GSERM - Oslo 2019 GLS-ARMA and Dynamics

January 7, 2019 (afternoon session)

GLS Models

For:

$$Y_{it} = \mathbf{X}_{it}\beta + u_{it}$$

i.i.d. uits require:

$$\mathbf{u}\mathbf{u}' \equiv \mathbf{\Omega} = \sigma^2 \mathbf{I}$$

$$= \begin{pmatrix} \sigma^2 & 0 & \cdots & 0 \\ 0 & \sigma^2 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \sigma^2 \end{pmatrix}$$

GLS Models

That is, within units:

- $Var(u_{it}) = Var(u_{is}) \ \forall \ t \neq s$ (temporal homoscedasticity)
- $Cov(u_{it}, u_{is}) = 0 \ \forall \ t \neq s$ (no within-unit autocorrelation)

and between units:

- $Var(u_{it}) = Var(u_{jt}) \ \forall \ i \neq j \ (cross-unit homoscedasticity)$
- Cov $(u_{it}, u_{jt}) = 0 \ \forall \ i \neq j$ (no between-unit / spatial correlation)

The Key: Ω

Estimator:

$$\hat{\beta}_{\textit{GLS}} = (\mathbf{X}' \mathbf{\Omega}^{-1} \mathbf{X})^{-1} \mathbf{X}' \mathbf{\Omega}^{-1} \mathbf{Y}$$

with:

$$\widehat{\mathsf{V}(\beta_{\mathit{GLS}})} = (\mathsf{X}'\Omega^{-1}\mathsf{X})^{-1}$$

Two approaches:

- ullet Use OLS \hat{u}_{it} s to get $oldsymbol{\hat{\Omega}}$ ("feasible GLS")
- \bullet Use substantive knowledge about the data to structure Ω

Parks' Approach

Assume:

- $E(u_{it}^2) = E(u_{is}^2) \forall t \neq s$
- $E(u_{it}, u_{jt}) = \sigma_{ij} \ \forall \ i \neq j$,
- $E(u_{it}, u_{js}) = 0 \ \forall \ i \neq j, t \neq s$
- $E(u_{it}, u_{is}) = \rho \text{ or } \rho_i$

(B&K: "panel error assumptions").

Then

- 1. Use OLS to generate $\hat{u}s \rightarrow \hat{\rho} \ (\rightarrow \hat{\Omega})$,
- 2. Use $\hat{\rho}$ for Prais-Winsten.

This method was widely used prior to B&K (1995)

Parks' Problems

$$\boldsymbol{\Omega} = \begin{pmatrix} \boldsymbol{\Sigma} & \boldsymbol{0} & \cdots & \boldsymbol{0} \\ \boldsymbol{0} & \boldsymbol{\Sigma} & \cdots & \boldsymbol{0} \\ \vdots & \vdots & \ddots & \vdots \\ \boldsymbol{0} & \boldsymbol{0} & \cdots & \boldsymbol{\Sigma} \end{pmatrix} = \boldsymbol{\Sigma} \otimes \boldsymbol{I}_{N}$$

where

$$\Sigma = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \cdots & \sigma_{1N} \\ \sigma_{12} & \sigma_2^2 & \cdots & \sigma_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{1N} & \sigma_{2N} & \cdots & \sigma_N^2 \end{pmatrix}$$

Means:

- $\frac{N(N-1)}{2}$ distinct contemporaneous correlations,
- NT observations,
- $\rightarrow 2T/(N+1)$ observations per $\hat{\sigma}$

