

# Scheduling of Washing Cycles

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**Abstract**—We present a case study of the specification of a washing systems, with cycles which can be launched in parallel and how we generated AIGER benchmarks for this problem.

## I. INTRODUCTION

The original AIGER format [1] is a safety property specification used for model checking. Its extended version was introduced in 2014 by Jacobs [2] to represent safety objectives for controller synthesis. It was first used in the Synthesis Competition 2014, a satellite event of the 26th International Conference on Computer Aided Verification 2014.

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## II. THE PROBLEM

We consider the design of a controller for a washing system for vegetables or fruits. The user can press a button which should initiate the arrival of water in a tank where the produce has been placed. After a determined time, the controller should open the valve to remove the water from inside the tank. We consider several such tanks put in parallel with a centralized controller, which has one button per tank, and a light that should be on whenever one of the tanks contain water.

For each tank  $i$ , we have an (uncontrollable) input  $\text{push}_i$  which is on when the corresponding button is pressed by the user, a controllable input  $\text{fill}_i$  which release water into the tank when on, and a controllable input  $\text{empty}_i$  which removes water from the tank. This is illustrated in Fig. 1. We also have a controllable input  $\text{light}$  which is on when the light is on.

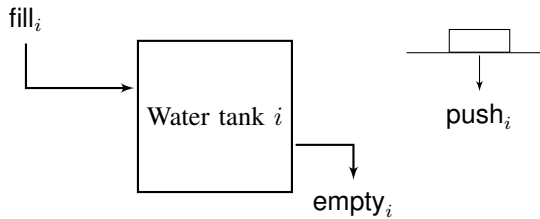


Fig. 1. A water tank. The input  $\text{fill}_i$  controls the arrival of water into the tank: if it is on, the valve is open and the water flows in. The input  $\text{empty}_i$  controls the departure of water out of the tank: if it is on, the valve is open and the water flows out. The washing cycle is initiated by pushing a button, which puts the inputs  $\text{push}_i$  to true.

## III. ENCODING OF THE PROBLEM BY SAFETY SPECIFICATION

We encode the specification for the controllers using rational expressions which denote the occurrence of an error in

the execution. We assume there are  $n$  tanks, numbered from 1 to  $n$ .

a) *Specification of each tanks*: First, an error occurs if a button was pressed but the tank is not filled after some delay smaller than  $d \in \mathbb{N}$ :

$$A_i = \text{true}^* \cdot \{\text{push}_i\} \cdot \{\neg \text{fill}_i\}^d.$$

The tank should also be filled only if the button was pushed:

$$B_i = \text{true}^* \cdot \{\neg \text{push}_i\}^d \cdot \{\text{fill}_i\}.$$

There is an error if the valve is not open after a delay exactly  $k$ , or if the tank was emptied to early (before  $k$  steps).

$$C_i = \text{true}^* \cdot \{\text{fill}_i\} \cdot \text{true}^k \cdot \{\neg \text{empty}_i\}$$

$$C'_i = \text{true}^* \cdot \{\text{fill}_i\} \cdot (\text{true} \mid \varepsilon)^{k-1} \{\text{empty}_i\}$$

b) *Light specification*: Now the light should be on if, and only if, one of the  $n$  tanks is being filled, so the following expression denotes error:

$$D = \text{true}^* \cdot \left\{ \text{light} \neq \bigvee_{i \in [1, n]} \text{fill}_i \right\}.$$

c) *Mutual exclusion*: Some of the tanks can be provided in water through the same pipe. In that case, the system should not fill to of them at the same time, otherwise the tanks would not recieve enough water. This is illustrated in Fig. 2. We write  $P$  for the sets of pipe, and for a pipe  $p \in P$ , we write  $i \in p$  to denote that the tank  $i$  is alimented by pipe  $p$ . We encode the mutual exclusion constraint by raising an error for the following expression:

$$E = \text{true}^* \cdot \left\{ \bigvee_{p \in P} \bigwedge_{i, j \in p} \text{fill}_i \right\}$$

## IV. TRANSLATION TO AIGER

We consider the safety specification given by the language:

$$\mathcal{L} = \bigcup_{i \in [1, n]} (L(A_i) \cup L(B_i) \cup L(C_i) \cup L(C'_i)) \cup L(D) \cup L(E)$$

Where  $L(A)$  denotes the languages associated to expression  $A$ . The error output of the AIGER files will be set to true whenever the current prefix belong to the language  $\mathcal{L}$ . To produce the AIGER file, the rational expressions are translated to non-deterministic automata  $\mathcal{A}$ , then each state of  $\mathcal{A}$  is encoded by a latch in the AIGER file. During an execution of

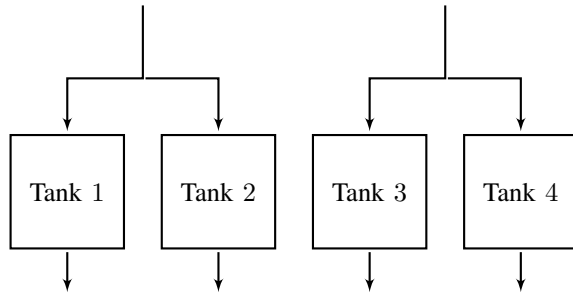


Fig. 2. A system with 4 water tanks. Tanks 1 and 2 are alimented by the same pipe and so do tanks 3 and 4.

the circuit, a latch  $l$  is on if, and only if there is an execution of  $\mathcal{A}$  on the word that as been read that leads to the state corresponding to latch  $l$ . The error latch is put to true if, and only if, one of the latches corresponding to accepting states is on.

In the benchmark package, the AIGER files are named `cycle_sched_n_d_p.aag` where  $n$  is the number of tanks,  $d$  is the maximum delay between `pushi` and `filli` and is equal to  $k$  the exact delay between `filli` and `emptyi`, and  $p$  is the number of tanks that are alimented by the same pipes.

The program that has been used to generate AIGER files from rationnal expressions can be downloaded from the following address: <https://github.com/romainbrenquier/Speculoos>.

#### REFERENCES

- [1] A. Biere. Aiger format and toolbox. [Online]. Available: <http://fmv.jku.at/aiger/>
- [2] S. Jacobs. (2014, February) Extended aiger format for synthesis (v0.1). [Online]. Available: <http://www.syntcomp.org/wp-content/uploads/2014/02/Format.pdf>