A library of antiassociative magmas of small order

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Chapter 1

smallantimagmas automatic generated documentation

1.1 smallantimagmas automatic generated documentation of properties

1.1.1 IsAntiassociative (for IsMagma)

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.1.2 IsLeftCyclic (for IsMagma)

1.1.3 IsRightCyclic (for IsMagma)

1.1.4 IsLeftCancellative (for IsMagma)

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display( MultiplicationTable(M) );
[ [ 2, 1 ],
       [ 2, 1 ] ]
gap> IsRightCancellative(M);
false
gap> IsLeftCancellative(M);
true
gap> List(AllSmallAntimagmas(2), M -> IsLeftCancellative(M));
[ true, false ]
```

1.1.5 IsRightCancellative (for IsMagma)

```
gap> List(AllSmallAntimagmas(2), M -> IsRightCancellative(M));
[ false, true ]
```

1.1.6 IsCancellative (for IsMagma)

```
gap> List(AllSmallAntimagmas(2), M -> IsCancellative(M));
[ false, false ]
```

1.1.7 IsLeftFPFInducted (for IsMagma)

```
gap> Display( MultiplicationTable( SmallAntimagma(2, 2) ) );
[ [ 2, 2 ],
      [ 1, 1 ] ]
gap> IsLeftFPFInducted( SmallAntimagma(2, 2) );
true
```

1.1.8 IsRightFPFInducted (for IsMagma)

```
gap> Display( MultiplicationTable( SmallAntimagma(2, 1) ) );
[ [ 2, 1 ],
      [ 2, 1 ] ]
gap> IsRightFPFInducted( SmallAntimagma(2, 1) );
true
```

1.1.9 IsLeftDerangementInducted (for IsMagma)

▷ IsLeftDerangementInducted(M)

(property)

Returns: true or false

is a left-hand sided derangment inducted m.

1.1.10 IsRightDerangementInducted (for IsMagma)

▷ IsRightDerangementInducted(M)

(property)

Returns: true or false

is a right-hand sided derangment inducted m.

```
gap> M := SmallAntimagma(2, 1);
  <magma with 2 generators>
  gap> IsLeftFPFInducted(M);
  false
  gap> IsRightFPFInducted(M);
  true
  gap> IsRightDerangementInducted(M);
  true
```

1.1.11 IsLeftAlternative (for IsMagma)

```
▷ IsLeftAlternative(M)
Returns: true or false
is a left-alternative magma M.
```

(property)

Example _____

1.1.12 IsRightAlternative (for IsMagma)

 \triangleright IsRightAlternative(M)

(property)

Returns: true or false

is a right-alternatve magma M.

Example -

1.2 smallantimagmas automatic generated documentation of attributes

1.2.1 AssociativityIndex (for IsMagma)

```
▷ AssociativityIndex(M)
```

(attribute)

identifies associativity index of M.

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>
gap> AssociativityIndex(OneSmallAntimagma(2));
0
gap> OneSmallGroup(4);
<pc group of size 4 with 2 generators>
gap> AssociativityIndex(OneSmallGroup(4));
64
gap> AssociativityIndex(OneSmallGroup(4)) = 4 ^ 3;
true
```

1.2.2 DiagonalOfMultiplicationTable (for IsMagma)

▷ DiagonalOfMultiplicationTable(M)

(attribute)

computes diaognal of multiplication table of M.

```
Example

gap> List(AllSmallAntimagmas(3), M -> DiagonalOfMultiplicationTable((M)));

[[2, 1, 1], [2, 1, 1],
      [2, 3, 2], [2, 1, 1],
      [2, 1, 1], [2, 1, 2],
      [2, 3, 2], [2, 1, 2],
      [2, 3, 1], [2, 3, 1]
]
```

1.2.3 CommutativityIndex (for IsMagma)

▷ CommutativityIndex(M)

(attribute)

identifies commutativity index of M.

_____ Example _____

1.2.4 AnticommutativityIndex (for IsMagma)

▷ AnticommutativityIndex(M)

(attribute)

calculates anticommutativity index of M.

Example -

1.2.5 SquaresIndex (for IsMagma)

> SquaresIndex(M) (attribute)

computes squares index of M so the order of $\{m^2 | m \in M\}$.

```
gap> List(AllSmallAntimagmas(2), M -> List(M, m -> m * m) );
[ [ m2, m1 ], [ m2, m1 ] ]
gap> List(AllSmallAntimagmas(2), M -> SquaresIndex(M ));
[ 2, 2 ]
gap> List(AllSmallAntimagmas(3), M -> SquaresIndex(M ));
[ 2, 2, 2, 2, 2, 2, 2, 3, 3 ]
```

1.2.6 IdSmallAntimagma (for IsMagma)

▷ IdSmallAntimagma(M)

(attribute)

identifies class of antiassociative magma M.

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.2.7 LeftOrder (for IsExtLElement)

▷ LeftOrder([m])

(attribute)

returns a left order of element m.

1.2.8 RightOrder (for IsExtRElement)

RightOrder([m])
 (attribute)

returns a right order of element m.

1.2.9 LeftOrdersOfElements (for IsMagma)

▷ LeftOrdersOfElements([m])

(attribute)

returns a left order of element m.

1.2.10 RightOrdersOfElements (for IsMagma)

▷ RightOrdersOfElements([m])

(attribute)

returns a left order of element m.