Panel-Corrected Standard Errors

Key to PCSEs:

$$\hat{\sigma}_{ij} = \frac{\sum_{t=1}^{T} \hat{u}_{it} \hat{u}_{jt}}{T}$$

Define:

$$\mathbf{U}_{T\times N} = \begin{pmatrix} \hat{u}_{11} & \hat{u}_{21} & \cdots & \hat{u}_{N1} \\ \hat{u}_{12} & \hat{u}_{22} & \cdots & \hat{u}_{N2} \\ \vdots & \vdots & \ddots & \vdots \\ \hat{u}_{1T} & \hat{u}_{2T} & \cdots & \hat{u}_{NT} \end{pmatrix}$$

$$\boldsymbol{\hat{\Sigma}} = \frac{(\boldsymbol{U}'\boldsymbol{U})}{T}$$

$$\hat{\Omega}_{\textit{PCSE}} = \frac{\left(\textbf{U}'\textbf{U}\right)}{\textit{T}} \otimes \textbf{I}_{\textit{T}}$$

Panel-Corrected Standard Errors

Correct formula:

$$\mathsf{Cov}(\hat{\beta}_{\textit{PCSE}}) = (\mathbf{X}'\mathbf{X})^{-1}[\mathbf{X}'\mathbf{\Omega}\mathbf{X}](\mathbf{X}'\mathbf{X})^{-1}$$

General Issues

PCSEs:

- Do not fix unit-level heterogeneity (a la "fixed" / "random" effects)
- Do not deal with dynamics
- \bullet Depend critically on the "panel data assumptions" of Park / B&K

Panel Assumptions and Numbers of Parameters to be Estimated

Panel Assumptions	No AR(1)	Common $\hat{ ho}$	Separate $\hat{ ho_i}$ s
$\sigma_i^2 = \sigma^2$, $Cov(\sigma_{it}, \sigma_{jt}) = 0$	k + 1	k+2	k + N + 1
$\sigma_i^2 \neq \sigma^2$, $Cov(\sigma_{it}, \sigma_{jt}) = 0$	k + N	k + N + 1	k + 2N
$\sigma_i^2 \neq \sigma^2$, $Cov(\sigma_{it}, \sigma_{jt}) \neq 0$	$\frac{N(N-1)}{2} + k + N$	$\frac{N(N-1)}{2} + k + N + 1$	$\frac{N(N-1)}{2} + k + 2N$

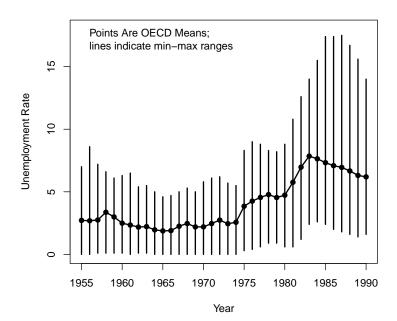
Example: Central Banks, Unions, Unemployment

- Hall and Franzese (1998 IO)
- 18 OECD countries, 1955-1990 (N = 18, T = 36, NT = 648)
- *Y* = unemployment
- Covariates: GDP, openness, union density, left cabinets, central bank independence, coordinated wage bargaining, interaction

