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Resolutions of the ground ring

TietzeReducedResolution(R) Inputs a $\mathbb{Z}G$ -resolution R and returns a $\mathbb{Z}G$ -resolution S which is obtained from R ResolutionArithmeticGroup("PSL(4,Z)",n) Inputs a positive integer n and one of the following strings:

 $"SL(2,Z)" \ , "SL(3,Z)" \ , "PGL(3,Z[i])" \ , "PGL(3,Eisenstein_Integers)" \ , "PSL(4,Z)" \ , "PSL(4,Z)_b" \ , "PSL(4,Z)_c" \ , or one of the following strings$

"SL(2,Z[sqrt(-2)])", "SL(2,Z[sqrt(-7)])", "SL(2,Z[sqrt(-11)])", "SL(2,Z[sqrt(-19)])", "SL(2,Z[sqrt(-43)])", "SL(2,Z[sqrt(-43)])", "SL(2,Z[sqrt(-10)])", "S

It returns n terms of a free ZG-resolution for the group G described by the string. (Subscripts $_{\rm b}$, $_{\rm c}$, $_{\rm d}$ denote alter

Data for the first list of resolutions was provided provided by MATHIEU DUTOUR. Data for the second list was provided by MATHIEU DUTOUR. FreeGResolution(P,n) FreeGResolution(P,n,p) Inputs a non-free ZG-resolution P with finite stabilizer group ResolutionGTree(P,n) Inputs a non-free ZG-resolution P of dimension 1 (i.e. a G-tree) with finite stabilizer grou ResolutionSL2Z(p,n) Inputs positive integers m, n and returns n terms of a ZG-resolution for the group G = SL(2)ResolutionAbelianGroup(L,n) ResolutionAbelianGroup(G,n) Inputs a list $L := [m_1, m_2, ..., m_d]$ of nonnegative ResolutionAlmostCrystalGroup(G, n) Inputs a positive integer n and an almost crystallographic pcp group G. It ResolutionAlmostCrystalQuotient(G,n,c) ResolutionAlmostCrystalQuotient(G,n,c,false) An almost ResolutionArtinGroup(D,n) Inputs a Coxeter diagram D and an integer n > 1. It returns n terms of a free ZG-resolutionArtinGroup(D,n) Inputs a Coxeter diagram D and an integer n > 1. ResolutionAsphericalPresentation(F,R,n) Inputs a free group F, a set R of words in F which constitute an a ResolutionBieberbachGroup(G) ResolutionBieberbachGroup(G, v) Inputs a torsion free crystallogic ResolutionCoxeterGroup(D,n) Inputs a Coxeter diagram D and an integer n > 1. It returns k terms of a free ZG-ResolutionDirectProduct(R,S) ResolutionDirectProduct(R,S,"internal") Inputs a $\mathbb{Z}G$ -resolution \mathbb{R} and $Resolution Extension (g,R,S) \quad Resolution Extension (g,R,S,"TestFiniteness") \\ Resolution Extension (g,R,S) \\ Resolution (g$ ResolutionFiniteDirectProduct(R,S) ResolutionFiniteDirectProduct(R,S, "internal") Inputs a Ze ResolutionFiniteExtension(gensE,gensG,R,n) ResolutionFiniteExtension(gensE,gensG,R,n,true) ResolutionFiniteGroup(gens,n) ResolutionFiniteGroup(gens,n,true) ResolutionFiniteGroup(gens ResolutionFiniteSubgroup(R,K) ResolutionFiniteSubgroup(R,gensG,gensK) Inputs a ZG-resolution for a ResolutionGraphOfGroups (D,n) ResolutionGraphOfGroups (D,n,L) Inputs a graph of groups D and a positive D and D are D and D are D and D are D and D are D and D are D and D are $Resolution \verb|NilpotentGroup(G,n)| Resolution \verb|NilpotentGroup(G,n,"TestFiniteness"|) Inputs a nilpotent and the substitution an$ $Resolution Normal Series (L,n) \\ Resolution Normal Series (L,n,true) \\ Resolution Normal Series (L,n,fall true) \\ Resolution Normal Series (L,n,fall tru$ ${\tt ResolutionPrimePowerGroup(P,n)} \quad {\tt ResolutionPrimePowerGroup(G,n,p)} \ \, {\tt Inputs} \ \, a \ \, p\hbox{-}{\tt group} \ \, P \ \, {\tt and integer} \ \, n > 0 \ \, p\ \, {\tt and integer} \ \, n > 0 \ \, {\tt and integer} \ \,$ ResolutionSmallFpGroup(G,n) ResolutionSmallFpGroup(G,n,p) Inputs a small finitely presented group (ResolutionSubgroup(R,K) Inputs a ZG-resolution for an (infinite) group G and a subgroup K of finite index |G:R|ResolutionSubnormalSeries (L,n) Inputs a positive integer n and a list $L = [L_1, ..., L_k]$ of subgroups L_i of a fin ConjugatedResolution(R,x) Inputs a ZG-resoluton R and an element x from some group containing G. It returns RecalculateIncidenceNumbers (R) Inputs a ZG-resoluton R which arises as the cellular chain complex of a regul

Resolutions of modules

Resolution FpG Module (M,n) Inputs an FpG-module M and a positive integer n. It returns n terms of a minimal free

Induced equivariant chain maps

 \mid EquivariantChainMap(R,S,f) Inputs a ZG-resolution R, a ZG'-resolution S, and a group homomorphism f:G —

Functors

ExtendScalars (R,G,EltsG) Inputs a ZH-resolution R, a group G containing H as a subgroup, and a list EltsG of HomToIntegers (X) Inputs either a ZG-resolution X=R, or an equivariant chain map $X=(F:R\longrightarrow S)$. It returns HomToIntegersModP(R) Inputs a ZG-resolution R and returns the cochain complex obtained by applying HomZG HomToIntegralModule(R,f) Inputs a ZG-resolution R and a group homomorphism $f:G\longrightarrow GL_n(Z)$ to the group TensorWithIntegralModule(R,f) Inputs a ZG-resolution R and a group homomorphism $f:G\longrightarrow GL_n(Z)$ to the HomToGModule(R,A) Inputs a ZG-resolution R and an abelian G-outer group G. It returns the G-cocomplex obtain InduceScalars (R,hom) Inputs a G-resolution G and a surjective group homomorphism G in G in G if each question TensorWithIntegers (X) Inputs either a G-resolution G and a equivariant chain map G in G is in NamesOfComTensorWithIntegers (R) Inputs a G-resolution G for which "filteredDimension" lies in NamesOfComTensorWithIntegers (X,rho) Inputs either a G-resolution G-re

