smallantimagmas

A library of antiassociative magmas of small order

0.2.9

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Kamil Zabielski

Kamil Zabielski

Address: Department of Theoretical Computer Science
Białystok University of Technology
Wiejska 45A
15-325 Białystok
Poland

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1.1 smallantimagmas automatic generated documentation of properties

1.1.1 IsAntiassociative (for IsMagma)

▷ `IsAntiassociative(`*M*`)` (property)

Returns: `true` or `false`

identifies whether magma *M* is antiassociative.

Example

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.1.2 IsLeftCyclic (for IsMagma)

▷ `IsLeftCyclic(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cyclic `m`.

1.1.3 IsRightCyclic (for IsMagma)

▷ `IsRightCyclic(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cyclic `m`.

1.1.4 IsLeftCancellative (for IsMagma)

▷ `IsLeftCancellative(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cancellative `m`.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display( MultiplicationTable(M) );
[ [  2,   1 ],
  [  2,   1 ] ]
gap> IsRightCancellative(M);
false
gap> IsLeftCancellative(M);
true
gap> List(AllSmallAntimagmas(2), M -> IsLeftCancellative(M));
[ true, false ]
```

1.1.5 IsRightCancellative (for IsMagma)

▷ `IsRightCancellative(`*M*`)` (property)

Returns: `true` or `false`

if magma is right cancellative `m`.

Example

```
gap> List(AllSmallAntimagmas(2), M -> IsRightCancellative(M));
[ false, true ]
```

1.1.6 IsCancellative (for IsMagma)

▷ `IsCancellative(`*M*`)` (property)

Returns: `true` or `false`

if magma is cancellative `m`.

Example

```
gap> List(AllSmallAntimagmas(2), M -> IsCancellative(M));
[ false, false ]
```

1.2 smallantimagmas automatic generated documentation of attributes

1.2.1 AssociativityIndex (for IsMagma)

▷ `AssociativityIndex(`*M*`)` (attribute)

identifies associativity index of `M`.

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>
gap> AssociativityIndex(OneSmallAntimagma(2));
0
gap> OneSmallGroup(4);
<pc group of size 4 with 2 generators>
gap> AssociativityIndex(OneSmallGroup(4));
64
gap> AssociativityIndex(OneSmallGroup(4)) = 4 ^ 3;
true
```

1.2.2 DiagonalOfMultiplicationTable (for IsMagma)

▷ `DiagonalOfMultiplicationTable(M)` (attribute)

computes diaognal of multiplication table of `M`.

Example

```
gap> List(AllSmallAntimagmas(3), M -> DiagonalOfMultiplicationTable((M)));
[ [ 2, 1, 1 ], [ 2, 1, 1 ],
  [ 2, 3, 2 ], [ 2, 1, 1 ],
  [ 2, 1, 1 ], [ 2, 1, 2 ],
  [ 2, 3, 2 ], [ 2, 1, 2 ],
  [ 2, 3, 1 ], [ 2, 3, 1 ]
]
```

1.2.3 CommutativityIndex (for IsMagma)

▷ `CommutativityIndex(M)` (attribute)

identifies commutativity index of `M`.

Example

```
```

1.2.4 AnticommutativityIndex (for IsMagma)

▷ `AnticommutativityIndex(M)` (attribute)

calculates anticommutativity index of `M`.

Example

```
```

1.2.5 SquaresIndex (for IsMagma)

▷ `SquaresIndex(M)` (attribute)

computes squares index of `M` so the order of $\left\{m^2 | m \in M\right\}$.

Example

```
gap> List(AllSmallAntimagmas(2), M -> List(M, m -> m * m) );
[ [ m2, m1 ], [ m2, m1 ] ]
gap> List(AllSmallAntimagmas(2), M -> SquaresIndex(M ));
[ 2, 2 ]
gap> List(AllSmallAntimagmas(3), M -> SquaresIndex(M ));
[ 2, 2, 2, 2, 2, 2, 2, 2, 3, 3 ]
```

1.2.6 IdSmallAntimagma (for IsMagma)

▷ `IdSmallAntimagma(M)` (attribute)

identifies class of antiassociative magma `M`.

```
Example
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.2.7 LeftOrder (for IsExtLElement)

▷ `LeftOrder([m])` (attribute)

returns a left order of element `m`.

1.2.8 RightOrder (for IsExtRElement)

▷ `RightOrder([m])` (attribute)

returns a right order of element `m`.

1.2.9 LeftOrdersOfElements (for IsMagma)

▷ `LeftOrdersOfElements([m])` (attribute)

returns a left order of element `m`.

1.2.10 RightOrdersOfElements (for IsMagma)

▷ `RightOrdersOfElements([m])` (attribute)

returns a left order of element `m`.

1.3 smallantimagmas automatic generated documentation of global functions

1.3.1 AllSubmagmas

▷ `AllSubmagmas(M)` (function)

builds a collection of non-isomorphic submagmas of `M`.