Example: Data

```
> summary(HF)
                                                                cbi
   country
                    year
                                    ue
                                                  inf
Min.
       : 1.0
               Min.
                      :1955
                              Min. : 0.0
                                             Min. :-1.7
                                                           Min. :0.12
1st Qu.: 5.0
               1st Qu.:1964
                              1st Qu.: 1.6
                                             1st Qu.: 3.2
                                                           1st Qu.:0.41
Median: 9.5
               Median:1972
                              Median: 3.0
                                             Median: 4.9
                                                           Median:0.47
Mean
       :10.3
               Mean
                      :1972
                              Mean
                                   : 4.0
                                             Mean : 6.0
                                                           Mean
                                                                  :0.50
3rd Qu.:15.0
               3rd Qu.:1981
                              3rd Qu.: 5.7
                                             3rd Qu.: 7.7
                                                           3rd Qu.:0.61
                                     :17.5
                                             Max. :27.2
Max.
       :21.0
               Max.
                      :1990
                              Max.
                                                           Max. :0.93
  cwagebrg
                   GDP_PC
                                                 uden
                                                               lcab
                                  open
        :0.00
                      :7.6
                             Min.
                                                   :0.10
                                                                  :0.00
Min.
               Min.
                                    :0.07
                                            Min.
                                                           Min.
1st Qu.:0.25
               1st Qu.:8.9
                             1st Qu.:0.31
                                            1st Qu.:0.32
                                                           1st Qu.:0.00
Median:0.50
               Median:9.2
                             Median:0.43
                                            Median:0.41
                                                          Median:0.07
Mean :0.49
               Mean :9.1
                             Mean :0.46
                                            Mean :0.44
                                                          Mean :0.31
3rd Qu.:0.75
               3rd Qu.:9.4
                             3rd Qu.:0.54
                                            3rd Qu.:0.56
                                                          3rd Qu.:0.58
        :1.00
               Max.
                      :9.8
                             Max.
                                    :1.40
                                            Max.
                                                   :0.85
                                                          Max.
                                                                 :1.00
Max.
   wagexcbi
                  HasLCAB
       :0.00
Min.
               Min. :1
1st Qu.:0.04
               1st Qu.:1
Median:0.21
               Median :1
Mean
       :0.25
               Mean
                      : 1
3rd Qu.:0.37
               3rd Qu.:1
Max.
       :0.70
               Max.
                      :1
```

Unemployment in 18 Nations, 1955-1990



Example: OLS

```
> summary(HF.OLS)
Oneway (individual) effect Pooling Model
Balanced Panel: n=18, T=36, N=648
Residuals :
  Min. 1st Qu. Median 3rd Qu.
                             Max.
-5.120 -1.500 -0.241 1.230
                            9.290
Coefficients :
          Estimate Std. Error t-value
                                     Pr(>|t|)
(Intercept) -13.579
                      2.328 -5.83 0.0000000086 ***
GDP_PC
            5.119 0.418 12.24
                                      < 2e-16 ***
open
uden
           0.709 0.808 0.88
                                        0.38
          0.236 0.293 0.81
lcab
                                        0.42
                   1.097 4.71 0.0000030150 ***
chi
           5.169
cwagebrg
           -1.292 0.792
                            -1.63
                                        0.10
wagexcbi
           -7.030 1.505
                            -4.67 0.0000036327 ***
---
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Total Sum of Squares:
                    6500
Residual Sum of Squares: 3730
R-Squared:
             0.426
Adj. R-Squared: 0.421
F-statistic: 67.9634 on 7 and 640 DF, p-value: <2e-16
```

Example: Prais-Winsten

```
> HF.prais <- prais.winsten(ue~GDP_PC+open+uden+lcab+cbi+cwagebrg+wagexcbi,
                      data=HF,iter=100)
> HF.prais
Residuals:
  Min 10 Median
                     30
                           Max
-8.456 -0.431 -0.144 0.314 4.615
Coefficients:
        Estimate Std. Error t value Pr(>|t|)
Intercept -15.2783
                    2.2128 -6.90 1.2e-11 ***
GDP_PC
        2.3415 0.2515 9.31 < 2e-16 ***
open -0.3491 0.7950 -0.44 0.6608
uden 5.5466 1.1492 4.83 1.7e-06 ***
lcab -0.0593 0.1861 -0.32 0.7501
chi
       -3.4801
                   2.4753 -1.41 0.1602
cwagebrg -10.5954 2.0019 -5.29 1.7e-07 ***
wagexcbi 10.6805
                    3.4942 3.06 0.0023 **
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 0.95 on 640 degrees of freedom
Multiple R-squared: 0.279, Adjusted R-squared: 0.27
F-statistic: 31 on 8 and 640 DF, p-value: <2e-16
 Rho Rho.t.statistic Iterations
0.94
                          10
```