Chain complexes

ChainComplex(T) Inputs a pure cubical complex, or cubical complex, or simplicial complex T and returns the (ofter ChainComplexOfPair(T,S) Inputs a pure cubical complex or cubical complex T and contractible subcomplex S. It ChevalleyEilenbergComplex(X,n) Inputs either a Lie algebra X = A (over the ring of integers Z or over a field K SuspendedChainComplex(C) Inputs a chain complex C and returns the chain complex S defined by applying the deReducedSuspendedChainComplex(C) Inputs a chain complex S and returns the chain complex S defined by applying CoreducedChainComplex(C) CoreducedChainComplex(C, 2) Inputs a chain complex S and returns a quasi-isom TensorProductOfChainComplexes(C,D) Inputs two chain complexes S and S of the same characteristic and return LefschetzNumber(F) Inputs a chain map S: S with common source and target. It returns the Lefschetz number

Sparse Chain complexes

SparseMat (A) Inputs a matrix A and returns the matrix in sparse format.

TransposeOfSparseMat(A) Inputs a sparse matrix A and returns its transpose sparse format.

ReverseSparseMat(A) Inputs a sparse matrix A and modifies it by reversing the order of the columns. This function SparseRowMult(A,i,k) Multiplies the i-th row of a sparse matrix A by k. The sparse matrix A is modified but not be SparseRowInterchange(A,i,k) Interchanges the i-th and j-th rows of a sparse matrix A by k. The sparse matrix A SparseRowAdd(A,i,j,k) Adds k times the j-th row to the i-th row of a sparse matrix A. The sparse matrix A is modified sparseSemiEchelon(A) Converts a sparse matrix A to semi-echelon form (which means echelon form up to a permitankMatDestructive(A) Returns the rank of a sparse matrix A. The sparse matrix A is modified during the calcular RankMat(A) Returns the rank of a sparse matrix A.

SparseChainComplex(Y) Inputs a regular CW-complex Y and returns a sparse chain complex which is chain homo SparseChainComplexOfRegularCWComplex(Y) Inputs a regular CW-complex Y and returns its cellular chain complex SparseBoundaryMatrix(C,n) Inputs a sparse chain complex C and integer n. Returns the n-th boundary matrix of Bettinumbers(C,n) Inputs a sparse chain complex C and integer n. Returns the n-th Netti number of the chain complex C and integer D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D and integer D are the n-th Netti number of the chain complex D are the n-th Netti number of the chain complex D are the n-th Netti number of the chain complex D are the n-th Netti number of the chain complex D are the n-th Netti number of the chain complex D are the n-th Netti number of the chain complex D are the n-th Netti number of th

Homology and cohomology groups

Cohomology (X,n) Inputs either a cochain complex X = C (or G-cocomplex C) or a cochain map $X = (C \longrightarrow D)$ in CohomologyModule (C, n) Inputs a G-cocomplex C together with a non-negative integer n. It returns the cohomologymodule (C, n) Inputs a G-cocomplex C together with a non-negative integer n. CohomologyPrimePart (C, n, p) Inputs a cochain complex C in characteristic 0, a positive integer n, and a prime p. GroupCohomology(X,n) GroupCohomology(X,n,p) Inputs a positive integer n and either a finite group X = G or GroupHomology (X,n) GroupHomology (X,n,p) Inputs a positive integer n and either afinite group X=G or a nilp PersistentHomologyOfQuotientGroupSeries(S,n) PersistentHomologyOfQuotientGroupSeries(S,n,p, PersistentCohomologyOfQuotientGroupSeries(S,n) PersistentCohomologyOfQuotientGroupSeries(S, UniversalBarCode("UpperCentralSeries",n,d) UniversalBarCode("UpperCentralSeries",n,d,k) Inpu PersistentHomologyOfSubGroupSeries(S,n) PersistentHomologyOfSubGroupSeries(S,n,p,Resolution PersistentHomologyOfFilteredChainComplex(C,n,p) Inputs a filtered chain complex C (of characteristic O PersistentHomologyOfCommutativeDiagramOfPGroups(D,n) Inputs a commutative diagram D of finite p-groups(D,n) PersistentHomologyOfFilteredCubicalComplex (M,n) Inputs a filtered pure cubical complex M and a non-neg PersistentHomologyOfPureCubicalComplex (L, n, p) Inputs a positive integer n, a prime p and an increasing ch ZZPersistentHomologyOfPureCubicalComplex(L,n,p) Inputs a positive integer n, a prime p and any sequence RipsHomology (G,n) RipsHomology (G,n,p) Inputs a graph G, a non-negative integer n (and optionally a prime number of G). BarCode(P) Inputs an integer persistence matrix P and returns the same information in the form of a binary matrix (BarCodeDisplay(P) BarCodeDisplay(P, "mozilla") BarCodeCompactDisplay(P) BarCodeCompactDisplay Homology (X, n) Inputs either a chain complex X = C or a chain map $X = (C \longrightarrow D)$. If X = C then the torsion coeff HomologyPb(C,n) This is a back-up function which might work in some instances where Homology(C,n) fails. It is HomologyVectorSpace(X,n) Inputs either a chain complex X = C or a chain map $X = (C \longrightarrow D)$ in prime charact HomologyPrimePart (C, n, p) Inputs a chain complex C in characteristic 0, a positive integer n, and a prime p. It re LeibnizAlgebraHomology (A,n) Inputs a Lie or Leibniz algebra X = A (over the ring of integers Z or over a field A Lie Algebra Homology (A, n) Inputs a Lie algebra A (over the integers or a field) and a positive integer n. It returns t PrimePartDerivedFunctor(G,R,F,n) Inputs a finite group G, a positive integer n, at least n+1 terms of a $\mathbb{Z}P$ -res RankHomologyPGroup(G,n) RankHomologyPGroup(R,n) RankHomologyPGroup(G,n,"empirical") Inputs a (s RankPrimeHomology (G, n) Inputs a (smallish) p-group G together with a positive integer n. It returns a function di

Poincare series

EfficientNormalSubgroups (G) EfficientNormalSubgroups (G,k) Inputs a prime-power group G and, optional ExpansionOfRationalFunction (f,n) Inputs a positive integer n and a rational function f(x) = p(x)/q(x) where PoincareSeries (G,n) PoincareSeries (R,n) PoincareSeries (L,n) PoincareSeries (G) Inputs a finite group G, a prime G, and a positive integer G. It returns a quotient of polynomials G inputs a finite 2-group G and returns a quotient of polynomials G inputs a G inputs a G and returns the rank of the largest elementary abelian subgroup.