```
Example
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> List(AllSmallAntimagmas(2), M -> AllSubmagmas(M));
[ [ <magma with 1 generator> ], [ <magma with 1 generator> ] ]
```

1.3.2 MagmaIsomorphismInvariantsMatch

▷ `MagmaIsomorphismInvariantsMatch(M)` (function)

computes isomorphism invariants of *M*.

1.3.3 IsMagmaIsomorphic

▷ `IsMagmaIsomorphic(M, N)` (function)

identifies whether magmas *M*, *N* are isomorphic.

```
Example
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> T := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> IsMagmaIsomorphic(M, M);
true
gap> IsMagmaIsomorphic(M, T);
true
gap> IsMagmaIsomorphic(M, N);
false
```

1.3.4 IsMagmaAntiisomorphic

▷ `IsMagmaAntiisomorphic([M, N])` (function)

identifies whether magmas *M*, *N* are antiisomorphic.

```
Example
gap> N := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, M);
false
gap> IsMagmaAntiisomorphic(M, N);
true
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
```

1.3.5 TransposedMagma

▷ `TransposedMagma([M])` (function)

generates transposed magma *M*.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
gap> IsMagmaIsomorphic(M, TransposedMagma(TransposedMagma(M)));
true
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display(MultiplicationTable(M));
[ [  2,  1 ],
  [  2,  1 ] ]
gap> Display(MultiplicationTable(TransposedMagma(M)));
[ [  2,  2 ],
  [  1,  1 ] ]
```

1.3.6 LeftPower

▷ LeftPower(*[m, k]*) (function)

returns a left *k*-power of element *m*.

1.3.7 RightPower

▷ RightPower(*[m, k]*) (function)

returns a right *k*-power of element *m*.

1.3.8 AllSmallAntimagmas

▷ AllSmallAntimagmas(*n*) (function)

returns all antiassociative magmas of specified size *n* (a number)

Example

```
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> AllSmallAntimagmas(3);
[
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>
]
```

1.3.9 NrSmallAntimagmas

▷ NrSmallAntimagmas(*n*) (function)

counts number of antiassociative magmas of specified size *n* (a number).

Example

```
gap> NrSmallAntimagmas(2);
2
gap> NrSmallAntimagmas(3);
10
gap> NrSmallAntimagmas(4);
17780
```

1.3.10 SmallAntimagma

▷ `SmallAntimagma(n, i)` (function)

returns antiassociative magma of id `[n, i]`.

Example

```
gap> SmallAntimagma(2, 1);
<magma with 2 generators>
gap> SmallAntimagma(4, 5);
<magma with 4 generators>
```

1.3.11 OneSmallAntimagma

▷ `OneSmallAntimagma(n)` (function)

returns a random antiassociative magma of size `n`.

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>

gap> OneSmallAntimagma(3);
<magma with 3 generators>
```

1.3.12 ReallyAllSmallAntimagmas

▷ `ReallyAllSmallAntimagmas(n)` (function)

returns really-all antiassociative magmas, isomorphic, of specified size `n` (a number)

Example

```
gap> ReallyAllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
```

1.3.13 ReallyNrSmallAntimagmas

▷ `ReallyNrSmallAntimagmas(n)` (function)

counts number of antiassociative magmas of specified size `n` (a number)

Example

```
gap> ReallyNrSmallAntimagmas(3);
52
```

1.3.14 AntimagmaGeneratorPossibleDiagonals

▷ `AntimagmaGeneratorPossibleDiagonals(n)` (function)

returns all possible diagonals of multiplication table for `[n]`-antimagma.

Example

```
gap> AntimagmaGeneratorPossibleDiagonals(2);
[ [ 2, 1 ] ]
gap> AntimagmaGeneratorPossibleDiagonals(3);
[
  [ 2, 1, 1 ], [ 2, 1, 2 ], [ 2, 3, 1 ], [ 2, 3, 2 ],
  [ 3, 1, 1 ], [ 3, 1, 2 ], [ 3, 3, 1 ], [ 3, 3, 2 ]
]
```

1.3.15 AntimagmaGeneratorFilterNonIsomorphicMagmas

▷ `AntimagmaGeneratorFilterNonIsomorphicMagmas(Ms)` (function)

filters non-isomorphic magmas `m`.

1.4 smallantimagmas automatic generated documentation of methods

1.4.1 MagmaIsomorphism (for IsMagma, IsMagma)

▷ `MagmaIsomorphism(M, N)` (operation)

computes an isomoprhism between magmas `M`, `N`.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> MagmaIsomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

1.4.2 MagmaAntiisomorphism (for IsMagma, IsMagma)

▷ `MagmaAntiisomorphism(M, N)` (operation)

creates an antiisomoprhism between magmas `M`, `N`.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> MagmaAntiisomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

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