Example: GLS with Homoscedastic AR(1) Errors

```
> HF.GLS <- gls(ue~GDPPC+open+uden+lcab+cbi+cwagebrg+wagexcbi,
                          HF,correlation=corAR1(form=~1|country))
> summary(HF.GLS)
Generalized least squares fit by REML
 Model: ue ~ GDPPC + open + uden + lcab + cbi + cwagebrg + wagexcbi
 Data: HF
  AIC BIC logLik
  1484 1529 -732
Correlation Structure: AR(1)
Formula: ~1 | country
Parameter estimate(s):
Phi
0 99
Coefficients:
           Value Std.Error t-value p-value
(Intercept)
              43
                       7.3
                              5.8
                                    0.000
GDPPC
              -4
                       0.7
                             -5.5
                                   0.000
              -1
                      0.8
                            -1.8
                                  0.072
open
uden
              1
                      2.2
                            0.3
                                  0.792
1 cab
               0
                      0.1
                             -0.7 0.473
chi
              -1
                      7.5
                             -0.2
                                   0.848
cwagebrg
              -5
                      6.4
                             -0.8
                                   0 402
wagexcbi
               3
                     11 7
                              0.3
                                  0.770
Correlation:
        (Intr) GDPPC open uden lcab cbi
                                                cwgbrg
GDPPC
        -0.827
open
       0.124 -0.207
uden -0.145 0.017 -0.048
1 cab
     0.041 -0.054 0.005 -0.003
chi
        -0.421 -0.100 0.033 0.069 0.009
cwagebrg -0.371 -0.065 0.018 -0.084 -0.014 0.721
wagexcbi 0.334 0.082 -0.028 0.017 0.004 -0.813 -0.905
Standardized residuals:
  Min
        Q1 Med
                        Max
-1.49 -0.64 -0.20 0.46 2.55
```

More GLS: Unit-Wise Heteroscedisticity

```
> HF.GLS2 <- gls(ue~GDPPC+open+uden+lcab+cbi+cwagebrg+wagexcbi,
               HF, correlation=corAR1(form=~1|country),
               weights = varIdent(form = ~1|country))
> summary(HF.GLS2)
Generalized least squares fit by REML
   AIC BIC logLik
 1326 1446 -636
Correlation Structure: AR(1)
Formula: ~1 | country
Parameter estimate(s):
Phi
0.98
Variance function:
Structure: Different standard deviations per stratum
Formula: ~1 | country
Parameter estimates:
1.00 0.19 0.75 0.54 0.60 1.00 0.95 0.32 0.88 0.89 0.78 1.09 0.92 0.57 0.33 0.38 0.86 0.60
Coefficients:
           Value Std.Error t-value p-value
(Intercept) 21.1
                              4.5 0.0000
GDPPC
            -1 6
                       0.4
                           -4.3 0.0000
open
            -2.2
                       0.6
                            -3.4 0.0008
uden
            0.9
                      1.5
                            0.6.0.5415
1 cab
            -0.1
                       0.1
                            -1.2 0.2206
           -1.9
                       7.3
                           -0.3 0.7984
chi
cwagebrg
           -6.3
                      4.7
                            -1.3 0.1794
wagexcbi
           5.0
                            0.5 0.5996
```

Example: PCSEs

> library(lmtest) > coeftest(HF.OLS,vcov=vcovBK) t test of coefficients: Estimate Std. Error t value Pr(>|t|) (Intercept) -13.579 7.320 -1.86 0.064 . GDP PC 1.603 0.821 1.95 0.051 . 1.304 3.93 0.000096 *** 5.119 open 0.709 2.518 0.28 uden 0.778 1 cab 0.236 0.668 0.35 0.724 5.169 3.439 1.50 0.133 cbi cwagebrg -1.292 2.478 -0.52 0.602 wagexcbi -7.030 4.726 -1.49 0.137 ___ Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1