Cohomology ring structure

IntegralCupProduct(R,u,v,p,q) IntegralCupProduct(R,u,v,p,q,P,Q,N) (Various functions used to continuous conti

Cohomology rings of *p***-groups (mainly**

$$p = 2$$

The functions on this page were written by PAUL SMITH. (They are included in HAP but they are also independently included in Paul Smiths HAPprime package.)

 $\label{localized} {\tt Mod2CohomologyRingPresentation(G,n)} \quad {\tt Mod2Coh$

Commutator and nonabelian tensor computations

BaerInvariant(G,c) Inputs a nilpotent group G and integer c>0. It returns the Baer invariant $M^(c)(G)$ defined as Coclass(G) Inputs a group G of prime-power order p^n and nilpotency class c say. It returns the integer r=n-c. EpiCentre(G,N) EpiCentre(G) Inputs a finite group G and normal subgroup N and returns a subgroup $Z^*(G,N)$ NonabelianExteriorProduct(G,N) Inputs a finite group G and normal subgroup N. It returns a record E with the NonabelianSymmetricKernel(G) NonabelianSymmetricSquare(G,m) Inputs a finite or nilpotent infinite group NonabelianTensorProduct(G,N) Inputs a finite group G and normal subgroup G. It returns a record G with the NonabelianTensorSquare(G) NonabelianTensorSquare(G,m) Inputs a finite or nilpotent infinite group G and RelativeSchurMultiplier(G,N) Inputs a finite group G and normal subgroup G such that the induced homomorphis ThirdHomotopyGroupOfSuspensionB(G) ThirdHomotopyGroupOfSuspensionB(G,m) Inputs a finite or nilpotent group G and an integer G. It returns the G-th term of the upper G-th term of G-th term of G-th term of

Lie commutators and nonabelian Lie tensors

Functions on this page are joint work with HAMID MOHAMMADZADEH, and implemented by him.

LieCoveringHomomorphism(L) Inputs a finite dimensional Lie algebra L over a field, and returns a surjective Lie heibnizQuasiCoveringHomomorphism(L) Inputs a finite dimensional Lie algebra L over a field, and returns a surjective LieEpiCentre(L) Inputs a finite dimensional Lie algebra L over a field, and returns an ideal $Z^*(L)$ of the centre of LieExteriorSquare(L) Inputs a finite dimensional Lie algebra L over a field. It returns a record E with the follow LieTensorSquare(L) Inputs a finite dimensional Lie algebra E over a field and returns a record E with the follow LieTensorCentre(L) Inputs a finite dimensional Lie algebra E over a field and returns the largest ideal E0 such that

Generators and relators of groups

CayleyGraphOfGroupDisplay(G,X) CayleyGraphOfGroupDisplay(G,X,"mozilla") Inputs a finite group G IdentityAmongRelatorsDisplay(R,n) IdentityAmongRelatorsDisplay(R,n,"mozilla") Inputs a free G IsAspherical(F,R) Inputs a free group G and a set G of words in G. It performs a test on the 2-dimensional CW-PresentationOfResolution(R) Inputs at least two terms of a reduced G-resolution G and returns a record G words in G-resolution G and returns a generating set G-resolution G-res

Orbit polytopes and fundamental domains

CoxeterComplex(D) CoxeterComplex(D,n) Inputs a Coxeter diagram D of finite type. It returns a non-free ZW-r ContractibleGcomplex("PSL(4,Z)") Inputs one of the following strings:

 $"SL(2,Z)" \ , "SL(3,Z)" \ , "PGL(3,Z[i])" \ , "PGL(3,Eisenstein_Integers)" \ , "PSL(4,Z)" \ , "PSL(4,Z)_b" \ , "PSL(4,Z)_c" \ , "PSL(4,Z)_c"$

or one of the following strings

"SL(2,O-2)", "SL(2,O-7)", "SL(2,O-11)", "SL(2,O-19)", "SL(2,O-43)", "SL(2,O-67)", "SL(2,O-163)"

It returns a non-free ZG-resolution for the group G described by the string. The stabilizer groups of cells are finite. (

Data for the first list of non-free resolutions was provided provided by MATHIEU DUTOUR. Data for the second list QuotientOfContractibleGcomplex(C,D) Inputs a non-free ZG-resolution C and a finite subgroup D of G which TruncatedGComplex(R,m,n) Inputs a non-free ZG-resolution R and two positive integers m and n. It returns the non-free D-resolution D-reso

Cocycles

CcGroup(A,f) Inputs a G-module A (i.e. an abelian G-outer group) and a standard 2-cocycle f $GxG - \cdots > A$. It CocycleCondition(R,n) Inputs a resolution R and an integer n>0. It returns an integer matrix M with the following StandardCocycle(R,f,n)

StandardCocycle(R,f,n,q) Inputs a ZG-resolution R (with contracting homotopy), a positive integer n and an in Syzygy(R,g) Inputs a ZG-resolution R (with contracting homotopy) and a list g = [g[1], ..., g[n]] of elements in G.

Words in free ZG-modules

AddFreeWords(v, w) Inputs two words v, w in a free ZG-module and returns their sum v + w. If the characteristic v AddFreeWordsModP(v, w, v) Inputs two words v, w in a free ZG-module and the characteristic v of v. It returns the AlgebraicReduction(v)

AlgebraicReduction(w,p) Inputs a word w in a free ZG-module and returns a reduced version of the word in wl Multiply Word(n,w) Inputs a word w and integer n. It returns the scalar multiple $n \cdot w$.

Negate([i,j]) Inputs a pair [i,j] of integers and returns [-i,j].

NegateWord(w) Inputs a word w in a free ZG-module and returns the negated word -w.

