n. Returns a bijective homomorphism f:G SolutionsMatDestructive (M, B) Inputs an $m \times n$ matrix M and a $k \times n$ matrix B over a field. It returns a $k \times mmat$ TestHap () This runs a representative sample of HAP functions and checks to see that they produce the correct output

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