(function)

1.3 smallantimagmas automatic generated documentation of global functions

1.3.1 AllSubmagmas

```
▷ AllSubmagmas(M) (function)
```

builds a collection of non-isomorphic submagmas of M.

```
gap> AllSmallAntimagmas(2);

[ <magma with 2 generators>, <magma with 2 generators> ]

gap> List(AllSmallAntimagmas(2), M -> AllSubmagmas(M));

[ [ <magma with 1 generator> ], [ <magma with 1 generator> ] ]
```

1.3.2 MagmaIsomorphismInvariantsMatch

→ MagmaIsomorphismInvariantsMatch(M) (function)

computes isomorphism invariants of M.

1.3.3 IsMagmaIsomorphic

▷ IsMagmaIsomorphic(M, N)

identifies whether magmas M, N are isomorphic.

```
gap> M := SmallAntimagma(2, 1);
  <magma with 2 generators>
  gap> N := SmallAntimagma(2, 2);
  <magma with 2 generators>
  gap> T := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
  <magma with 2 generators>
  gap> IsMagmaIsomorphic(M, M);
  true
  gap> IsMagmaIsomorphic(M, T);
  true
  gap> IsMagmaIsomorphic(M, N);
  false
```

1.3.4 IsMagmaAntiisomorphic

```
▷ IsMagmaAntiisomorphic([M, N])

(function)
```

identifies whether magmas M, N are antiisomorphic.

```
gap> N := SmallAntimagma(2, 1);

<magma with 2 generators>
gap> M := SmallAntimagma(2, 1);

<magma with 2 generators>
```

```
gap> N := SmallAntimagma(2, 2);
    <magma with 2 generators>
    gap> IsMagmaAntiisomorphic(M, M);
    false
    gap> IsMagmaAntiisomorphic(M, N);
    true
    gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
    true
```

1.3.5 TransposedMagma

▷ TransposedMagma([M])

(function)

generates transposed magma M.

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
gap> IsMagmaIsomorphic(M, TransposedMagma(TransposedMagma(M)));
true
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display(MultiplicationTable(M));
[[ 2,  1 ],
  [ 2,  1 ]]
gap> Display(MultiplicationTable(TransposedMagma(M)));
[[ 2,  2 ],
  [ 1,  1 ]]
```

1.3.6 LeftPower

```
▷ LeftPower([m, k])

(function)
```

returns a left k-power of element m.

1.3.7 RightPower

```
▷ RightPower([m, k])

(function)
```

returns a right k-power of element m.

1.3.8 AllSmallAntimagmas

```
\triangleright AllSmallAntimagmas(n) (function)
```

returns all antiassociative magmas of specified size n (a number)

1.3.9 NrSmallAntimagmas

▷ NrSmallAntimagmas(n)

(function)

counts number of antiassociative magmas of specified size n (a number).

```
gap> NrSmallAntimagmas(2);
2
gap> NrSmallAntimagmas(3);
10
gap> NrSmallAntimagmas(4);
17780
```

1.3.10 SmallAntimagma

```
▷ SmallAntimagma(n, i)
```

(function)

returns antiassociative magma of id [n, i].

```
gap> SmallAntimagma(2, 1);

<magma with 2 generators>
gap> SmallAntimagma(4, 5);

<magma with 4 generators>
```

1.3.11 OneSmallAntimagma

```
▷ OneSmallAntimagma(n)
```

(function)

returns a random antiassociative magma of size n.

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>

gap> OneSmallAntimagma(3);
<magma with 3 generators>
```

1.3.12 ReallyAllSmallAntimagmas

⊳ ReallyAllSmallAntimagmas(n)

(function)

returns really-all antiassociative magmas, isomorphic, of specified size n (a number)

```
gap> ReallyAllSmallAntimagmas(2);

[ <magma with 2 generators>, <magma with 2 generators> ]
```

1.3.13 ReallyNrSmallAntimagmas

(function)

counts number of antiassociative magmas of specified size n (a number)

```
gap> ReallyNrSmallAntimagmas(3);
52
```

1.3.14 AntimagmaGeneratorPossibleDiagonals

(function)

returns all possible diagonals of multiplication table for [n] -antimagma.

```
Example

gap> AntimagmaGeneratorPossibleDiagonals(2);
[[2, 1]]
gap> AntimagmaGeneratorPossibleDiagonals(3);
[
[2, 1, 1], [2, 1, 2], [2, 3, 1], [2, 3, 2],
[3, 1, 1], [3, 1, 2], [3, 3, 1], [3, 3, 2]
]
```

1.3.15 AntimagmaGeneratorFilterNonIsomorphicMagmas

▷ AntimagmaGeneratorFilterNonIsomorphicMagmas(Ms)

(function)

filters non-isomorphic magmas m.

1.4 smallantimagmas automatic generated documentation of methods

1.4.1 MagmaIsomorphism (for IsMagma, IsMagma)

```
▷ MagmaIsomorphism(M, N)
```

(operation)

computes an isomoprhism between magmas M, N.

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> MagmaIsomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

1.4.2 MagmaAntiisomorphism (for IsMagma, IsMagma)

▷ MagmaAntiisomorphism(M, N)

(operation)

creates an antiisomoprhism between magmas M, N.

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> MagmaAntiisomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

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