PrintZGword(w, elts) Inputs a word w in a free ZG-module and a (possibly partial but sufficient) listing elts of the TietzeReduction(S,w) Inputs a set S of words in a free ZG-module, and a word w in the module. The function resolutionBoundaryOfWord(R,n,w) Inputs a resolution R, a positive integer n and a list w representing a word in

FpG-modules

CompositionSeriesOfFpgModules (M) Inputs an FpG-module M and returns a list of FpG-modules that constitu FpGModule(A,P) FpGModule(A,G,p) Inputs a p-group P and a matrix A whose rows have length a multiple of the FpGModuleDualBasis (M) Inputs an FpG-module M. It returns a record R with two components: R. freeModule is FpGModuleHomomorphism(M,N,A) FpGModuleHomomorphismNC(M,N,A) Inputs FpG-modules M and N over a DesuspensionFpGModule (M,n) DesuspensionFpGModule (R,n) Inputs a positive integer n and and FpG-module (R,n)RadicalOfFpGModule (M) Inputs an FpG-module M with G a p-group, and returns the Radical of M as an FpG-m RadicalSeriesOfFpGModule(M) Inputs an FpG-module M and returns a list of FpG-modules that constitute the GeneratorsOfFpgModule (M) Inputs an FpG-module M and returns a matrix whose rows correspond to a minima ImageOfFpGModuleHomomorphism(f) Inputs an FpG-module homomorphism $f: M \longrightarrow N$ and returns its image GroupAlgebraAsFpGModule(G) Inputs a p-group G and returns its mod p group algebra as an FpG-module. IntersectionOfFpGModules (M, N) Inputs two FpG-modules M, N arising as submodules in a common free mod IsFpGModuleHomomorphismData(M, N, A) Inputs FpG-modules M and N over a common p-group G. Also inputs MaximalSubmoduleOfFpGModule (M) Inputs an FpG-module M and returns one maximal FpG-submodule of M. MaximalSubmodulesOfFpgModule(M) Inputs an FpG-module M and returns the list of maximal FpG-submodule MultipleOfFpGModule(w,M) Inputs an FpG-module M and a list $w := [g_1,...,g_t]$ of elements in the group G = MProjectedFpGModule (M, k) Inputs an FpG-module M of ambient dimension n|G|, and an integer k between 1 and RandomHomomorphismOfFpGModules (M, N) Inputs two FpG-modules M and N over a common group G. It return Rank(f) Inputs an FpG-module homomorphism $f: M \longrightarrow N$ and returns the dimension of the image of f as a vec SumOfFpGModules (M, N) Inputs two FpG-modules M,N arising as submodules in a common free module $(FG)^n$ v SumOp(f,g) Inputs two FpG-module homomorphisms $f,g:M \longrightarrow N$ with common sorce and common target. It is VectorsToFpGModuleWords(M,L) Inputs an FpG-module M and a list $L = [v_1, \dots, v_k]$ of vectors in M. It returns

Meataxe modules

 ${\tt DesuspensionMtxModule(M)} \ \ Inputs \ a \ meataxe \ module \ \textit{M} \ \ over \ the \ field \ of \ \textit{p} \ \ elements \ and \ returns \ an \ FpG-module \ \textit{$FpG_to_MtxModule(M)}$ \ Inputs \ an \ FpG-module \ \textit{M} \ \ and \ returns \ an \ isomorphic \ meataxe \ module.$

GeneratorsOfMtxModule(M) Inputs a meataxe module M acting on, say, the vector space V. The function returns a

G-Outer Groups

 $\mathtt{GOuterGroup}(\mathtt{E}, \mathtt{N})$ $\mathtt{GOuterGroup}()$ Inputs a group E and normal subgroup N. It returns N as a G-outer group when ${\tt GOuterGroupHomomorphismNC(A,B,phi)}$ ${\tt GOuterGroupHomomorphismNC()}$ Inputs G-outer groups A and B with GOuterHomomorphismTester(A,B,phi) Inputs G-outer groups A and B with common acting group, and a group h Centre(A) Inputs G-outer group A and returns the group theoretic centre of ActedGroup(A) as a G-outer group. DirectProductGog(A,B) DirectProductGog(Lst) Inputs G-outer groups A and B with common acting group, as

Cat-1-groups

AutomorphismGroupAsCatOneGroup(G) Inputs a group G and returns the Cat-1-group C corresponding to the cross HomotopyGroup(C,n) Inputs a cat-1-group C and an integer n. It returns the nth homotopy group of C.

HomotopyModule(C, 2) Inputs a cat-1-group C and an integer n=2. It returns the second homotopy group of C as a QuasiIsomorph(C) Inputs a cat-1-group C and returns a cat-1-group D for which there exists some homomorphism ModuleAsCatOneGroup(G, alpha, M) Inputs a group G, an abelian group G and a homomorphism G: $G \to Aut(M)$. MooreComplex(C) Inputs a cat-1-group G and returns its Moore complex as a G-complex (i.e. as a complex of ground NormalSubgroupAsCatOneGroup(G, N) Inputs a group G with normal subgroup G. It returns the Cat-1-group G condot Inputs a cat-1-group G obtained from the Xmod package and returns a cat-1-group G for which IsHa

Simplicial groups

NerveOfCatOneGroup(G, n) Inputs a cat-1-group G and a positive integer n. It returns the low-dimensional part of

This function applies both to cat-1-groups for which IsHapCatOneGroup(G) is true, and to cat-1-groups produced us

This function was implemented by VAN LUYEN LE.

This function was implemented by VAN LUYEN LE.

EilenbergMacLaneSimplicialGroupMap(f,n,dim) Inputs a group homomorphism f:G o Q, a positive integer

This function was implemented by VAN LUYEN LE.

MooreComplex(G) Inputs a simplicial group G and returns its Moore complex as a G-complex.

This function was implemented by VAN LUYEN LE.

 ${\tt ChainComplexOfSimplicialGroup(G)\ Inputs\ a\ simplicial\ group\ G\ and\ returns\ the\ cellular\ chain\ complex\ C\ of\ a\ G\ of\ a\ G\ of\ a\ of\ of\ a\ of\ a$

This function was implemented by VAN LUYEN LE.

SimplicialGroupMap(f) Inputs a homomorphism $f: G \to Q$ of simplicial groups. The function returns an induced

This function was implemented by VAN LUYEN LE.