Alternative Approach: pcse

```
> HF.lm<-lm(ue~GDP_PC+open+uden+lcab+cbi+cwagebrg+wagexcbi,data=HF)
> HF.pcse<-pcse(HF.lm,groupN = HF$country, groupT = HF$year)</pre>
```

> summary(HF.pcse)

Results:

	Estimate	PCSE	t	value	Pr(> t)
(Intercept)	-13.58	4.74		-2.87	4.3e-03
GDP_PC	1.60	0.53		3.01	2.7e-03
open	5.12	0.53		9.71	7.0e-21
uden	0.71	0.53		1.35	1.8e-01
lcab	0.24	0.27		0.88	3.8e-01
cbi	5.17	0.85		6.10	1.9e-09
cwagebrg	-1.29	0.77		-1.67	9.6e-02
wagexcbi	-7.03	1.05		-6.68	5.3e-11

[#] Valid Obs = 648; # Missing Obs = 0; Degrees of Freedom = 640.

General advice...

Lagged: Y?

$$Y_{it} = \phi Y_{it-1} + \mathbf{X}_{it} \boldsymbol{\beta}_{LDV} + \epsilon_{it}$$

If ϵ_{it} is perfect...

- $\hat{\beta}_{LDV}$ is biased (but consistent),
- O(bias) = $\frac{-1+3\beta_{LDV}}{T}$

If ϵ_{it} is autocorrelated...

- $\hat{\beta}_{LDV}$ is biased and inconsistent
- IV is one (bad) option...

Lagged Ys and GLS-ARMA

Can rewrite:

$$Y_{it} = \mathbf{X}_{it} \boldsymbol{\beta}_{AR} + u_{it}$$

 $u_{it} = \phi u_{it-1} + \eta_{it}$

as

$$Y_{it} = \mathbf{X}_{it}\beta_{AR} + \phi u_{it-1} + \eta_{it}$$

$$= \mathbf{X}_{it}\beta_{AR} + \phi(\mathbf{Y}_{it-1} - \mathbf{X}_{it-1}\beta_{AR}) + \eta_{it}$$

$$= \phi \mathbf{Y}_{it-1} + \mathbf{X}_{it}\beta_{AR} + \mathbf{X}_{it-1}\psi + \eta_{it}$$

where $\psi = \phi \beta_{AR}$ and $\psi = 0$ (by assumption).

Lagged Ys and World Domination

In:

$$Y_{it} = \phi Y_{it-1} + \mathbf{X}_{it} \beta_{LDV} + \epsilon_{it}$$

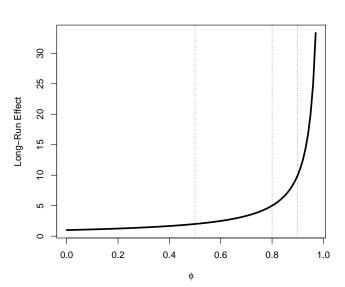
Achen: Bias "deflates" $\hat{\beta}$ relative to $\hat{\phi}$, "suppress" the effects of **X**...

Keele & Kelly (2006):

- ullet Contingent on ϵs having autocorrelation
- Key: In LDV, long-run impact of a unit change in X is:

$$\hat{\beta}_{LR} = \frac{\hat{\beta}_{LDV}}{1 - \hat{\phi}}$$

Long-Run Impact for $\hat{eta}=1$



Lagged Ys and Unit Effects

Consider:

$$Y_{it} = \phi Y_{it-1} + \mathbf{X}_{it} \boldsymbol{\beta} + \alpha_i + u_{it}.$$

If we omit the unit effects, we have:

$$Y_{it} = \phi Y_{it-1} + \mathbf{X}_{it} \boldsymbol{\beta} + u_{it}^*$$

with

$$u_{it}^* = \alpha_i + u_{it}$$

Lagging yields:

$$Y_{it-1} = \phi Y_{it-2} + \mathbf{X}_{it-1} \boldsymbol{\beta} + \alpha_i + u_{it-1}$$

which means

$$Cov(Y_{it-1}, u_{it}^*) \neq 0.$$

"Nickell" Bias

Bias in $\hat{\phi}$ is

- toward zero when $\phi > 0$,
- increasing in ϕ .

