

1. Question 1

(a) $S \rightarrow 00S1$

$$S \rightarrow 1S00$$

The first two are clear rules of the language. When adding a single 1, you must also add two 0's

$$S \rightarrow SS$$

Concatenating two existing strings in the grammar will also produce a valid string. Both have the correct relationship between 1's and 0's, so the relationship does not change when they are combined

$$S \rightarrow 0S1S0$$

The forth rule allows the concatenation of two existing strings, and adding two 0's and a 1, allowing for "random" placement of 1's and 0's.

$$S \rightarrow \lambda$$

The fifth rule allows for the termination of a derivation

$$S \rightarrow 00S1$$

Rule 1

$$00S1 \rightarrow 00[1S00]1$$

Rule 2

(b) $00[1S00]1 \rightarrow 00[1[0S1S0]00]1$

Rule 4

$$00[1[0S1S0]00]1 \rightarrow 001010001$$

Rule 5 for both S