HomotopyGroup(G,n) Inputs a simplicial group G and a positive integer n. The integer n must be less than the leng Representation of elements in the bar resolution For a group G we denote by $B_n(G)$ the free $\mathbb{Z}G$ -modulous formula G and G are the sum of the su

We represent a word

$$w = h_1 \cdot [g_{11}|g_{12}|...|g_{1n}] - h_2 \cdot [g_{21}|g_{22}|...|g_{2n}] + ... + h_k \cdot [g_{k1}|g_{k2}|...|g_{kn}]$$

in $B_n(G)$ as a list of lists:

$$[[+1, h_1, g_{11}, g_{12}, ..., g_{1n}], [-1, h_2, g_{21}, g_{22}, ... | g_{2n}] + ... + [+1, h_k, g_{k1}, g_{k2}, ..., g_{kn}].$$

BarResolutionBoundary (w) This function inputs a word w in the bar resolution module $B_n(G)$ and returns its ima

This function was implemented by VAN LUYEN LE.

BarResolutionHomotopy(w) This function inputs a word w in the bar resolution module $B_n(G)$ and returns its ima

This function is currently being implemented by VAN LUYEN LE.

Representation of elements in the bar complex For a group G we denote by $BC_n(G)$ the free abelian grou

We represent a word

$$w = [g_{11}|g_{12}|...|g_{1n}] - [g_{21}|g_{22}|...|g_{2n}] + ... + [g_{k1}|g_{k2}|...|g_{kn}]$$

in $BC_n(G)$ as a list of lists:

$$[[+1, g_{11}, g_{12}, ..., g_{1n}], [-1, g_{21}, g_{22}, ... | g_{2n}] + ... + [+1, g_{k1}, g_{k2}, ..., g_{kn}].$$

BarComplexBoundary (w) This function inputs a word w in the n-th term of the bar complex $BC_n(G)$ and returns its

This function was implemented by VAN LUYEN LE.

BarResolutionEquivalence(R) This function inputs a free ZG-resolution R. It returns a component object HE wi

$$equiv(n,-): B_n(G) \rightarrow B_{n+1}(G)$$

satisfying w - $\psi(\phi(w)) = d(n+1, equiv(n, w)) + equiv(n-1, d(n, w))$. where $d(n, -1) : B_n(G) \to B_{n-1}(G)$ is the boundary

This function was implemented by VAN LUYEN LE.

BarComplexEquivalence(R)

This function inputs a free ZG-resolution R. It first constructs the chain complex T = TensorWithIntegerts(R). The function returns a component object HE with components

- HE!.phi(n,w) is a function which inputs a non-negative integer n and a word w in $BC_n(G)$. It returns the image of w in T_n under a chain equivalence $\phi: BC_n(G) \to T_n$.
- HE!.psi(n,w) is a function which inputs a non-negative integer n and an element w in T_n . It returns the image of w in $BC_n(G)$ under a chain equivalence $\psi: T_n \to BC_n(G)$.
- HE!.equiv(n,w) is a function which inputs a non-negative integer n and a word w in $BC_n(G)$. It returns the image of w in $BC_{n+1}(G)$ under a homomorphism $equiv(n,-):BC_n(G) \to BC_{n+1}(G)$ satisfying

$$w - \psi(\phi(w)) = d(n+1, equiv(n, w)) + equiv(n-1, d(n, w)).$$

where $d(n, -): BC_n(G) \to BC_{n-1}(G)$ is the boundary homomorphism in the bar complex.

This function was implemented by VAN LUYEN LE.

Representation of elements in the bar cocomplex

For a group G we denote by $BC^n(G)$ the free abelian group with basis the lists $[g_1|g_2|...|g_n]$ where the g_i range over G.

We represent a word

$$w = [g_{11}|g_{12}|...|g_{1n}] - [g_{21}|g_{22}|...|g_{2n}] + ... + [g_{k1}|g_{k2}|...|g_{kn}]$$
in $BC^n(G)$ as a list of lists:
$$[[+1, g_{11}, g_{12}, ..., g_{1n}], [-1, g_{21}, g_{22}, ...|g_{2n}] + ... + [+1, g_{k1}, g_{k2}, ..., g_{kn}].$$
BarCocomplexCoboundary(w)

This function inputs a word w in the n-th term of the bar cocomplex $BC^n(G)$ and returns its image under the coboundary homomorphism $d^n:BC^n(G)\to BC^{n+1}(G)$ in the bar cocomplex.

This function was implemented by VAN LUYEN LE.

Coxeter diagrams and graphs of groups

CoxeterDiagramComponents(D) Inputs a Coxeter diagram D and returns a list $[D_1,...,D_d]$ of the maximal connection D and D and D and D and D and D are turns the degree of D (i.e. the number D and D and D are turns the degree of D (i.e. the number D and D and D are turns the corresponding finitely presented D and D and returns the corresponding finitely presented D and returns the corresponding finitely presented D and returns D and returns the corresponding finitely presented D and returns D and returns D and returns D and returns D and D and returns D and D and returns D and D and D and returns D and D and D and returns D and returns the full sub-diagram D and D and returns D and returns the full sub-diagram D and returns are trices. It returns the full sub-diagram D and returns its set of vertices.

EvenSubgroup(G) Inputs a group G and returns a subgroup G^+ . The subgroup is that generated by all products xy GraphOfGroupsDisplay(D) GraphOfGroupsDisplay(D, "web browser") Inputs a graph of groups D and di GraphOfResolutions(D,n) Inputs a graph of groups D and a positive integer n. It returns a graph of resolutions GraphOfGroups(D) Inputs a graph of resolutions D and returns the corresponding graph of groups.

GraphOfResolutionsDisplay(D) Inputs a graph of resolutions D and displays it as a .gif file. It uses the Mozill GraphOfGroupsTest(D) Inputs an object D and itries to test whether it is a Graph of Groups. However, it DOES Inputs a graph of groupsToContractibleGcomplex(D,G) Inputs a graph of groups D which is a tree, and also inputs the full TreeOfResolutionsToContractibleGcomplex(D,G) Inputs a graph of resolutions D which is a tree, and also in D which is a tree, and D which is a tree D which in D which is a tree D which is a tree D which is a tree D

#

Torsion subcomplexes

The torsion subcomplexes subpackage has been conceived and implemented by ALEXANDER D. RAHM. IsPnormal(G, p) Inputs a finite group G and a prime p. Checks if the group G is p-normal for the prime p. Zasse TorsionSubcomplex(groupName, p) Inputs a cell complex with action of a group. In HAP, presently the follows:

```
"SL(2,O-2)", "SL(2,O-7)", "SL(2,O-11)", "SL(2,O-19)", "SL(2,O-43)", "SL(2,O-67)", "SL(2,O-163)",
```

where the symbol O[-m] stands for the ring of integers in the imaginary quadratic number field Q(sqrt(-m)), the latte

The function TorsionSubcomplex prints the cells with p-torsion in their stabilizer on the screen and returns the incide

It is also possible to input the cell complexes

```
"SL(2,Z)", "SL(3,Z)", "PGL(3,Z[i])", "PGL(3,Eisenstein_Integers)", "PSL(4,Z)", "PSL(4,Z)_b", "PSL(4,Z)_c",
```

provided by MATHIEU DUTOUR.