<u>Including</u> unit effects still yields bias in $\hat{\phi}$ of $O(\frac{1}{T})$, and bias in $\hat{\beta}$.

Solutions:

- Difference/GMM estimation
- Bias correction approaches

First Difference Estimation

$$Y_{it} - Y_{it-1} = \phi(Y_{it-1} - Y_{it-2}) + (\mathbf{X}_{it} - \mathbf{X}_{it-1})\beta + (\alpha_i - \alpha_i) + (u_{it} - u_{it-1})$$

$$\Delta Y_{it} = \phi \Delta Y_{it-1} + \Delta \mathbf{X}_{it}\beta + \Delta u_{it}$$

Anderson/Hsiao: If \nexists autocorrelation, then use ΔY_{it-2} or Y_{it-2} as instruments for ΔY_{it-1} ...

- Consistent in theory,
- ullet in practice, the former is preferred, and both have issues if ϕ is high;
- both are inefficient.

Arellano & Bond (also Wawro): Use all lags of Y_{it} and \mathbf{X}_{it} from t-2 and before.

- "Good" estimates, better as $T \to \infty$,
- Easy to handle higher-order lags of Y,
- Easy software (plm in R , xtabond in Stata).
- Model is fixed effects...
- \mathbf{Z}_i has T-p-1 rows, $\sum_{i=p}^{T-2} i$ columns \to difficulty of estimation declines in p, grows in T.

Bias-Correction Models

Kiviet (1995, 1999; Bun and Kiviet 2003; Bruno 2005a,b): Derive the bias in $\hat{\phi}$ and $\hat{\beta}$, then correct it...

- \bullet More accurate than the instrumental-variables/GMM estimators of A&H/A&B...
- ...especially when T is small; but not as T gets reasonably large $(T \approx 20)$

Stationarity: Quick Intro

Mean stationarity:

$$\mathsf{E}(Y_t) = \mu \ \forall \ t$$

Variance stationarity:

$$Var(Y_t) = E[(Y_t - \mu)^2] \equiv \sigma_Y^2 \ \forall \ t$$

Covariance stationarity:

$$\mathsf{Cov}(Y_t,Y_{t-s}) = \mathsf{E}[(Y_t - \mu)(Y_{t-s} - \mu)] = \gamma_s \; \forall \; s$$

I(1) Series and Unit Roots

I(1) ("integrated") series:

$$Y_t = Y_{t-1} + u_t$$

vs. AR(1) series:

$$Y_t = \rho Y_{t-1} + u_t$$

or trending series:

$$Y_t = \beta t + u_t$$

Differencing:

$$\Delta Y_t \equiv Y_t - Y_{t-1} = Y_t + u_t - Y_{t-1}$$
$$= u_t$$

and

$$\Delta Y_t \equiv Y_t - Y_{t-1} = \beta t + u_t - (\beta(t-1) + u_{t-1})$$

$$= \beta t + u_t - \beta t + \beta - u_{t-1}$$

$$= u_t - u_{t-1} + \beta$$

I(1) series (continued)

More generally:

- $|\rho| > 1$
 - Series is nonstationary / explosive
 - Past shocks have a greater impact than current ones
 - Uncommon
- $|\rho| < 1$
 - Stationary series
 - ullet Effects of shocks die out exponentially according to ho
 - Is mean-reverting
- $|\rho|=1$
 - Nonstationary series
 - Shocks persist at full force
 - Not mean-reverting; variance increases with t

Unit Root Tests: Dickey-Fuller

Two steps:

- Estimate $Y_t = \rho Y_{t-1} + u_t$,
- test the hypothesis that $\hat{\rho} = 0$, but
- this requires that the us are uncorrelated.