DisplayAvailableCellComplexes(); Displays the cell complexes that are available in HAP.

VisualizeTorsionSkeleton(groupName, p) Executes the function TorsionSubcomplex(groupName, p) and viReduceTorsionSubcomplex(groupName, p) This function start with the same operations as the function Torsion

It prints on the screen which cells to merge and which edges to cut off in order to reduce the p-torsion subcomplex w

Simplicial Complexes

Homology(T,n) Homology(T) Inputs a pure cubical complex, or cubical complex, or simplicial complex T and a nor RipsHomology(G,n) RipsHomology(G,n,p) Inputs a graph G, a non-negative integer n (and optionally a prime nor Bettinumbers(T,n) Bettinumbers(T) Inputs a pure cubical complex, or cubical complex, simplicial complex ChainComplex(T) Inputs a pure cubical complex, or simplicial complex T and returns the (often CechComplexOfPureCubicalComplex(T) Inputs a d-dimensional pure cubical complex T and returns a simplicial PureComplexToSimplicialComplex(T,k) Inputs either a d-dimensional pure cubical complex T or a d-dimensional RipsChainComplex(G,n) Inputs a graph T and a non-negative integer T and returns T terms of a chain complex T vectorsToSymmetricMatrix(M) VectorsToSymmetricMatrix(M,distance) Inputs a matrix T and returns MaximalSimplicesToSimplicialComplex(L) Inputs a list T whose entries are lists of vertices representing the m SkeletonOfSimplicialComplex(S,k) Inputs a simplicial complex T and returns the graph of T.

ContractibleSubcomplexOfSimplicialComplex(S) Inputs a simplicial complex S and returns a (probably maximathComponentsOfSimplicialComplex(S,n) Inputs a simplicial complex S and a nonnegative integer n. If n=0 QuillenComplex(G) Inputs a finite group G and returns, as a simplicial complex, the order complex of the poset of SymmetricMatrixToIncidenceMatrix(S,t) SymmetricMatrixToIncidenceMatrix(S,t,d) Inputs a symmetric IncidenceMatrixToGraph(M) Inputs a symmetric O/1 matrix O/1 matri

PathComponentsOfGraph(G,n) Inputs a graph G and a nonnegative integer n. If n=0 the number of path compone ContractGraph(G) Inputs a graph G and tries to remove vertices and edges to produce a smaller graph G' such that GraphDisplay(G) This function uses GraphViz software to display a graph G.

SimplicialMap(K,L,f) SimplicialMapNC(K,L,f) Inputs simplicial complexes K, L and a function f:K!.vertia ChainMapOfSimplicialMap(f) Inputs a simplicial map $f:K \to L$ and returns the corresponding chain map $C_*(f)$: SimplicialNerveOfGraph(G,d) Inputs a graph G and returns a d-dimensional simplicial complex K whose 1-skelling simplifies simplified simplifies K whose 1-skelling simplifies K whose

Cubical Complexes

ArrayToPureCubicalComplexA,n) Inputs an integer array A of dimension d and an integer n. It returns a d-dimen PureCubicalComplexA, n) Inputs a binary array A of dimension d. It returns the corresponding d-dimensional pure FramedPureCubicalComplex (M) Inputs a pure cubical complex M and returns the pure cubical complex with a bound of the complex M and M are the cubical complex M are the cubical complex M and M are RandomCubeOfPureCubicalComplex(M) Inputs a pure cubical complex M and returns a pure cubical complex R w PureCubicalComplexIntersection(S,T) Inputs two pure cubical complexes with common dimension and array PureCubicalComplexUnion(S,T) Inputs two pure cubical complexes with common dimension and array size. It re PureCubicalComplexDifference(S,T) Inputs two pure cubical complexes with common dimension and array size ReadImageAsPureCubicalComplex("file.png", n) Reads an image file ("file.png", "file.eps", "file.bmp" etc) a ReadLinkImageAsPureCubicalComplex("file.png") ReadLinkImageAsPureCubicalComplex("file.png") ReadImageSequenceAsPureCubicalComplex("directory", n) Reads the name of a directory containing a sequence Size (T) This returns the number of non-zero entries in the binary array of the cubical complex, or pure cubical com-Dimension(T) This returns the dimension of the cubical complex, or pure cubical complex T. WritePureCubicalComplexAsImage(T, "filename", "ext") Inputs a 2-dimensional pure cubical complex T, and ViewPureCubicalComplex(T) ViewPureCubicalComplex(T, "mozilla") Inputs a 2-dimensional pure cubical c Homology(T, n) Homology(T) Inputs a pure cubical complex, or cubical complex, or simplicial complex T and a non-Bettinumbers (T, n) Bettinumbers (T) Inputs a pure cubical complex, or cubical complex, simplicial complex or DirectProductOfPureCubicalComplexes(M,N) Inputs two pure cubical complexes M,N and returns their direct SuspensionOfPureCubicalComplex (M) Inputs a pure cubical complex M and returns a pure cubical complex with EulerCharacteristic (T) Inputs a pure cubical complex, or cubical complex, or simplicial complex T and returns PathComponentOfPureCubicalComplex (T, n) Inputs a pure cubical complex T and an integer n in the rane $1, \dots, T$ ChainComplex(T) Inputs a pure cubical complex, or cubical complex, or simplicial complex T and returns the (often ChainComplexOfPair(T,S) Inputs a pure cubical complex or cubical complex T and subcomplex S. It returns the ExcisedPureCubicalPair(T,S) Inputs a pure cubical complex T and subcomplex S. It returns the pair $T \setminus intS$, SChainInclusionOfPureCubicalPair(S,T) Inputs a pure cubical complex T and subcomplex S. It returns the cha ChainMapOfPureCubicalPairs (M, S, N, T) Inputs a pure cubical complex N and subcomplexes M, T and S in T. I ContractPureCubicalComplex(T) Inputs a pure cubical complex T of dimension d and removes d-dimensional cContractedComplex(T) Inputs a pure cubical complex T and returns a structural copy of the complex obtained fro ZigZagContractedPureCubicalComplex(T) Inputs a pure cubical complex T and returns a homotopy equivalent ContractCubicalComplex(T) Inputs a cubical complex T and removes cells without changing the homotopy type DVFReducedCubicalComplex(T) Inputs a cubical complex T and returns a non-regular cubical complex R by cons SkeletonOfCubicalComplex(T,n) Inputs a cubical complex, or pure cubical complex T and positive integer n. It ${\tt ContractibleSubomplexOfPureCubicalComplex(T)}$ Inputs a pure cubical complex T and returns a maximal contractible T and T are the contractible T and TAcyclicSubomplexOfPureCubicalComplex(T) Inputs a pure cubical complex T and returns a (not necessarily co HomotopyEquivalentMaximalPureCubicalSubcomplex(T,S) Inputs a pure cubical complex T together with a p HomotopyEquivalentMinimalPureCubicalSubcomplex(T,S) Inputs a pure cubical complex T together with a p BoundaryOfPureCubicalComplex(T) Inputs a pure cubical complex T and returns its boundary as a pure cubical TSingularitiesOfPureCubicalComplex(T, radius, tolerance) Inputs a pure cubical complex T together with a ThickenedPureCubicalComplex(T) Inputs a pure cubical complex T and returns a pure cubical complex S. If a expression of the second complex T and T are the second complex T are the second complex T and T are the second complex T are the second complex T are the second complex T and T are the second complex CropPureCubicalComplex(T) Inputs a pure cubical complex T and returns a pure cubical complex S obtained from BoundingPureCubicalComplex(T) Inputs a pure cubical complex T and returns a contractible pure cubical compl MorseFiltration(M,i,t,bool) MorseFiltration(M,i,t) Inputs a pure cubical complex M of dimension d, are ComplementOfPureCubicalComplex(T) Inputs a pure cubical complex T and returns a pure cubical complex S. A

PureCubicalComplexToTextFile(file,M) Inputs a pure cubical complex M and a string containing the address of ThickeningFiltration(M,n) ThickeningFiltration(M,n,k) Inputs a pure cubical complex M and a positive Dendrogram(M) Inputs a filtered pure cubical complex M and returns data that specifies the dendrogram (or phyloged DendrogramDisplay(M) Inputs a filtered pure cubical complex M, or alternatively inputs the out from the command DendrogramToPersistenceMat(D) Inputs the output of the function Dendrogram(M) and returns the corresponding ReadImageAsFilteredCubicalComplex(file,n) Inputs a string containing the path to an image file, together will ComplementOfFilteredCubicalComplex(M) Inputs a filtered pure cubical complex M and returns the complement PersistentHomologyOfFilteredCubicalComplex(M,n) Inputs a filtered pure cubical complex M and a non-negative complex M and a non-negative cubical cubi

Regular CW-Complexes

SimplicialComplexToRegularCWComplex(K) Inputs a simplicial complex K and returns the corresponding regular CubicalComplexToRegularCWComplex(K,n) Inputs a pure cubical cubicalCellsOfRegularCWComplex(Y) CriticalCellsOfRegularCWComplex(Y,n) Inputs a regular CW-complex(Y) Inputs a regular CW-complex Y and returns the cellular chain complex of a CW-complex Y who ChainComplexOfRegularCWComplex(Y) Inputs a regular CW-complex Y and returns the cellular chain complex of FundamentalGroup(Y) FundamentalGroup(Y,n) Inputs a regular CW-complex Y and, optionally, the number of

Knots and Links

PureCubicalKnot(L) PureCubicalKnot(n,i) Inputs a list L = [[m1,n1],[m2,n2],...,[mk,nk]] of pairs of integers ViewPureCubicalKnot(L) Inputs a pure cubical link L and displays it.

 ${\tt KnotSum}({\tt K,L})$ Inputs two pure cubical knots ${\tt K}, {\tt L}$ and returns their sum as a pure cubical knot. This function is not ${\tt KnotGroup}({\tt K})$ Inputs a pure cubical link ${\tt K}$ and returns the fundamental group of its complement. The group is returned alexanderMatrix(G) Inputs a finitely presented group ${\tt G}$ whose abelianization is infinite cyclic. It returns the AlexanderPolynomial(K) AlexanderPolynomial(G) Inputs either a pure cubical knot ${\tt K}$ or a finitely presented appropriate CubicalComplex(K) Inputs an \$n\$-dimensional pure cubical complex ${\tt K}$ and returns an n-1-dimensional pure CubicalComplex(file) ReadPDBfileAsPureCubicalComplex(file, m, c) Inputs a protection of the complex of the complex of the cubicalComplex of the cubical

Commutative diagrams and abstract categories

COMMUTATIVE DIAGRAMS

HomomorphismChainToCommutativeDiagram(H) Inputs a list $H = [h_1, h_2, ..., h_n]$ of mappings such that the compound NormalSeriesToQuotientDiagram(L) NormalSeriesToQuotientDiagram(L,M) Inputs an increasing (or decreased NerveOfCommutativeDiagram(D) Inputs a commutative diagram D and returns the commutative diagram ND congroupHomologyOfCommutativeDiagram(D,n) GroupHomologyOfCommutativeDiagram(D,n,prime) GroupPersistentHomologyOfCommutativeDiagramOfPGroups(D,n) Inputs a commutative diagram D of finite p-groupPortional D of finite D-groupPortional D-groupPortional

ABSTRACT CATEGORIES

CategoricalEnrichment(X, Name) Inputs a structure X such as a group or group homomorphism, together with together the IdentityArrow(X) Inputs an object X in some category, and returns the identity arrow on the object X.

InitialArrow(X) Inputs an object X in some category, and returns the arrow from the initial object in the category TerminalArrow(X) Inputs an object X in some category, and returns the arrow from X to the terminal object in the HasInitialObject(Name) Inputs the name of a category and returns true or false depending on whether the category HasTerminalObject(Name) Inputs the name of a category and returns true or false depending on whether the category Source(f) Inputs an arrow f in some category, and returns its source.