But suppose:

$$\Delta Y_t = \sum_{i=1}^p d_i \Delta Y_{t-i} + u_t$$

which yields

$$Y_t = Y_{t-1} + \sum_{i=1}^{p} d_i \Delta Y_{t-i} + u_t.$$

D.F. tests will be incorrect.

Unit Root Alternatives

Augmented Dickey-Fuller Tests:

• Estimate

$$\Delta Y_t = Y_{t-1} + \sum_{i=1}^{p} d_i \Delta Y_{t-i} + u_t$$

• Test $\hat{\rho} = 0$

Phillips-Perron Tests:

• Estimate:

$$\Delta Y_t = \alpha + \rho Y_{t-1} + u_t$$

- Calculate modified test statistics (Z_{ρ} and Z_{t})
- Test $\hat{\rho} = 0$

Issues with Unit Roots in Panel Data

- Short series + Asymptotic tests → "borrow strength"
- Requires uniform unit roots across is
- Various alternatives:
 - Maddala and Wu (1999)
 - Hadri (2000)
 - Levin, Lin and Chu (2002)
- What to do?
 - Difference the data...
 - Error-correction models

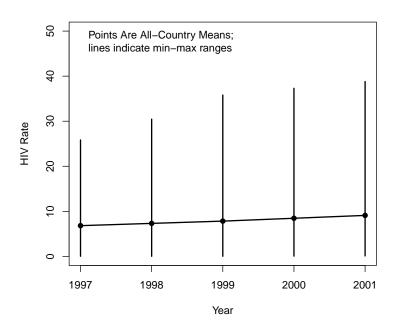
Example: HIV/AIDS in Africa, 1997-2001

> summary(AIDS	3)				
ccode	year	lnAIDS	lnAIDSlag	warlag	popden
Min. :404	Min. :1997	Min. :-3.8	Min. :-4	Min. :0.00	Min. :0.00
1st Qu.:451	1st Qu.:1998	1st Qu.: 0.6	1st Qu.: 1	1st Qu.:0.00	1st Qu.:0.01
Median:506	Median:1999	Median: 1.6	Median : 2	Median:0.00	Median:0.03
Mean :510	Mean :1999	Mean : 1.2	Mean : 1	Mean :0.14	Mean :0.06
3rd Qu.:560	3rd Qu.:2000	3rd Qu.: 2.4	3rd Qu.: 2	3rd Qu.:0.00	3rd Qu.:0.07
Max. :651	Max. :2001	Max. : 3.7	Max. : 4	Max. :1.00	Max. :0.57
			NA's :46		

refsin

Min. : 0 1st Qu.: 1 Median : 10 Mean : 56 3rd Qu.: 46 Max. :543

HIV/AIDS in Africa, 1997-2001



Panel Unit Root Tests: R

```
> lnAIDS<-cbind(AIDS$ccode,AIDS$year,AIDS$lnAIDS)
> purtest(lnAIDS,exo="trend",test=c("levinlin"))
Levin-Lin-Chu Unit-Root Test (ex. var.: Individual Intercepts and Trend)
data: lnAIDS
z.x1 = 3e+12, p-value <2e-16
alternative hypothesis: stationarity
> purtest(lnAIDS,exo="trend",test=c("hadri"))
Hadri Test (ex. var.: Individual Intercepts and Trend)
data: lnATDS
z = 60, p-value <2e-16
alternative hypothesis: at least one series has a unit root
> purtest(lnAIDS,exo="trend",test=c("ips"))
Im-Pesaran-Shin Unit-Root Test (ex. var.: Individual Intercepts and Trend)
data: lnATDS
z = 4, p-value = 0.0002
alternative hypothesis: stationarity
```

Final Thoughts: Dynamic Panel Models

- N vs. T...
- Are dynamics nuisance or substance?
- What problem(s) do you really care about?