Target (f) Inputs an arrow f in some category, and returns its target.

CategoryName(X) Inputs an object or arrow X in some category, and returns the name of the category.

"*", "=", "+", "-" Composition of suitable arrows f,g is given by f*g when the source of f equals the target Object(X) Inputs an object X in some category, and returns the GAP structure Y such that X = CategoricalEnricher IsCategoryObject(X) Inputs X and returns true if X is an object in some category.

IsCategoryArrow(X) Inputs X and returns true if X is an arrow in some category.

Arrays and Pseudo lists

Array(A,f) Inputs an array A and a function f. It returns the the array obtained by applying f to each entry of A (at PermuteArray(A,f) Inputs an array A of dimension d and a permutation f of degree at most d. It returns the array ArrayDimension(A) Inputs an array A and returns its dimension.

ArrayDimensions (A) Inputs an array A and returns its dimensions.

ArraySum(A) Inputs an array A and returns the sum of its entries.

ArrayValue(A,x) Inputs an array A and a coordinate vector x. It returns the value of the entry in A with coordinate ArrayValueFunctions(d) Inputs a positive integer d and returns an efficient version of the function ArrayValue for ArrayAssign(A,x,n) Inputs an array A and a coordinate vector x and an integer n. It sets the entry of A with coord ArrayAssignFunctions(d) Inputs a positive integer d and returns an efficient version of the function ArrayAssign ArrayIterate(d) Inputs a positive integer d and returns a function ArrayIt(Dimensions,f). This function inputs a BinaryArrayToTextFile(file,A) Inputs a string containing the address of a file, and an array A of 0s and 1s. The FrameArray(A) Inputs an array A and returns the array obtained by appending a 0 to the beginning and end of each UnframeArray(A) Inputs an array A and returns the array obtained by removing the first and last entry in each "row Add(L,x) Let L be a pseudo list of length n, and x an object compatible with the entries in L. If x is not in L then thi Append(L,K) Let L be a pseudo list and K a list whose objects are compatible with those in L. This operation applied ListToPseudoList(L) Inputs a list L and returns the pseudo list representation of L.

Parallel Computation - Core Functions

ChildProcess() ChildProcess("computer.ac.wales") ChildProcess(["-m", "100000M", "-T"]) Child

- open a shell on thishost
- cd .ssh
- Is
- -> if id_dsa, id_rsa etc exists, skip the next two steps!
- ssh-keygen -t rsa
- ssh-keygen -t dsa
- scp *.pub user@remotehost:~/
- ssh remotehost -l user
- cat id_rsa.pub >> .ssh/authorized_keys
- cat id_dsa.pub >> .ssh/authorized_keys
- rm id_rsa.pub id_dsa.pub
- exit

You should now be able to connect from "thishost" to "remotehost" without a password prompt.) ChildClose(s) This closes the stream s to a child GAP process.

ChildCommand("cmd;",s) This runs a GAP command "cmd;" on the child process accessed by the stream s. Here NextAvailableChild(L) Inputs a list L of child processes and returns a child in L which is ready for computation IsAvailableChild(s) Inputs a child process s and returns true if s is currently available for computations, and false ChildPut(A, "B",s) This copies a GAP object A on the parent process to an object B on the child process s. (The ChildGet("A",s) This functions copies a GAP object A on the child process s and returns it on the parent process. HAPPrintTo("file",R) Inputs a name "file" of a new text file and a HAP object R. It writes the object R to "file". HAPRead("file",R) Inputs a name "file" containing a HAP object R and returns the object. Currently this is only in the child process and returns the object.

Parallel Computation - Extra Functions

ChildFunction("function(arg);",s) This runs the GAP function "function(arg);" on a child process accessed to ChildRead(s) This returns, as a string, the output of the last application of ChildFunction("function(arg);",s). ChildReadEval(s) This returns, as an evaluated string, the output of the last application of ChildFunction("function("function")]. ParallelList(I,fn,L) Inputs a list I, a function fn such that fn(x) is defined for all x in I, and a list of children I.

Some functions for accessing basic data

BoundaryMap(C) Inputs a resolution, chain complex or cochain complex C and returns the function C!.boundary. BoundaryMatrix(C,n) Inputs a chain or cochain complex C and integer n>0. It returns the n-th boundary map of C Dimension(C)

Dimension(M) Inputs a resolution, chain complex or cochain complex C and returns the function C!. dimension. A EvaluateProperty(X, "name") Inputs a component object X (such as a ZG-resolution or chain map) and a string GroupOfResolution(R) Inputs a ZG-resolution R and returns the group G.

Length (R) Inputs a resolution R and returns its length (i.e. the number of terms of R that HAP has computed).

Map(f) Inputs a chain map, or cochain map or equivariant chain map f and returns the mapping function (as oppose Source(f) Inputs a chain map, or cochain map, or equivariant chain map, or FpG-module homomorphism f and re Target(f) Inputs a chain map, or cochain map, or equivariant chain map, or FpG-module homomorphism f and re

Miscellaneous

SL2Z(p) SL2Z(1/m) Inputs a prime p or the reciprocal 1/m of a square free integer m. In the first case the function BigStepLCS(G,n) Inputs a group G and a positive integer n. It returns a subseries $G = L_1 > L_2 > \dots L_k = 1$ of the low Classify(L,Inv) Inputs a list of objects L and a function Inv which computes an invariant of each object. It returns RefineClassification(C,Inv) Inputs a list C := Classify(L,OldInv) and returns a refined classification according Compose(f,g) Inputs two FpG-module homomorphisms $f: M \longrightarrow N$ and $g: L \longrightarrow M$ with Source(f) = Target(g) HAPcopyright() This function provides details of HAP'S GNU public copyright licence.

IsLieAlgebraHomomorphism(f) Inputs an object f and returns true if f is a homomorphism $f:A\longrightarrow B$ of Lie a IsSuperperfect(G) Inputs a group G and returns "true" if both the first and second integral homology of G is triv MakeHAPManual() This function creates the manual for HAP from an XML file.

PermToMatrixGroup(G,n) Inputs a permutation group G and its degree n. Returns a bijective homomorphism f: SolutionsMatDestructive(M,B) Inputs an $m \times n$ matrix M and a $k \times n$ matrix B over a field. It returns a $k \times m$ matrix B over a field. It returns a B over a

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